

Problem 4.11.1

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Problem

Find the coordinates of the point where the line $\frac{x-1}{3} = \frac{y+4}{7} = \frac{z+4}{2}$ cuts the XY-plane

Declaration of variables

The line equation is

$$\mathbf{r} = \mathbf{a} + t\mathbf{b} \quad (1.1)$$

where \mathbf{a} is the point on line and \mathbf{b} is the direction vector

$$\mathbf{a} = \begin{pmatrix} 1 \\ -4 \\ -4 \end{pmatrix} \text{ and } \mathbf{b} = \begin{pmatrix} 3 \\ 7 \\ 2 \end{pmatrix} \quad (1.2)$$

The normal vector to XY plane is

$$\mathbf{n} = \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \quad (1.3)$$

The plane equation of the XY-plane is

$$\mathbf{n}^T \mathbf{x} = 0 \implies \begin{pmatrix} 0 & 0 & 1 \end{pmatrix} \mathbf{x} = 0 \quad (1.4)$$

Solving

Substituting the line into the plane equation gives

$$\mathbf{n}^T (\mathbf{a} + t\mathbf{b}) = 0 \quad (1.5)$$

$$\mathbf{n}^T \mathbf{a} + t (\mathbf{n}^T \mathbf{b}) = 0 \quad (1.6)$$

$$t (\mathbf{n}^T \mathbf{b}) = -\mathbf{n}^T \mathbf{a} \quad (1.7)$$

$$t = -\frac{\mathbf{n}^T \mathbf{a}}{\mathbf{n}^T \mathbf{b}} \quad (1.8)$$

$$t = -\frac{\begin{pmatrix} 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 \\ -4 \\ -4 \end{pmatrix}}{\begin{pmatrix} 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 3 \\ 7 \\ 2 \end{pmatrix}} = -\frac{-4}{2} \quad (1.9)$$

$$\implies t = 2 \quad (1.10)$$

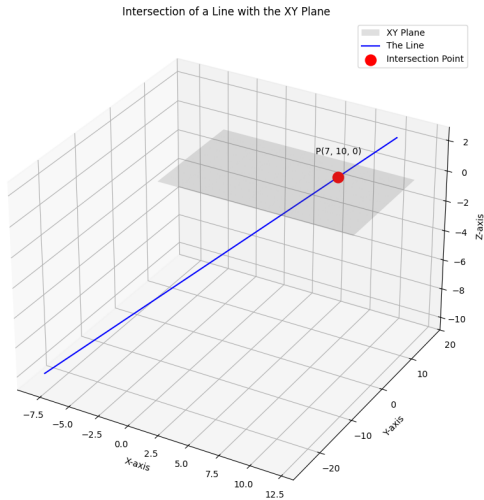
Conclusion

The intersection point is

$$\mathbf{r} = \mathbf{a} + t\mathbf{b} = \begin{pmatrix} 1 \\ -4 \\ -4 \end{pmatrix} + 2 \begin{pmatrix} 3 \\ 7 \\ 2 \end{pmatrix} \quad (1.11)$$

$$\mathbf{r} = \begin{pmatrix} 7 \\ 10 \\ 0 \end{pmatrix} \quad (1.12)$$

Plot



C Code

```
void get_intersection_data(double* out_data) {
    double point_a[3] = {1.0, -4.0, -4.0};
    double dir_d[3] = {3.0, 7.0, 2.0};
    double lambda = 2.0;

    double Px = point_a[0] + lambda * dir_d[0];
    double Py = point_a[1] + lambda * dir_d[1];
    double Pz = point_a[2] + lambda * dir_d[2];

    out_data[0] = Px;
    out_data[1] = Py;
    out_data[2] = Pz;
    out_data[3] = point_a[0];
    out_data[4] = point_a[1];
    out_data[5] = point_a[2];
    out_data[6] = dir_d[0];
    out_data[7] = dir_d[1];
    out_data[8] = dir_d[2];
}
```


Python Code for Calling

```
import ctypes
import numpy as np

def get_line_data_from_c():

    lib = ctypes.CDLL('./coord.so')
    double_array_9 = ctypes.c_double * 9
    lib.get_intersection_data.argtypes = [ctypes.POINTER(ctypes.
        c_double)]

    out_data_c = double_array_9()
    lib.get_intersection_data(out_data_c)
    all_data = np.array(out_data_c)
    # Split the data into the three vectors
    intersection_P = all_data[0:3]
    point_a = all_data[3:6]
    dir_d = all_data[6:9]

    return intersection_P, point_a, dir_d
```

Python Code for Plotting

```
#Code by GVV Sharma
#September 12, 2023
#Revised July 21, 2024
#released under GNU GPL
import sys #for path to external scripts
sys.path.insert(0, '/workspaces/urban-potato/matgeo/codes/
    CoordGeo/')
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

#local imports
from line.funcs import *
from triangle.funcs import *

from call import get_line_data_from_c
```

Python Code for Plotting

```
# Get the intersection point P, and the line's defining vectors a  
and d  
P, point_a, dir_d = get_line_data_from_c()  
print(f"Intersection Point: ({P[0]:.0f}, {P[1]:.0f}, {P[2]:.0f})"  
      )  
  
lambda_vals = np.array([-3, 3])  
line_points = point_a + lambda_vals[:, np.newaxis] * dir_d  
  
a_plane, b_plane, c_plane, d_plane = 0, 0, 1, 0  
x = np.linspace(-4, 12, 10)  
y = np.linspace(-5, 15, 10)  
X_plane, Y_plane = np.meshgrid(x, y)  
  
Z_plane = (-a_plane * X_plane - b_plane * Y_plane - d_plane) /  
           c_plane  
  
fig = plt.figure(figsize=(10, 10))  
ax = fig.add_subplot(111, projection='3d')
```

Python Code for Plotting

```
ax.plot_surface(X_plane, Y_plane, Z_plane, alpha=0.2, color='gray',
               label='XY Plane')
ax.plot(line_points[:, 0], line_points[:, 1], line_points[:, 2],
       'b-', label='The Line')
ax.scatter(P[0], P[1], P[2], color='red', s=150, label='Intersection Point')
ax.text(P[0], P[1], P[2] + 1.5, f'P({P[0]:.0f}, {P[1]:.0f}, {P[2]:.0f})',
       ha='center')

ax.set_title('Intersection of a Line with the XY Plane')
ax.set_xlabel('X-axis')
ax.set_ylabel('Y-axis')
ax.set_zlabel('Z-axis')

ax.legend()
ax.grid(True)
plt.show()
plt.savefig('../figs/fig1.png')
```