## 4.3.36

## Puni Aditya - EE25BTECH11046

**Question:** 

The line  $\mathbf{r} = (2\hat{i} - 3\hat{j} - \hat{k}) + \lambda(\hat{i} - \hat{j} + 2\hat{k})$  lies in the plane  $\mathbf{r} \cdot (3\hat{i} + \hat{j} - \hat{k}) + 2 = 0$ .

## **Solution:**

Let the line L be  $\mathbf{r} = \mathbf{a} + \lambda \mathbf{b}$  and the plane P be  $\mathbf{r}^{\mathsf{T}} \mathbf{n} = c$  where

$$\mathbf{a} = \begin{pmatrix} 2 \\ -3 \\ -1 \end{pmatrix}, \mathbf{b} = \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix}, \mathbf{n} = \begin{pmatrix} 3 \\ 1 \\ -1 \end{pmatrix}, \mathbf{c} = -2$$

$$\mathbf{b}^{\mathsf{T}}\mathbf{n} = \begin{pmatrix} 1 & -1 & 2 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ -1 \end{pmatrix} \tag{1}$$

$$= (1)(3) + (-1)(1) + (2)(-1)$$
 (2)

1

$$= 3 - 1 - 2 \tag{3}$$

$$\mathbf{b}^{\mathsf{T}}\mathbf{n} = 0 \tag{4}$$

 $\mathbf{b}^{\mathsf{T}}\mathbf{n} = 0$ , the line L is parallel to plane P.

$$\mathbf{a}^{\mathsf{T}}\mathbf{n} = \begin{pmatrix} 2 & -3 & -1 \end{pmatrix} \begin{pmatrix} 3 \\ 1 \\ -1 \end{pmatrix} \tag{5}$$

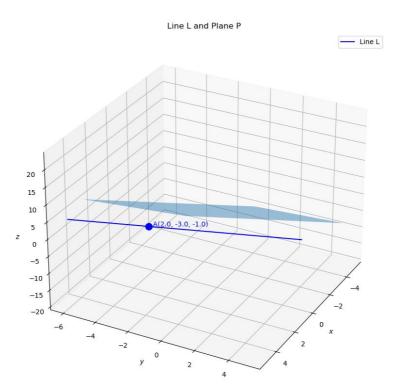
$$= (2)(3) + (-3)(1) + (-1)(-1)$$
(6)

$$= 6 - 3 + 1 \tag{7}$$

$$= 4 \neq c \tag{8}$$

 $\mathbf{a}^{\mathsf{T}}\mathbf{n} \neq c$ , the point **a** doesn't line in the plane P. Hence, the line L containing **a** also doesn't lie in the plane.

The given statement is false.



Plot