## EE25btech11028 - J.Navya sri

## **Ouestion:**

Find the equation of the plane passing through the intersection of the planes

$$(r) \cdot (\hat{i} + \hat{j} + \hat{k}) = 1$$

and

$$(r)\cdot(2\hat{i}+3\hat{j}-\hat{k})+4=0$$

and parallel to the X-axis. Hence, find the distance of the plane from the X-axis.

## **Solution:**

Step 1: Plane through the intersection of the two given planes

The two given planes are

$$\Pi_1: x + y + z = 1 \tag{1}$$

1

$$\Pi_2: 2x + 3y - z + 4 = 0 \tag{2}$$

A plane passing through their intersection can be written as

$$\Pi: (x+y+z-1) + \lambda(2x+3y-z+4) = 0$$
 (3)

Expanding:

$$x + y + z - 1 + \lambda(2x + 3y - z + 4) = 0$$
 (4)

$$x(1+2\lambda) + y(1+3\lambda) + z(1-\lambda) + (-1+4\lambda) = 0$$
 (5)

Step 2: Condition for the plane to be parallel to the X-axis

A plane is parallel to the X-axis if the coefficient of x is zero:

$$1 + 2\lambda = 0 \quad \Rightarrow \quad \lambda = -\frac{1}{2} \tag{6}$$

Step 3: Substitute  $\lambda = -\frac{1}{2}$ 

$$y\left(1+3\left(-\frac{1}{2}\right)\right)+z\left(1-\left(-\frac{1}{2}\right)\right)+\left(-1+4\left(-\frac{1}{2}\right)\right)=0\tag{7}$$

$$y(-\frac{1}{2}) + z(\frac{3}{2}) - 3 = 0 \tag{8}$$

Multiply through by 2:

$$-y + 3z - 6 = 0 \implies y - 3z + 6 = 0$$
 (9)

So, the required plane is

$$y - 3z + 6 = 0 \tag{10}$$

Step 4: Distance from the X-axis

The *X*-axis is the line y = 0, z = 0.

Distance from a plane y - 3z + 6 = 0 to a point (0, 0, 0) on the X-axis is

$$d = \frac{|y_0 - 3z_0 + 6|}{\sqrt{1^2 + (-3)^2}} = \frac{|0 - 0 + 6|}{\sqrt{1 + 9}} = \frac{6}{\sqrt{10}}$$
(11)

Distance = 
$$\frac{6}{\sqrt{10}}$$
 (12)

## **Graph presentation:**

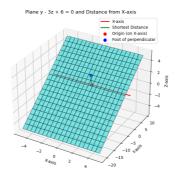


Fig. 1