```
In [34]: #Import necessary libraries
         import pandas as pd
         import numpy as np
         import plotly.express as px
         import matplotlib.pyplot as plt
         import seaborn as sns
         import opendatasets as od
         from sklearn.preprocessing import StandardScaler
         from sklearn.datasets import make blobs
         from sklearn.cluster import KMeans
         from sklearn.metrics import silhouette samples, silhouette score
         import matplotlib.cm as cm
         # import warnings filter
         import warnings #import simplefilter
         # ignore all future warnings
         from sklearn.decomposition import PCA
In [3]: #Download the ALS patients dataset from bellevue.edu
         od.download("https://content.bellevue.edu/cst/dsc/630/als data.csv")
```

Using downloaded and verified file: .\als data.csv

```
In [4]: #Read csv into python dataframe
        als df = pd.read csv("als data.csv")
        als df.head(5)
        print(als df.shape)
        (2223, 101)
```

1. Remove any data that is not relevant to the patient's ALS condition.

```
In [5]: #Dropping the columns Subject ID and ID are irrelevant to the patients condition
        als df = als df.drop(['ID', 'SubjectID'], axis=1)
        als df.shape
        (2223, 99)
Out[5]:
```

2. Apply a standard scalar to the data.

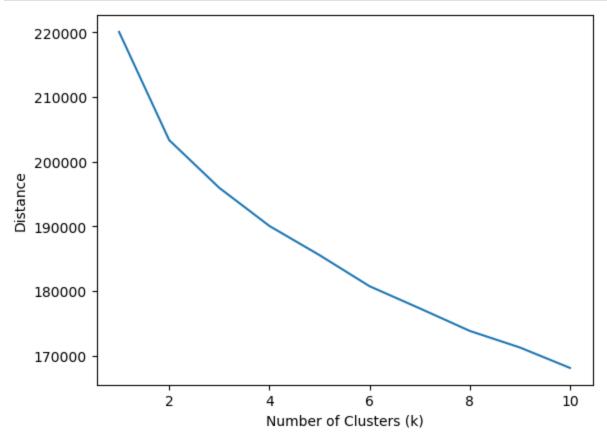
```
In [6]: X = StandardScaler().fit transform(als df.values)
        X.shape
        (2223, 99)
Out[6]:
```

3. Create a plot of the cluster silhouette score versus the number of clusters in a K-means cluster.

Elbow Method

```
In [27]: range_n_clusters = [1, 2, 3, 4, 5, 6]
         avg distance=[]
         for n clusters in range n clusters:
             clusterer = KMeans(n clusters=n clusters, random state=42).fit(X)
             avg distance.append(clusterer.inertia )
         style.use("fivethirtyeight")
```

```
plt.plot(range_n_clusters, avg_distance)
plt.xlabel("Number of Clusters (k)")
plt.ylabel("Distance")
plt.show()
```



There is a fall in the slope at 2 making this an optimal point of k where an elbow occurs.

Silhouette Method

```
range n clusters = [2, 3, 4, 5, 6]
In [29]:
         silhouette avg n clusters = []
         for n clusters in range n clusters:
             # Create a subplot with 1 row and 2 columns
             fig, (ax1, ax2) = plt.subplots(1, 2)
             fig.set size inches(18, 7)
             # The 1st subplot is the silhouette plot
             \# The silhouette coefficient can range from -1, 1 but in this example all
             # lie within [-0.1, 1]
             ax1.set xlim([-0.1, 1])
             \# The (n_clusters+1)*10 is for inserting blank space between silhouette
             # plots of individual clusters, to demarcate them clearly.
             ax1.set ylim([0, len(X) + (n clusters + 1) * 10])
             # Initialize the clusterer with n clusters value and a random generator
             # seed of 10 for reproducibility.
             clusterer = KMeans(n clusters=n clusters, random state=42)
             cluster labels = clusterer.fit predict(X)
             # The silhouette score gives the average value for all the samples.
             # This gives a perspective into the density and separation of the formed
             # clusters
             silhouette avg = silhouette score(X, cluster labels)
             print("For n clusters =", n clusters,
                   "The average silhouette score is :", silhouette avg)
```

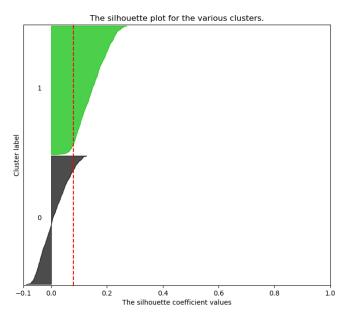
```
silhouette_avg_n_clusters.append(silhouette avg)
    # Compute the silhouette scores for each sample
    sample silhouette values = silhouette samples(X, cluster labels)
    y lower = 10
    for i in range(n clusters):
        # Aggregate the silhouette scores for samples belonging to
        # cluster i, and sort them
        ith cluster silhouette values = \
            sample silhouette values[cluster labels == i]
        ith cluster silhouette values.sort()
        size cluster i = ith cluster silhouette values.shape[0]
        y upper = y lower + size cluster i
        color = cm.nipy spectral(float(i) / n clusters)
        ax1.fill betweenx(np.arange(y lower, y upper),
                          0, ith cluster silhouette values,
                          facecolor=color, edgecolor=color, alpha=0.7)
        # Label the silhouette plots with their cluster numbers at the middle
        ax1.text(-0.05, y lower + 0.5 * size cluster i, str(i))
        # Compute the new y lower for next plot
        y lower = y upper + 10 # 10 for the 0 samples
    ax1.set title("The silhouette plot for the various clusters.")
    ax1.set xlabel("The silhouette coefficient values")
    ax1.set ylabel("Cluster label")
    # The vertical line for average silhouette score of all the values
    ax1.axvline(x=silhouette_avg, color="red", linestyle="--")
    ax1.set yticks([]) # Clear the yaxis labels / ticks
    ax1.set xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])
    # 2nd Plot showing the actual clusters formed
    colors = cm.nipy spectral(cluster labels.astype(float) / n clusters)
    ax2.scatter(X[:, 0], X[:, 1], marker='.', s=30, lw=0, alpha=0.7,
                c=colors, edgecolor='k')
    # Labeling the clusters
    centers = clusterer.cluster centers
    # Draw white circles at cluster centers
    ax2.scatter(centers[:, 0], centers[:, 1], marker='o',
                c="white", alpha=1, s=200, edgecolor='k')
    for i, c in enumerate(centers):
       ax2.scatter(c[0], c[1], marker='$%d$' % i, alpha=1,
                    s=50, edgecolor='k')
    ax2.set title("The visualization of the clustered data.")
    ax2.set xlabel("Feature space for the 1st feature")
    ax2.set ylabel("Feature space for the 2nd feature")
    plt.suptitle(("Silhouette analysis for KMeans clustering on sample data "
                  "with n clusters = %d" % n clusters),
                 fontsize=14 )
plt.show()
#style.use("fivethirtyeight")
plt.plot(range n clusters, silhouette avg n clusters)
```

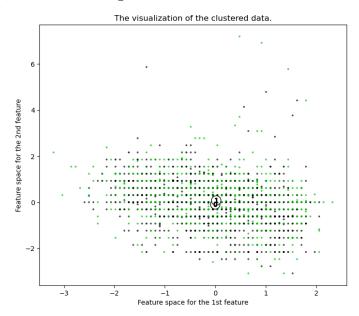
plt.xlabel("Number of Clusters (k)")

```
plt.ylabel("silhouette score")
plt.show()
```

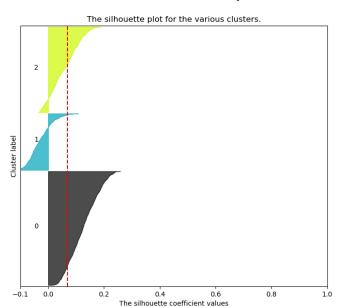
```
For n_clusters = 2 The average silhouette_score is : 0.07878005888570402
For n_clusters = 3 The average silhouette_score is : 0.0687707291658565
For n_clusters = 4 The average silhouette_score is : 0.06973816142698218
For n_clusters = 5 The average silhouette_score is : 0.05697679932842005
For n_clusters = 6 The average silhouette_score is : 0.06477886829610223
```

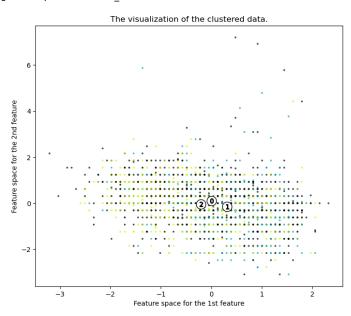
Silhouette analysis for KMeans clustering on sample data with $n_{clusters} = 2$

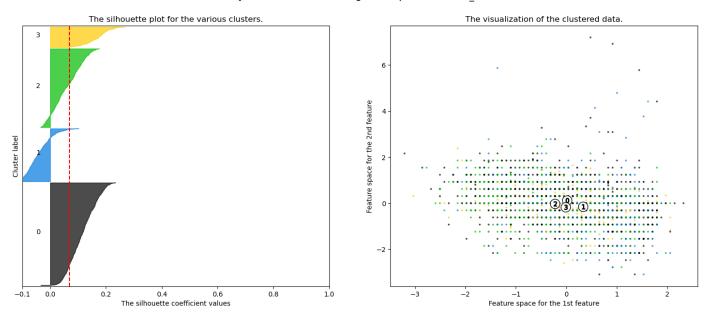




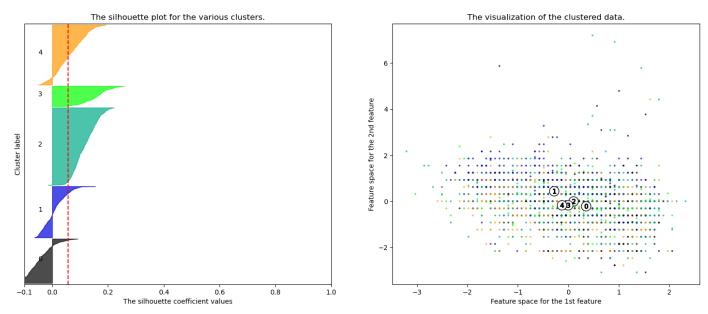
Silhouette analysis for KMeans clustering on sample data with n_clusters = 3



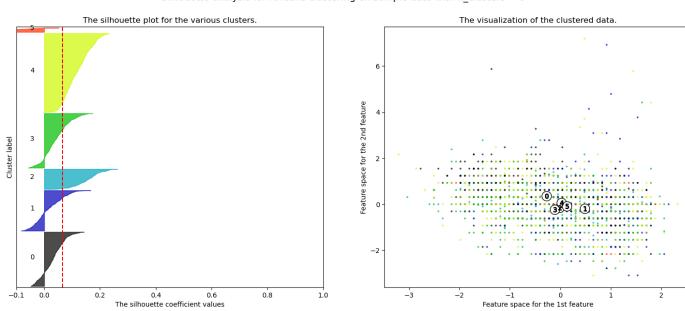


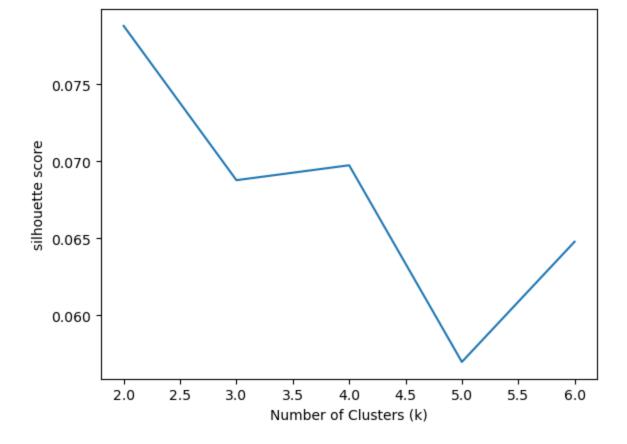


Silhouette analysis for KMeans clustering on sample data with $n_{clusters} = 5$



Silhouette analysis for KMeans clustering on sample data with $n_clusters = 6$





4. Use the plot created in (3) to choose an optimal number of clusters for K-means. Justify your choice.

Considering a good average silhouette score to be 0.6, we can see that all the clusters have an average or above average silhouette score (closer to 1), so none of the cluster values can be considered bad picks for the given dataset. However, plotting the average silhouette scores for each k shows that the best choice for k is 2 since it has the maximum score (0.07878005888570402). The same can be seen with the elbow method.

5. Fit a K-means model to the data with the optimal number of clusters chosen in part (4).

```
In [32]: ## Using cluster value as 2
kmeans = KMeans(n_clusters=2,random_state=42)
y_pred = clusterer.fit_predict(X)
In [66]: X.shape
Out[66]: (2223, 99)
```

6. Fit a PCA transformation with two features to the scaled data.

```
In [111... # PCA with 2 components
    pca = PCA(n_components=2)

# Fit the PCA
    als_pca = pca.fit_transform(X)

# Convert the array to a dataframe
    als_pca_df = pd.DataFrame(data=als_pca, columns = ['PC1', 'PC2'])
```

```
# Add the cluster label to the dataframe
als_pca_df['Cluster'] = y_pred
# View the dataframe
als_pca_df
```

Out[111]:

	PC1	PC2	Cluster
0	-1.426745	-2.319821	1
1	-1.440234	-4.871695	1
2	1.617854	-0.428724	3
3	-1.919993	2.095371	4
4	0.297709	0.166822	3
•••			
2218	-4.477580	1.200880	4
2219	-0.398958	-1.877658	1
2220	-0.432900	4.244527	0
2221	-0.330782	3.316474	0
2222	1.468011	0.582497	1

2223 rows × 3 columns

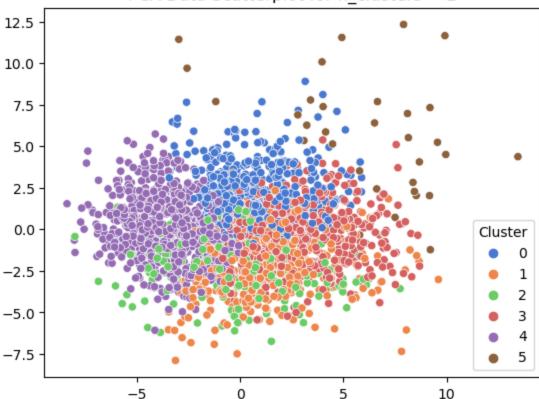
```
In [132... # PCA with 0.95 components - Preserving 95% variability
    pca95 = PCA(n_components=0.95)

# Fit the PCA
    als_pca95 = pca95.fit_transform(X)
```

7. Make a scatterplot of the PCA transformed data coloring each point by its cluster value.

```
In [138... sns.scatterplot(x=als_pca[:,0],y= als_pca[:,1], hue=als_pca_df['Cluster'], palette="mute
plt.title('PCA Data Scatterplot for n_clusters = 2')
plt.show()
```





We can see that the six classes are not distinct and separable. We can conclude that the compressed data representation is most likely not sufficient for a classification model. We can compare the variance in the overall dataset to what was captured from our two primary components using .explained_variance ratio.

8. Summarize your results and make a conclusion.

Explained Variance Ratio is a metric to evaluate the usefulness of principal components and to choose the required number of components in PCA model.

The first component captures about 11% of the variability in the dataset and the second component captures about 18% of the variability in the dataset.

```
In [139... # Show the variance between the 95 features within the PCA.
    explained_variance95 = pca95.explained_variance_ratio_
    #print(explained_variance95)

print(als_pca95.shape)
    print(np.cumsum(pca95.explained_variance_ratio_*100))
```

```
print ( "Components: ", pca95.n components , "\nExplained Variance Ratio: ",
       round(pca95.explained variance_ratio_.sum(),2), "\nExplained Variance Ratio Perce
       round((pca95.explained variance ratio .sum()*100),0), "%")
#This means the algorithm has found 51 principal components to preserve 95% of the varia
(2223, 51)
[11.33054801 17.77716422 23.99783515 28.68285436 33.01802793 36.97855333
 40.63106296 43.6899421 46.60948437 49.45114771 52.261072 54.91592997
 57.27689185 59.52139181 61.4972152 63.42645056 65.29367809 67.02418318
 68.72087263 70.39066976 71.90290606 73.34905753 74.75731891 76.10100861
 77.40957246 78.62924786 79.78411219 80.92651388 82.01868752 83.02175144
 83.95510689 84.85985614 85.69405746 86.45576388 87.20433762 87.92015811
 88.59692932 89.2091541 89.80772165 90.39619586 90.97393967 91.54459472
 92.03275947 92.47197562 92.88669521 93.29690325 93.67715102 94.04412358
 94.3943873 94.72853861 95.03388671]
Components: 51
Explained Variance Ratio: 0.95
Explained Variance Ratio Percentage: 95.0 %
```

We will need to choose the number of components to include in our model by adding the explained variance ratio of each component until we reach a total of around 0.8 or 80% to avoid overfitting. From the above we can see that we achieve 80% around 27. Which makes 27 the ideal number of components to include in our model.

```
In [149... # PCA with 27 components
         pca27 = PCA(n components=27)
         # Fit the PCA
         als pca27 = pca27.fit transform(X)
In [150... | # Show the variance between the 27 features within the PCA.
         explained variance27 = pca27.explained variance ratio
         #print(explained variance95)
         print(als pca27.shape)
         print(np.cumsum(pca27.explained variance ratio *100))
        print ( "Components: ", pca27.n components , "\nExplained Variance Ratio: ",
                round(pca27.explained variance ratio .sum(),2), "\nExplained Variance Ratio Perce
                round((pca27.explained variance ratio .sum()*100),0), "%")
         #This means the algorithm has found 51 principal components to preserve 95% of the varia
         (2223, 27)
         [11.33054801 17.77716417 23.99783503 28.68285329 33.01802681 36.97855193
          40.63105519 43.68991785 46.60945789 49.45111909 52.26104073 54.91589297
         57.27675844 59.5211446 61.49643199 63.4256169 65.29250974 67.0214756
          68.71804571 70.38458662 71.8961343 73.34045553 74.74786173 76.08894146
          77.39327485 78.61151636 79.7611911 ]
        Components: 27
        Explained Variance Ratio: 0.8
        Explained Variance Ratio Percentage: 80.0 %
```

References

- 1. Sklearn.preprocessing.StandardScaler. scikit. (n.d.). https://scikit-learn.org/stable/modules/generated/sklearn.preprocessing.StandardScaler.html
- 2. Pramoditha, R. (2023, February 2). Principal Component Analysis (PCA) with Scikit-Learn. Medium. https://medium.com/data-science-365/principal-component-analysis-pca-with-scikit-learn-