

5.3.12

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Question:

Solve for x and y

$$x + y = 6, 2x - 3y = 4$$

Solution:

Let :

$$\mathbf{r}_1 = \begin{pmatrix} 1 & 1 \end{pmatrix} \mathbf{x} = 6 \quad (0.1)$$

$$\mathbf{r}_2 = \begin{pmatrix} 2 & -3 \end{pmatrix} \mathbf{x} = 4 \quad (0.2)$$

The augmented matrix of the above equations is given by,

$$\begin{pmatrix} 1 & 1 & 6 \\ 2 & -3 & 4 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - 2R_1} \begin{pmatrix} 1 & 1 & 6 \\ 0 & -5 & -8 \end{pmatrix} \quad (0.3)$$

$$\begin{pmatrix} 1 & 1 & 6 \\ 0 & -5 & -8 \end{pmatrix} \xrightarrow{R_1 \leftarrow 5R_1 + R_2} \begin{pmatrix} 5 & 0 & 22 \\ 0 & -5 & -8 \end{pmatrix} \quad (0.4)$$

$$5x = 22 \quad x = \frac{22}{5} \quad (0.5)$$

$$-5y = -8 \quad y = \frac{8}{5} \quad (0.6)$$

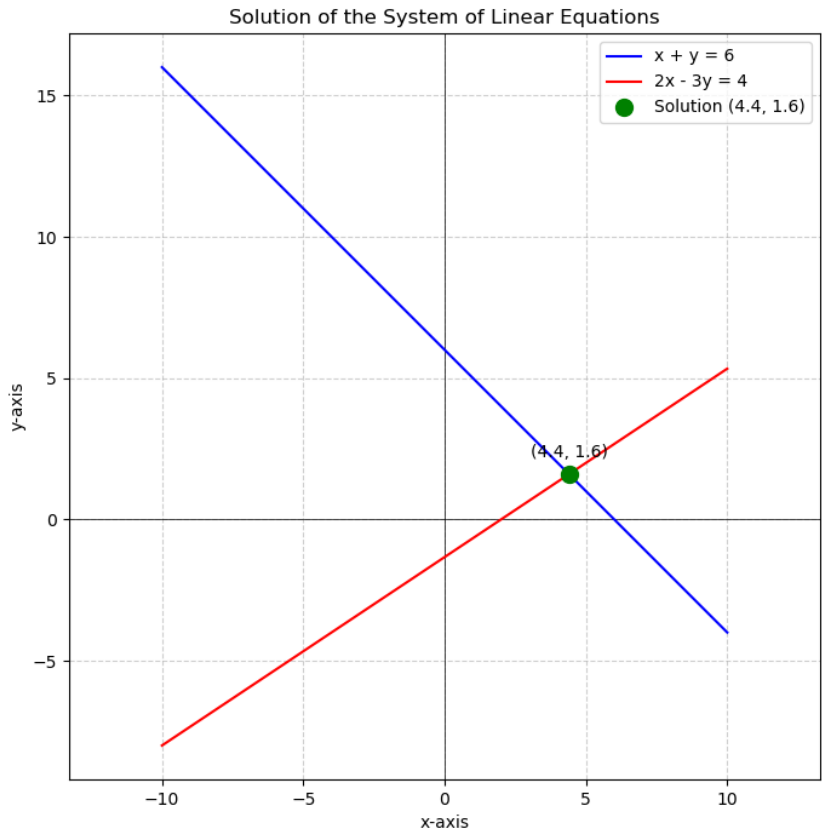


Fig. 0.1