## Question 2.3.3

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## 1 Question:

If  $\mathbf{a}$ ,  $\mathbf{b}$ ,  $\mathbf{c}$  are three non-zero unequal vectors such that  $\mathbf{a}^T\mathbf{b} = \mathbf{a}^T\mathbf{c}$ , then find the angle between  $\mathbf{a}$  and  $\mathbf{b} - \mathbf{c}$ .

## 2 Solution:

Given that  $\mathbf{a}^{\mathrm{T}}\mathbf{b} = \mathbf{a}^{\mathrm{T}}\mathbf{c}$ , we can rewrite this as:

$$\mathbf{a}^{\mathrm{T}}\mathbf{b} - \mathbf{a}^{\mathrm{T}}\mathbf{c} = 0 \tag{1}$$

$$\mathbf{a}^{\mathrm{T}}(\mathbf{b} - \mathbf{c}) = 0 \tag{2}$$

This implies that the dot product of  $\mathbf{a}$  and  $\mathbf{b} - \mathbf{c}$  is zero, ie these are orthogonal matrices. Therefore, the angle between  $\mathbf{a}$  and  $\mathbf{b} - \mathbf{c}$  is  $90^{\circ}$ .