EE25BTECH11001 - Aarush Dilawri

Question:

Given vertices A(-4, -5), B(-1, -6), C(-5, 7) and D(4, 5) of a quadrilateral. Find the area of quadrilateral *ABCD*.

Solution:

Given vertices $\mathbf{A} = \begin{pmatrix} -4 \\ -5 \end{pmatrix}$, $\mathbf{B} = \begin{pmatrix} -1 \\ -6 \end{pmatrix}$, $\mathbf{C} = \begin{pmatrix} -5 \\ 7 \end{pmatrix}$, $\mathbf{D} = \begin{pmatrix} 4 \\ 5 \end{pmatrix}$. We split the quadrilateral into triangles $\triangle ABC$ and $\triangle ACD$ and add them to get the answer.

Area of $\triangle ABC$:

$$Area_{ABC} = \frac{1}{2} \left\| (\mathbf{B} - \mathbf{A}) \times (\mathbf{C} - \mathbf{A}) \right\| = 17.5 \tag{1}$$

Area of $\triangle ACD$:

$$Area_{ACD} = \frac{1}{2} \left\| (\mathbf{C} - \mathbf{A}) \times (\mathbf{D} - \mathbf{A}) \right\| = 53$$
 (2)

Total area of quadrilateral (sum of triangle areas):

$$Area_{ABCD} = Area_{ABC} + Area_{ACD} = 70.5$$
 (3)

See Fig. 0,

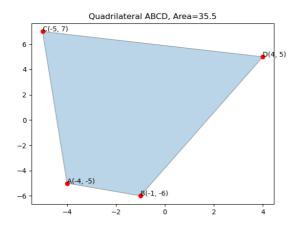


Fig. 0