

## 5.8.2

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# Question

10 students of Class X took part in a Mathematics quiz. If the number of girls is 4 more than the number of boys, find the number of boys and girls who took part in the quiz.

# Solution

Let the number of girls in the class be  $g$ , and the number of boys be  $b$ .  
Let the vector representing this data be

$$\mathbf{x} = \begin{pmatrix} g \\ b \end{pmatrix} \quad (1)$$

Since the total number of students in the class is 10,  $g + b = 10$  which can be expressed as:

$$\begin{pmatrix} 1 \\ 1 \end{pmatrix}^T \mathbf{x} = 10 \quad (2)$$

Since there are 4 more girls than boys,  $b + 4 = g$ , which can be expressed as:

$$\begin{pmatrix} -1 \\ 1 \end{pmatrix}^T \mathbf{x} = -4 \quad (3)$$

# Solution

Organising these two equations into a matrix:

$$\begin{pmatrix} 1 & 1 \\ -1 & 1 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 10 \\ -4 \end{pmatrix} \quad (4)$$

Forming an augmented matrix and performing row operations:

$$\begin{pmatrix} 1 & 1 & 10 \\ -1 & 1 & -4 \end{pmatrix} \xrightarrow{R_2 \rightarrow R_2 + R_1} \quad (5)$$

$$\begin{pmatrix} 1 & 1 & 10 \\ 0 & 2 & 6 \end{pmatrix} \xrightarrow{R_2 \rightarrow R_2/2} \quad (6)$$

$$\begin{pmatrix} 1 & 1 & 10 \\ 0 & 1 & 3 \end{pmatrix} \xrightarrow{R_1 \rightarrow R_1 - R_2} \quad (7)$$

# Solution

$$\begin{pmatrix} 1 & 0 & 7 \\ 0 & 1 & 3 \end{pmatrix} \quad (8)$$

Therefore:

$$\mathbf{x} = \begin{pmatrix} 7 \\ 3 \end{pmatrix} \quad (9)$$

$$g = 7 \quad (10)$$

$$b = 3 \quad (11)$$

# Python Code

```
import numpy as np
import numpy.linalg
import matplotlib.pyplot as plt

answer = numpy.linalg.solve([[1,1],[-1,1]], [10,-4])

answer[0] = round(answer[0],2)
answer[1] = round(answer[1],2)
print(answer)
```

# Python Code

```
fig = plt.figure(figsize =(6,6))
ax = fig.add_subplot(111)

X = np.linspace(-20,20,2)

Y1 = (10-X)
Y2 = (X-4)

ax.plot(X, Y1, label='Line 1')
ax.plot(X, Y2, label='Line 2')
ax.scatter(answer[0], answer[1], label=f'({answer[0]}, {answer
[1]})')
ax.grid(True)
ax.legend()
plt.show()
```

# Plot

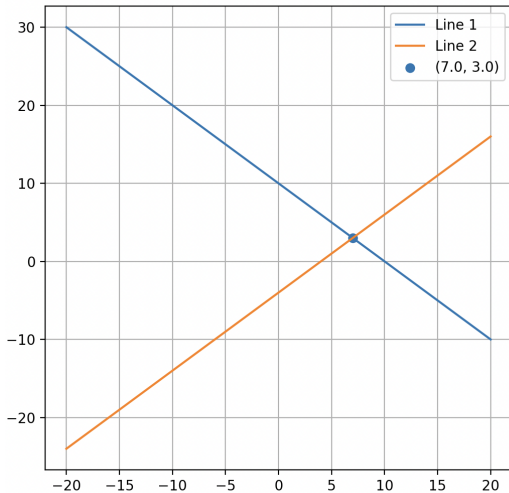


Figure: Plot