EE25BTECH11013 - Bhargav

Question:

1200 men and 500 women can build a bridge in 2 weeks. 900 men and 250 women will take 3 weeks to build the same bridge. How many men will be needed to build the bridge in one week?

Solution:

Let one man complete work in x weeks and one woman complete work in y weeks In one week a man can complete $\frac{1}{x}$ work and woman can complete $\frac{1}{y}$

$$\frac{1200}{x} + \frac{500}{y} = \frac{1}{2} \tag{0.1}$$

$$\frac{900}{x} + \frac{250}{y} = \frac{1}{3} \tag{0.2}$$

$$\begin{pmatrix} 1200 & 500 \\ 900 & 250 \end{pmatrix} \begin{pmatrix} \frac{1}{x} \\ \frac{1}{y} \end{pmatrix} = \begin{pmatrix} \frac{1}{2} \\ \frac{1}{3} \end{pmatrix}$$
 (0.3)

This can be converted into an augmented matrix and can be solved by Gaussian elimination:

$$\begin{pmatrix} 1200 & 500 & \left| \begin{array}{c} \frac{1}{2} \\ 900 & 250 \end{array} \right| \begin{array}{c} \frac{1}{2} \\ \frac{1}{3} \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - 3R_1/4} \begin{pmatrix} 1200 & 500 & \left| \begin{array}{c} \frac{1}{2} \\ 0 & 1 \end{array} \right| \begin{array}{c} \frac{1}{3000} \end{pmatrix}$$
 (0.4)

$$\frac{R_1 \leftarrow R_1 / 1200}{R_1 \leftarrow R_1 - 500R_2} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{vmatrix} \frac{1}{3600} \\ \frac{3000}{3000} \end{pmatrix}$$
(0.5)

$$\begin{pmatrix} \frac{1}{x} \\ \frac{1}{y} \end{pmatrix} = \begin{pmatrix} \frac{1}{3600} \\ \frac{1}{3000} \end{pmatrix} \tag{0.6}$$

A man can finish the work in 3600 weeks, a woman can finish the work in 3000 weeks

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