

1.5.16

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# Question

**Question:** Find the point  $A$  if  $AB$  is a diameter of the circle with center  $C = (3, -1)$  and point  $B = (2, 6)$ .

# given data

Point	Vector
B	$\begin{pmatrix} 2 \\ 6 \end{pmatrix}$
C	$\begin{pmatrix} 3 \\ -1 \end{pmatrix}$

# Section Formula

If a point  $P$  divides the line joining  $A$  and  $B$  internally in the ratio  $m : n$ , then

$$\mathbf{P} = \frac{k\mathbf{B} + \mathbf{A}}{k + 1} = \begin{pmatrix} \mathbf{A} & \mathbf{B} \end{pmatrix} \begin{pmatrix} \frac{1}{k+1} \\ \frac{k}{k+1} \end{pmatrix}$$

substitute values:

$$\begin{pmatrix} 3 \\ -1 \end{pmatrix} = \left( \mathbf{A} \begin{pmatrix} 2 \\ 6 \end{pmatrix} \right) \begin{pmatrix} \frac{1}{2} \\ \frac{1}{2} \end{pmatrix}.$$

$$2 \begin{pmatrix} 3 \\ -1 \end{pmatrix} = \mathbf{A} + \begin{pmatrix} 2 \\ 6 \end{pmatrix} \Rightarrow \mathbf{A} = 2 \begin{pmatrix} 3 \\ -1 \end{pmatrix} - \begin{pmatrix} 2 \\ 6 \end{pmatrix} = \begin{pmatrix} 4 \\ -8 \end{pmatrix}.$$

# Rank Verification

Check collinearity of  $A, B, C$ :

$$\begin{pmatrix} \mathbf{C} - \mathbf{A} & \mathbf{B} - \mathbf{A} \end{pmatrix} = \begin{pmatrix} 3 - 4 & 2 - 4 \\ -1 - (-8) & 6 - (-8) \end{pmatrix} = \begin{pmatrix} -1 & -2 \\ 7 & 14 \end{pmatrix} = 0$$

Thus, rank = 1 and points are collinear.

$$\mathbf{A} = \begin{pmatrix} 4 \\ -8 \end{pmatrix}$$

# Figure

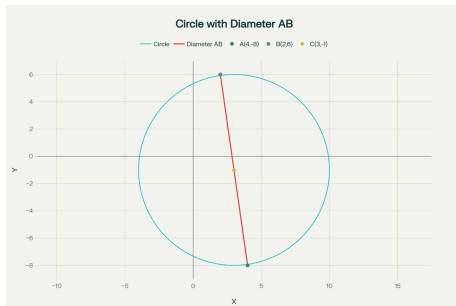


Figure:

```
import matplotlib.pyplot as plt

# Center C = (3, -1)
# B = (2, 6)
# Let A = (x, y). Midpoint formula: center = (A + B) / 2 =>
# 3 = (x + 2) / 2, -1 = (y + 6) / 2
# Solve for (x, y):
# x = 2*3 - 2 = 4
# y = 2*(-1) - 6 = -8

A = np.array([4, -8])
B = np.array([2, 6])
C = np.array([3, -1])
```



# Python Code

```
# For the circle, radius = distance(center, B)
import numpy as np
def dist(P, Q):
    return np.sqrt((P[0] - Q[0])**2 + (P[1] - Q[1])**2)
radius = dist(C, B)

fig, ax = plt.subplots(figsize=(7,7))

# Plot the circle
circle = plt.Circle(C, radius, color='blue', fill=False,
                    linestyle='dotted', label='Circle')
ax.add_patch(circle)

# Plot A, B, C
ax.scatter(*A, color='red', label='A (unknown, solved)')
ax.scatter(*B, color='green', label='B (2, 6)')
ax.scatter(*C, color='orange', label='Center (3, -1)')
```

```
# Plot line AC
ax.plot([A[0], C[0]], [A[1], C[1]], [A[2], C[2]], color='purple',
        label='Line AC')

# Annotate points
ax.text(*A, ' A', color='red', fontsize=10)
ax.text(*B, ' B', color='green', fontsize=10)
ax.text(*C, ' C', color='blue', fontsize=10)
```

# Python Code

```
# Draw diameter AB
ax.plot([A[0], B[0]], [A[1], B[1]], color='purple', linewidth=2,
        linestyle='--', label='Diameter AB')

# Annotate
ax.annotate('A'+str(A), (A[0], A[1]), xytext=(10, -10),
            textcoords='offset points')
ax.annotate('B'+str(B), (B[0], B[1]), xytext=(-40, 10),
            textcoords='offset points')
ax.annotate('C'+str(C), (C[0], C[1]), xytext=(5, -10), textcoords
            ='offset points')

ax.set_xlim(C[0] - radius - 2, C[0] + radius + 2)
ax.set_ylim(C[1] - radius - 2, C[1] + radius + 2)
ax.set_aspect('equal')
ax.grid(True)
plt.legend()
plt.title('Circle with Diameter AB')
plt.xlabel('x')
```

# C Code

```
#include <stdio.h>

int main() {
    // Given values
    int xB = 2, yB = 6;
    int xC = 3, yC = -1; // Center of the circle

    // Calculate coordinates of A using midpoint formula
    int xA = 2 * xC - xB;
    int yA = 2 * yC - yB;

    // Print result
    printf("Coordinates of point A are: (%d, %d)\n", xA, yA);

    // Verify midpoint
    float midX = (xA + xB) / 2.0;
    float midY = (yA + yB) / 2.0;
    printf("Midpoint of A and B is: (%.1f, %.1f)\n", midX, midY);
```

```
import subprocess

# Compile the C program
subprocess.run(["gcc", "midpoint.c", "-o", "midpoint"])

# Run the compiled C program
result = subprocess.run(["./midpoint"], capture_output=True, text=True)

# Print the output from the C program
print(result.stdout)
```

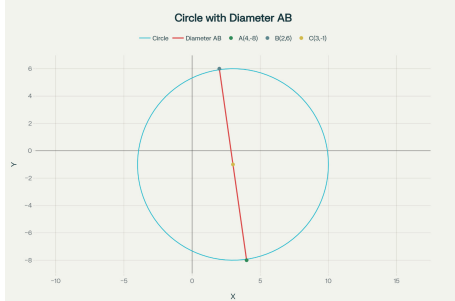


Figure: