

Matrices in Geometry 4.7.35

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Question: If the line drawn from the point $(-2, -1, -3)$ meets a plane at right angle at the point $(1, -3, 3)$, find the equation of the plane.

Solution: We have two points $\mathbf{A} = \begin{pmatrix} -2 \\ -1 \\ -3 \end{pmatrix}$ and $\mathbf{B} = \begin{pmatrix} 1 \\ -3 \\ 3 \end{pmatrix}$

We have to find the equation for the plane that passes through \mathbf{B} and is perpendicular to the line that joins \mathbf{A} and \mathbf{B} .

For that we first need the normal vector \mathbf{n} to this plane, which will be:

$$\mathbf{n} = \mathbf{Q} - \mathbf{P} \implies \mathbf{n} = \begin{pmatrix} 3 \\ -2 \\ 6 \end{pmatrix} \quad (1)$$

Therefore, the equation of this plane is given by

$$\mathbf{n}^T \mathbf{x} = d \quad (2)$$

Since the point \mathbf{B} lies on this plane, it should satisfy this equation.

$$\mathbf{n}^T \mathbf{B} = d \implies \begin{pmatrix} 3 & -2 & 6 \end{pmatrix} \begin{pmatrix} 1 \\ -3 \\ 3 \end{pmatrix} = d \implies d = 27 \quad (3)$$

Therefore, the equation of this plane is

$$\mathbf{n}^T \mathbf{x} = 27 \implies \begin{pmatrix} 3 & -2 & 6 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = 27 \implies 3x - 2y + 6z = 27 \quad (4)$$

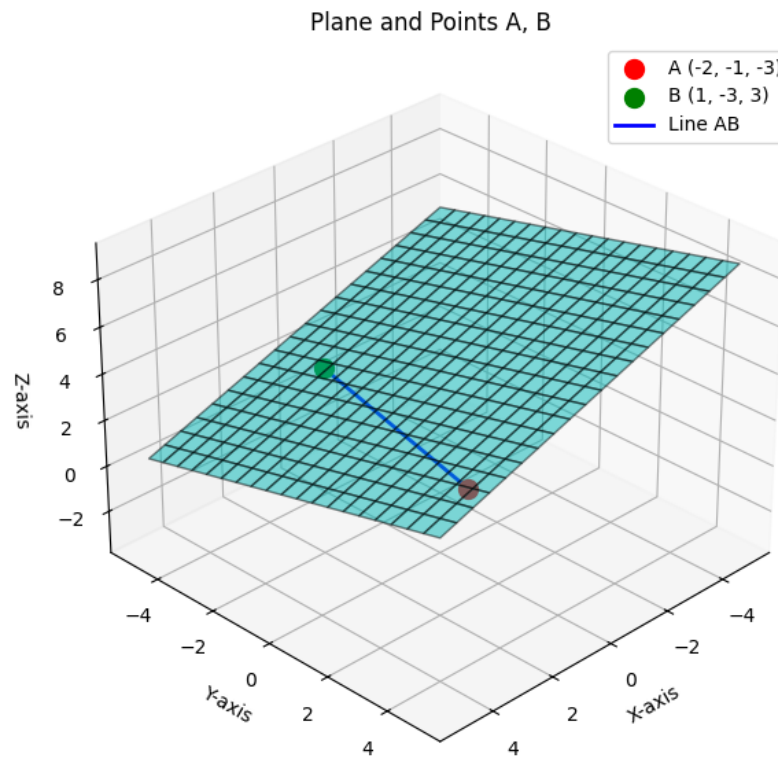


Fig. 1: Figure for 4.7.35