AI25BTECH11003 - Bhavesh Gaikwad

Question: Prove that points A(2,1), B(0,5) and C(-1,2) are collinear.

Solution:

$$B-A = \begin{pmatrix} 0-2 \\ 5-1 \end{pmatrix} = \begin{pmatrix} -2 \\ 4 \end{pmatrix} \qquad C-A = \begin{pmatrix} -1-2 \\ 2-1 \end{pmatrix} = \begin{pmatrix} -3 \\ 1 \end{pmatrix}$$
$$M = \begin{pmatrix} B-A & C-A \end{pmatrix} = \begin{pmatrix} -2 & -3 \\ 4 & 1 \end{pmatrix}$$

Row-reduce to compute the rank:

$$\begin{pmatrix} -2 & -3 \\ 4 & 1 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 + 2R_1} \begin{pmatrix} -2 & -3 \\ 0 & -5 \end{pmatrix}$$

The echelon form has two nonzero rows, hence $rank(M)=2\neq 1$

Therefore, The points
$$A(2, 1)$$
, $B(0, 5)$ and $C(-1, 2)$ are not collinear. (0.1)

1

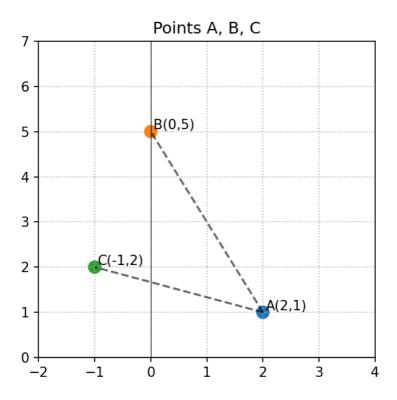


Fig. 0.1: Graph