

Matgeo Presentation - Problem 2.5.2

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Problem Statement

Verify the type of triangle formed by the points: $A(-4,0)$, $B(4,0)$, $C(0,3)$.

Solution: Setup

$$\mathbf{A} = \begin{pmatrix} -4 \\ 0 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 4 \\ 0 \end{pmatrix}, \quad \mathbf{C} = \begin{pmatrix} 0 \\ 3 \end{pmatrix}$$

Vectors:

$$\mathbf{AB} = \mathbf{B} - \mathbf{A} = \begin{pmatrix} 8 \\ 0 \end{pmatrix}, \quad \mathbf{AC} = \mathbf{C} - \mathbf{A} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}, \quad \mathbf{BC} = \mathbf{C} - \mathbf{B} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}$$

Solution: Right-Angle Check

Step 2: Check for Right-Angled triangle (perpendicular sides)

Dot product should be 0.

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 8 \\ 0 \end{pmatrix}, \quad \mathbf{C} - \mathbf{A} = \begin{pmatrix} 4 \\ 3 \end{pmatrix}, \quad (\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{A}) = \begin{pmatrix} 8 & 0 \end{pmatrix} \begin{pmatrix} 4 \\ 3 \end{pmatrix} = 32 \quad (0.1)$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} -8 \\ 0 \end{pmatrix}, \quad \mathbf{C} - \mathbf{B} = \begin{pmatrix} -4 \\ 3 \end{pmatrix}, \quad (\mathbf{A} - \mathbf{B})^\top (\mathbf{C} - \mathbf{B}) = \begin{pmatrix} -8 & 0 \end{pmatrix} \begin{pmatrix} -4 \\ 3 \end{pmatrix} = 32 \quad (0.2)$$

$$\mathbf{A} - \mathbf{C} = \begin{pmatrix} -4 \\ -3 \end{pmatrix}, \quad \mathbf{B} - \mathbf{C} = \begin{pmatrix} 4 \\ -3 \end{pmatrix}, \quad (\mathbf{A} - \mathbf{C})^\top (\mathbf{B} - \mathbf{C}) = \begin{pmatrix} -4 & -3 \end{pmatrix} \begin{pmatrix} 4 \\ -3 \end{pmatrix} = -7 \quad (0.3)$$

Since no pair of sides is perpendicular, the triangle is not right-angled.

Solution:Isosceles triangle check

$$\text{Midpoint of } AB : \quad \mathbf{M} = \frac{\mathbf{A} + \mathbf{B}}{2} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad (0.4)$$

$$\mathbf{C} - \mathbf{M} = \begin{pmatrix} 0 \\ 3 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 3 \end{pmatrix} \quad (0.5)$$

$$\mathbf{B} - \mathbf{A} = \begin{pmatrix} 8 \\ 0 \end{pmatrix} \quad (0.6)$$

$$(\mathbf{B} - \mathbf{A})^\top (\mathbf{C} - \mathbf{M}) = (8 \ 0) \begin{pmatrix} 0 \\ 3 \end{pmatrix} = 0 \quad (0.7)$$

Hence, C lies on the perpendicular bisector of AB .

$AC = BC = 5 \implies \triangle ABC$ is isosceles.

Conclusion

Therefore, the triangle with vertices $(-4, 0)$, $(4, 0)$, $(0, 3)$ is an **isosceles triangle** with $AC = BC = 5$.

C Source Code: points.c

```
#include <math.h>

// Compute dot product of 2D vectors
double dot_product(double *u, double *v) {
    return u[0]*v[0] + u[1]*v[1];
}

// Compute squared norm of 2D vector
double norm_squared(double *u) {
    return u[0]*u[0] + u[1]*u[1];
}
```

Python Script: call c.py

```
import ctypes
import numpy as np
import matplotlib.pyplot as plt

lib = ctypes.CDLL("./points.so")

lib.dot_product.argtypes = [ctypes.POINTER(ctypes.c_double),
                             ctypes.POINTER(ctypes.c_double)]
lib.dot_product.restype = ctypes.c_double

lib.norm_squared.argtypes = [ctypes.POINTER(ctypes.c_double)]
lib.norm_squared.restype = ctypes.c_double

A = np.array([-4.0, 0.0])
B = np.array([4.0, 0.0])
C = np.array([0.0, 3.0])

AB = B - A
AC = C - A
BC = C - B

dp1 = lib.dot_product(AB.ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
                      AC.ctypes.data_as(ctypes.POINTER(ctypes.c_double)))
dp2 = lib.dot_product((-AB).ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
                      BC.ctypes.data_as(ctypes.POINTER(ctypes.c_double)))
dp3 = lib.dot_product((-AC).ctypes.data_as(ctypes.POINTER(ctypes.c_double)),
                      (-BC).ctypes.data_as(ctypes.POINTER(ctypes.c_double)))
```


Python Script: call c.py

```
AB2 = lib.norm_squared(AB.ctypes.data_as(ctypes.POINTER(ctypes.c_double)))
AC2 = lib.norm_squared(AC.ctypes.data_as(ctypes.POINTER(ctypes.c_double)))
BC2 = lib.norm_squared(BC.ctypes.data_as(ctypes.POINTER(ctypes.c_double)))

print("Dot_products:", dp1, dp2, dp3)
print("Squared_lengths: AB^2=", AB2, "AC^2=", AC2, "BC^2=", BC2)

plt.plot([A[0], B[0]], [A[1], B[1]], 'r-', label='AB')
plt.plot([A[0], C[0]], [A[1], C[1]], 'g-', label='AC')
plt.plot([B[0], C[0]], [B[1], C[1]], 'b-', label='BC')

plt.scatter([A[0], B[0], C[0]], [A[1], B[1], C[1]], color='black')
plt.text(A[0], A[1], 'A(-4,0)', ha='right', va='top')
plt.text(B[0], B[1], 'B(4,0)', ha='left', va='top')
plt.text(C[0], C[1], 'C(0,3)', ha='center', va='bottom')

plt.axis('equal')
plt.legend()
plt.grid(True)
plt.show()
```

Python Script: plot.py

```
import matplotlib.pyplot as plt
import numpy as np

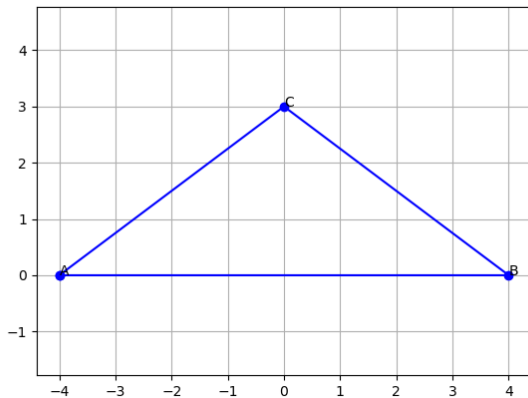
A = np.array([-4, 0])
B = np.array([4, 0])
C = np.array([0, 3])

plt.plot([A[0], B[0]], [A[1], B[1]], 'r-', label='AB')
plt.plot([A[0], C[0]], [A[1], C[1]], 'g-', label='AC')
plt.plot([B[0], C[0]], [B[1], C[1]], 'b-', label='BC')

plt.scatter([A[0], B[0], C[0]], [A[1], B[1], C[1]], color='black')
plt.text(A[0], A[1], 'A(-4,0)', ha='right', va='top')
plt.text(B[0], B[1], 'B(4,0)', ha='left', va='top')
plt.text(C[0], C[1], 'C(0,3)', ha='center', va='bottom')

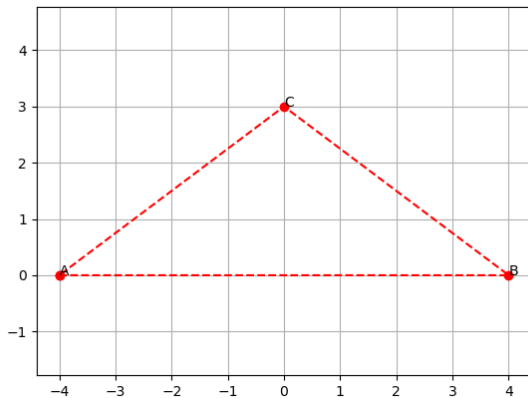
plt.axis('equal')
plt.legend()
plt.grid(True)
plt.show()
```

Result Plot



Triangle ABC plotted using shared output

Result Plot



Triangle *ABC* plotted using direct python