## 1.7.4

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September 8,2025

### Question

Using vectors, prove that the points (2,-1,3), (3,-5,1), and (-1,11,9) are collinear.

### Theoretical Solution

#### **Solution:**

Let 
$$\mathbf{A} \begin{pmatrix} 2 \\ -1 \\ 3 \end{pmatrix} \mathbf{B} \begin{pmatrix} 3 \\ -5 \\ 1 \end{pmatrix} \mathbf{C} \begin{pmatrix} -1 \\ 11 \\ 9 \end{pmatrix}$$
 be vectors Points  $\mathbf{A}, \mathbf{B}, \mathbf{C}$  are defined to be collinear if

$$rank(\mathbf{B} - \mathbf{A} \quad \mathbf{C} - \mathbf{A}) = 1$$
  
 $rank\mathbf{A} = rank\mathbf{A}^T$ 

$$\mathbf{A}^{\mathsf{T}} = \begin{pmatrix} 1 & -4 & -2 \\ -3 & 12 & 6 \end{pmatrix}$$

$$R_2 = R_2 + 3R_2$$

#### Theoretical Solution

$$\mathbf{A}^T = \begin{pmatrix} 1 & -4 & -2 \\ 0 & 0 & 0 \end{pmatrix}$$

 $\mathbf{A}^T = \begin{pmatrix} 1 & -4 & -2 \\ 0 & 0 & 0 \end{pmatrix}$  which has rank 1.So we can conclude that the given points are collinear.

#### C Code

```
#include <stdio.h>
// Function to compute cross product of two vectors in 3D
void crossProduct(int v1[3], int v2[3], int cross[3]) {
   cross[0] = v1[1]*v2[2] - v1[2]*v2[1];
   cross[1] = v1[2]*v2[0] - v1[0]*v2[2];
   cross[2] = v1[0]*v2[1] - v1[1]*v2[0];
// Function to check if three points are collinear in 3D
int areCollinear(int A[3], int B[3], int C[3]) {
    int AB[3], AC[3], cross[3];
   for (int i = 0; i < 3; i++) {
       AB[i] = B[i] - A[i];
       AC[i] = C[i] - A[i]:
   }
```

#### C Code

```
crossProduct(AB, AC, cross);
   return (cross[0] == 0 && cross[1] == 0 && cross[2] == 0);
int main() {
    int A[3] = \{2, -1, 3\};
   int B[3] = \{3, -5, 1\};
    int C[3] = \{-1, 11, 9\};
   if (areCollinear(A, B, C))
       printf("The points are collinear.\n");
   else
       printf("The points are not collinear.\n");
   return 0;
```

# Python Code

```
import matplotlib.pyplot as plt
 from mpl toolkits.mplot3d import Axes3D
 import numpy as np
 # Points
 A = np.array([2, -1, 3])
B = np.array([3, -5, 1])
 C = np.array([-1, 11, 9])
 # Check collinearity (print for reference)
 AB = B - A
 AC = C - A
 print("Vector AB:", AB)
 print("Vector AC:", AC)
```

# Python Code

```
# Verify if AC is a scalar multiple of AB
if np.allclose(AC, (AC[0]/AB[0]) * AB):
    print("Points are collinear")
else:
    print("Points are not collinear")
# 3D Plot
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
# Plot points
ax.scatter(*A, color='red', label='A(2, -1, 3)')
ax.scatter(*B, color='green', label='B(3, -5, 1)')
ax.scatter(*C, color='blue', label='C(-1, 11, 9)')
# Plot line through A in direction of AB (which also passes
    through B and C)
```

# Python Code

```
t = np.linspace(-2, 2, 100)
line = A[:, None] + np.outer(AB, t)
ax.plot(line[0], line[1], line[2], 'k--', label='Line through A,
    B, and C')
# Labels and legend
ax.set_xlabel('X')
ax.set_ylabel('Y')
ax.set_zlabel('Z')
ax.legend()
ax.set title('Collinear Points in 3D')
# Save figure as PNG
plt.savefig("collinear points.png")
# Show plot
plt.show()
```

### Plot

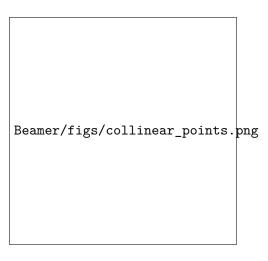


Figure: