Matgeo-4.13.4

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Question

Q-4.13.4 Solve the simultaneous linear equations

$$5u - 4v + 8 = 0$$
, $7u + 6v - 9 = 0$.

Solution

$$5u - 4v = -8 \tag{1}$$

$$7u + 6v = 9 \tag{2}$$

Writing in matrix form,

$$\begin{pmatrix} 5 & -4 \\ 7 & 6 \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} -8 \\ 9 \end{pmatrix} \tag{3}$$

Augmented matrix,

$$\begin{pmatrix}
5 & -4 & -8 \\
7 & 6 & 9
\end{pmatrix}$$

(4)

Row operation: $R_2 \rightarrow 5R_2 - 7R_1$,

$$\begin{pmatrix} 5 & -4 & -8 \\ 0 & 58 & 101 \end{pmatrix}$$

(5)

Normalize second row: $R_2 \rightarrow \frac{R_2}{58}$,

Solution

$$\begin{pmatrix} 5 & -4 & -8 \\ 0 & 1 & \frac{101}{58} \end{pmatrix}$$

Eliminate above: $R_1 \rightarrow R_1 + 4R_2$,

$$\begin{pmatrix}
5 & 0 & -\frac{30}{29} \\
0 & 1 & \frac{101}{58}
\end{pmatrix}$$

Normalize first row: $R_1 \rightarrow \frac{R_1}{5}$,

$$\begin{pmatrix}
1 & 0 & -\frac{6}{29} \\
0 & 1 & \frac{101}{58}
\end{pmatrix}$$

(6)

(7)

(8)

Solution

Thus, the solution vector is

Plot

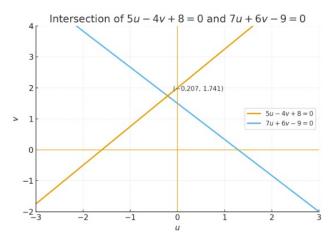


Figure: Intersection of 5u - 4v + 8 = 0 and 7u + 6v - 9 = 0 at $\left(-\frac{6}{29}, \frac{101}{58}\right)$.