

2.10.30

EE25BTECH11001 - Aarush Dilawri

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Solution

We have position vectors

$$\mathbf{A} = \begin{pmatrix} 60 \\ 3 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 40 \\ -6 \end{pmatrix}, \quad \mathbf{C} = \begin{pmatrix} a \\ -52 \end{pmatrix}. \quad (1)$$

Now,

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} -20 \\ -9 \end{pmatrix}, \quad (2)$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} a - 60 \\ -55 \end{pmatrix}. \quad (3)$$

Solution

For collinearity, we require

$$\text{rank} \begin{pmatrix} \mathbf{B} - \mathbf{A} & \mathbf{C} - \mathbf{A} \end{pmatrix} = 1 \quad (4)$$

$$\text{rank} \begin{pmatrix} -20 & a - 60 \\ -9 & -55 \end{pmatrix} = 1 \quad (5)$$

$$R_2 \rightarrow R_1 - \frac{20}{9}R_2 \quad (6)$$

$$\begin{pmatrix} -20 & a-60 \\ -9 & -55 \end{pmatrix} R_2 \rightarrow R_1 - \frac{20}{9}R_2 \quad \begin{pmatrix} -20 & a-60 \\ 0 & a + \frac{560}{9} \end{pmatrix} \quad (7)$$

$$\text{rank} \begin{pmatrix} -20 & a-60 \\ 0 & a + \frac{560}{9} \end{pmatrix} = 1 \quad (8)$$

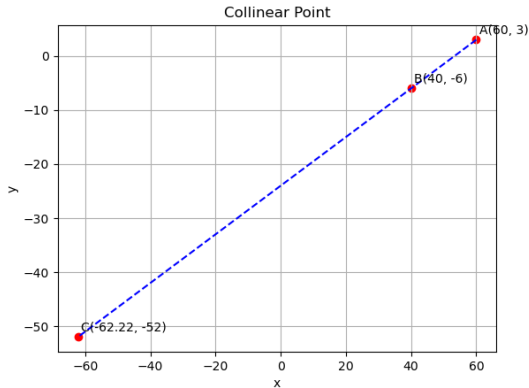
Solution

Therefore, equating the last row to 0, we have

$$a + \frac{560}{9} = 0 \implies a = -\frac{560}{9} \quad (9)$$

Therefore, the answer is (d) None of these.

Figure



C Code (code.c)

```
#include <stdio.h>

double find_a(double x1, double y1, double x2, double y2, double y3) {
    double u1 = x2 - x1;
    double u2 = y2 - y1;
    double v2 = y3 - y1;

    double lambda = v2 / u2;

    double a = x1 + lambda * u1;
    return a;
}
```


Python Code (code.py)

```
import numpy as np
import matplotlib.pyplot as plt
```

```
x1, y1 = 60, 3
x2, y2 = 40, -6
y3 = -52
```

```
u1, u2 = (x2 - x1), (y2 - y1)
lambda_val = (y3 - y1) / u2
a = x1 + lambda_val * u1
print("Value of a=", a)
```

```
A = np.array([x1, y1])
B = np.array([x2, y2])
C = np.array([a, y3])
```

Python Code (code.py)

```
plt.scatter([A[0], B[0], C[0]], [A[1], B[1], C[1]], color="blue")

plt.text(A[0] + 1, A[1] + 1, "A(60,-3)", fontsize=10, color="black")
plt.text(B[0] + 1, B[1] + 1, "B(40,-6)", fontsize=10, color="black")
plt.text(C[0] + 1, C[1] + 1, f"C({a:.2f},{-52})", fontsize=10, color="black")

plt.plot([A[0], B[0], C[0]], [A[1], B[1], C[1]], linestyle="--", color="red")

plt.xlabel("x")
plt.ylabel("y")
plt.title("Collinear-Points")
plt.grid(True)
plt.show()
```

Python Code (nativecode.py)

```
import ctypes
import numpy as np
import matplotlib.pyplot as plt

lib = ctypes.CDLL("./code.so")
lib.find_a.argtypes = [ctypes.c_double, ctypes.c_double,
                       ctypes.c_double, ctypes.c_double,
                       ctypes.c_double]
lib.find_a.restype = ctypes.c_double

x1, y1 = 60, 3
x2, y2 = 40, -6
y3 = -52

a = lib.find_a(x1, y1, x2, y2, y3)
print("Value of a=", a)
```

Python Code (nativecode.py)

```
plt.scatter([A[0], B[0], C[0]], [A[1], B[1], C[1]], color="red")

plt.text(A[0] + 1, A[1] + 1, "A(60,-3)", fontsize=10, color="black")
plt.text(B[0] + 1, B[1] + 1, "B(40,-6)", fontsize=10, color="black")
plt.text(C[0] + 1, C[1] + 1, f"C({a:.2f},-52)", fontsize=10, color="black")

plt.plot([A[0], B[0], C[0]], [A[1], B[1], C[1]], linestyle="--", color="blue")

plt.xlabel("x")
plt.ylabel("y")
plt.title("Collinear-Points")
plt.grid(True)
plt.show()
```