### 1.5.13

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### Question

Find the ratio in which the Y-axis divides the line segment joining the points  $\mathbf{A}(5,-6)$  and  $\mathbf{B}(-1,-4)$ . Also find the coordinates of the point of intersection.

### Equation

Let the Y-axis divide the line segment  ${\bf B}-{\bf A}$  at point  ${\bf C}$  in the ratio m:1. Since  ${\bf C}$  lies on Y-axis, let

$$\mathbf{C} = \begin{pmatrix} 0 \\ y \end{pmatrix}$$

The point A, B, C are collinear.

$$\implies$$
 rank  $\left(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A}\right) = 1$  (1)

#### Theoretical Solution

$$\begin{pmatrix} -6 & -5 \\ 2 & a+6 \end{pmatrix} []R_2 \to \frac{1}{3}R_1 + R_2 \begin{pmatrix} -6 & -5 \\ 0 & a + \frac{13}{3} \end{pmatrix}$$
 (2)

The number of nonzero rows in the row reduced matrix (also known as *echelon form*) is defined as the rank. For above matrix to be of rank 1,

$$a + \frac{13}{3} = 0 \tag{3}$$

$$a = \frac{-13}{3} \tag{4}$$

.. The coordinates of the point of intersection are

$$\mathbf{C} = \begin{pmatrix} 0 \\ \frac{-13}{3} \end{pmatrix}$$

#### Theoretical Solution

Substituting the values of A, B and C,

$$k = \frac{\left(5 \quad \frac{-5}{3}\right) \left(\frac{1}{\frac{-1}{3}}\right)}{\left\| \left(\frac{1}{\frac{-1}{3}}\right) \right\|^2} = 5 \tag{5}$$

Thus, the ratio in which the point  ${\bf C}$  divides the line segment  ${\bf B}-{\bf A}$  is  ${\bf 5:1}$ .

#### C Code

```
#include <stdio.h>
#include <math.h>
void function(double *P, double *B, double *A , int m, int k) {
   for ( int i = 0 ; i < m ; i++ ) {
      P[i] = (1*A[i] + k*B[i])/(k+1) ;
   }
}</pre>
```

```
problem.argtypes = [
    ctypes.POINTER(ctypes.c_double),
    ctypes.POINTER(ctypes.c_double),
    ctypes.POINTER(ctypes.c_double),
    ctypes.c_int,
    ctypes.c int,
|problem.restype = None # void function
m = 2
k = 5
A = np.array([[5, -6]], dtype=np.float64)
|B = np.array([[-1, -4]], dtype=np.float64)
P = np.zeros(m, dtype=np.float64)
```

```
problem.function(
   P.ctypes.data as(ctypes.POINTER(ctypes.c double)),
   B.ctypes.data as(ctypes.POINTER(ctypes.c double)),
   A.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
   m. #len(P) alternate
   k
A = np.array([5, -6]).reshape(-1, 1)
B = np.array([-1, -4]).reshape(-1,1)
P = P.reshape(-1,1)
```

```
plt.plot([A[0,0], B[0,0]], [A[1,0], B[1,0]], 'g--', label="Line
    Segment AB")
plot coords = np.block([[A, B, P]])
plt.scatter(plot coords[0,:], plot coords[1,:], color='blue')
vert_labels = [
    f'A({A[0,0]}, {A[1,0]})',
    f'B({B[0,0]}, {B[1,0]})',
    f'P({P[0,0]}, {P[1,0]:.2f})'
```

```
for i, txt in enumerate(vert labels):
    plt.annotate(txt,
           (plot coords[0,i],plot coords[1,i]),
           textcoords="offset points",
           xytext=(0,10),
           ha='center')
plt.xlabel('$x$')
plt.ylabel('$y$')
plt.title("Line Segment AB Divided by Y-axis")
plt.legend(loc='best')
plt.grid()
plt.axis('equal')
plt.savefig("../figs/plot.png")
plt.show()
```

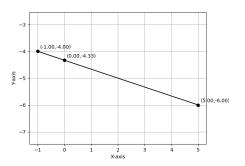


Figure: Plot of Intersection of AB by Y-axis