MatGeo Assignment - Problem 1.5.12

EE25BTECH11024

IIT Hyderabad

September 15, 2025

Problem Statement

In what ratio does the point P(-4, y) divide the line segment joining A(-6, 10) and B(3, -8)? Hence, find the value of y.

Solution: Using the Rank Criterion

We are given three points:

$$A = \begin{pmatrix} -6\\10 \end{pmatrix}, \quad P = \begin{pmatrix} -4\\y \end{pmatrix}, \quad B = \begin{pmatrix} 3\\-8 \end{pmatrix} \tag{1}$$

The points A, P, B are collinear if

$$\mathsf{rank}\big(\begin{pmatrix} P-A & B-A \end{pmatrix}\big) = 1 \tag{2}$$

Thus, the matrix is

$$M = \begin{pmatrix} 2 & 9 \\ y - 10 & -18 \end{pmatrix} \tag{3}$$

Perform the row operations: $R_1 \leftarrow R_1/2$ and $R_2 \leftarrow R_2 - R_1(y-10)$ which results in

Solution:

$$\begin{pmatrix} 1 & 9/2 \\ 0 & -9/2(y-6) \end{pmatrix} \tag{4}$$

If y is not equal to 6, then we perform $R_2 \leftarrow R_2/(-9/2(y-6))$ to get an identity matrix. But then the rank will be 2

For the rank to be 1, the second row must be all zeros:

$$y - 6 = 0 \implies y = 6$$

Using the vector formula,

$$k = \frac{(\mathbf{A} - \mathbf{P})^{\top} (\mathbf{P} - \mathbf{B})}{\|\mathbf{P} - \mathbf{B}\|^2}$$
 (5)

Substitute y = 6: Compute the numerator:

$$(\mathbf{A} - \mathbf{P})^{\top} (\mathbf{P} - \mathbf{B}) = (-2)(-7) + (4)(14) = 14 + 56 = 70$$
 (6)

Solution:

Compute the denominator:

$$\|\mathbf{P} - \mathbf{B}\|^2 = (-7)^2 + (14)^2 = 49 + 196 = 245$$
 (7)

Thus,

$$k = \frac{70}{245} = \frac{2}{7} \tag{8}$$

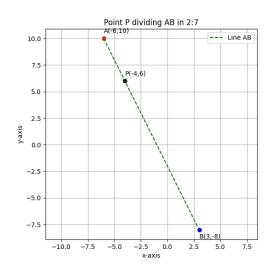
Therefore,

$$y=6, \quad k=\frac{2}{7} \tag{9}$$

See the graphical representation in Figure 1.



Resulting Graph



Python Code: plot.py (Native)

```
import numpy as np
import matplotlib.pyplot as plt
# Given points
A = np.array([-6, 10])
B = np.array([3, -8])
P = np.array([-4, 6]) # Found from calculation
# Plotting
plt.figure(figsize=(6,6))
plt.plot([A[0], B[0]], [A[1], B[1]], 'g--', label="Line AB")
plt.scatter(*A, color="red")
plt.scatter(*B, color="blue")
plt.scatter(*P, color="black")
# Labels
plt.text(A[0], A[1]+0.5, "A(-6,10)", fontsize=10)
plt.text(B[0], B[1]-0.8, "B(3,-8)", fontsize=10)
plt.text(P[0], P[1]+0.5, "P(-4.6)", fontsize=10)
```

Python Code (Native Implementation – plot.py)

```
plt.xlabel("x-axis")
plt.ylabel("y-axis")
plt.title("Point P dividing AB in 2:7")
plt.legend()
plt.grid(True)
plt.axis("equal")
plt.savefig("fig.png")
plt.show()
```

C Code (Shared Library – find point.c)

```
#include <stdio.h>
void find_point(double *px, double *py) {
    // A(-6,10), B(3,-8)
    double x1 = -6, y1 = 10, x2 = 3, y2 = -8;
    int m = 2, n = 7; // ratio

    *px = (m*x2 + n*x1) / (m+n);
    *py = (m*y2 + n*y1) / (m+n);
}
```

Python Code: call.py (C + Python)

```
import ctypes
import numpy as np
import matplotlib.pyplot as plt
# Load shared object
so = ctypes.CDLL("./find_point.so")
# Prepare arguments
px = ctypes.c_double()
py = ctypes.c_double()
so.find_point(ctypes.byref(px), ctypes.byref(py))
A = np.array([-6, 10])
B = np.array([3, -8])
P = np.array([px.value, py.value])
# Plot
plt.figure(figsize=(6,6))
plt.plot([A[0], B[0]], [A[1], B[1]], 'g--', label="Line
                                                              4 3 b 3 € 40 Q (
```

Python Code (C Integrated – call.py)

```
plt.scatter(*A, color="red")
plt.scatter(*B, color="blue")
plt.scatter(*P, color="black")
plt.text(A[0], A[1]+0.5, "A(-6,10)", fontsize=10)
plt.text(B[0], B[1]-0.8, "B(3,-8)", fontsize=10)
plt.text(P[0], P[1]+0.5, f"P({px.value:.1f},{py.value:.1f})", fontsize
    =10)
plt.xlabel("x-axis")
plt.ylabel("y-axis")
plt.title("Point P from C code")
plt.legend()
plt.grid(True)
plt.axis("equal")
plt.show()
```