## EE25btech11028 - J.Navya sri

## **Question:**

Find the equation of the plane passing through the intersection of the planes

$$(r) \cdot (\hat{i} + \hat{j} + \hat{k}) = 1$$

and

$$(r)\cdot(2\hat{i}+3\hat{j}-\hat{k})+4=0$$

and parallel to the X-axis. Hence, find the distance of the plane from the X-axis.

## **Solution:**

Step1:Plane through Intersection and Distance from X-axis

Let the equations of the given planes be:

$$(r) \cdot (\hat{i} + \hat{j} + \hat{k}) = 1 \tag{1}$$

$$(r)\cdot(2\hat{i}+3\hat{j}-\hat{k})=4\tag{2}$$

Any plane passing through their intersection can be written as:

$$(r) \cdot (\hat{i} + \hat{j} + \hat{k}) - 1 + \lambda ((r) \cdot (2\hat{i} + 3\hat{j} - \hat{k}) - 4) = 0$$
(3)

Expanding:

$$\left((\hat{i}+\hat{j}+\hat{k})+\lambda(2\hat{i}+3\hat{j}-\hat{k})\right)\cdot\left(r\right)=1+4\lambda\tag{4}$$

The normal vector of the plane is:

$$(N) = (1+2\lambda)\hat{i} + (1+3\lambda)\hat{j} + (1-\lambda)\hat{k}$$
(5)

Step2:Parallel to X-Axis

Since the plane is parallel to the X-axis, its normal must be perpendicular to the X-axis:

$$1 + 2\lambda = 0 \implies \lambda = -\frac{1}{2} \tag{6}$$

Substitute  $\lambda = -\frac{1}{2}$ :

$$(N) = 0 \cdot \hat{i} + \left(1 + 3\left(-\frac{1}{2}\right)\right)\hat{j} + \left(1 - \left(-\frac{1}{2}\right)\right)\hat{k} = -\frac{1}{2}\hat{j} + \frac{3}{2}\hat{k}$$
 (7)

Equation of the plane:

$$-\frac{1}{2}y + \frac{3}{2}z = 1 + 4\left(-\frac{1}{2}\right) = -1\tag{8}$$

$$-\frac{1}{2}y + \frac{3}{2}z + 1 = 0 \quad \Rightarrow \quad -y + 3z + 2 = 0 \tag{9}$$

Step3:Distance from X-Axis

The X-axis is the line y = 0, z = 0.

Distance from the plane to the X-axis (taking point (0,0,0)) is:

$$D = \frac{|-0+3\cdot 0+2|}{\sqrt{(-1)^2+3^2}} = \frac{2}{\sqrt{10}}$$
 (10)

Final Answers:

• Required plane: -y + 3z + 2 = 0• Distance from X-axis:  $\frac{2}{\sqrt{10}}$ 

## **Graph presentation:**

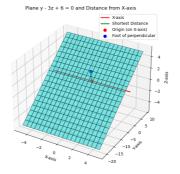


Fig. 1