Question 2.3.3

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1 Question:

If \mathbf{a} , \mathbf{b} , \mathbf{c} are three non-zero unequal vectors such that $\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \cdot \mathbf{c}$, then find the angle between \mathbf{a} and $\mathbf{b} - \mathbf{c}$.

2 Solution:

The dot product formula is

$$\mathbf{a} \cdot \mathbf{b} = |\mathbf{a}||\mathbf{b}|\cos\theta \tag{1}$$

Where θ is the angle between vectors **a** and **b**.

$$\therefore \theta = \arccos(\frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}||\mathbf{b}|}) \tag{2}$$

In this case, we would need to find

$$\theta = \arccos(\frac{\mathbf{a} \cdot (\mathbf{b} - \mathbf{c})}{|\mathbf{a}||\mathbf{b} - \mathbf{c}|}) \tag{3}$$

$$\theta = \arccos(\frac{\mathbf{a} \cdot \mathbf{b} - \mathbf{a} \cdot \mathbf{c}}{|\mathbf{a}||\mathbf{b} - \mathbf{c}|}) \tag{4}$$

$$\theta = \arccos(0) = 90^{\circ} \tag{5}$$

$$\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \cdot \mathbf{c} \text{ and } |\mathbf{a}| \neq 0, |\mathbf{b} - \mathbf{c}| \neq 0$$
(6)

Therefore, the angle between the vectors \mathbf{a} and $\mathbf{b} - \mathbf{c}$ is 90°.