

5.2.68

AI25BTECH11001 - ABHISEK MOHAPATRA

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Question: Solve $2x + 3y = 11$ and $2x + 4y = -24$ and hence find the value of m for which $y = mx + 3$.

Solution: Given:

$$2x + 3y = 11 \quad (0.1)$$

And,

$$2x + 4y = -24 \quad (0.2)$$

So,

$$\begin{pmatrix} 2 & 3 \\ 2 & 4 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 11 \\ -24 \end{pmatrix} \quad (0.3)$$

Augmented Matrix:

$$\left(\begin{array}{cc|c} 2 & 3 & 11 \\ 2 & 4 & -24 \end{array} \right) \quad (0.4)$$

$$\xrightarrow{R_2 \rightarrow R_2 - R_1} \left(\begin{array}{cc|c} 2 & 3 & 11 \\ 0 & 1 & -35 \end{array} \right) \quad (0.5)$$

$$\xrightarrow{R_1 \rightarrow R_1 - 3R_2} \left(\begin{array}{cc|c} 2 & 0 & 116 \\ 0 & 1 & -35 \end{array} \right) \quad (0.6)$$

$$\Rightarrow \left(\begin{array}{cc|c} 1 & 0 & 58 \\ 0 & 1 & -35 \end{array} \right) \quad (0.7)$$

So,

$$\mathbf{x} = \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 58 \\ -35 \end{pmatrix} \quad (0.8)$$

Given,

$$y = mx + 3 \quad (0.9)$$

$$\Rightarrow m = \frac{y - 3}{x} = -\frac{19}{29} \quad (0.10)$$

So, $m = -\frac{19}{29}$

Graph:

