### 1.6.9

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## Question

if three points 
$$\begin{pmatrix} h \\ 0 \end{pmatrix}$$
,  $\begin{pmatrix} a \\ b \end{pmatrix}$ ,  $\begin{pmatrix} 0 \\ k \end{pmatrix}$  lie on a line, show that

$$\frac{a}{h} + \frac{b}{k} = 1$$



# Solution

Point	Name
(h, 0)	Point A
(0, k)	Point B
(a,b)	Point C

Table: Variables Used

#### Solutions

If the rank of the Collinearity matrix is 1, then the points are collinear The Collinearity matrix is given by

$$\stackrel{C_1 \to \frac{C_1}{-h}}{\longleftrightarrow} \begin{pmatrix} \frac{a-h}{-h} & b \\ 1 & k \end{pmatrix} \tag{2}$$

$$\stackrel{C_2 \to \frac{C_2}{k}}{\longleftrightarrow} \begin{pmatrix} \frac{a-h}{-h} & \frac{b}{k} \\ 1 & 1 \end{pmatrix} \tag{3}$$

$$\stackrel{R_1 \to C_1 - C_2}{\longleftrightarrow} \begin{pmatrix} \frac{a - h}{-h} - \frac{b}{k} & \frac{b}{k} \\ 0 & 1 \end{pmatrix} \tag{4}$$

### Solution

since the rank of matrix=1

$$\frac{a-h}{-h} - \frac{b}{k} = 0 \implies \frac{a}{h} + \frac{b}{k} = 1$$

# Graph

## Refer to Fig.

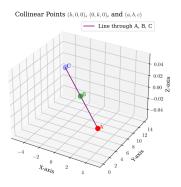


Figure:

```
# Plotting points A(1, -2, -8), B(5, 0, -2), and C(11, 3, 7)
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

# Define the points as numpy arrays
A = np.array([1, -2, -8])
B = np.array([5, 0, -2])
C = np.array([11, 3, 7])
```

```
import matplotlib
import matplotlib.pyplot as plt
import numpy as np
from mpl_toolkits.mplot3d import Axes3D
# Use LaTeX-compatible font settings
matplotlib.use('pgf')
plt.rcParams.update({
    text.usetex: True,
    font.family: lmodern,
    font.size: 11,
})
# Define points A and B
h. k = 5.7
A = np.array([h, 0, 0])
B = np.array([0, k, 0])
```

Compute a third point C that lies on the line AB using Vaishnavi - EE25BTECH11059

```
# 3D Plot
fig = plt.figure(figsize=(8, 6))
ax = fig.add subplot(111, projection='3d')
# Plot the points
ax.scatter(points[:,0], points[:,1], points[:,2], color=['red',
    green', 'blue'], s=100)
ax.plot(points[:,0], points[:,1], points[:,2], color='purple',
    label='Line through A, B, C')
# Annotate the points
ax.text(*A, ' A', color='red')
ax.text(*B, ' B', color='green')
ax.text(*C, ' C', color='blue')
```

```
# Axis labels
ax.set xlabel('X-axis')
ax.set ylabel('Y-axis')
ax.set_zlabel('Z-axis')
ax.set title(r'Collinear Points (h,0,0), (0,k,0), and (a,b,c)
    )$')
ax.legend()
ax.grid(True)
# Save the figure
fig.savefig(collinear_3d_plot.png)
```

#### C Code

```
#include <stdio.h>
#include <stdbool.h>
// Function to check collinearity using the matrix method
bool check_collinearity_matrix(int h, int a, int b, int k) {
    if (h == 0 || k == 0) {
       printf( Invalid input: h and k must be non-zero.\n);
       return false;
   }
   // Step 1: Construct the matrix from vector differences
    int row1 col1 = a - h;
    int row1 col2 = b;
    int row2 col1 = -h;
    int row2 col2 = k;
   printf(Collinearity matrix before row operations:\n);
   printf([ %d\t%d ]\n, row1 col1, row1 col2);
    printf([ %d\t%d ]\n, row2 col1, row2 col2);
```

```
printf(\nAfter row operation R1 = R1 - R2:\n);
printf([ %d\t%d ]\n, row2_col1, row2_col2);
// Step 3: Check the condition (a/h + b/k == 1) without
   floating point
int lhs = a * k + b * h:
int rhs = h * k;
printf(\nChecking condition: (a/h + b/k == 1)\n);
printf(Computed: (%d * %d + %d * %d) = %d \ n, a, k, b, h, lhs)
printf(Expected: (%d * %d) = %d \ n, h, k, rhs);
```

#### C Code

```
printf(Checking collinearity for points:\n);
printf(A = (\%d, 0), B = (\%d, \%d), C = (0, \%d) \n\n, h, a, b, k
   );
if (check_collinearity_matrix(h, a, b, k)) {
   printf(\nPoints are collinear (Matrix rank = 1 and a/h +
       b/k = 1).(n):
} else {
   printf(\n Points are NOT collinear (Condition fails).\n);
}
return 0;
```

# Python and C Code

```
import subprocess
# Compile the C program
subprocess.run([gcc, points.c, -o, points])
# Run the compiled C program
result = subprocess.run([./points], capture_output=True, text=
    True)
# Print the output from the C program (solution)
print(result.stdout)
```