## EE25BTECH11034 - Kishora Karthik

## **Question:**

Check if the point A(2,7) lies on the perpendicular bisector of line segment joining the points P(6,5) and Q(0,-4).

## Formulae:

The equation of the perpendicular bisector of PQ is

$$\left(\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2}\right)^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = 0 \tag{1}$$

Solution: The given points are,

$$\mathbf{A} = \begin{pmatrix} 2 \\ 7 \end{pmatrix} \tag{2}$$

$$\mathbf{P} = \begin{pmatrix} 6 \\ 5 \end{pmatrix} \tag{3}$$

$$\mathbf{Q} = \begin{pmatrix} 0 \\ -4 \end{pmatrix} \tag{4}$$

$$\mathbf{P} - \mathbf{Q} = \begin{pmatrix} 6 \\ 5 \end{pmatrix} - \begin{pmatrix} 0 \\ -4 \end{pmatrix} \tag{5}$$

$$\mathbf{P} - \mathbf{Q} = \begin{pmatrix} 6 \\ 9 \end{pmatrix} \tag{6}$$

$$\frac{\mathbf{P} + \mathbf{Q}}{2} = \frac{\binom{6}{5} + \binom{0}{-4}}{2} \tag{7}$$

$$\frac{\mathbf{P} + \mathbf{Q}}{2} = \frac{\binom{6}{1}}{2} \tag{8}$$

$$\frac{\mathbf{P} + \mathbf{Q}}{2} = \begin{pmatrix} 3\\0.5 \end{pmatrix} \tag{9}$$

$$\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2} = \begin{pmatrix} 2 \\ 7 \end{pmatrix} - \begin{pmatrix} 3 \\ 0.5 \end{pmatrix} \tag{10}$$

$$\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2} = \begin{pmatrix} -1\\ 6.5 \end{pmatrix} \tag{11}$$

$$\left(\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2}\right)^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = \begin{pmatrix} -1 & 6.5 \end{pmatrix} \begin{pmatrix} 6 \\ 9 \end{pmatrix}$$
 (12)

$$\left(\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2}\right)^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = (-1)(6) + (6.5)(9)$$
(13)

$$\left(\mathbf{A} - \frac{\mathbf{P} + \mathbf{Q}}{2}\right)^{\mathsf{T}} (\mathbf{P} - \mathbf{Q}) = 52.5 \neq 0 \tag{14}$$

The equation of perpendicular bisector is not satisfied.

Therefore, point A does not lie on the perpendicular bisector of line segment joining the points P and Q.

