

1.11.15

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Question:

Write the direction ratios of the vector $3\mathbf{a} + 2\mathbf{b}$ where $\mathbf{a} = \vec{i} + \vec{j} - 2\vec{k}$ and $\mathbf{b} = 2\vec{i} - 4\vec{j} + 5\vec{k}$.

Solution:

The given vectors \mathbf{a} and \mathbf{b} are

$$\mathbf{a} = \begin{pmatrix} 1 \\ 1 \\ -2 \end{pmatrix} \quad (0.1)$$

$$\mathbf{b} = \begin{pmatrix} 2 \\ -4 \\ 5 \end{pmatrix} \quad (0.2)$$

The direction ratios of the vector $3\mathbf{a} + 2\mathbf{b}$ are

$$3\mathbf{a} + 2\mathbf{b} = \begin{pmatrix} a & b \end{pmatrix} \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad (0.3)$$

$$3\mathbf{a} + 2\mathbf{b} = \begin{pmatrix} 1 & 2 \\ 1 & -4 \\ -2 & 5 \end{pmatrix} \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad (0.4)$$

$$3\mathbf{a} + 2\mathbf{b} = \begin{pmatrix} 3(1) + 2(2) \\ 3(1) + 2(-4) \\ 3(-2) + 2(5) \end{pmatrix} \quad (0.5)$$

$$3\mathbf{a} + 2\mathbf{b} = \begin{pmatrix} 7 \\ -5 \\ 4 \end{pmatrix} \quad (0.6)$$

3D Vector Visualization: $3a + 2b$ Direction Ratios: (7.0, -5.0, 4.0)

