Part 1: PCA and Variance Threshold in a Linear Regression

1. Import the housing data as a data frame and ensure that the data is loaded properly.

```
In [1]:
        #Import necessary libraries
        import pandas as pd
        import numpy as np
        from sklearn.model selection import train test split
        from sklearn.linear model import LinearRegression
        import matplotlib.pyplot as plt
        from sklearn.metrics import mean squared error, r2 score, mean absolute error
        from math import sqrt
        from sklearn.preprocessing import StandardScaler
        from sklearn.decomposition import PCA
        from sklearn import preprocessing
        from sklearn.feature selection import VarianceThreshold
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.metrics import confusion matrix
        import seaborn as sns
        import pydotplus
        from IPython.display import Image
        from sklearn import tree
        from sklearn.feature selection import SelectKBest
        from sklearn.feature selection import chi2
        from sklearn.metrics import accuracy score
        from sklearn.preprocessing import scale
In [2]: housing_df = pd.read csv("train.csv")
        print(housing df.shape)
In [3]:
        housing df.head(5)
        (1460, 81)
Out[3]:
           Id MSSubClass MSZoning LotFrontage LotArea Street Alley LotShape LandContour Utilities ... PoolAre
        0 1
                               RL
                                         65.0
                                                 8450
                                                                                        AllPub ...
                      60
                                                       Pave
                                                            NaN
                                                                      Reg
                                                                                   Lvl
                      20
                                RL
                                         0.08
                                                 9600
                                                           NaN
                                                                                        AllPub ...
                                                       Pave
                                                                      Reg
                                                                                   Lvl
          3
                      60
                                         68.0
                                                                                        AllPub ...
        2
                               RL
                                                11250
                                                       Pave NaN
                                                                       IR1
                                                                                   Lvl
                                                                                        AllPub ...
                                         60.0
                                                 9550
                                                       Pave NaN
        3 4
                      70
                                RL
                                                                       IR1
                                                                                   Lvl
          5
                      60
                               RI
                                         84.0
                                                14260
                                                       Pave NaN
                                                                       IR1
                                                                                   ΙvΙ
                                                                                        AllPub ...
```

5 rows × 81 columns

2. Drop the "Id" column and any features that are missing more than 40% of their values.

```
In [4]: housing_df.drop('Id',axis=1,inplace=True)
housing_df.head(5)
```

 ${\tt Out[4]:} \qquad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{Street} \quad \textbf{Alley} \quad \textbf{LotShape} \quad \textbf{LandContour} \quad \textbf{Utilities} \quad \textbf{LotConfig} \quad ... \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{Street} \quad \textbf{Alley} \quad \textbf{LotShape} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{LotFrontage} \quad \textbf{LotArea} \quad \textbf{MSSubClass} \quad \textbf{MSZoning} \quad \textbf{MSZoni$

| 0 | 60 | RL | 65.0 | 8450 | Pave | NaN | Reg | Lvl | AllPub | Inside | |
|---|----|----|------|-------|------|-----|-----|-----|--------|--------|--|
| 1 | 20 | RL | 80.0 | 9600 | Pave | NaN | Reg | Lvl | AllPub | FR2 | |
| 2 | 60 | RL | 68.0 | 11250 | Pave | NaN | IR1 | Lvl | AllPub | Inside | |
| 3 | 70 | RL | 60.0 | 9550 | Pave | NaN | IR1 | Lvl | AllPub | Corner | |
| 4 | 60 | RL | 84.0 | 14260 | Pave | NaN | IR1 | Lvl | AllPub | FR2 | |

5 rows × 80 columns

```
In [5]: housing df null = housing df.isnull().sum() / len(housing df) #Calculate % of null value
       housing_df null
Out[5]: MSSubClass MSZoning
                       0.000000
                      0.000000
                      0.177397
       LotFrontage
       LotArea
                      0.000000
       Street
                      0.000000
       MoSold
                      0.000000
       YrSold
                      0.000000
       SaleType
                      0.000000
       SaleCondition 0.000000
       SalePrice
                      0.000000
       Length: 80, dtype: float64
In [6]: missing_features = housing_df_null[housing df null > 0.40].index #Identify columns with
       missing features
       Index(['Alley', 'FireplaceQu', 'PoolQC', 'Fence', 'MiscFeature'], dtype='object')
Out[6]:
In [7]: #Drop the columns with over 40% missing values
```

| In [8]: | housing_df.head(5) |
|---------|--------------------|
|---------|--------------------|

housing df.drop(missing features, axis=1, inplace=True)

| Out[8]: | | MSSubClass | MSZoning | LotFrontage | LotArea | Street | LotShape | LandContour | Utilities | LotConfig | LandSlope |
|---------|---|------------|----------|-------------|---------|--------|----------|-------------|-----------|-----------|-----------|
| | 0 | 60 | RL | 65.0 | 8450 | Pave | Reg | Lvl | AllPub | Inside | Gtl |
| | 1 | 20 | RL | 80.0 | 9600 | Pave | Reg | Lvl | AllPub | FR2 | Gtl |
| | 2 | 60 | RL | 68.0 | 11250 | Pave | IR1 | Lvl | AllPub | Inside | Gtl |
| | 3 | 70 | RL | 60.0 | 9550 | Pave | IR1 | Lvl | AllPub | Corner | Gtl |
| | 4 | 60 | RL | 84.0 | 14260 | Pave | IR1 | Lvl | AllPub | FR2 | Gtl |

5 rows × 75 columns

```
In [9]: housing_df.shape #Display the number of rows and columns in the dataframe

Out[9]: (1460, 75)
```

3. For numerical columns, fill in any missing data with the median value.

```
In [10]: #Identify numeric columns in the dataframe
housing_df.select_dtypes(include=np.number).columns
Index(['MSSubClass', 'LotFrontage', 'LotArea', 'OverallQual', 'OverallCond',
```

```
'BsmtUnfSF', 'TotalBsmtSF', '1stFlrSF', '2ndFlrSF', 'LowQualFinSF',
               'GrLivArea', 'BsmtFullBath', 'BsmtHalfBath', 'FullBath', 'HalfBath',
               'BedroomAbvGr', 'KitchenAbvGr', 'TotRmsAbvGrd', 'Fireplaces',
               'GarageYrBlt', 'GarageCars', 'GarageArea', 'WoodDeckSF', 'OpenPorchSF',
               'EnclosedPorch', '3SsnPorch', 'ScreenPorch', 'PoolArea', 'MiscVal',
               'MoSold', 'YrSold', 'SalePrice'],
              dtype='object')
In [11]: #Look for the number of missing values in the numeric fields of the dataframe
        housing df.select dtypes([np.number]).isnull().sum()
       MSSubClass 0
Out[11]: LotFrontage
                       259
        LotArea
                        0
        OverallQual
OverallCond
        YearBuilt
        YearRemodAdd
        MasVnrArea
        BsmtFinSF1
                        0
        BsmtFinSF2
        BsmtUnfSF
                        0
        TotalBsmtSF
                        0
        1stFlrSF
        2ndFlrSF
       LowQualFinSF 0
        GrLivArea
       GrLivarea
BsmtFullBath
BsmtHalfBath
                        0
                        0
       FullBath
HalfBath
BedroomAbvGr
KitchenAbvGr
                        0
                        0
        TotRmsAbvGrd
                        0
        Fireplaces
        GarageYrBlt 81
GarageCars 0
        GarageArea
                        0
        WoodDeckSF
                        0
        OpenPorchSF
        EnclosedPorch
                        0
        3SsnPorch
        ScreenPorch
        PoolArea
                        0
        MiscVal
                        0
        MoSold
        YrSold
                         0
        SalePrice
        dtype: int64
In [12]: #Median before the update
        housing df.select dtypes([np.number]).median()
       MSSubClass 50.0
Out[12]: LotFrontage
                        69.0
        LotArea
                         9478.5
        OverallQual
                        6.0
        OverallCond
                           5.0
                        1973.0
        YearBuilt
        YearRemodAdd
MasVnrArea
                        1994.0
                         0.0
        BsmtFinSF1
                         383.5
        BsmtFinSF2
BsmtUnfSF
                          0.0
                          477.5
        TotalBsmtSF
                         991.5
```

'YearBuilt', 'YearRemodAdd', 'MasVnrArea', 'BsmtFinSF1', 'BsmtFinSF2',

Out[10]:

```
1stFlrSF
                1087.0
                0.0
2ndFlrSF
LowQualFinSF
                 0.0
               1464.0
GrLivArea
BsmtFullBath
                0.0
BsmtHalfBath
                 0.0
FullBath
                  2.0
HalfBath
                  0.0
BedroomAbvGr
                 3.0
KitchenAbvGr
                 1.0
TotRmsAbvGrd
                 6.0
Fireplaces
                  1.0
GarageYrBlt
              1980.0
GarageCars
                2.0
GarageArea
                480.0
WoodDeckSF
                 0.0
OpenPorchSF
                 25.0
EnclosedPorch
                 0.0
3SsnPorch
                  0.0
ScreenPorch
                 0.0
PoolArea
                 0.0
MiscVal
                  0.0
MoSold
                  6.0
               2008.0
YrSold
SalePrice
             163000.0
dtype: float64
```

In [13]: #Filling the missing/null values in the dataframe with the median
housing_df.fillna(housing_df.select_dtypes([np.number]).median().iloc[0],inplace=True)

In [14]: #Look for the number of missing values in the numeric fields of the dataframe after upda
housing_df.select_dtypes([np.number]).isnull().sum()

0 MSSubClass Out[14]: LotFrontage 0 LotArea 0 OverallQual OverallCond YearBuilt YearRemodAdd 0 MasVnrArea 0 BsmtFinSF1 BsmtFinSF2 0 BsmtUnfSF TotalBsmtSF 1stFlrSF 2ndFlrSF 0 LowQualFinSF GrLivArea 0 BsmtFullBath 0 BsmtHalfBath FullBath HalfBath BedroomAbvGr 0 KitchenAbvGr 0 TotRmsAbvGrd 0 Fireplaces 0 GarageYrBlt 0 GarageCars 0 GarageArea WoodDeckSF 0 OpenPorchSF 0

EnclosedPorch 0
3SsnPorch 0
ScreenPorch 0

```
SalePrice
        dtype: int64
In [15]: #Median after the update
        housing df.select dtypes([np.number]).median()
       MSSubClass 50.0
LotFrontage 63.0
Out[15]:
       LotFrontage
       LotArea
                        9478.5
       OverallQual
OverallCond
                        6.0
                           5.0
        YearBuilt
                        1973.0
       YearRemodAdd
                       1994.0
        MasVnrArea
                        0.0
        BsmtFinSF1
                         383.5
        BsmtFinSF2
                         0.0
        BsmtUnfSF
                         477.5
       TotalBsmtSF
1stFlrSF
2ndFlrSF
                        991.5
                      1087.0
                        0.0
       LowQualFinSF
GrLivArea
                        1464.0
                        0.0
        BsmtFullBath
        BsmtHalfBath
                           0.0
        FullBath
                           2.0
       HalfBath
                          0.0
        BedroomAbvGr
                          3.0
       KitchenAbvGr
TotRmsAbvGrd
                           1.0
                        6.0
       Fireplaces
                           1.0
                        1977.0
       GarageYrBlt
       GarageCars
GarageArea
WoodDeckSF
                        2.0
                         480.0
                         0.0
       OpenPorchSF 25.0
EnclosedPorch 0.0
        3SsnPorch
                           0.0
        ScreenPorch
                          0.0
                           0.0
        PoolArea
       MiscVal
                           0.0
       MoSold
                           6.0
                        2008.0
        YrSold
        SalePrice 163000.0
        dtype: float64
```

4. For categorical columns, fill in any missing data with the most common value (mode).

In [16]: #Identify categorical columns and their most common values
housing_df.select_dtypes([object]).mode()

| Out[16]: | | MSZoning | Street LotShape | | LandContour | Utilities | LotConfig | LandSlope | Neighborhood | Condition1 | Condit |
|----------|---|----------|-----------------|-----|-------------|-----------|-----------|-----------|--------------|------------|--------|
| | 0 | RL | Pave | Reg | Lvl | AllPub | Inside | Gtl | NAmes | Norm | 1 |

1 rows × 38 columns

PoolArea MiscVal MoSold YrSold

0

In [17]: #Replace missing values in categorical columns with their most common values housing df.fillna(housing df.select dtypes([object]).mode().iloc[0],inplace=True)

housing_df.head(5)

| Out[17]: | | MSSubClass | MSZoning | LotFrontage | LotArea | Street | LotShape | LandContour | Utilities | LotConfig | LandSlope |
|----------|---|------------|----------|-------------|---------|--------|----------|-------------|-----------|-----------|-----------|
| | 0 | 60 | RL | 65.0 | 8450 | Pave | Reg | Lvl | AllPub | Inside | Gtl |
| | 1 | 20 | RL | 80.0 | 9600 | Pave | Reg | Lvl | AllPub | FR2 | Gtl |
| | 2 | 60 | RL | 68.0 | 11250 | Pave | IR1 | Lvl | AllPub | Inside | Gtl |
| | 3 | 70 | RL | 60.0 | 9550 | Pave | IR1 | Lvl | AllPub | Corner | Gtl |
| | 4 | 60 | RL | 84.0 | 14260 | Pave | IR1 | Lvl | AllPub | FR2 | Gtl |

5 rows × 75 columns

```
housing df.select dtypes([object]).isnull().sum()
In [18]:
        MSZoning
Out[18]:
        Street
                        0
        LotShape
        LandContour
                        0
        Utilities
        LotConfig
                        0
        LandSlope
        Neighborhood
                        0
        Condition1
                        0
        Condition2
                        0
        BldgType
                        0
        HouseStyle
                        0
        RoofStyle
                        0
        RoofMatl
        Exterior1st
                        0
        Exterior2nd
                        0
                        0
        MasVnrType
        ExterQual
        ExterCond
                        0
        Foundation
                        0
        BsmtQual
        BsmtCond
                       0
        BsmtExposure
                        0
        BsmtFinType1
                        0
        BsmtFinType2
        Heating
                        0
        HeatingQC
        CentralAir
                        0
        Electrical
        KitchenQual
                        0
        Functional
                        0
                        0
        GarageType
        GarageFinish
                       0
        GarageQual
                        0
        GarageCond
                        0
        PavedDrive
                        0
                        0
        SaleType
        SaleCondition
        dtype: int64
```

5. Convert the categorical columns to dummy variables.

In [19]: housing_dummy_df = pd.get_dummies(housing_df, columns = housing_df.select_dtypes([object housing_dummy_df.head(5)

Out[19]: MSSubClass LotFrontage LotArea OverallQual OverallCond YearBuilt YearRemodAdd MasVnrArea BsmtFin

| 0 | 60 | 65.0 | 8450 | 7 | 5 | 2003 | 2003 | 196.0 | |
|---|----|------|-------|---|---|------|------|-------|--|
| 1 | 20 | 80.0 | 9600 | 6 | 8 | 1976 | 1976 | 0.0 | |
| 2 | 60 | 68.0 | 11250 | 7 | 5 | 2001 | 2002 | 162.0 | |
| 3 | 70 | 60.0 | 9550 | 7 | 5 | 1915 | 1970 | 0.0 | |
| 4 | 60 | 84.0 | 14260 | 8 | 5 | 2000 | 2000 | 350.0 | |

5 rows × 282 columns

6. Split the data into a training and test set, where the SalePrice column is the target.

```
In [20]: x = housing_dummy_df.loc[:,housing_dummy_df.columns != 'SalePrice']
#get the target
y = housing_dummy_df['SalePrice']

#split the data into training and test sets (80% Training/20% Test)
x_train, x_test, y_train, y_test = train_test_split(x, y, test_size = 0.2, random_state=

In [21]: x_train.shape, x_test.shape, y_train.shape, y_test.shape

Out[21]: ((1168, 281), (292, 281), (1168,), (292,))
```

7. Run a linear regression and report the R2-value and RMSE on the test set.

Coefficient of Determination (R2): 0.8709058563473847

8. Fit and transform the training features with a PCA so that 90% of the variance is retained (see section 9.1 in the Machine Learning with Python Cookbook).

```
In [25]: # Load the data
# Standardize the feature matrix
standard_scalar = StandardScaler()
features = standard_scalar.fit_transform(x_train)
# Create a PCA that will retain 90% of variance
pca = PCA(n_components=0.9, whiten=True)
# Conduct PCA
features_pca = pca.fit_transform(scale(features))
```

9. How many features are in the PCA-transformed matrix?

```
In [26]: print("Original number of features:", features.shape[1])
    print("Reduced number of features:", features_pca.shape[1])

Original number of features: 281
Reduced number of features: 139
```

10. Transform but DO NOT fit the test features with the same PCA.

```
In [27]: test_features = standard_scalar.transform(x test)
        test features
        array([[ 0.07765223, 0.56347098, 0.19172366, ..., -0.12153092,
Out[27]:
                 0.46955369, -0.30599503],
               [0.4342622, -0.27716525, -0.21701974, ..., -0.12153092,
                 0.46955369, -0.30599503],
               [-0.8733077, -0.69748336, -0.07327578, ..., -0.12153092,
                 0.46955369, -0.30599503],
                . . . ,
               [-0.63556772, -0.27716525, 0.02609901, ..., -0.12153092,
                 0.46955369, -0.305995031,
               [-0.63556772, 0.77363004, 0.0083716, ..., -0.12153092,
                -2.12968191, -0.30599503],
                [0.07765223, 0.77363004, 0.02609901, ..., -0.12153092,
                -2.12968191, 3.26802693]])
In [28]: test_features_pca = pca.transform(test features) #Transfor with the same PCA.
         test features pca.shape
        (292, 139)
Out[28]:
```

11. Repeat step 7 with your PCA transformed data.

```
In [31]: print("Root Mean Squared Error (RMSE):", sqrt(mean_squared_error(y_test, pca_predictions
    print("Coefficient of Determination (R2):", r2_score(y_test, pca_predictions))
```

Root Mean Squared Error (RMSE): 32908.91879995908 Coefficient of Determination (R2): 0.8481484106916732

12. Take your original training features (from step 6) and apply a minmax scaler to them.

```
In [32]: #Create scaler
    minmax_scale = preprocessing.MinMaxScaler(feature_range=(0, 1))
In [33]: # Scale feature
    scaled feature = minmax scale.fit transform(x train)
```

```
scaled feature
       array([[0.41176471, 0.15753425, 0.03494823, ..., 0.
                                                        , 1.
Out[33]:
                     , 0.13356164, 0.04440394, ..., 0.
                                                        , 1.
                     ],
                    , 0.15068493, 0.03490149, ..., 0.
                                                      , 0.
             1.
                     ],
             [0.29411765, 0.13356164, 0.02609082, ..., 0.
             0. ],
             [0.82352941, 0. , 0.00177616, ..., 0.
                                                        , 1.
             0. ],
             [0.05882353, 0.3390411 , 0.07805744, ..., 0.
                                                        , 1.
             0. 11)
```

13. Find the min-max scaled features in your training set that have a variance above 0.1 (see Section 10.1 in the Machine Learning with Python Cookbook).

```
In [34]: # Create thresholder
               thresholder = VarianceThreshold(threshold=.1)
In [35]: # Create high variance feature matrix
               features high variance = thresholder.fit transform(scaled feature)
In [36]: # View high variance feature matrix
               features high variance[0:3]
              array([[0.88333333, 0.5
                                                       , 1. , 0. , 0.
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                           0.
                                                           , 0.
                                                                                                        , 0. 11)
```

14. Transform but DO NOT fit the test features with the same steps applied in steps 11 and 12.

```
# Scale feature
In [37]:
         scaled test feature = minmax scale.transform(x test)
         scaled test feature
        array([[0.23529412, 0.20205479, 0.05204609, ..., 0.
Out[37]:
                [0.32352941, 0.13356164, 0.0331861 , ..., 0.
                                                                    , 1.
                          , 0.09931507, 0.03981864, ..., 0.
                0.
                          ],
                [0.05882353, 0.13356164, 0.04440394, ..., 0.
                                                                    , 1.
                [0.05882353, 0.21917808, 0.04358597, ..., 0.
                                                                    , 0.
                0. ],
                [0.23529412, 0.21917808, 0.04440394, ..., 0.
                                                                    , 0.
                       ]])
In [38]: # Create high variance feature matrix
         test features high variance = thresholder.transform(scaled test feature)
         # View high variance feature matrix
         test features high variance[0:3]
                                   , 1.
                                               , 0.
        array([[0.85 , 0.5
                                                            , 0.
Out[38]:
                         , 0.
                                     , 1.
                                                 , 0.
                                                              , 1.
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```

15. Repeat step 7 with the high variance data.

```
In [39]: #lr_model = LinearRegression()
# Train the model
lr_model.fit(features_high_variance,y_train)
# Use model to make predictions on test set
high_variance_predictions = lr_model.predict(test_features_high_variance)

print("Root Mean Squared Error (RMSE):", sqrt(mean_squared_error(y_test, high_variance_p
print("Coefficient of Determination (R2):", r2_score(y_test, high_variance_predictions))
```

Root Mean Squared Error (RMSE): 55034.32256655691 Coefficient of Determination (R2): 0.5753223910429259

16. Summarize your findings.

Findings: In linear regression, the R2 value is between 0 and 1 and is a measure of how well the regression predictions approximate real values (goodness of fit of a model). Among the models run above, I see Linear Regression Model gives a better result for R2 compared to the other 2 model trainings.

Linear Regression Model

Root Mean Squared Error (RMSE): 30342.908937203494

Coefficient of Determination (R2): 0.8709058563473847

PCA Transformed Model

Root Mean Squared Error (RMSE): 32908.91879995908

Coefficient of Determination (R2): 0.8481484106916732

Min-Max Transformed Model

Root Mean Squared Error (RMSE): 55034.32256655691

Coefficient of Determination (R2): 0.5753223910429259

Part 2: Categorical Feature Selection

1. Import the data as a data frame and ensure it is loaded correctly.

```
In [40]: mushroom_df = pd.read_csv("mushrooms.csv")
    print(mushroom_df.shape)
    mushroom_df.head(5)
```

(8124, 23)

Out[40]:

| | class | cap- shape | cap- surface | cap- color | bruises | odor | gill- attachment | | | gill- color | ••• | stalk- surface- below- ring | stalk- color- above- ring | stalk- color- below- ring | |
|---|-------|---------------|-----------------|---------------|---------|------|---------------------|---|---|----------------|-----|--------------------------------------|------------------------------------|------------------------------------|--|
| 0 | р | х | S | n | t | р | f | С | n | k | | S | W | W | |
| 1 | е | х | S | у | t | а | f | С | b | k | | S | W | W | |
| 2 | е | b | S | w | t | 1 | f | С | b | n | | S | W | W | |
| 3 | р | х | у | W | t | р | f | С | n | n | | S | W | W | |
| 4 | е | х | S | g | f | n | f | W | b | k | | S | W | W | |

5 rows × 23 columns

2. Convert the categorical features (all of them) to dummy variables.

```
In [41]: mushroom_dummy_df = pd.get_dummies(mushroom_df, columns = mushroom_df.select_dtypes([obj
mushroom_dummy_df.head(5)
```

|]: | | class_e | class_p | cap- shape_b | cap- shape_c | | • | • | • | cap- surface_f | - | ••• | population_s |
|----|---|---------|---------|-----------------|-----------------|---|---|---|---|-------------------|---|-----|--------------|
| | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | | 1 |
| | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | | 0 |
| | 2 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | | 0 |
| | 3 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | | 1 |
| | 4 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | | 0 |

5 rows × 119 columns

Out[41]

3. Split the data into a training and test set.

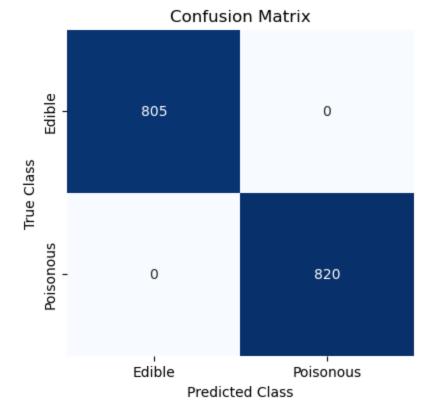
```
In [42]: x = mushroom_dummy_df.drop(['class_e','class_p'], axis = 1)
y = mushroom_dummy_df['class_e']

#split the data into training and test sets (80% Training/20% Test)
x_train, x_test, y_train, y_test = train_test_split(x, y, test_size = 0.2, random_state=
```

4. Fit a decision tree classifier on the training set.

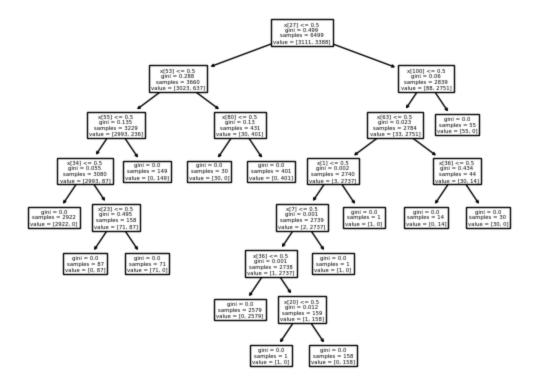
```
In [43]: # Create decision tree classifier object
    decisiontree = tree.DecisionTreeClassifier(random_state=1)
    dt_model = decisiontree.fit(x_train, y_train)
    y_pred = dt_model.predict(x_test)
    y_pred
Out[43]: array([1, 0, 0, ..., 0, 1, 1], dtype=uint8)
```

5. Report the accuracy and create a confusion matrix for the model prediction on the test set.

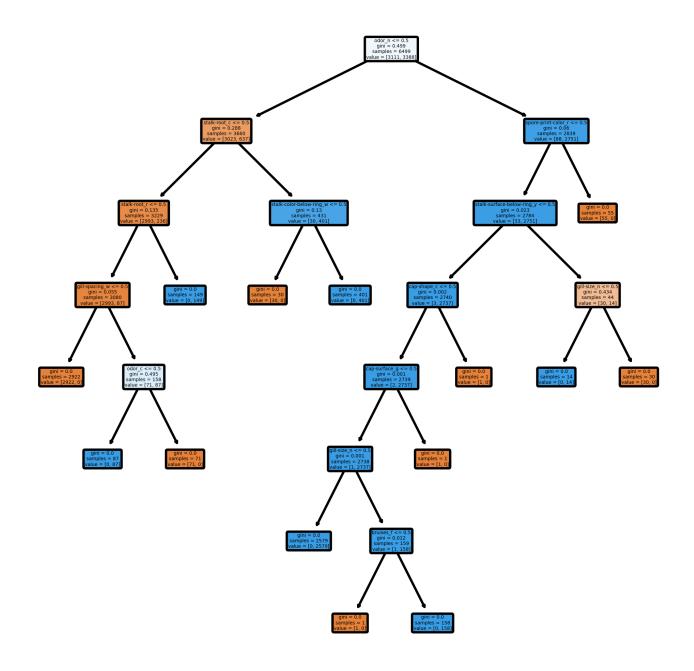


6. Create a visualization of the decision tree.

```
tree.plot tree(decisiontree)
In [46]:
                 [\text{Text}(0.5625, 0.9375, 'x[27] \le 0.5 \text{ ngini} = 0.499 \text{ nsamples} = 6499 \text{ nvalue} = [3111, 338]
Out[46]:
                81'),
                  7]'),
                  Text(0.1875, 0.6875, 'x[55] \le 0.5 \le 0.135 \le 3229 \le [2993, 23]
                  Text(0.125, 0.5625, 'x[34] \le 0.5 \neq 0.055 = 0.055 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0.080 = 0
                  Text(0.0625, 0.4375, 'gini = 0.0\nsamples = 2922\nvalue = [2922, 0]'),
                  Text(0.1875, 0.4375, 'x[23] \le 0.5 = 0.495 = 158 = [71, 87]'),
                  Text(0.125, 0.3125, 'gini = 0.0 \times 87 = 87 = [0, 87]'),
                  Text(0.25, 0.3125, 'gini = 0.0\nsamples = 71\nvalue = [71, 0]'),
                  Text(0.25, 0.5625, 'gini = 0.0\nsamples = 149\nvalue = [0, 149]'),
                  Text(0.4375, 0.6875, 'x[80] \le 0.5 \neq 0.13 = 0.13 = 431 \neq 0.13 = [30, 401]'),
                  Text(0.375, 0.5625, 'qini = 0.0\nsamples = 30\nvalue = [30, 0]'),
                  Text(0.5, 0.5625, 'gini = 0.0\nsamples = 401\nvalue = [0, 401]'),
                  Text(0.8125, 0.8125, 'x[100] \le 0.5 = 0.06 = 2839 = [88, 2751]'),
                  Text(0.75, 0.6875, 'x[63] \le 0.5 \le 0.023 \le 2784 \le [33, 2751]'),
                  Text(0.625, 0.5625, 'x[1] \leq 0.5\ngini = 0.002\nsamples = 2740\nvalue = [3, 2737]'),
                  Text(0.5625, 0.4375, 'x[7] \le 0.5 = 0.001 = 0.001 = 2739 = [2, 2737]')
                  Text(0.5, 0.3125, 'x[36] \le 0.5 / gini = 0.001 / samples = 2738 / value = [1, 2737]'),
                  Text(0.4375, 0.1875, 'gini = 0.0\nsamples = 2579\nvalue = [0, 2579]'),
                  Text(0.5625, 0.1875, 'x[20] <= 0.5 \cdot ngini = 0.012 \cdot nsamples = 159 \cdot nvalue = [1, 158]'),
                  Text(0.5, 0.0625, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
                  Text(0.625, 0.0625, 'gini = 0.0\nsamples = 158\nvalue = [0, 158]'),
                  Text(0.625, 0.3125, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
                  Text(0.6875, 0.4375, 'gini = 0.0\nsamples = 1\nvalue = [1, 0]'),
                  Text(0.875, 0.5625, 'x[36] \le 0.5 \le 0.434 \le 4 \le 4 \le [30, 14]'),
                  Text(0.8125, 0.4375, 'gini = 0.0\nsamples = 14\nvalue = [0, 14]'),
                  Text(0.9375, 0.4375, 'gini = 0.0\nsamples = 30\nvalue = [30, 0]'),
                  Text(0.875, 0.6875, 'qini = 0.0\nsamples = 55\nvalue = [55, 0]')]
```



```
In [47]: fig, axes = plt.subplots(nrows = 1,ncols = 1,figsize = (5,5), dpi=500)
    tree.plot_tree(decisiontree, feature_names=x.columns,filled=True, rounded=True);
    fig.savefig('imagename.png')
```



7. Use a χ 2-statistic selector to pick the five best features for this data (see section 10.4 of the Machine Learning with Python Cookbook).

```
# Convert to categorical data by converting data to integers
In [48]:
         features = x train.astype(int)
         # Select five features with highest chi-squared statistics
         chi2 selector = SelectKBest(chi2, k=5)
         features kbest = chi2 selector.fit transform(features, y train)
         features kbest
        array([[0, 1, 0, 0, 0],
Out[48]:
                [0, 1, 0, 0, 0],
                [0, 0, 1, 1, 1],
                . . . ,
                [1, 0, 0, 1, 1],
                [0, 0, 0, 0, 0],
                [1, 0, 0, 0, 0]])
In [49]: # Show results
```

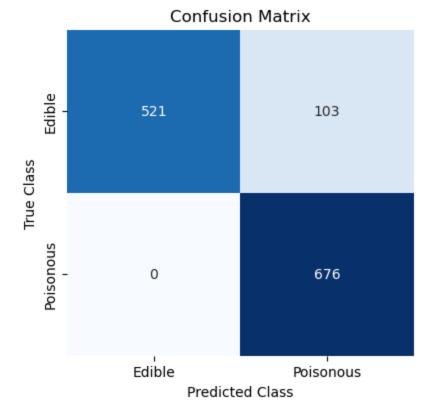
```
print("Original number of features:", features.shape[1])
print("Reduced number of features:", features_kbest.shape[1])
Original number of features: 117
Reduced number of features: 5
```

8. Which five features were selected in step 7? Hint: Use the get_support function.

```
In [50]:
         # Get columns to keep and create new dataframe with those only
          cols = chi2 selector.get support(indices = True)
          features df = features.iloc[:,cols]
          print(features df.shape)
          features df.head(5)
          (6499, 5)
Out[50]:
               odor_f odor_n gill-color_b stalk-surface-above-ring_k stalk-surface-below-ring_k
                                                                                      0
          1610
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          2000
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                                                              0
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```

9. Repeat steps 4 and 5 with the five best features selected in step 7.

```
In [51]: x_best_5_train, x_best_5_test, y_best_5_train, y_best 5 test = train test split(features)
        decisiontree = tree.DecisionTreeClassifier(random state=1)
In [52]:
         dt model = decisiontree.fit(x best 5 train, y best 5 train)
         y best 5 pred = dt model.predict(x best 5 test)
         y best 5 pred
        array([0, 1, 1, ..., 1, 1], dtype=uint8)
Out[52]:
In [53]: score = round(accuracy_score(y_best_5 test, y best 5 pred)*100,2)
         print("Test Accuracy: {}%".format(score))
        Test Accuracy: 92.08%
         # Create confusion matrix
In [54]:
         best matrix = confusion matrix(y best 5 test, y best 5 pred)
        best matrix
        array([[521, 103],
Out[54]:
               [ 0, 676]], dtype=int64)
        x axis labels = ["Edible", "Poisonous"]
In [55]:
         y axis labels = ["Edible", "Poisonous"]
         #HeatMap
         f, ax = plt.subplots(figsize = (4,4))
         sns.heatmap(best matrix, annot=True, cbar=None, cmap="Blues",fmt = ".0f", xticklabels=x
         plt.title("Confusion Matrix"), plt.tight layout()
         plt.ylabel("True Class"), plt.xlabel("Predicted Class")
         plt.show()
```



10. Summarize your findings.

Findings: With all the features in the first Decision Tree Classifier there was 100% accuracy, and after reducing to 5 best features using X2 it went down to 92.08%. This revised accuracy is still high with only 5 features instead of 117. We get a relatively good accuracy percentage with 95% reduction in features.