12.330

EE25BTECH11004 - Aditya Appana

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Question

If a weight of P = 100N is supported by two massless strings connected to the walls as shown in the figure, the value of T_1 is ______ N.

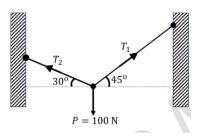


Figure 1: Figure

Solution

$$\mathbf{T_1} + \mathbf{T_2} = -\mathbf{P} \tag{1}$$

$$\mathbf{T_1} = ||T_1|| \begin{pmatrix} \cos 45^\circ \\ \sin 45^\circ \end{pmatrix} \tag{2}$$

$$\mathbf{T_1} + \mathbf{T_2} = -\mathbf{P}$$

$$\mathbf{T_1} = \|T_1\| \begin{pmatrix} \cos 45^{\circ} \\ \sin 45^{\circ} \end{pmatrix}$$

$$\mathbf{T_2} = \|T_2\| \begin{pmatrix} \cos 180 - 30^{\circ} \\ \sin 180 - 30^{\circ} \end{pmatrix} = \|T_2\| \begin{pmatrix} \cos 150^{\circ} \\ \sin 150^{\circ} \end{pmatrix}$$
(3)

$$\mathbf{P} = -\|P\| \begin{pmatrix} \cos -90^{\circ} \\ \sin -90^{\circ} \end{pmatrix} = -100 \begin{pmatrix} \cos(-90^{\circ}) \\ \sin(-90^{\circ}) \end{pmatrix}$$
(4)

Therefore:

$$||T_1|| \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix} + ||T_2|| \begin{pmatrix} -\frac{\sqrt{3}}{2} \\ \frac{1}{2} \end{pmatrix} = 100 \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$
 (5)

$$\begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{\sqrt{3}}{2} \\ \frac{1}{\sqrt{2}} & \frac{1}{2} \end{pmatrix} \begin{pmatrix} ||T_1|| \\ ||T_2|| \end{pmatrix} = \begin{pmatrix} 0 \\ 100 \end{pmatrix}$$
 (6)

Organising the data into an augmented matrix and obtaining RREF:

$$\begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{\sqrt{3}}{2} & 0\\ \frac{1}{\sqrt{2}} & \frac{1}{2} & 100 \end{pmatrix} \xrightarrow{R_2 \to R_2 - R_1} \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{\sqrt{3}}{2} & 0\\ 0 & \frac{1}{2} + \frac{\sqrt{3}}{2} & 100 \end{pmatrix}$$
(7)

$$||T_2|| = \frac{200}{1 + \sqrt{3}} = 73.205N \tag{8}$$

$$||T_1|| = \frac{\sqrt{3}}{\sqrt{2}} ||T_2|| = 89.658N \tag{9}$$

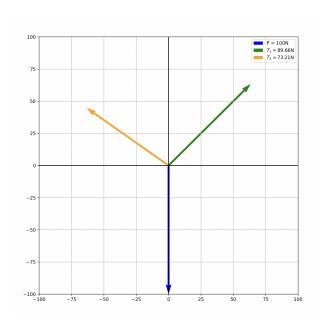


Figure 2: Plot