## EE25btech11028 - J.Navya sri

## **Question:**

Find the equation of the plane through the points

$$(2,1,0), (3,-2,-2), (3,1,7).$$

Solution: The given points are

$$P_1 = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix}, \quad P_2 = \begin{pmatrix} 3 \\ 2 \\ -2 \end{pmatrix}, \quad P_3 = \begin{pmatrix} 3 \\ 1 \\ 7 \end{pmatrix}.$$

Step 1: General plane equation

$$ax + by + cz + d = 0 \tag{1}$$

1

Step 2: Substitution of points

Substituting each point:

$$2a + b + d = 0 \tag{2}$$

$$3a + 2b - 2c + d = 0 (3)$$

$$3a + b + 7c + d = 0 (4)$$

Step 3: Matrix form

$$\begin{pmatrix}
2 & 1 & 0 & 1 \\
3 & 2 & -2 & 1 \\
3 & 1 & 7 & 1
\end{pmatrix}
\begin{pmatrix}
a \\
b \\
c \\
d
\end{pmatrix}
\begin{pmatrix}
0 \\
0 \\
0
\end{pmatrix}$$
(5)

Step 4: Solving the system

From (2):

$$d = -2a - b \tag{6}$$

Substitute in (3):

$$3a + 2b - 2c - 2a - b = 0 \implies a + b - 2c = 0$$
 (7)

Substitute in (4):

$$3a + b + 7c - 2a - b = 0 \implies a + 7c = 0$$
 (8)

$$a = -7c \tag{9}$$

$$-7c + b - 2c = 0 \quad \Rightarrow \quad b = 9c \tag{10}$$

From (6):

$$d = -2(-7c) - 9c = 5c \tag{11}$$

## Step 5: Final result

$$\begin{pmatrix} a \\ b \\ c \\ d \end{pmatrix} = c \begin{pmatrix} -7 \\ 9 \\ 1 \\ 5 \end{pmatrix}$$

Choosing c = 1, the plane equation is

$$-7x + 9y + z + 5 = 0 ag{12}$$

Or equivalently,

$$7x - 9y - z - 5 = 0$$
 (13)

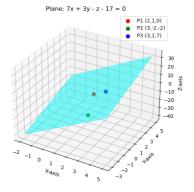


Fig. 1