## EE25BTECH11052 - Shriyansh Kalpesh Chawda

## **Question:**

Find the vector equation of the line passing through (1, 2, 3) and perpendicular to the  $\mathbf{r} \cdot (\hat{i} + 2\hat{j} - 5\hat{k}) + 9 = 0$ .

## **Solution**

The plane is given by

$$\mathbf{r} \cdot (1, 2, -5) + 9 = 0 \tag{0.1}$$

so the plane's normal vector is

$$\mathbf{n} = \begin{pmatrix} 1 \\ 2 \\ -5 \end{pmatrix}. \tag{0.2}$$

The required line is perpendicular to the plane, so its direction vector lies in the row space. Thus, the line direction vector can be chosen as

$$\mathbf{d} = \mathbf{n} = \begin{pmatrix} 1 \\ 2 \\ -5 \end{pmatrix}. \tag{0.3}$$

Using the point

$$\mathbf{a} = \begin{pmatrix} 1\\2\\3 \end{pmatrix}, \tag{0.4}$$

the vector equation of the line is

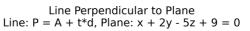
$$\mathbf{r} = \mathbf{a} + t\mathbf{d} \tag{0.5}$$

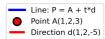
$$\mathbf{r} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} + t \begin{pmatrix} 1 \\ 2 \\ -5 \end{pmatrix}, \quad t \in \mathbb{R}. \tag{0.6}$$

In symmetric form, the line is

$$\frac{x-1}{1} = \frac{y-2}{2} = \frac{z-3}{-5}. (0.7)$$

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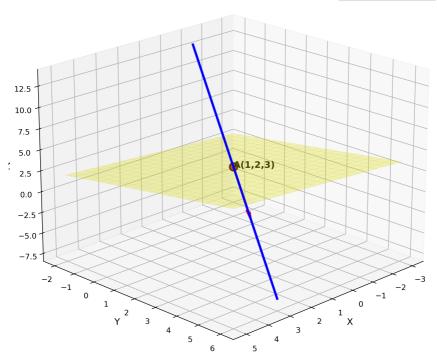


Fig. 0.1