

# Matrices in Geometry 5.2.40

EE25BTECH11037 - Divyansh

**Question:** Solve

$$\begin{aligned} \frac{4}{x} + 3y &= 14 \\ \frac{3}{x} - 4y &= 23 \end{aligned}$$

**Solution:** We have the following two equations as:

$$\begin{pmatrix} 4 & 3 \\ 3 & -4 \end{pmatrix} \begin{pmatrix} \frac{1}{x} \\ y \end{pmatrix} = \begin{pmatrix} 14 \\ 23 \end{pmatrix} \quad (1)$$

Writing the augmented matrix for these equations,

$$\left( \begin{array}{cc|c} 4 & 3 & 14 \\ 3 & -4 & 23 \end{array} \right) \xrightarrow{R_1 \rightarrow R_1/4} \left( \begin{array}{cc|c} 1 & 3/4 & 7/2 \\ 3 & -4 & 23 \end{array} \right) \xrightarrow{R_2 \rightarrow R_2 - 3R_1} \left( \begin{array}{cc|c} 1 & 3/4 & 7/2 \\ 0 & -25/4 & 25/2 \end{array} \right) \xrightarrow{R_2 \rightarrow \frac{-4}{25}R_2} \quad (2)$$

$$\left( \begin{array}{cc|c} 1 & 3/4 & 7/2 \\ 0 & 1 & -2 \end{array} \right) \xrightarrow{R_1 \rightarrow R_1 - \frac{3}{4}R_2} \left( \begin{array}{cc|c} 1 & 0 & 5 \\ 0 & 1 & -2 \end{array} \right) \quad (3)$$

This implies that

$$\begin{pmatrix} \frac{1}{x} \\ y \end{pmatrix} = \begin{pmatrix} 5 \\ -2 \end{pmatrix} \Rightarrow x = \frac{1}{5}, y = -2 \quad (4)$$

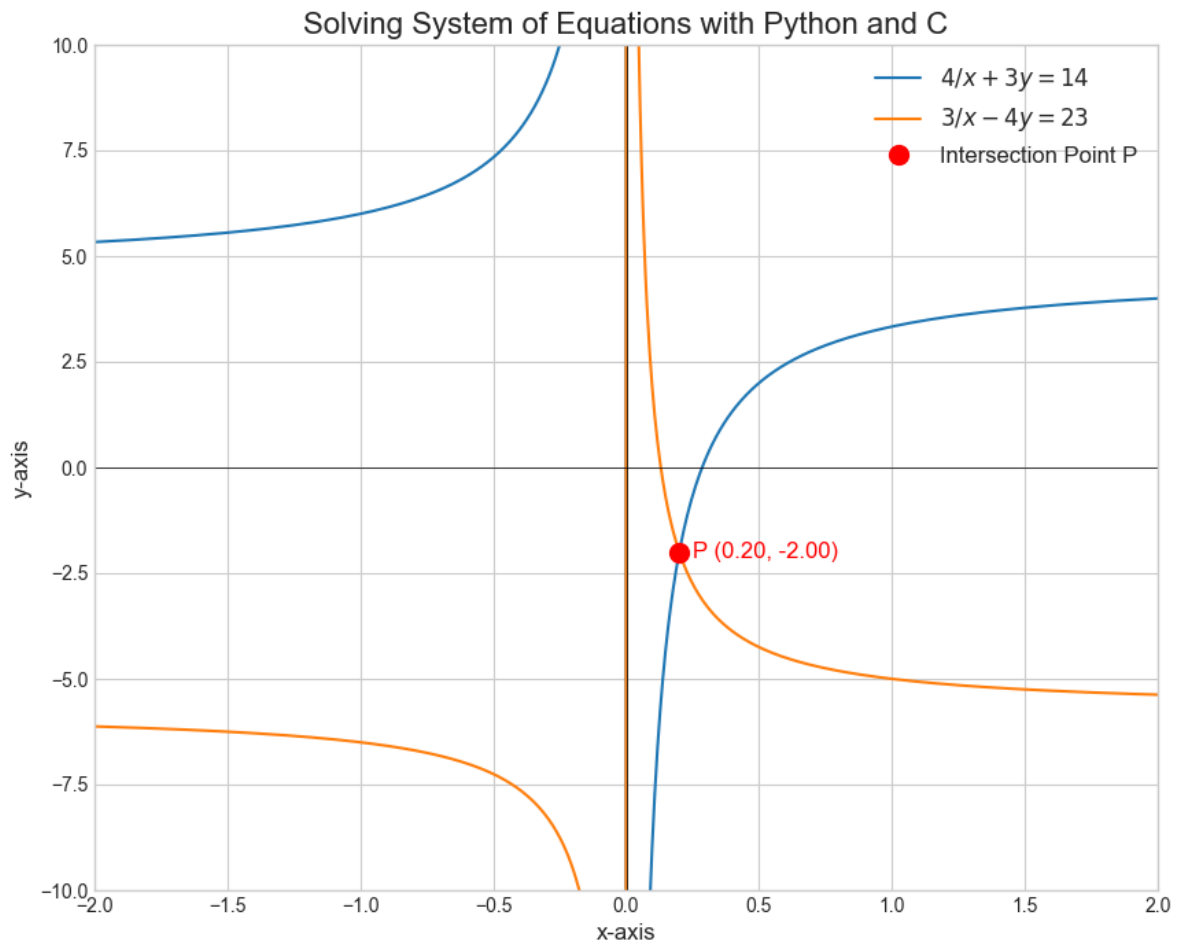


Fig. 1: Graph for 5.2.40