

## 1.10.7

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# Question

Find a unit vector in the direction of the vector  $PQ$ , where  $P$  and  $Q$  have co-ordinates  $(5,0,8)$  and  $(3,3,2)$ , respectively.

# Theoretical Solution

Given,

The points:

$$\mathbf{P} = \begin{pmatrix} 5 \\ 0 \\ 8 \end{pmatrix} \quad \mathbf{Q} = \begin{pmatrix} 3 \\ 3 \\ 2 \end{pmatrix} \quad (1)$$

Let the required unit vector be  $\mathbf{x}$ , then

The formula for unit vector along a line joining two points

$$\mathbf{x} = \frac{\mathbf{X}}{\|\mathbf{X}\|} \quad (2)$$

The vector along  $\mathbf{P}$  and  $\mathbf{Q}$  is

$$\mathbf{X} = \mathbf{Q} - \mathbf{P} \quad (3)$$

# Theoretical Solution

$$\mathbf{X} = \begin{pmatrix} 5 \\ 0 \\ 8 \end{pmatrix} - \begin{pmatrix} 3 \\ 3 \\ 2 \end{pmatrix} \quad (4)$$

$$\mathbf{X} = \begin{pmatrix} 5 - 3 \\ 0 - 3 \\ 8 - 2 \end{pmatrix} \quad (5)$$

$$\mathbf{X} = \begin{pmatrix} 2 \\ -3 \\ 6 \end{pmatrix} \quad (6)$$

Magnitude of the vector  $\mathbf{X}$  is

$$\|\mathbf{X}\| = \sqrt{\mathbf{X}^T \mathbf{X}} \quad (7)$$

# Theoretical Solution

$$\|\mathbf{X}\| = \sqrt{(2, -3, 6) \begin{pmatrix} 2 \\ -3 \\ 6 \end{pmatrix}} \quad (8)$$

$$\|\mathbf{X}\| = \sqrt{(2)^2 + (-3)^2 + (6)^2} \quad (9)$$

$$\|\mathbf{X}\| = \sqrt{49} \quad (10)$$

$$\|\mathbf{X}\| = 7 \quad (11)$$

# Theoretical Solution

Then the unit vector,

$$\mathbf{x} = \frac{1}{7} (\mathbf{X}) = \frac{1}{7} \begin{pmatrix} 2 \\ -3 \\ 6 \end{pmatrix} \quad (12)$$

$$\mathbf{x} = \frac{1}{7} \begin{pmatrix} 2 \\ -3 \\ 6 \end{pmatrix} \quad (13)$$

$$\mathbf{x} = \left( \frac{2}{7}, \frac{-3}{7}, \frac{6}{7} \right) \quad (14)$$

Therefore the required unit vector is

$$\mathbf{x} = \left( \frac{2}{7}, \frac{-3}{7}, \frac{6}{7} \right)$$

# C Code- Computing the unit vector

```
// file: unitvec3d.c
#include <math.h>

#ifdef _WIN32
#define API __declspec(dllexport)
#else
#define API
#endif

// Compute unit vector from P to Q in 3D
// Inputs: P[3], Q[3]
// Output: unit[3]
// Returns: 0 on success, -1 if P=Q
```



# C Code - Computing the unit vector

```
API int unit_vector_3d(const double* P, const double* Q,  
    double* unit) {  
    double dx = Q[0] - P[0];  
    double dy = Q[1] - P[1];  
    double dz = Q[2] - P[2];  
    double norm = sqrt(dx*dx + dy*dy + dz*dz);  
    if (norm == 0.0) return -1;  
    unit[0] = dx / norm;  
    unit[1] = dy / norm;  
    unit[2] = dz / norm;  
    return 0;  
}
```

# Python Code using shared output

```
import ctypes, os, math
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

# Load library
if os.name == 'nt':
    libname = 'unitvec3d.dll'
else:
    libname = './libunitvec3d.so'
lib = ctypes.CDLL(libname)

# Function signature
lib.unit_vector_3d.argtypes = [
    ctypes.POINTER(ctypes.c_double),
    ctypes.POINTER(ctypes.c_double),
    ctypes.POINTER(ctypes.c_double),
]
```

# Python Code using shared output

```
lib.unit_vector_3d.restype = ctypes.c_int

def unit_vector_from_c(P, Q):
    P_arr = (ctypes.c_double * 3)(*P)
    Q_arr = (ctypes.c_double * 3)(*Q)
    U_arr = (ctypes.c_double * 3)()
    ret = lib.unit_vector_3d(P_arr, Q_arr, U_arr)
    if ret != 0:
        raise ValueError(P and Q coincide.)
    return [U_arr[0], U_arr[1], U_arr[2]]

# Example points
P = (5.0, 0.0, 8.0)
Q = (3.0, 3.0, 2.0)
```

# Python Code using shared output

```
# Get unit vector
u = unit_vector_from_c(P, Q)
PQ = [Q[i]-P[i] for i in range(3)]
print(Unit vector:, u)

# --- Plot ---
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')

# Plot points
ax.scatter(*P, color=red, s=60, label=P)
ax.scatter(*Q, color=blue, s=60, label=Q)

# Vector PQ
ax.quiver(P[0], P[1], P[2], PQ[0], PQ[1], PQ[2], color=green,
          label=PQ)
```

# Python Code using shared output

```
        # Unit vector (length 1)
ax.quiver(P[0], P[1], P[2], u[0], u[1], u[2], color=orange, label
          =Unit vector)

ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
ax.legend()
plt.show()
```

# Plot by python using shared output from c

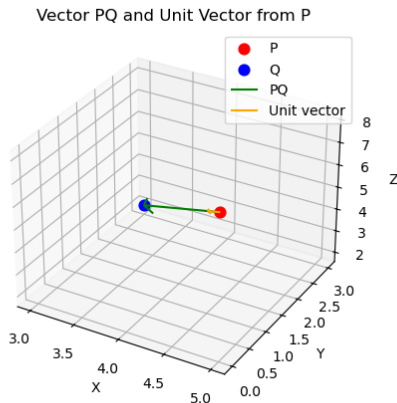


Figure: Plot of the unit vector along PQ

# Python code for the plot

```
import math
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

def unit_vector(P, Q):
    Compute unit vector from P to Q in 3D.
    dx, dy, dz = Q[0]-P[0], Q[1]-P[1], Q[2]-P[2]
    norm = math.sqrt(dx*dx + dy*dy + dz*dz)
    if norm == 0:
        raise ValueError(P and Q are the same point, unit vector
                           undefined.)
    return (dx/norm, dy/norm, dz/norm)

# Example points
P = (5, 0, 8)
Q = (3, 3, 2)
```

# Python code for the plot

```
# Compute vector PQ and unit vector
PQ = (Q[0]-P[0], Q[1]-P[1], Q[2]-P[2])
u = unit_vector(P, Q)

print(Vector PQ =, PQ)
print(Unit vector =, u)

# --- Plot ---
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')

# Plot points
ax.scatter(*P, color=red, s=60, label=P)
ax.scatter(*Q, color=blue, s=60, label=Q)

# Vector PQ (green arrow)
ax.quiver(P[0], P[1], P[2], PQ[0], PQ[1], PQ[2],
          color=green, label=PQ, arrow_length_ratio=0.1)
```



# Python code for plot

```
# Unit vector (orange arrow, length 1)
ax.quiver(P[0], P[1], P[2], u[0], u[1], u[2],
          color=orange, label=Unit vector, arrow_length_ratio=0.2)

# Labels and aesthetics
ax.set_xlabel(X)
ax.set_ylabel(Y)
ax.set_zlabel(Z)
ax.legend()
ax.set_title(Vector PQ and Unit Vector from P)
ax.grid(True)

plt.show()
```

### Vector PQ and Unit Vector from P

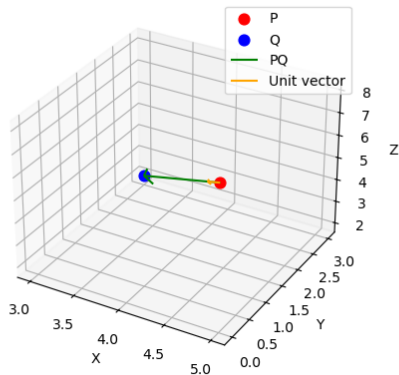


Figure: Plot for the unit vector along PQ