

# MATGEO Presentation: 4.11.32

Subhodeep Chakraborty  
ee25btech11055,  
IIT Hyderabad.

October 5, 2025

## 1 Problem

## 2 Solution

- Plot

## 3 C Code

## 4 Python Code

- Using shared objects
- Plot
- In pure Python
- Plot

## Problem Statement

Find the equation of the line passing through  $(2, -1, 2)$  and  $(5, 3, 4)$  and of the plane passing through  $(2, 0, 3)$ ,  $(1, 1, 5)$  and  $(3, 2, 4)$ . Also, find their point of intersection. (12, 2018)

## Given data

Given:

$$\mathbf{A} = \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} \quad (3.1)$$

$$\mathbf{B} = \begin{pmatrix} 5 \\ 3 \\ 4 \end{pmatrix} \quad (3.2)$$

$$\mathbf{P} = \begin{pmatrix} 2 \\ 0 \\ 3 \end{pmatrix} \quad (3.3)$$

$$\mathbf{Q} = \begin{pmatrix} 1 \\ 1 \\ 5 \end{pmatrix} \quad (3.4)$$

$$\mathbf{R} = \begin{pmatrix} 3 \\ 2 \\ 4 \end{pmatrix} \quad (3.5)$$

# Formulae

We know, for line  $\mathbf{x} = \mathbf{h} + k\mathbf{m}$  and plane  $\mathbf{n}^\top \mathbf{y} = 1$ ,

$$\mathbf{h} = \mathbf{A} \quad (3.6)$$

$$\mathbf{m} = \mathbf{B} - \mathbf{A} \quad (3.7)$$

$$(P \quad Q \quad R)^\top \mathbf{n} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad (3.8)$$

## Solving

Thus

$$(P \quad Q \quad R)^{\top} \mathbf{n} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad (3.9)$$

$$\begin{pmatrix} 2 & 0 & 3 \\ 1 & 1 & 5 \\ 3 & 2 & 4 \end{pmatrix} \mathbf{n} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad (3.10)$$

## Solving

On solving

$$\xleftrightarrow{R_2=2R_2-R_1; R_3=2R_3-3R_1} \left( \begin{array}{ccc|c} 2 & 0 & 3 & 1 \\ 0 & 2 & 7 & 1 \\ 0 & 4 & 2 & -1 \end{array} \right) \quad (3.11)$$

$$\xleftrightarrow{R_3=R_3-2R_2} \left( \begin{array}{ccc|c} 2 & 0 & 3 & 1 \\ 0 & 2 & 7 & 1 \\ 0 & 0 & -12 & -3 \end{array} \right) \quad (3.12)$$

$$\xleftrightarrow{R_1=4R_1+R_3; R_2=12R_2+7R_3} \left( \begin{array}{ccc|c} 8 & 0 & 0 & 1 \\ 0 & 24 & 0 & -9 \\ 0 & 0 & -12 & -3 \end{array} \right) \quad (3.13)$$

$$\xleftrightarrow{R_1=R_1/8; R_2=R_2/24; R_3=-R_3/12} \left( \begin{array}{ccc|c} 1 & 0 & 0 & 1/8 \\ 0 & 1 & 0 & -3/8 \\ 0 & 0 & 1 & 1/4 \end{array} \right) \quad (3.14)$$

$$\mathbf{n} = \frac{1}{8} \begin{pmatrix} 1 \\ -3 \\ 2 \end{pmatrix} \quad (3.15)$$

## Solving

So we have:

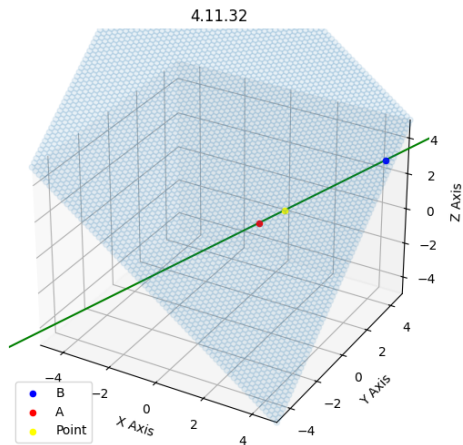
$$\mathbf{n}^\top \mathbf{h} = \frac{1}{8} (1 \quad -3 \quad 2) \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} = \frac{9}{8} \quad (3.16)$$

$$\mathbf{n}^\top \mathbf{m} = \frac{1}{8} (1 \quad -3 \quad 2) \begin{pmatrix} 3 \\ 4 \\ 2 \end{pmatrix} = -\frac{5}{8} \quad (3.17)$$

$$\mathbf{x} = \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} + \begin{pmatrix} \frac{1-9/8}{-5/8} \end{pmatrix} \begin{pmatrix} 3 \\ 4 \\ 2 \end{pmatrix} = \begin{pmatrix} 13/5 \\ -1/5 \\ 12/5 \end{pmatrix} \quad (3.18)$$



# Plot



## C code for generating points on line

```
void point_gen(const double* P1, const double* P2, double t, double
    * result_point) {
    result_point[0] = P1[0] + t * (P2[0] - P1[0]);
    result_point[1] = P1[1] + t * (P2[1] - P1[1]);
    result_point[2] = P1[2] + t * (P2[2] - P1[2]);
}
```

## C code for generating points on plane

```
void generate_plane_points(  
    // Output params  
    double* x_coords, double* y_coords, double* z_coords,  
    // Grid params  
    double x_min, double x_max, int x_steps,  
    double y_min, double y_max, int y_steps,  
    // Plane stuff  
    double n1, double n2, double n3, double c) {  
    double x_step_val = (x_max - x_min) / (x_steps - 1);  
    double y_step_val = (y_max - y_min) / (y_steps - 1);  
    int index = 0;  
    for (int i = 0; i < x_steps; i++) {  
        for (int j = 0; j < y_steps; j++) {  
            double current_x = x_min + i * x_step_val;  
            double current_y = y_min + j * y_step_val;  
            double current_z;
```

```

// Vertical plane check
if ((c < 1e-9)&&(c > -1e-9)) {
    current_z = 0.0;
} else {
    current_z = (-n1 * current_x - n2 * current_y + c) /
                n3;
}
x_coords[index] = current_x;
y_coords[index] = current_y;
z_coords[index] = current_z;
index++;
}
}
}

```

## Python code for plotting using C

```
import ctypes
import numpy as np
import numpy.linalg as LA
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

libline = ctypes.CDLL("./line.so")

get_point = libline.point_gen
get_point.argtypes = [
    ctypes.POINTER(ctypes.c_double), # P1
    ctypes.POINTER(ctypes.c_double), # P2
    ctypes.c_double, # t
    ctypes.POINTER(ctypes.c_double), # result_point
]
get_point.restype = None
```

```
lib = ctypes.CDLL("./plane.so")
```

```
lib.generate_plane_points.argtypes = [  
    ctypes.POINTER(ctypes.c_double),  
    ctypes.POINTER(ctypes.c_double),  
    ctypes.POINTER(ctypes.c_double),  
    ctypes.c_double,  
    ctypes.c_double,  
    ctypes.c_int,  
    ctypes.c_double,  
    ctypes.c_double,  
    ctypes.c_int,  
    ctypes.c_double,  
    ctypes.c_double,  
    ctypes.c_double,  
    ctypes.c_double,  
]  
lib.generate_plane_points.restype = None
```

```
DoubleArray3 = ctypes.c_double * 3
```

```
a = DoubleArray3(2, -1, 2)
```

```
b = DoubleArray3(5, 3, 4)
```

```
p = DoubleArray3(2, 0, 3)
```

```
q = DoubleArray3(1, 1, 5)
```

```
r = DoubleArray3(3, 2, 4)
```

```
l1 = DoubleArray3(-28, -41, -18)
```

```
l2 = DoubleArray3(32, 39, 22)
```

```
n = DoubleArray3(0.2, -0.2, 0.2)
```

```
c = 1
```

```
fig = plt.figure(figsize=(8, 6))
```

```
ax = fig.add_subplot(111, projection="3d")
```

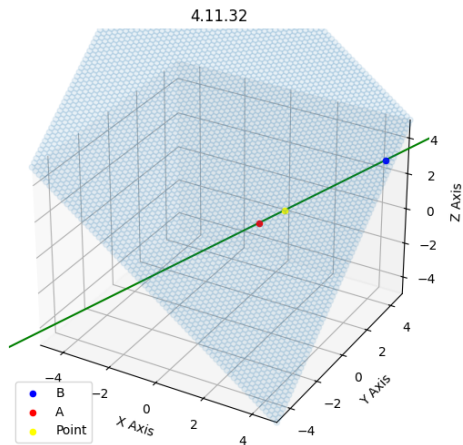
```
t_values = np.linspace(0, 1, 100)
```

```
line_points_x, line_points_y, line_points_z = [], [], []
```

```
ax.plot(  
    line_points_x,  
    line_points_y,  
    line_points_z,  
    color=" gray" ,  
)  
ax.scatter(b[0], b[1], b[2], color=" blue" , label=" b" )  
ax.scatter(a[0], a[1], a[2], color=" red" , label=" a" )  
ax.scatter(c[0], c[1], c[2], color=" green" , label=" Point" )  
  
ax.set_xlabel(" X Axis" )  
ax.set_ylabel(" Y Axis" )  
ax.set_zlabel(" Z Axis" )  
ax.set_title(" 2.9.6" )  
ax.legend()  
ax.grid(True)  
plt.savefig("../figs/plot.png" )  
plt.show()
```



# Plot



## Pure Python code

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D

a = np.array([5, 1, 6]).T
b = np.array([3, 4, 1]).T
c = np.array([13 / 5, 23 / 5, 0])

fig = plt.figure(figsize=(8, 8))
ax = fig.add_subplot(111, projection="3d")

ax.plot([a[0], c[0]], [a[1], c[1]], [a[2], c[2]], color="blue", label="b")

ax.scatter(b[0], b[1], b[2], color="blue", label="b")
ax.scatter(a[0], a[1], a[2], color="red", label="a")
ax.scatter(c[0], c[1], c[2], color="green", label="Point")
```

## Pure Python code

```
ax.text(a[0], a[1], a[2], "A")
ax.text(b[0], b[1], b[2], "B")
ax.text(c[0], c[1], c[2], "Point")

ax.set_xlabel("X-axis")
ax.set_ylabel("Y-axis")
ax.set_zlabel("Z-axis")
ax.set_title("2.9.6")
ax.set_xlim([-5, 5])
ax.set_ylim([-5, 5])
ax.set_zlim([-5, 5])
ax.legend()
ax.grid(True)

plt.savefig("../figs/python.png")
plt.show()
```

# Plot

4.11.32

