AI25BTECH11023 - Pratik R

QUESTION

If the distance of the point (1, 1, 1) from the plane $x - y + z + \lambda = 0$ is $\frac{5}{\sqrt{3}}$, find the value(s) of λ .

Solution:

Equation of plane is given by

$$n^{\mathsf{T}}x = -\lambda; \tag{0.1}$$

where $n^{\top} = \begin{pmatrix} 1 & -1 & 1 \end{pmatrix}$.

Let the distance of point P(1,1,1) from the plane is d.

$$d = \frac{\|n^\top P + \lambda\|}{\|n\|} \tag{0.2}$$

then value of λ is given by

$$\lambda = +d||n|| - n^{\mathsf{T}}P \text{ or} \tag{0.3}$$

$$\lambda = -d||n|| - n^{\mathsf{T}}P\tag{0.4}$$

Solving these Equations we get

$$\implies \lambda = +4$$
 (0.5)

$$= -6 \tag{0.6}$$

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3D Plane and Point A

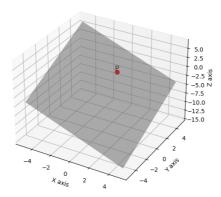


Fig. 0.1: plane



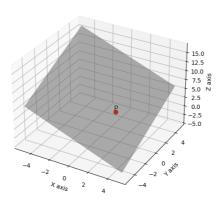


Fig. 0.2: plane