

Problem 1.4.25

EE25BTECH11009 – Anshu Kumar Ram

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Question

Find the position vector of a point R which divides the line joining two points P and Q whose position vectors are $2\vec{a} + \vec{b}$ and $\vec{a} - 3\vec{b}$ externally in the ratio $1 : 2$.

Solution Step 1

Step 1: Represent points in coordinates

$$\vec{P} = 2\vec{a} + \vec{b} = \begin{pmatrix} 2 \\ 1 \end{pmatrix} \quad (1)$$

$$\vec{Q} = \vec{a} - 3\vec{b} = \begin{pmatrix} 1 \\ -3 \end{pmatrix} \quad (2)$$

Step 2: Apply section formula (external division)

$$\vec{R} = \frac{1 \cdot \vec{Q} - 2 \cdot \vec{P}}{1 - 2} \quad (3)$$

$$= \frac{1}{-1} \left(\begin{pmatrix} 1 \\ -3 \end{pmatrix} - 2 \begin{pmatrix} 2 \\ 1 \end{pmatrix} \right) \quad (4)$$

$$= - \begin{pmatrix} -3 \\ -5 \end{pmatrix} \quad (5)$$

$$= \begin{pmatrix} 3 \\ 5 \end{pmatrix} \quad (6)$$

$$\vec{R} = 3\vec{a} + 5\vec{b} \quad (7)$$

Graphical Representation

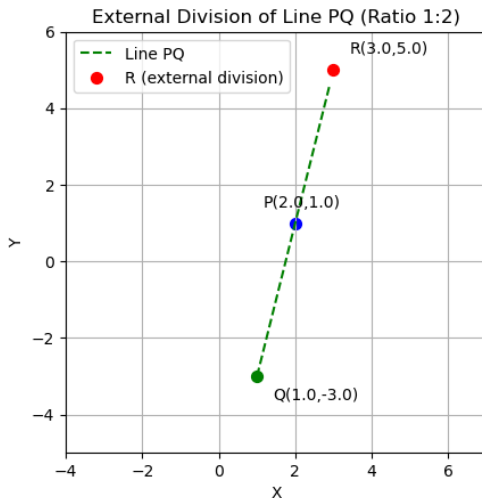


Figure: Graph for Question 2

C Code: section() Function

```
1 void section(double* P, double* Q, double* R, int m) {  
2     for (int i = 0; i < m; i++) {  
3         R[i] = (Q[i] - 2 * P[i]) / (1 - 2);  
4     }  
5 }
```

C Code: line_gen() Function

```
1 void line_gen(double* X, double* Y, const double* A, const double* B, int n, int m) {
2     double temp[2];
3     for (int i = 0; i < 2; i++) {
4         temp[i] = (B[i] - A[i]) / (double)n;
5     }
6     for (int i = 0; i <= n; i++) {
7         X[i] = A[0] + temp[0] * i;
8         Y[i] = A[1] + temp[1] * i;
9     }
10 }
```

Python + C: Load Library

```
1 import ctypes
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 handc = ctypes.CDLL("./func.so")
6
7 # section function
8 handc.section.argtypes = [
9     ctypes.POINTER(ctypes.c_double),
10    ctypes.POINTER(ctypes.c_double),
11    ctypes.POINTER(ctypes.c_double),
12    ctypes.c_int
13 ]
14 handc.section.restype = None
15
16 # line_gen function
17 handc.line_gen.argtypes = [
18     ctypes.POINTER(ctypes.c_double),
19     ctypes.POINTER(ctypes.c_double),
20     ctypes.POINTER(ctypes.c_double),
21     ctypes.POINTER(ctypes.c_double),
22     ctypes.c_int,
23     ctypes.c_int
24 ]
25 handc.line_gen.restype = None
```


Python + C: Compute & Plot

```
1 m = 2
2 a = np.array([1,0], dtype=np.float64)
3 b = np.array([0,1], dtype=np.float64)
4 P = 2*a + b
5 Q = a - 3*b
6 R = np.zeros(m, dtype=np.float64)
7
8 handc.section(P.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
9               Q.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
10              R.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
11              m)
12
13 n = 20
14 X_1 = np.zeros(n, dtype=np.float64)
15 Y_1 = np.zeros(n, dtype=np.float64)
16 handc.line_gen(X_1.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
17               Y_1.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
18               Q.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
19               R.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
20               n, m)
21
22 plt.plot(X_1, Y_1, "g--", label="Line PQ")
23 plt.scatter(P[0], P[1], color="blue", s=50)
24 plt.scatter(Q[0], Q[1], color="green", s=50)
25 plt.scatter(R[0], R[1], color="red", s=50, label="R")
26 plt.show()
```

Pure Python: Functions & Setup

```
1 import sys
2 sys.path.insert(0, '/home/anshu-ram/matgeo/codes/CoordGeo')
3 import numpy as np
4 import matplotlib.pyplot as plt
5
6 from line.funcs import *
7 from triangle.funcs import *
8 from conics.funcs import circ_gen
9
10 def section_point(P, Q, m, n, external=True):
11     if external:
12         return (m*Q - n*P)/(m-n)
13     else:
14         return (m*Q + n*P)/(m+n)
```

Pure Python: Compute & Plot

```
1 a = np.array([1,0]).reshape(-1,1)
2 b = np.array([0,1]).reshape(-1,1)
3 P = 2*a + b
4 Q = a - 3*b
5 R = section_point(P, Q, 1, 2, external=True)
6
7 x_PQ = line_gen_num(P, Q, 20)
8 x_PR = line_gen_num(P, R, 20)
9 x_QR = line_gen_num(Q, R, 20)
10
11 plt.plot(x_PQ[0,:], x_PQ[1,:], "g--", label="Line PQ")
12 plt.plot(x_PR[0,:], x_PR[1,:], "r--", label="Line PR")
13 plt.plot(x_QR[0,:], x_QR[1,:], "b--", label="Line QR")
14 tri_coords = np.hstack((P,Q,R))
15 plt.scatter(tri_coords[0,:], tri_coords[1,:])
16 plt.show()
```