

Matgeo-2.7.11

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Question

Q 2.7.11. Find the area of the triangle with vertices $A = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$,
 $B = \begin{pmatrix} -4 \\ 6 \end{pmatrix}$, $C = \begin{pmatrix} -3 \\ -5 \end{pmatrix}$.

Solution

Given: The vertices of the triangle are

$$A = \begin{pmatrix} 1 \\ -1 \end{pmatrix}, \quad B = \begin{pmatrix} -4 \\ 6 \end{pmatrix}, \quad C = \begin{pmatrix} -3 \\ -5 \end{pmatrix}.$$

The area of a triangle with vertices A, B, C is given by

$$\Delta = \frac{1}{2} |\det((B - A \quad C - A))| = \frac{1}{2} \|(B - A) \times (C - A)\|,$$

where the cross product in 2D is interpreted as the determinant of a 2×2 matrix.

$$B - A = \begin{pmatrix} -4 \\ 6 \end{pmatrix} - \begin{pmatrix} 1 \\ -1 \end{pmatrix} = \begin{pmatrix} -5 \\ 7 \end{pmatrix}, \quad C - A = \begin{pmatrix} -3 \\ -5 \end{pmatrix} - \begin{pmatrix} 1 \\ -1 \end{pmatrix} = \begin{pmatrix} -4 \\ -4 \end{pmatrix}.$$

Now,

$$\det \begin{pmatrix} -5 & -4 \\ 7 & -4 \end{pmatrix} = (-5)(-4) - (7)(-4) = 20 + 28 = 48.$$

Solution

Hence,

$$\Delta = \frac{1}{2} |48| = 24.$$

Final Answer:

24

Plot

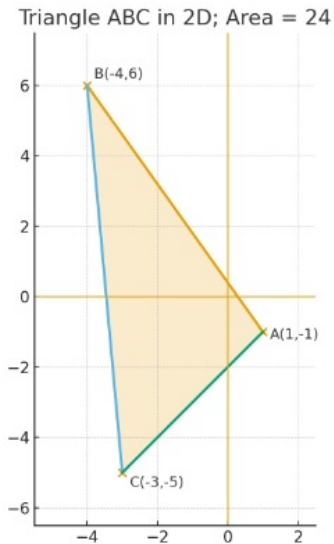


Figure: Triangle ABC with $A(1, -1)$, $B(-4, 6)$, $C(-3, -5)$; area = 24.