

5.4.22

INDHIRESH S- EE25BTECH11027

Question. Using elementary transformations, find the inverse of the following matrices

$$\begin{pmatrix} 6 & -3 \\ -2 & 1 \end{pmatrix}$$

Solution:

Let the given matrix be:

$$\mathbf{A} = \begin{pmatrix} 6 & -3 \\ -2 & 1 \end{pmatrix} \quad (1)$$

Now finding the inverse of a matrix by elementary operation.

Now forming the augmented matrix $[\mathbf{A}|\mathbf{I}]$

$$[\mathbf{A}|\mathbf{I}] = \left(\begin{array}{cc|cc} 6 & -3 & 1 & 0 \\ -2 & 1 & 0 & 1 \end{array} \right) \quad (2)$$

$$\left(\begin{array}{cc|cc} 6 & -3 & 1 & 0 \\ -2 & 1 & 0 & 1 \end{array} \right) \xleftrightarrow{R_2 \leftarrow R_2 + \frac{1}{3}R_1} \left(\begin{array}{cc|cc} 6 & -3 & 1 & 0 \\ 0 & 0 & \frac{1}{3} & 1 \end{array} \right) \quad (3)$$

From above we can observe that the rank of the left-side augmented matrix is 1

Therefore the matrix \mathbf{A} is singular and hence the inverse does not exist for the given matrix