EE25BTECH11023 - Venkata Sai

Question:

Solve the following system of linear equations

$$\frac{x}{a} - \frac{y}{b} = 0 \tag{1}$$

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$$ax + by = a^2 + b^2 \tag{2}$$

Solution: Given

$$\frac{x}{a} - \frac{y}{b} = 0 \implies bx = ay \tag{3}$$

$$bx - ay = 0 (4)$$

$$ax + by = a^2 + b^2 \tag{5}$$

As a matrix equation

$$\begin{pmatrix} b & -a & 0 \\ a & b & a^2 + b^2 \end{pmatrix} \xrightarrow{R_2 \to bR_2 - aR_1} \begin{pmatrix} b & -a & 0 \\ 0 & b^2 + a^2 & (a^2 + b^2)b \end{pmatrix}$$
 (6)

$$(b^2 + a^2)y = (a^2 + b^2)b (7)$$

$$\implies y = b$$
 (8)

Substituting in equation (3)

$$bx = ab \implies x = a$$
 (9)

Hence x = a, y = b is the solution for given system of linear equations

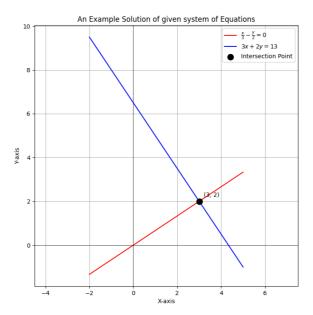


Fig. 0.1