

## Question

The area of a triangle formed by vertices **O**, **A** and **B**, where  $\mathbf{OA} = \hat{i} + 2\hat{j} + 3\hat{k}$  and  $\mathbf{OB} = -3\hat{i} - 2\hat{j} + \hat{k}$  is

## Solution

Represent the vectors in matrix form:

$$\mathbf{OA} = \begin{pmatrix} 1 \\ 2 \\ 3 \end{pmatrix}, \quad \mathbf{OB} = \begin{pmatrix} -3 \\ 1 \\ 1 \end{pmatrix} \quad (1)$$

The area of triangle  $OAB$  is given by:

$$\text{Area} = \frac{1}{2} \|\mathbf{OA} \times \mathbf{OB}\| \quad (2)$$

Compute the cross product using determinant:

$$\mathbf{OA} \times \mathbf{OB} = \det \begin{pmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 2 & 3 \\ -3 & 1 & 1 \end{pmatrix} \quad (3)$$

Simplifying:

$$= -\hat{i} - 10\hat{j} + 7\hat{k} \Rightarrow \mathbf{OA} \times \mathbf{OB} = \begin{pmatrix} -1 \\ -10 \\ 7 \end{pmatrix} \quad (4)$$

Magnitude of the cross product:

$$\|\mathbf{OA} \times \mathbf{OB}\| = \sqrt{(-1)^2 + (-10)^2 + 7^2} = \sqrt{1 + 100 + 49} = \sqrt{150} \quad (5)$$

Final area:

$$\text{Area} = \frac{1}{2} \sqrt{150} \quad (6)$$

### Area of Triangle

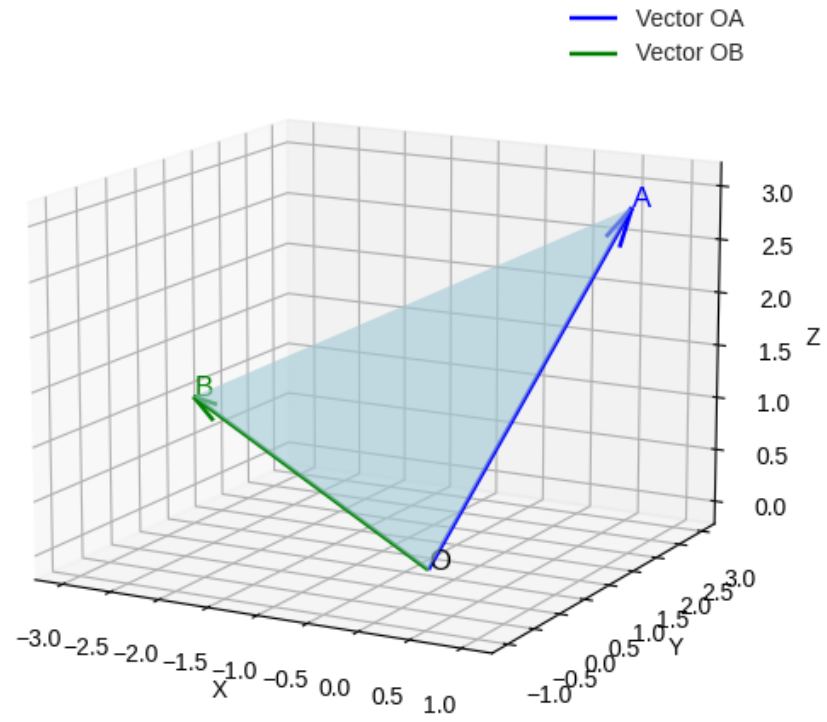


Figure 1