## EE25BTECH11019 - Darji Vivek M.

**Question:** 

If  $\mathbf{a} = \mathbf{i} + \mathbf{j} + \mathbf{k}$ ,  $\mathbf{a} \cdot \mathbf{b} = 1$  and  $\mathbf{a} \times \mathbf{b} = \mathbf{j} - \mathbf{k}$ , then  $\mathbf{b}$  is

(a) 
$$\mathbf{i} - \mathbf{j} + \mathbf{k}$$

(b) 
$$2j - k$$

**Solution:** 

$$\mathbf{a} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \quad \mathbf{b} = \begin{pmatrix} x \\ y \\ z \end{pmatrix} \tag{1}$$

1

Dot product condition:

$$x + y + z = 1 \tag{2}$$

Cross product condition gives

$$z - y = 0$$
,  $x - z = 1$ ,  $y - x = -1$  (3)

The first equation can be expressed as

$$\begin{pmatrix} 0 & 1 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = 0 \tag{4}$$

Collecting all equations:

$$\begin{pmatrix} 0 & 1 & -1 \\ 1 & 0 & -1 \\ 1 & 1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$$
 (5)

Solving,

Hence,

$$\mathbf{b} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} = \mathbf{i} \tag{7}$$

Therefore, the correct option is (c).

## Vectors a and b with coordinates

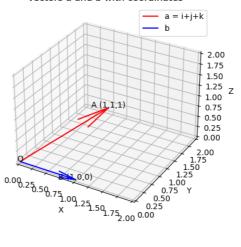


Fig. 4.1: plot