## EE25BTECH11043 - Nishid Khandagre

**Question**: If the coordinates of the middle point of the portion of a line intercepted between the coordinate axes is  $\binom{3}{2}$ , then the equation of the line will be?

**Solution:** The equation of line is

$$\mathbf{n}^{\mathsf{T}}\mathbf{x} = c \tag{0.1}$$

Where  $\mathbf{n} = \begin{pmatrix} n_1 \\ n_2 \end{pmatrix}$  is the normal vector and  $\mathbf{x} = \begin{pmatrix} x \\ y \end{pmatrix}$  is the position vector.

X-axis intercept  $y = 0 \Rightarrow x = \frac{c}{n_1}$ .

Thus, **A** is  $\binom{c}{n_1}$ .

Y-axis intercept  $x = 0 \Rightarrow y = \frac{c}{n_2}$ .

Thus, **B** is  $\binom{0}{\frac{c}{n_2}}$ .

Let M is the midpoint of A and B

Given  $\mathbf{M} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$ .

$$\mathbf{M} = \frac{\mathbf{A} + \mathbf{B}}{2} \tag{0.2}$$

$$\begin{pmatrix} 3 \\ 2 \end{pmatrix} = \begin{pmatrix} \frac{c}{2n_1} \\ \frac{c}{2n_2} \end{pmatrix}$$
(0.4)

$$\frac{c}{2n_1} = 3\tag{0.5}$$

$$\frac{c}{2n_2} = 2$$
 (0.6)

$$\frac{n_1}{n_2} = \frac{2}{3} \tag{0.7}$$

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Let  $n_1 = 2$  and  $n_2 = 3$ . Then

$$c = 6 \times 2 = 12 \tag{0.8}$$

The final equation of the line is  $\mathbf{n}^{\mathsf{T}}\mathbf{x} = c$ 

$$\begin{pmatrix} 2 & 3 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = 12 \tag{0.9}$$

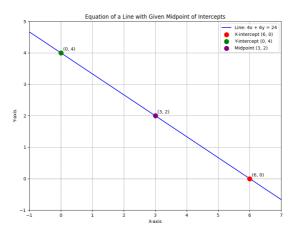


Fig. 0.1