2.4.29

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Question

The points A(2,9), B(a,5) and C(5,5) are the vertices of a triangle ABC right angled at B. Find the values of a and hence the area of $\triangle ABC$.

Theoretical Solution

Given the points A, B and C, also consider ${\bf c}$ to be vector opposite to side AB and ${\bf b}$, a similarly

$$\mathbf{A} = \begin{pmatrix} 2 \\ 9 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} a \\ 5 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 5 \\ 5 \end{pmatrix} \tag{1}$$

Since the sides c and a are perpendicular their inner product will be 0 Take the inner product of ${\bf c}$ and ${\bf a}$

Vector c:

$$\mathbf{c} = \mathbf{A} - \mathbf{B} = \begin{pmatrix} 2 - a \\ 9 - 5 \end{pmatrix} = \begin{pmatrix} 2 - a \\ 4 \end{pmatrix} \tag{2}$$

Vector a:

$$\mathbf{a} = \mathbf{B} - \mathbf{C} = \begin{pmatrix} a - 5 \\ 5 - 5 \end{pmatrix} = \begin{pmatrix} a - 5 \\ 0 \end{pmatrix} \tag{3}$$

Orthogonality \implies matrix product is zero :

Theoretical Solution

So
$$(2-a)(5-a) = 0 \implies a = 2$$
 or $a = 5$.
 $a = 5$ make **B=C**. $\therefore a = 2$

We can compute area using general formula since the vectors are perpendicular

$$AREA = \frac{1}{2} \times base \times height \tag{5}$$

Using (5)

$$\Delta = \frac{1}{2} \times \|\mathbf{A}\mathbf{B}\| \times \|\mathbf{B}\mathbf{C}\| \tag{6}$$

$$\therefore \Delta = \frac{1}{2} \times 4 \times 3 = 6 \tag{7}$$

Thus area of triangle is 6



C Code- Triangle Area function

Python Code using shared output

```
import ctypes
 import numpy as np
 import matplotlib.pyplot as plt
 # Load the shared C library
 lib = ctypes.CDLL(./trianglearea.so)
 lib.triangle area.argtypes = [ctypes.c float, ctypes.c float,
 ctypes.c_float, ctypes.c_float,
 ctypes.c_float, ctypes.c_float]
 lib.triangle area.restype = ctypes.c float
 # Vertices
 A = (2, 9)
B = (2, 5)
 C = (5, 5)
```

Python Code using shared output

```
# Call C function
 area = lib.triangle area(A[0], A[1], B[0], B[1], C[0], C[1])
 print(Area of triangle ABC (from C):, area)
 # Plot triangle
 x = [A[0], B[0], C[0], A[0]]
 y = [A[1], B[1], C[1], A[1]]
 |plt.plot(x, y, 'bo-')
 plt.text(A[0], A[1], A(2,9), fontsize=10, ha=right)
 plt.text(B[0], B[1], B(2,5), fontsize=10, ha=right)
plt.text(C[0], C[1], C(5,5), fontsize=10, ha=right)
plt.title(Right Triangle ABC)
plt.grid(True)
plt.axis(equal)
 plt.show()
```

Python Code using shared output

```
# Plotting
plt.figure(figsize=(6, 6))
plt.scatter(A[0], A[1], color='red', label='A(5,1)
plt.scatter(B[0], B[1], color='blue', label='B
   (-1.5)'
plt.scatter(midpoint[0], midpoint[1], color='black
    ', label='Midpoint')
# Perpendicular bisector line
plt.plot(x_vals, y_vals, 'g--', label='3x = 2y (
   Perp. bisector)')
# Mark example points
for p in points_to_check:
plt.scatter(p[0], p[1], label=fPoint {p})
```

Python Code

```
import numpy as np
import matplotlib.pyplot as plt
# Vertices
A = np.array([2, 9])
B = np.array([2, 5])
C = np.array([5, 5])
# Check right angle at B using dot product
AB = A - B
BC = C - B
print(Dot product ABBC =, np.dot(AB, BC))
```

Python Code

```
if np.dot(AB, BC) == 0:
 print(Right angle at B )
 # Area using determinant formula
 area = abs(np.linalg.det(np.array([
 [A[0], A[1], 1],
 [B[0], B[1], 1],
 [C[0], C[1], 1]
 1))) / 2
print(Area of triangle ABC (Python):, area)
 # Plot
 x = [A[0], B[0], C[0], A[0]]
 y = [A[1], B[1], C[1], A[1]]
```

Python Code

```
plt.plot(x, y, 'ro-')
plt.text(A[0], A[1], A(2,9), fontsize=10, ha=right)
plt.text(B[0], B[1], B(2,5), fontsize=10, ha=right)
plt.text(C[0], C[1], C(5,5), fontsize=10, ha=right)
plt.title(Right Triangle ABC (Pure Python))
plt.grid(True)
plt.axis(equal)
plt.show()
```

Plot by python using shared output from c

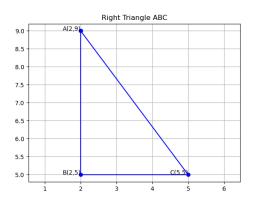


Figure: *

Plot by python only

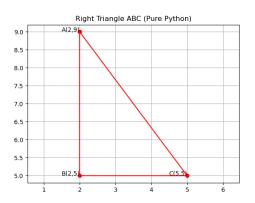


Figure: *