

1.9.10

EE25BTECH11021 - Dhanush sagar

question(1.9.10) :

The distance between the point $\mathbf{A} = \begin{pmatrix} 0 \\ 6 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} 0 \\ -2 \end{pmatrix}$ is (0.1)

solution :

$$\text{Let } \mathbf{A} = \begin{pmatrix} 0 \\ 6 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 0 \\ -2 \end{pmatrix}. \quad (0.2)$$

The distance between \mathbf{A} and \mathbf{B} is $d(\mathbf{A}, \mathbf{B}) = \|\mathbf{A} - \mathbf{B}\|_2$. (0.3)

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} - \begin{pmatrix} 0 \\ -2 \end{pmatrix} = \begin{pmatrix} 0 \\ 8 \end{pmatrix}. \quad (0.4)$$

$$\|\mathbf{A} - \mathbf{B}\|_2 = \sqrt{(\mathbf{A} - \mathbf{B})^T (\mathbf{A} - \mathbf{B})}. \quad (0.5)$$

$$= \sqrt{\begin{pmatrix} 0 & 8 \end{pmatrix} \begin{pmatrix} 0 \\ 8 \end{pmatrix}} = \sqrt{0^2 + 8^2} = \sqrt{64}. \quad (0.6)$$

conclusion : The distance between \mathbf{A} and \mathbf{B} is $= 8$. (0.7)

