

4.8.23

AI25BTECH11027 - NAGA BHUVANA

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Question:

Find the values of λ , for which the distance of point $(2, 1, \lambda)$ from plane $3x + 5y + 4z = 11$ is $2\sqrt{2}$ units.

Solution:

The normal vector of the plane is $\begin{pmatrix} 3 \\ 5 \\ 4 \end{pmatrix}$ and $\mathbf{P} = \begin{pmatrix} 2 \\ 1 \\ \lambda \end{pmatrix}$

The equation of the plane be $\mathbf{n}^T \mathbf{x} = 1$

$$distance = \frac{|\mathbf{n}^T \mathbf{p} - 1|}{\|\mathbf{n}\|} \quad (0.1)$$

$$2\sqrt{2} = \frac{|(3 \ 5 \ 4) \begin{pmatrix} 2 \\ 1 \\ \lambda \end{pmatrix} - 1|}{5\sqrt{2}} \quad (0.2)$$

$$\frac{|10 + 4\lambda|}{5\sqrt{2}} = 2\sqrt{2} \quad (0.3)$$

$$|10 + 4\lambda| = 20 \quad (0.4)$$

$$10 + 4\lambda = 20 \quad \text{or} \quad 10 + 4\lambda = -20 \quad (0.5)$$

$$4\lambda = 10 \quad \text{or} \quad 4\lambda = -30 \quad (0.6)$$

$$\lambda = \frac{5}{2} \quad \text{or} \quad -\frac{15}{2} \quad (0.7)$$

∴ The values of $\lambda = \frac{5}{2}$ or $-\frac{15}{2}$