1.8.18

EE25BTECH11001 - Aarush Dilawri

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Question

Question:

Given vertices $\mathbf{A}(-4,-5)$, $\mathbf{B}(-1,-6)$, $\mathbf{C}(-5,7)$ and $\mathbf{D}(4,5)$ of a quadrilateral. Find the area of quadrilateral *ABCD*.

Solution

Given vertices
$$\mathbf{A} = \begin{pmatrix} -4 \\ -5 \end{pmatrix}$$
, $\mathbf{B} = \begin{pmatrix} -1 \\ -6 \end{pmatrix}$, $\mathbf{C} = \begin{pmatrix} -5 \\ 7 \end{pmatrix}$, $\mathbf{D} = \begin{pmatrix} 4 \\ 5 \end{pmatrix}$.

We split the quadrilateral into triangles $\triangle ABC$ and $\triangle ACD$ and add them to get the answer.

Area of $\triangle ABC$

Area_{ABC} =
$$\frac{1}{2} \| (\mathbf{B} - \mathbf{A}) \times (\mathbf{C} - \mathbf{A}) \| = 17.5$$
 (1)

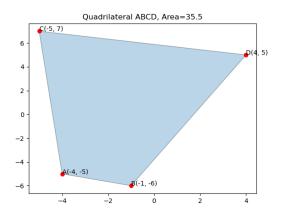
Area of $\triangle ACD$

Area_{ACD} =
$$\frac{1}{2} \| (\mathbf{C} - \mathbf{A}) \times (\mathbf{D} - \mathbf{A}) \| = 53$$
 (2)

Total Area

$$Area_{ABCD} = Area_{ABC} + Area_{ACD} = 70.5$$
 (3)

Figure



C Code (code.c)

```
#include <stdio.h>
#include <math.h>
double area_of_quadrilateral(double x1, double y1,
                            double x2, double y2,
                            double x3, double y3,
                            double x4, double y4) {
   double area = 0.5 * fabs(x1*y2 + x2*y3 + x3*y4 + x4*y1
                          -v1*x2 - v2*x3 - v3*x4 - v4*x1);
   return area;
```

Python Code (code.py)

import numpy as np import matplotlib.pyplot as plt

 $\times 1$, v1 = -4, -5

$$x2, y2 = -1, -6$$

 $x3, y3 = -5, 7$
 $x4, y4 = 4, 5$
area = $0.5 * abs(x1*y2 + x2*y4 + x4*y3 + x3*y1 - y1*x2 - y2*x4 - y4*x3 - y3*x1)$
print("Area:", area)
 $xs = [x1, x2, x4, x3, x1]$

ys = [y1, y2, y4, y3, y1]

Python Code (code.py)

```
plt.fill(xs, ys, alpha=0.3, edgecolor='black')
plt.scatter([x1, x2, x3, x4], [y1, y2, y3, y4], color='red')

points = {"A": (x1, y1), "B": (x2, y2), "C": (x3, y3), "D": (x4, y4)}

for p, (x, y) in points.items():
    plt.text(x, y, f"{p}{(x,y)}")

plt.title(f"Quadrilateral-ABCD,-Area={area}")
plt.show()
```

Python Code (nativecode.py)

```
import ctypes
import numpy as np
import matplotlib.pyplot as plt

lib = ctypes.CDLL("./code.so")
lib.area_of_quadrilateral.argtypes = [ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double, ctypes.c_double]
lib.area_of_quadrilateral.restype = ctypes.c_double
```

$$x1, y1 = -4, -5$$

$$x2, y2 = -1, -6$$

$$x3, y3 = -5, 7$$

$$x4, y4 = 4, 5$$

Python Code (nativecode.py)

```
"A": (x1, y1), "B": (x2, y2), "C": (x3, y3), "D": (x4, y4)}

for p, (x, y) in points.items():
    plt.text(x, y, f"{p}{(x,y)}")

plt.title(f"Quadrilateral-ABCD,-Area={area}")

plt.show()
```