4.8.19

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Question

If the distance of the point (1,1,1) from the plane $x-y+z+\lambda=0$ is $\frac{5}{\sqrt{3}}$, find the value(s) of λ .

Solution

Equation of plane is given by

$$n^{\top} x = -\lambda; \tag{1}$$

where
$$n^{\top} = \begin{pmatrix} 1 & -1 & 1 \end{pmatrix}$$
.

Solution

Let the distance of point P(1,1,1) from the plane is d.

$$d = \frac{||\mathbf{n}^{\top} P + \lambda||}{||\mathbf{n}||} \tag{2}$$

then value of λ is given by

$$\lambda = +d||n|| - n^{\top}P \text{ or} \tag{3}$$

$$\lambda = -d||n|| - n^{\top}P \tag{4}$$

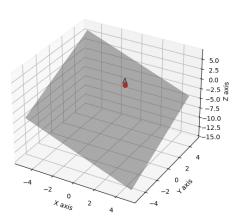
Solving these Equations we get

$$\implies \lambda = +4$$
 (5)

$$= -6 \tag{6}$$

plot

3D Plane and Point A



plot

3D Plane and Point A

