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# Matgeo-2.2.20

## AI25BTECH11027 - NAGA BHUVANA

### **Question:**

If the co-ordinates of the points A, B, C, D be (1,2,3),(4,5,7),(-4,3,-6) and (2,9,2) respectively, then find the angle between lines AB and CD.

#### **Solution:**

Let

$$\mathbf{A} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 4 \\ 5 \\ 7 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} -4 \\ 3 \\ -6 \end{pmatrix} \text{ and } \mathbf{D} = \begin{pmatrix} 2 \\ 9 \\ 2 \end{pmatrix}$$
 (1)

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 4 \\ 5 \\ 7 \end{pmatrix} - \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix} = \begin{pmatrix} 3 \\ 3 \\ 4 \end{pmatrix} \tag{2}$$

$$\mathbf{D} - \mathbf{C} = \begin{pmatrix} 2 \\ 9 \\ 2 \end{pmatrix} - \begin{pmatrix} -4 \\ 3 \\ -6 \end{pmatrix} = \begin{pmatrix} 6 \\ 6 \\ 8 \end{pmatrix} \tag{3}$$

Let the angle between  $\mathbf{B} - \mathbf{A}$  and  $\mathbf{D} - \mathbf{C}$  be  $\theta$ 

$$\cos \theta = \frac{\left(B - A\right)^{T} \left(D - C\right)}{\|\mathbf{B} - \mathbf{A}\|\|\mathbf{D} - \mathbf{C}\|} \tag{4}$$

$$\cos \theta = \frac{\left(3 \quad 3 \quad 4\right) \begin{pmatrix} 6\\6\\8 \end{pmatrix}}{\sqrt{34}\sqrt{136}} \tag{5}$$

$$\cos \theta = \frac{(3)(6) + (3)(6) + (4)(8)}{68} \tag{6}$$

$$\cos \theta = \frac{68}{68} \tag{7}$$

$$\cos \theta = 1 \tag{8}$$

$$\theta = 0^{\circ} \tag{9}$$

 $\therefore$  The angle between lines  $(\mathbf{B} - \mathbf{A})$  and  $(\mathbf{D} - \mathbf{C})$  is  $0^{\circ}$  (Collinear lines)

## Lines AB and CD in 3D

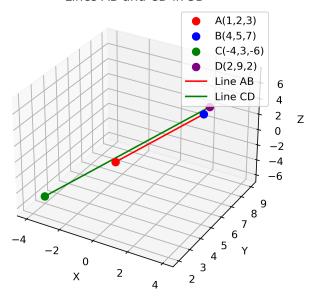


Fig. 1