

# 4.3.13

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## Question:

Equations of the diagonals of the square formed by the lines  $x = 0$ ,  $y = 0$ ,  $x = 1$  and  $y = 1$  are \_\_\_\_\_.

## Solution:

Let us solve the given equation theoretically and then verify the solution computationally.

According to the question,

The vertices of the square are ,

$$\mathbf{a} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \mathbf{c} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad \mathbf{d} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

To compute the equation of the diagonals , we can use the normal form of the equation, which is given by

$$\mathbf{n}^T \mathbf{x} = \mathbf{n}^T \mathbf{P}$$

where,

$\mathbf{n}$ -vector orthogonal to the direction vector

$$\mathbf{x} = \begin{pmatrix} x & y \end{pmatrix}^T$$

$\mathbf{P}$ =A point which lies along the vector

For diagonal  $\mathbf{c} - \mathbf{a}$ ,

$$\mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \mathbf{d}$$

where  $\mathbf{d}$  is the direction vector of diagonal.

$$\therefore \mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \left( \begin{pmatrix} 1 \\ 1 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} \right)$$

$$\Rightarrow \mathbf{n} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$\mathbf{n} = \begin{pmatrix} -1 \\ 1 \end{pmatrix} \quad \text{and} \quad \mathbf{P} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$\therefore \begin{pmatrix} -1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -1 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix} = 0$$

Similarly, for diagonal  $\mathbf{d} - \mathbf{b}$ ,

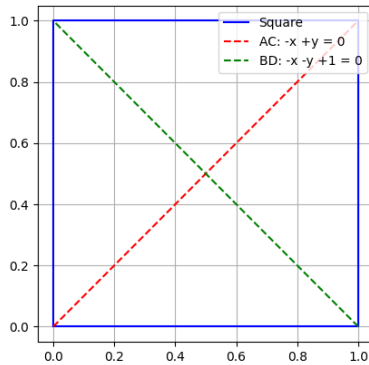
$$\therefore \mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \left( \begin{pmatrix} 0 \\ 1 \end{pmatrix} - \begin{pmatrix} 1 \\ 0 \end{pmatrix} \right)$$

$$\Rightarrow \mathbf{n} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$\mathbf{n} = \begin{pmatrix} -1 \\ -1 \end{pmatrix} \text{ and } \mathbf{P} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$\therefore \begin{pmatrix} -1 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -1 & -1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix} = -1$$

From the figure, it is clearly verified that the theoretical solution matches with the computational solution.



Plot of Square with diagonals