

Miscellaneous notes for *Tape and Tape* (2012a):

“A geometric setting for moment tensors”

Geophysical Journal International

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June 14, 2012

Browse a few related files in the `momenttensor` directory (see “Source” tab, then “Browse”) of <http://code.google.com/p/compearth/>

Or, from the command line of a terminal window (e.g., linux), check out the whole directory:
`svn checkout http://compearth.googlecode.com/svn/trunk/momenttensor/ momenttensor`

1 Computing source type coordinates on the fundamental lune

Here we present a guide for converting moment tensors to source types on the fundamental lune, then plotting. All equation references are for *Tape and Tape* (2012a).

1. Start with a moment tensor represented as a 3×3 symmetric matrix in some orthonormal basis (it does not matter which one). Compute the eigenvalues.
2. Sort the eigenvalues as $\lambda_1 \geq \lambda_2 \geq \lambda_3$. Then compute the (γ, β, ρ) coordinates with Eq. 21:

$$\begin{aligned}\tan \gamma &= \frac{-\lambda_1 + 2\lambda_2 - \lambda_3}{\sqrt{3}(\lambda_1 - \lambda_3)} \\ \cos \beta &= \frac{\lambda_1 + \lambda_2 + \lambda_3}{\sqrt{3}\|\mathbf{\Lambda}\|} \\ \rho &= \|\mathbf{\Lambda}\|\end{aligned}$$

(Here ρ is not needed, but it represents the seismic moment: $M_0 = \rho/\sqrt{2}$.) For latitude on the lune, use $\delta = \pi/2 - \beta$.

If you are starting with eigenvalues, rather than the moment tensor, then start with step 2.

1.1 Plotting in Mathematica

All 3D plots in *Tape and Tape* (2012a) were generated using Mathematica, which is commercial software. A Mathematica code to get started is available here:

<http://code.google.com/p/compearth/source/browse/trunk/momenttensor/plot/mma/Lune.nb>

1.2 Plotting in GMT

Generic Mapping Tools (GMT: *Wessel and Smith* (1991)) is open-source software. It provides numerous options for global projections. One example, the equal-area Hammer projection, is shown in Figure 3. The key command in GMT is `-JH0/3i -R-30/30/-90/90`; this specifies the projection and also the region of the fundamental lune (γ - δ coordinates). A script to generate these plots, `lune.pl`, is available here:

<http://code.google.com/p/compearth/source/browse/trunk/momenttensor/plot/gmt/>
This requires several text files as well. (The easiest thing is to check out the whole directory `momenttensor`; see link to `compearth` project at the top.)

The 2D plotting option was intentionally not included in *Tape and Tape* (2012a) for two reasons: (1) the projection distracts from the key point that the lune is part of the sphere; (2) the projection, while equal-area, distorts areas that are undistorted on the sphere. Nevertheless, a comparison between Figures 2 and 4 shows that the 2D version might be preferred for representing points that span the full lune. In either case, we note that the 2D lune is preferred over the T-k source-type plots (*Hudson et al.*, 1989; *Tape and Tape*, 2012b).

References

- Hudson, J. A., R. G. Pearce, and R. M. Rogers (1989), Source time plot for inversion of the moment tensor, *J. Geophys. Res.*, *94*(B1), 765–774.
- Tape, W., and C. Tape (2012a), A geometric setting for moment tensors, *Geophys. J. Int.*, *190*, 476–498.
- Tape, W., and C. Tape (2012b), A geometric comparison of source-type plots for moment tensors, *Geophys. J. Int.*, *190*, 499–510.
- Wessel, P., and W. H. F. Smith (1991), Free software helps map and display data, *Eos Trans. Am. Geophys. Un.*, *72*(41), 441 ff.

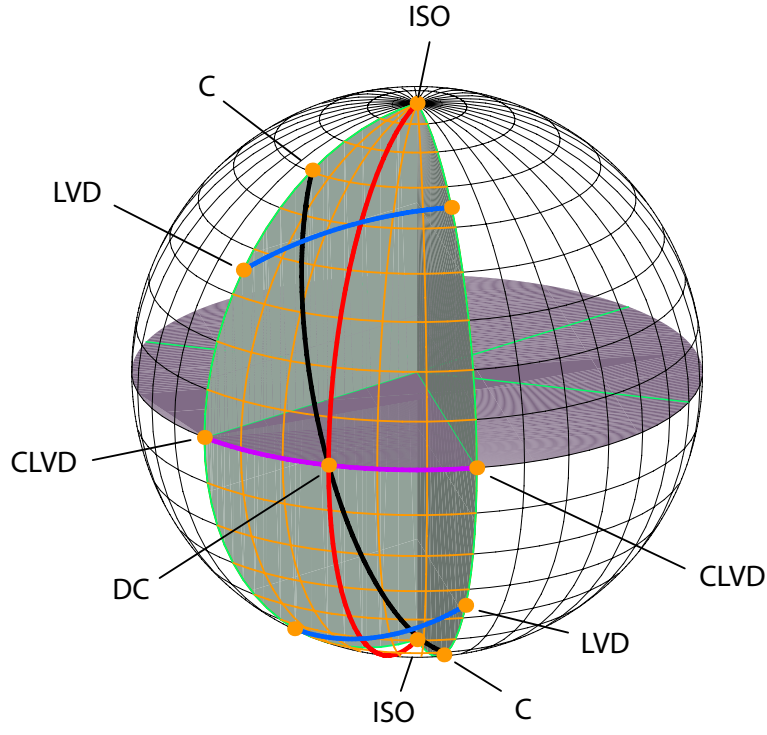


Figure 1: Fundamental lune representation of source types (*Tape and Tape*, 2012a, Figure 1). See 2D version in Figure 3.

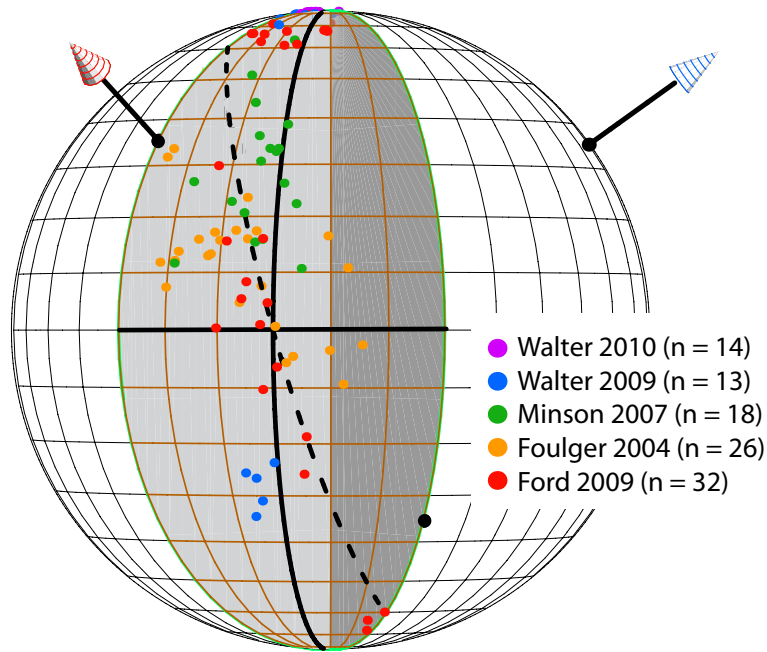


Figure 2: Five full moment tensor data sets plotted on the fundamental lune (*Tape and Tape*, 2012a, Figure 25). See 2D version in Figure 4.

Representation of source types on the fundamental lune

(W. Tape and C. Tape, 2012, GJI, "A geometric setting for moment tensors")

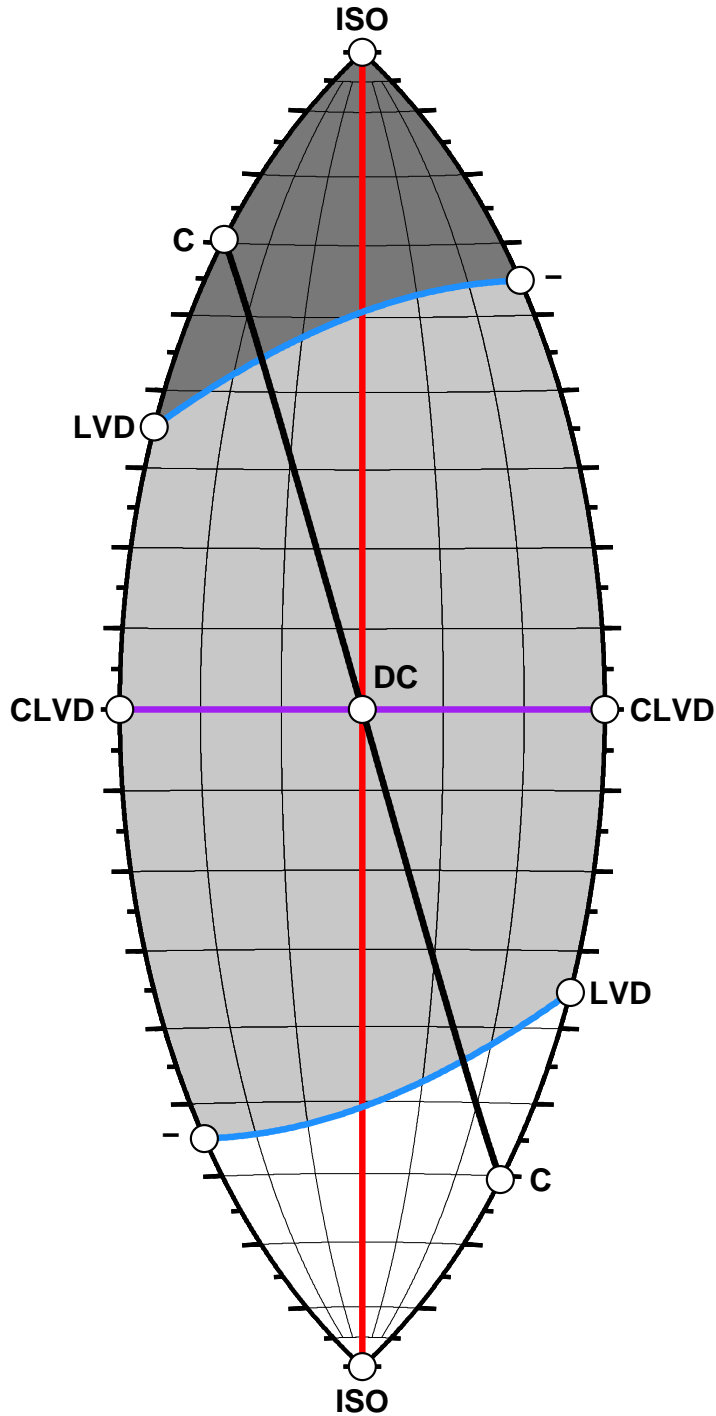


Figure 3: Home for source types, 2D version. See 3D version in Figure 1. The dark gray region at the top represents source types for which all vectors point outward. The white region at the bottom represents source types for which all vectors point inward.

Representation of source types on the fundamental lune

(W. Tape and C. Tape, 2012, GJI, "A geometric setting for moment tensors")

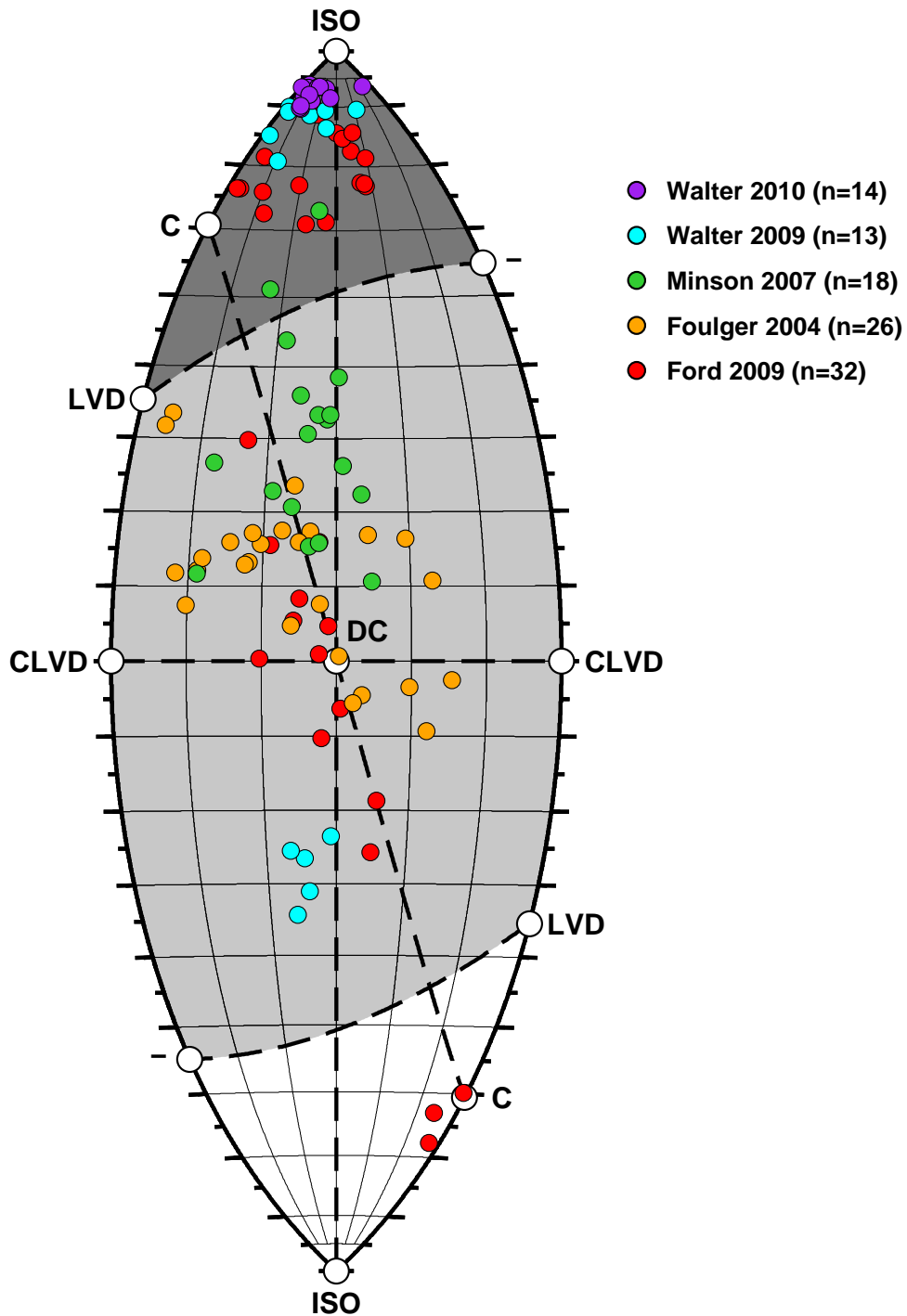


Figure 4: Five full moment tensor data sets plotted on the fundamental lune. See 3D version in Figure 2.