## AI25BTECH11033-SNEHAMRUDULA

If the point P(2, 1) lies on the line segment joining points A(4, 2) and B(8, 4), then

- 1)  $AP = \frac{1}{4}AB$
- 2)  $AP = \dot{P}E$
- 3)  $PB = \frac{1}{3}AB$
- $4) AP = \frac{3}{5}AB$
- 1) Given:

$$\mathbf{A} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}, \quad \mathbf{B} = \begin{pmatrix} 8 \\ 4 \end{pmatrix}, \quad \mathbf{P} = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

Direction vector:

$$\mathbf{m} = \mathbf{B} - \mathbf{A} = \begin{pmatrix} 8 \\ 4 \end{pmatrix} - \begin{pmatrix} 4 \\ 2 \end{pmatrix} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$$

Parameter:

$$k = \frac{(\mathbf{P} - \mathbf{A})^{\top} (\mathbf{B} - \mathbf{A})}{\|\mathbf{B} - \mathbf{A}\|^{2}} = \frac{\binom{2}{1} - \binom{4}{2}}{4^{2} + 2^{2}} = \frac{\binom{-2}{1}}{20} = \frac{-8 - 2}{20} = -\frac{1}{2}.$$

Hence.

$$\mathbf{P} = \mathbf{A} + k(\mathbf{B} - \mathbf{A}) = \mathbf{A} - \frac{1}{2}(\mathbf{B} - \mathbf{A})$$

Since k < 0, point P lies on the line AB but outside the segment (beyond A).

## 2) Lengths:

$$AB = \|\mathbf{B} - \mathbf{A}\| = \sqrt{4^2 + 2^2} = 2\sqrt{5}, \qquad AP = \|\mathbf{P} - \mathbf{A}\| = \|\begin{pmatrix} -2 \\ -1 \end{pmatrix}\| = \sqrt{5}.$$

Therefore.

$$AP = \frac{1}{2}AB.$$

3) Conclusion: The correct relation is

$$AP = \frac{1}{2}AB$$

and P does not lie on the segment AB. Hence, the given statement is **false**.

