

Matgeo Presentation - Problem 2.7.33

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Problem Statement

Find the value of p if

$$(2\hat{i} + 6\hat{j} + 27\hat{k}) \times (\hat{i} + 3\hat{j} + p\hat{k}) = 0.$$

solution

Solution:

The given vectors are

$$\mathbf{A} = \begin{pmatrix} 2 \\ 6 \\ 27 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ 3 \\ p \end{pmatrix}. \quad (0.1)$$

Since

$$\mathbf{A} \times \mathbf{B} = \mathbf{0}, \quad (0.2)$$

the vectors \mathbf{A} and \mathbf{B} are linearly dependent. Therefore, there exists a scalar t such that

$$\mathbf{B} = t\mathbf{A}. \quad (0.3)$$

Substituting the components,

$$\begin{pmatrix} 1 \\ 3 \\ p \end{pmatrix} = t \begin{pmatrix} 2 \\ 6 \\ 27 \end{pmatrix}. \quad (0.4)$$

solution

From the first coordinate,

$$1 = 2t \Rightarrow t = \frac{1}{2}. \quad (0.5)$$

From the second coordinate,

$$3 = 6t \Rightarrow t = \frac{1}{2}, \quad (0.6)$$

which is consistent with the first.

Finally, from the third coordinate,

$$p = 27t = 27 \cdot \frac{1}{2} = \frac{27}{2}. \quad (0.7)$$

C Source Code: cross.c

```
#include <stdio.h>

void cross_product(double a[3], double b[3], double result[3]) {
    result[0] = a[1]*b[2] - a[2]*b[1];
    result[1] = a[2]*b[0] - a[0]*b[2];
    result[2] = a[0]*b[1] - a[1]*b[0];
}

double find_p() {
    double a[3] = {2, 6, 27};
    double p = 27.0 / 2.0;
    double b[3] = {1, 3, p};
    double res[3];
    cross_product(a, b, res);
    if(res[0] == 0 && res[1] == 0 && res[2] == 0) {
        return p;
    }
    return -1;
}
```

Python Script: vector solve.py

```
import ctypes
import numpy as np
# Load shared library
lib = ctypes.CDLL("./cross.so")
lib.find_p.restype = ctypes.c_double
# Call C function
p = lib.find_p()
print("Computed value of p:", p)
# Verify using numpy
A = np.array([2, 6, 27])
B = np.array([1, 3, p])
cross_prod = np.cross(A, B)
print("Cross product A  $\times$  B =", cross_prod)
if np.allclose(cross_prod, [0, 0, 0]):
    print("✓ A and B are parallel. Solution verified.")
else:
    print("✗ Something went wrong.")
```

Python Script: plot vector.py

```
import numpy as np
import matplotlib.pyplot as plt
# Vectors
A = np.array([2, 6, 27])
p = 27/2
B = np.array([1, 3, p])
# Plot
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.quiver(0, 0, 0, A[0], A[1], A[2], color='r', label=f'A = {A}')
ax.quiver(0, 0, 0, B[0], B[1], B[2], color='b', label=f'B = {B}')
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
ax.legend()
plt.title("Vectors A and B (parallel)")
plt.savefig("vectors.png")
plt.show()
```

Result Plot

