

Application Problem

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Problem Statement

A fraction becomes $\frac{1}{3}$ when 1 is subtracted from the numerator and it becomes $\frac{1}{4}$ when 8 is added to the denominator. Find the fraction.

Solution

$$\frac{x-1}{y} = \frac{1}{3}, \quad (1)$$

$$\frac{x}{y+8} = \frac{1}{4} \quad (2)$$

$$3(x-1) - y = 0 \implies 3x - y - 3 = 0, \quad (3)$$

$$4x - (y+8) = 0 \implies 4x - y - 8 = 0 \quad (4)$$

$$(3 \quad -1) \begin{pmatrix} x \\ y \end{pmatrix} = 3, \quad (5)$$

$$(4 \quad -1) \begin{pmatrix} x \\ y \end{pmatrix} = 8 \quad (6)$$

Solution (cont..)

Augmented matrix:

$$\begin{pmatrix} 3 & -1 & 3 \\ 4 & -1 & 8 \end{pmatrix} \quad (7)$$

RREF using row operations:

$$R_2 \rightarrow R_2 - \frac{4}{3}R_1 \Rightarrow \begin{pmatrix} 3 & -1 & 3 \\ 0 & 1/3 & 4 \end{pmatrix} \Rightarrow \begin{pmatrix} 3 & -1 & 3 \\ 0 & 1 & 12 \end{pmatrix}, \quad (8)$$

$$R_1 \rightarrow R_1 + R_2 \Rightarrow \begin{pmatrix} 3 & 0 & 15 \\ 0 & 1 & 12 \end{pmatrix} \Rightarrow \begin{pmatrix} 1 & 0 & 5 \\ 0 & 1 & 12 \end{pmatrix} \quad (9)$$

Solution (cont..)

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 5 \\ 12 \end{pmatrix} \quad (10)$$

Hence, the fraction is:

$$\boxed{\frac{5}{12}}$$

Python Code (Plotting Line and Vectors)

```
import numpy as np
import matplotlib.pyplot as plt

m1, c1 = 1.5, 2
m2, c2 = -0.5, 5
A = np.array([0, c1])
B = np.array([0, c2])
x_intersect = (c2 - c1) / (m1 - m2)
y_intersect = m1 * x_intersect + c1
C = np.array([x_intersect, y_intersect])
triangle = np.array([A, B, C, A])
```

Python Code (cont..)

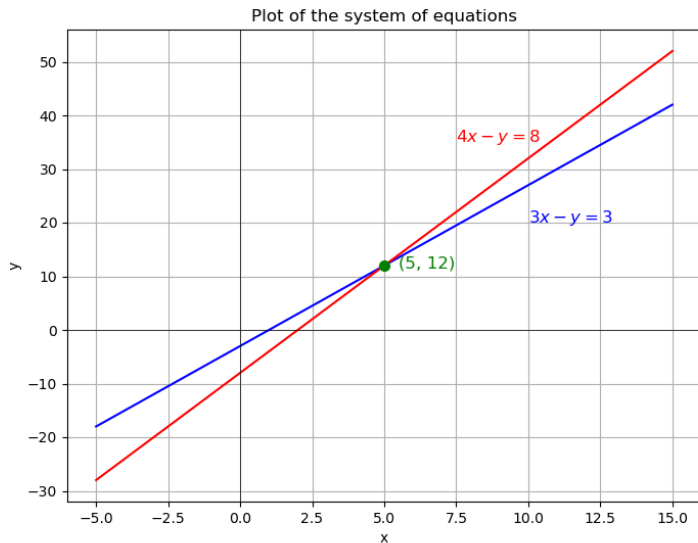
```
plt.figure(figsize=(6,6))
plt.plot(triangle[:,0], triangle[:,1], 'b-o', label='Triangle')
plt.axvline(0, color='k', linewidth=0.8)
plt.axhline(0, color='k', linewidth=0.8)
x_vals = np.linspace(min(0, C[0])-1, max(C[0]+1, 2), 100)
plt.plot(x_vals, m1*x_vals + c1, 'r--', label=f'y={m1}x+{c1}')
plt.plot(x_vals, m2*x_vals + c2, 'g--', label=f'y={m2}x+{c2}')
```

Python Code (cont..)

```
plt.scatter([A[0], B[0], C[0]], [A[1], B[1], C[1]], color='black')
plt.text(A[0]-0.3, A[1]+0.1, 'A')
plt.text(B[0]-0.3, B[1]+0.1, 'B')
plt.text(C[0]+0.1, C[1]+0.1, 'C')
plt.grid(True)
plt.axis('equal')
plt.title('Triangle formed by lines  $x=0$ ')

plt.show()
```


Plot



C Code (Computations)

```
#include <stdio.h>

void get_lines(double* x, double* y1, double* y2, int n) {
    for (int i = 0; i < n; i++) {
        y1[i] = 3*x[i] - 3.0;
        y2[i] = 4*x[i] - 8.0;
    }
}
```

Python Code (Using C)

```
import numpy as np
import matplotlib.pyplot as plt
import ctypes

lines_lib = ctypes.CDLL('./points.so')

n = 100
x = np.linspace(-5, 15, n)
y1 = np.zeros(n, dtype=np.float64)
y2 = np.zeros(n, dtype=np.float64)
```

Python Code (Cont..)

```
lines_lib.get_lines.argtypes = [  
    np.ctypeslib.ndpointer(dtype=np.float64, ndim=1, flags="C_CONTIGUOUS"),  
    np.ctypeslib.ndpointer(dtype=np.float64, ndim=1, flags="C_CONTIGUOUS"),  
    np.ctypeslib.ndpointer(dtype=np.float64, ndim=1, flags="C_CONTIGUOUS"),  
    ctypes.c_int  
]  
lines_lib.get_lines(x, y1, y2, n)  
  
plt.figure(figsize=(8, 6))  
plt.plot(x, y1, color='blue')  
plt.plot(x, y2, color='red')
```

Python Code (Cont..)

```
plt.text(10, 20, r'$3x-y=-3$', color='blue', fontsize=12)
plt.text(7.5, 35, r'$4x-y=-8$', color='red', fontsize=12)

plt.title("System of Equations")
plt.xlabel("x")
plt.ylabel("y")
plt.grid(True)
plt.axhline(0, color='black', linewidth=0.5)
plt.axvline(0, color='black', linewidth=0.5)
plt.show()
```