

# ASSIGNMENT 1: GATE 2010 IN: INSTRUMENTATION ENGINEERING

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- 1) The infinite series  $f(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \frac{x^7}{7!} \dots \infty$  converges to  
(GATE IN 2010)
- a)  $\cos(x)$                       b)  $\sin(x)$                       c)  $\sinh(x)$                       d)  $e^x$
- 2) The diameters of 10000 ball bearings were measured. The mean diameter and standard deviation were found to be  $10mm$  and  $0.05mm$  respectively. Assuming Gaussian distribution of measurements, it can be expected that the number of measurements more than  $10.15mm$  will be  
(GATE IN 2010)
- a) 230                      b) 115                      c) 15                      d) 2
- 3) A person weighing  $60kg$  receives radiation energy of  $0.3J$  over the entire body. The dose of radiation absorbed (in rad) is  
(GATE IN 2010)
- a) 0.005 rad                      b) 0.1 rad                      c) 0.3 rad                      d) 0.5 rad
- 4)  $u(t)$  represents the unit step function. The Laplace transform of  $u(t - \tau)$  is  
(GATE IN 2010)
- a)  $\frac{1}{s\tau}$                       b)  $\frac{1}{s-\tau}$                       c)  $\frac{e^{-s\tau}}{s}$                       d)  $e^{-s\tau}$
- 5) A measurement system with input  $x(t)$  and output  $y(t)$  is described by the differential equation  $3\frac{dy}{dt} + 5y = 8x$ . The static sensitivity of the system is  
(GATE IN 2010)
- a) 0.60                      b) 1.60                      c) 1.67                      d) 2.67
- 6) Poisson's ratio of a metal is 0.35. Neglecting piezo-resistance effect, the gage factor of a strain gage made of this metal is  
(GATE IN 2010)
- a) 0.65                      b) 1                      c) 1.35                      d) 1.70

7) Match the following:

P. Radiation Pyrometer	W. Angular velocity measurement
Q. Dall tube	X. Vacuum pressure measurement
R. Pirani gauge	Y. Flow measurement
S. Gyroscope	Z. Temperature measurement

(GATE IN 2010)

- a) P-Z, Q-W, R-X, S-Y  
b) P-Z, Q-Y, R-X, S-W

- c) P-W, Q-X, R-Y, S-Z  
d) P-Z, Q-X, R-W, S-Y

8) In a pulse code modulated (PCM) signal sampled at  $f_s$  and encoded into an  $n$ -bit code, the minimum bandwidth required for faithful reconstruction is

(GATE IN 2010)

- a)  $2nf_s$                       b)  $nf_s$                       c)  $\frac{nf_s}{2}$                       d)  $f_s$

9) A beam of unpolarized light is first passed through a linear polarizer and then through a quarter-wave plate. The emergent beam is

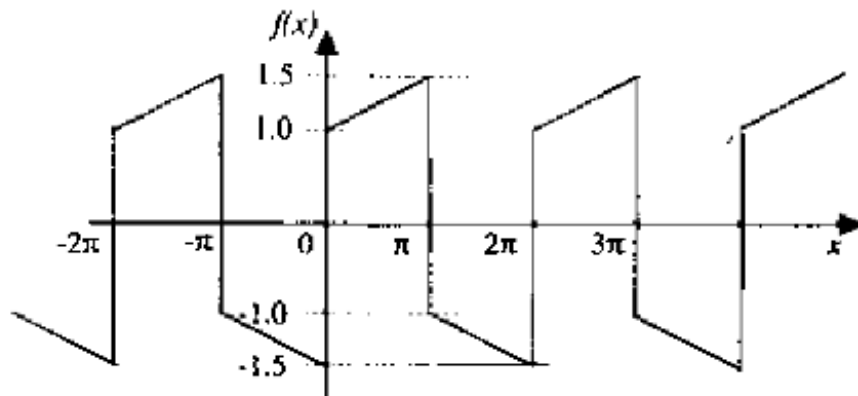
(GATE IN 2010)

- a) unpolarized                      c) circularly polarized  
b) linearly polarized                      d) elliptically polarized

10)  $f(x)$ , shown in the adjoining figure is represented by

$$f(x) = a_0 + \sum_{n=1}^{\infty} \{a_n \cos(nx) + b_n \sin(mx)\}$$

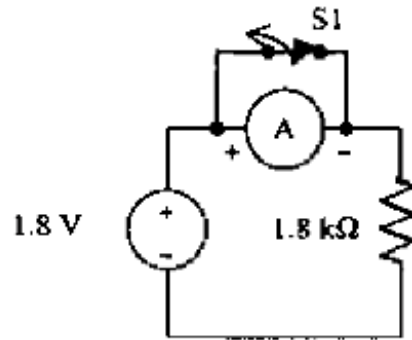
The value of  $a_0$  is



(GATE IN 2010)

- a) 0                      b)  $\frac{\pi}{2}$                       c)  $\pi$                       d)  $2\pi$

11) The PMMC ammeter A in the adjoining figure has a range of 0 to 3 mA. When switch S1 is opened, the pointer of the ammeter swings to the 1 mA mark, returns and settles at 0.9 mA. The meter is



(GATE IN 2010)

- a) critically damped and has a coil resistance of  $100 \Omega$
- b) critically damped and has a coil resistance of  $200 \Omega$
- c) under damped and has a coil resistance of  $100 \Omega$
- d) under damped and has a coil resistance of  $200 \Omega$

12) The open loop transfer function of a unity gain feedback system is given by:

$$G(s) = \frac{k(s+3)}{(s+1)(s+2)}$$

The range of positive values of  $k$  for which the closed loop system will remain stable is:

(GATE IN 2010)

- a)  $1 < k < 3$
- b)  $0 < k < 10$
- c)  $5 < k < \infty$
- d)  $0 < k < \infty$

13) A real  $n \times n$  matrix  $A = [a_{ij}]$  is defined as follows:

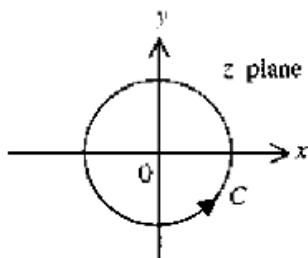
$$a_{ij} = i, \text{ if } i = j; \\ = 0, \text{ otherwise}$$

The summation of all eigenvalues of  $A$  is

(GATE IN 2010)

- a)  $n(n+1)/2$
- b)  $n(n-1)/2$
- c)  $\frac{n(n+1)(2n+1)}{6}$
- d)  $n^2$

14) The contour  $C$  in the adjoining figure is described by  $x^2 + y^2 = 16$ .



The value of

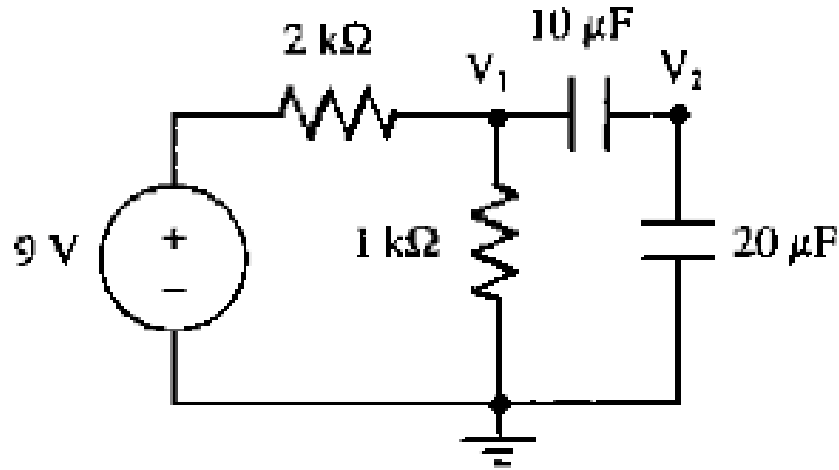
$$\oint_C \frac{z^2 + 8}{0.5z - 1.5j} dz$$

is (Note:  $j = \sqrt{-1}$ )

(GATE IN 2010)

- a)  $-2\pi j$                       b)  $2\pi j$                       c)  $4\pi j$                       d)  $-4\pi j$

15) In the dc circuit shown in the adjoining figure, the node voltage  $V_2$  at steady state is



(GATE IN 2010)

- a) 0 V                      b) 1 V                      c) 2 V                      d) 3 V

16) A  $100\ \Omega$ , 1 W resistor and a  $800\ \Omega$ , 2 W resistor are connected in series. The maximum dc voltage that can be applied continuously to the series circuit without exceeding the power limit of any of the resistors is

(GATE IN 2010)

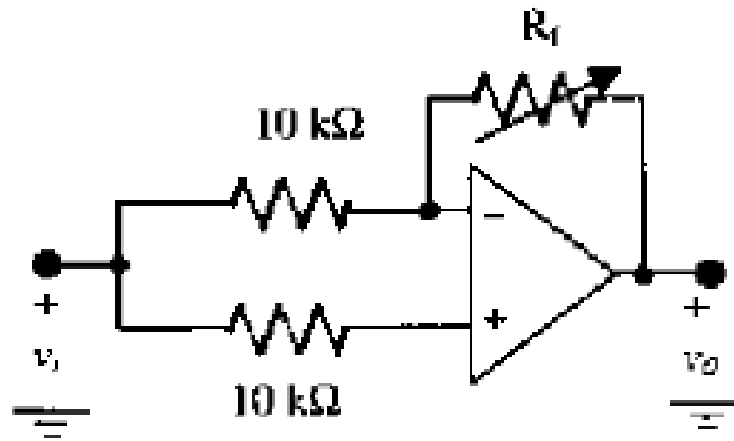
- a) 90 V                      b) 50 V                      c) 45 V                      d) 40 V

17) The seismic mass of an accelerometer oscillates sinusoidally at 100 Hz with a maximum displacement of 10 mm from its mean position. The peak acceleration of the seismic mass is

(GATE IN 2010)

- a)  $3947.84\ m/s^2$                       b)  $3141.50\ m/s^2$                       c)  $314.15\ m/s^2$                       d)  $100.00\ m/s^2$

18) In the ideal opamp circuit given in the adjoining figure, the value of  $R_f$  is varied from  $1\ k\Omega$  to  $100\ k\Omega$ . The gain  $G = (v_o/v_i)$  will



(GATE IN 2010)

- a) remain constant at +1  
 b) remain constant at -1  
 c) vary as  $-(R_f/10,000)$   
 d) vary as  $(1 + R_f/10,000)$

19) A signal with frequency components 50 Hz, 100 Hz and 200 Hz only is sampled at 150 samples/s. The ideally reconstructed signal will have frequency component(s) of

(GATE IN 2010)

- a) 50 Hz only  
 b) 75 Hz only  
 c) 50 Hz and 75 Hz  
 d) 50 Hz, 75 Hz and 100 Hz

20) The subroutine SBX given below is executed by an 8085 processor. The value in the accumulator immediately after the execution of the subroutine will be:

```
SBX: MVI A, 99h
      ADI 11h
      MOV C, A
      RET
```

(GATE IN 2010)

- a) 00h                      b) 11h                      c) 99h                      d) AAh

21) The integral  $\int_{-\infty}^{\infty} \delta(t - \pi/6) 6 \sin(t) dt$  evaluates to

(GATE IN 2010)

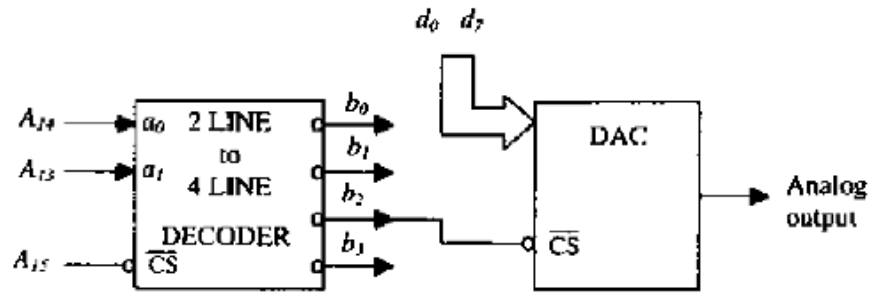
- a) 6                      b) 3                      c) 1.5                      d) 0

22) The deflection angle of the pointer of an ideal moving iron ammeter is  $20^\circ$  for 1.0 ampere dc current. If a current of  $3 \sin(314t)$  amperes is passed through the ammeter then the deflection angle is

(GATE IN 2010)

- a)  $0^\circ$                       b)  $42^\circ$                       c)  $60^\circ$                       d)  $90^\circ$

23) An 8-bit DAC is interfaced with a microprocessor having 16 address lines ( $A_0 \dots A_{15}$ ) as shown in the adjoining figure. A possible valid address for this DAC is



(GATE IN 2010)

- a) 3000h                      b) 4FFFh                      c) AFFFh                      d) C000h

24)  $H(z)$  is a discrete rational transfer function. To ensure that both  $H(z)$  and its inverse are stable its  
(GATE IN 2010)

- a) poles must be inside the unit circle and zeros must be outside the unit circle.  
 b) poles and zeros must be inside the unit circle.  
 c) poles and zeros must be outside the unit circle.  
 d) poles must be outside the unit circle and the zeros should be inside the unit circle.

25) The output voltage of a transducer with an output resistance of  $10\text{ k}\Omega$  is connected to an amplifier. The minimum input resistance of the amplifier so that the error in recording the transducer output does not exceed 2% is

(GATE IN 2010)

- a)  $10\text{ k}\Omega$                       b)  $49\text{ k}\Omega$                       c)  $490\text{ k}\Omega$                       d)  $1.2\text{ M}\Omega$

26) X and Y are non-zero square matrices of size  $n \times n$ . If  $XY = 0_{n \times n}$  then

(GATE IN 2010)

- a)  $|X| = 0$  and  $|Y| \neq 0$                       c)  $|X| = 0$  and  $|Y| = 0$   
b)  $|X| \neq 0$  and  $|Y| = 0$                       d)  $|X| \neq 0$  and  $|Y| \neq 0$

27) Consider the differential equation  $\frac{dy}{dx} + y = e^x$  with  $y(0) = 1$ . The value of  $y(1)$  is

(GATE IN 2010)

- a)  $e + e^{-1}$       b)  $\frac{1}{2}(e - e^{-1})$       c)  $\frac{1}{2}(e + e^{-1})$       d)  $2(e - e^{-1})$

28) The electric charge density in the region  $R: x^2 + y^2 \leq 1, y \leq 0$  is given as  $\sigma(x, y) = 1 \text{ C/m}^2$ , where  $x$  and  $y$  are in meters. The total charge (in coulomb) contained in the region  $R$  is (GATE IN 2010)

(GATE IN 2010)

- a)  $4\pi$                       b)  $2\pi$                       c)  $\pi/2$                       d) 0

29) The input  $x(t)$  and the corresponding output  $y(t)$  of a system are related by  $y(t) = \int_{-\infty}^{5t} x(\tau) d\tau$ . The system is (GATE IN 2010)

(GATE IN 2010)

- a) time invariant and causal                      c) time variant and noncausal  
b) time invariant and noncausal                d) time variant and causal

30) A digital filter having a transfer function  $H(z) = \frac{p_0 + p_1 z^{-1} + p_3 z^{-3}}{1 + d_3 z^{-3}}$  is implemented using Direct Form-I and Direct Form-II realizations of IIR structure. The number of delay units required in Direct Form-I and Direct Form-II realizations are, respectively (GATE IN 2010)

(GATE IN 2010)

- a) 6 and 6                  b) 6 and 3                  c) 3 and 3                  d) 3 and 2

31) The velocity  $v$  (in m/s) of a moving mass, starting from rest, is given as  $\frac{dv}{dt} = v+t$ . Using Euler forward difference method (also known as Cauchy-Euler method) with a step size of 0.1 s, the velocity at 0.2 s evaluates to \_\_\_\_\_ (GATE IN 2010)

(GATE IN 2010)

- a) 0.01 m/s                      b) 0.1 m/s                      c) 0.2 m/s                      d) 1 m/s

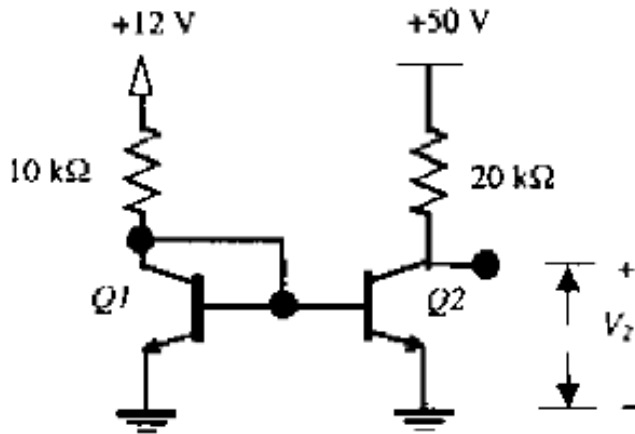
32) The rotor of the control transformer of a synchro pair gives a maximum voltage of 1.0 V at a particular position of the rotor of the control transmitter. The transmitter rotor is now rotated by  $30^\circ$  anticlockwise keeping the transformer rotor stationary. The transformer rotor voltage for this position is \_\_\_\_\_ (GATE IN 2010)

(GATE IN 2010)

- a) 1.0 V                      b) 0.866 V                      c) 0.5 V                      d) 0 V

33) The matched transistors Q1 and Q2 shown in the adjoining figure have  $\beta = 100$ . Assuming the base-emitter voltages to be 0.7 V, the collector-emitter voltage  $V_o$  of the transistor Q2 is

r O2 is



(GATE IN 2010)

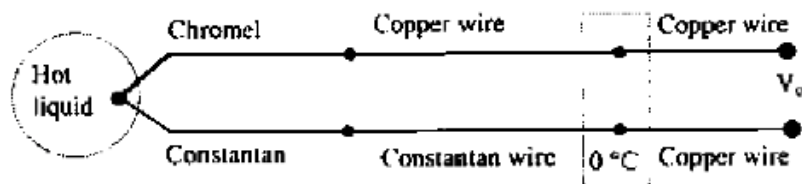
- a) 33.9 V                      b) 27.8 V                      c) 16.2 V                      d) 0.7 V

34) The volume of a cylinder is computed from measurements of its height ( $h$ ) and diameter ( $d$ ). A set of several measurements of height has an average value of 0.2 m and a standard deviation of 1%. The average value obtained for the diameter is 0.1 m and the standard deviation is 1%. Assuming the errors in the measurements of height and diameter are uncorrelated, the standard deviation of the computed volume is

(GATE IN 2010)

- a) 1.00%                      b) 1.73%                      c) 2.23%                      d) 2.41%

35) A thermocouple based temperature measurement system is shown in the adjoining figure. Relevant thermocouple emf data (in mV) is given below. The cold junction is kept at  $0^\circ\text{C}$ . The temperature is  $30^\circ\text{C}$  in the other parts of the system. The emf  $V_o$  is measured to be 26.74 mV. The temperature of the hot liquid is



Temperature	emf of Chromel-Constantan	emf of Copper-Constantan
$10^\circ\text{C}$	0.591	0.391
$20^\circ\text{C}$	1.192	0.789
$30^\circ\text{C}$	1.801	1.196
$370^\circ\text{C}$	26.549	19.027
$380^\circ\text{C}$	27.345	19.638

- a)  $370.0^\circ\text{C}$                       b)  $372.4^\circ\text{C}$                       c)  $376.6^\circ\text{C}$                       d)  $380.0^\circ\text{C}$

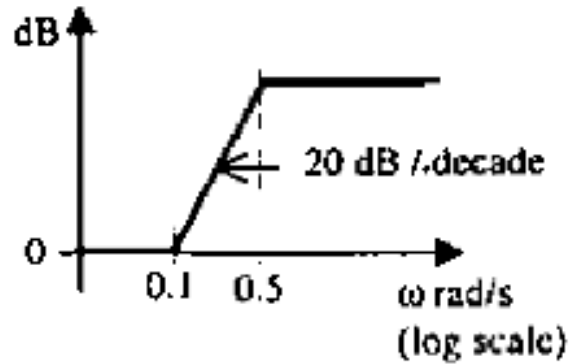
36) A differential pressure transmitter is used to measure the flow rate in a pipe. Due to aging, the sensitivity of the pressure transmitter is reduced by 5%. All other aspects of the flow meter remaining constant, change in the sensitivity of the flow measurement is

(GATE IN 2010)



- a) 10.0%                      b) 5.0%                      c) 2.5%                      d) 2.2%

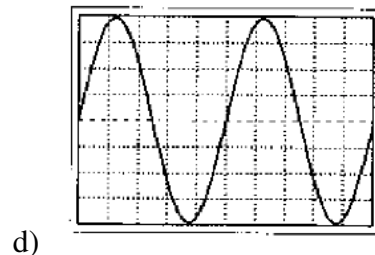
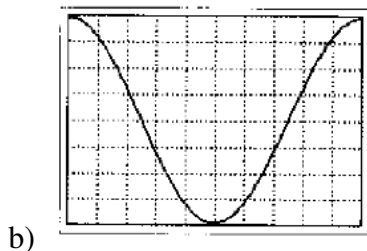
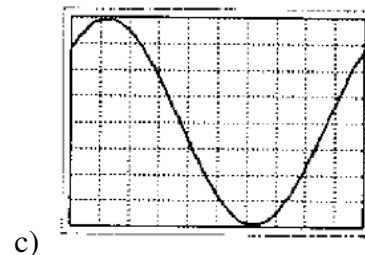
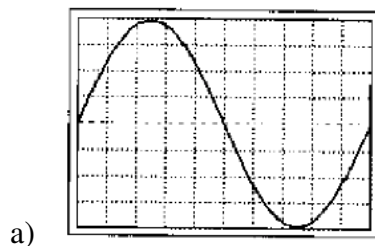
37) The asymptotic Bode magnitude plot of a lead network with its pole and zero on the left half of the s-plane is shown in the adjoining figure. The frequency at which the phase angle of the network is maximum (in rad/s) is



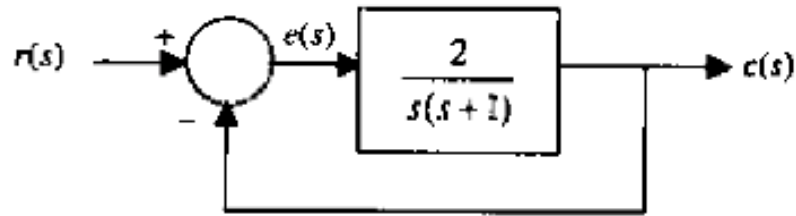
(GATE IN 2010)

- a)  $\frac{3}{\sqrt{10}}$                       b)  $\frac{1}{\sqrt{20}}$                       c)  $\frac{1}{20}$                       d)  $\frac{1}{30}$

38) In an analog single channel cathode ray oscilloscope (CRO), the x and y sensitivities are set as 1 ms/div and 1 V/div, respectively. The y-input is connected to a voltage signal  $4 \cos(200\pi t - 45^\circ)$  V. The trigger source is internal, level chosen is zero and the slope is positive. The display seen on the CRO screen is



39) A unit ramp input is applied to the system shown in the adjoining figure. The steady state error in its output is



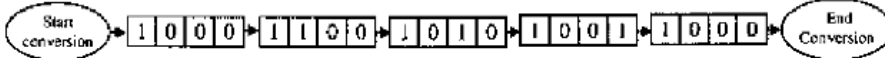
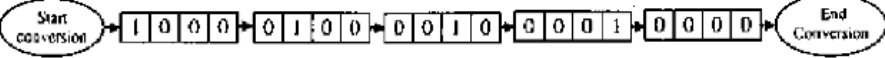
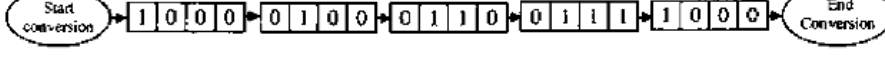

(GATE IN 2010)

- a) 0                      b) 0.5                      c) 1                      d) 2

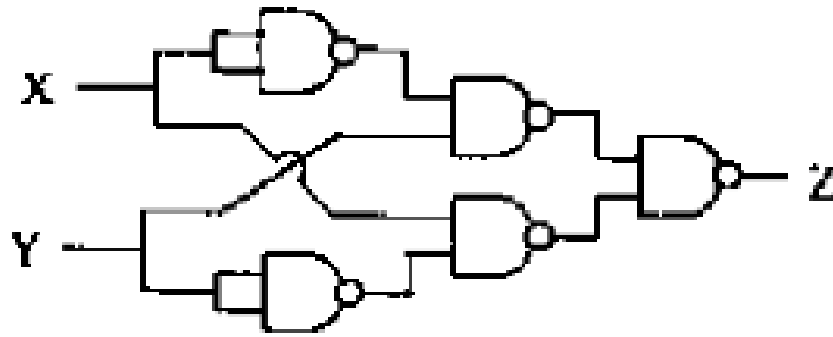
40) A unity feedback system has an open loop transfer function  $G(s) = \frac{k}{s(s+3)}$ . The value of  $k$  that yields a damping ratio of 0.5 for the closed loop system is (GATE IN 2010)

- a) 1                      b) 3                      c) 5                      d) 9

41) A 4-bit successive approximation type ADC has a full scale value of 15 V. The sequence of the states, the SAR will traverse, for the conversion of an input of 8.15 V is (GATE IN 2010)

- a) 
- b) 
- c) 
- d) 

42) The logic gate circuit shown in the adjoining figure realizes the function



(GATE IN 2010)

- a) XOR  
b) XNOR  
c) Half adder  
d) Full adder

43) In an 8085 processor, the main program calls the subroutine SUB1 given below. When the program returns to the main program after executing SUB1, the value in the accumulator is

Address	Opcode	Mnemonic
2000h	3E 00	SUB1: MVI A, 00h
2002h	CD 05 20	CALL SUB2
2005h	3C	SUB2: INR A
2006h	C9	RET

(GATE IN 2010)

- a) 00  
b) 01  
c) 02  
d) 03

44) Light coming out of an optical fiber is incident on a plane perpendicular to the fiber axis and 50 mm away from the end of the fiber. The light coming out creates a circular spot that can at most be of 20 mm diameter. Neglecting the diameter of the fiber, the numerical aperture of the fiber is, approximately,

(GATE IN 2010)

- a) 0.14  
b) 0.20  
c) 0.34  
d) 0.40

45) A solution "P" is put in a spectrophotometer cuvette of optical path length 1 cm. The transmittance is found to be 10%. Another solution "Q" has a transmittance of 40% under the same circumstances. If equal volumes of P and Q are mixed together, the transmittance of the resulting solution (assuming the constituents of P and Q do not react with each other) is, approximately,

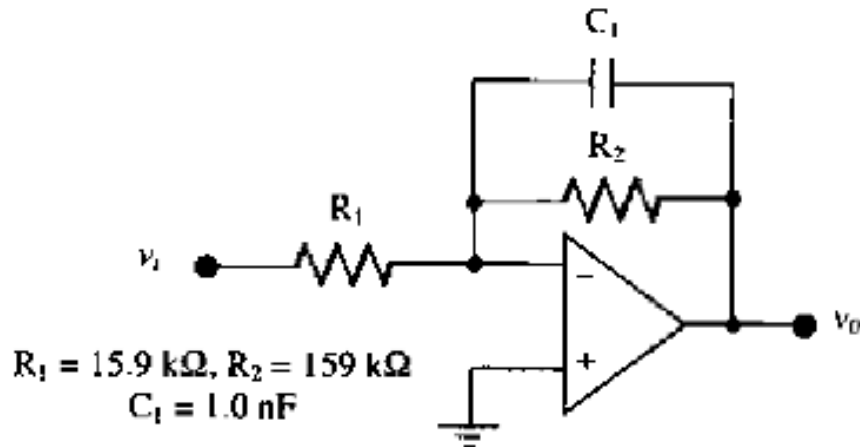
(GATE IN 2010)

- a) 15%  
b) 20%  
c) 25%  
d) 30%

- 46) 4-point DFT of a real discrete-time signal  $x[n]$  of length 4 is given by  $X[k]$ ,  $n = 0, 1, 2, 3$  and  $k = 0, 1, 2, 3$ . It is given that  $X[0] = 5$ ,  $X[1] = 1 + j1$ ,  $X[2] = 0.5$ .  $X[3]$  and  $x[0]$  respectively are  
(GATE IN 2010)

- a)  $1 - j$ , 1.875      b)  $1 - j$ , 1.500      c)  $1 + j$ , 1.875      d)  $0.1 - j0.1$ , 1.500

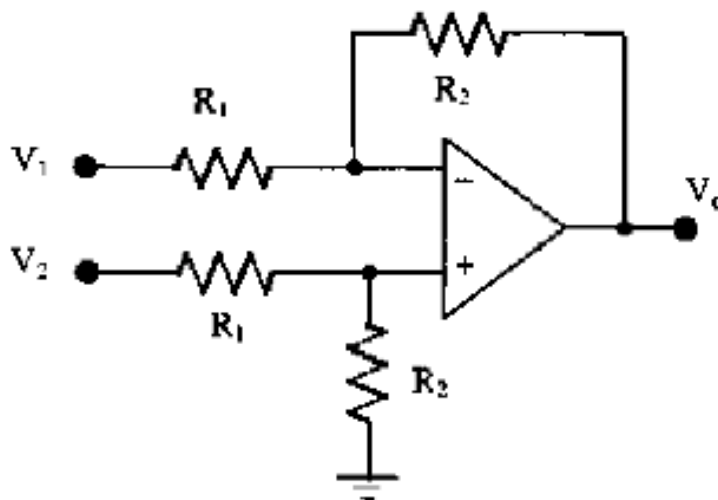
- 47) An active filter is shown in the adjoining figure. The dc gain and the 3 dB cut-off frequency of the filter respectively, are, nearly



(GATE IN 2010)

- a) 40 dB, 3.14 kHz      c) 20 dB, 6.28 kHz  
b) 40 dB, 1.00 kHz      d) 20 dB, 1.00 kHz

A differential amplifier is constructed using an ideal opamp as shown in the adjoining figure. The values of  $R_1$  and  $R_2$  are 47 kΩ and 470 kΩ respectively.



- 48) The input impedances seen looking into the terminals  $V_1$  and  $V_2$ , with respect to ground, respectively are  
(GATE IN 2010)

- a) 47 k $\Omega$  and 43 k $\Omega$   
 b) 47 k $\Omega$  and 47 k $\Omega$

- c) 47 k $\Omega$  and 517 k $\Omega$   
 d) 517 k $\Omega$  and 517 k $\Omega$

49)  $V_1$  and  $V_2$  are connected to voltage sources having an open circuit output of +1 V each and internal resistances of 13 k $\Omega$  and 3 k $\Omega$  respectively. The output voltage  $V_o$  is (GATE IN 2010)

- a) 0 V                      b) 0.15 V                      c) 1.5 V                      d) 10 V

A PMMC type ammeter has full scale current of 100  $\mu$ A and a coil resistance of 100  $\Omega$ .

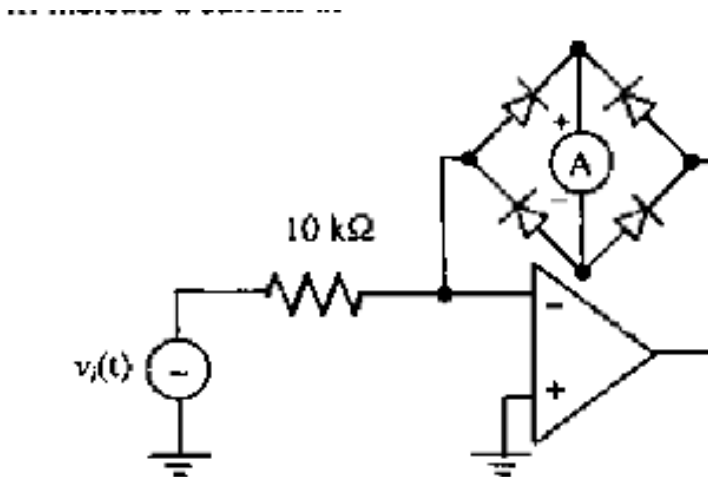
50) The resistance required to convert the 100  $\mu$ A ammeter into a 1A full scale dc ammeter is

(GATE IN 2010)

- a) 10 m $\Omega$  in series with the meter  
 b) 10 m $\Omega$  in parallel with the meter

- c) 1 m $\Omega$  in series with the meter  
 d) 1 m $\Omega$  in parallel with the meter

51) The above PMMC meter is connected in the circuit shown in the adjoining figure. The opamp is ideal. The voltage  $v_i(t) = 1.0 \sin 314t$  V. Assuming the source impedance of  $v_i(t)$  to be zero, the ammeter will indicate a current of



(GATE IN 2010)

- a) 100  $\mu$ A                      b) 70.7  $\mu$ A                      c) 63.7  $\mu$ A                      d) 31.8  $\mu$ A

A coil having an inductance (L) of 10 mH and resistance R is connected in series with an ideal 100  $\mu$ F capacitor (C). When excited by a voltage source of value  $10\sqrt{2} \cos(1000t)$  V, the series RLC circuit draws 20 W of power.

52) The value of the coil resistance R is

(GATE IN 2010)

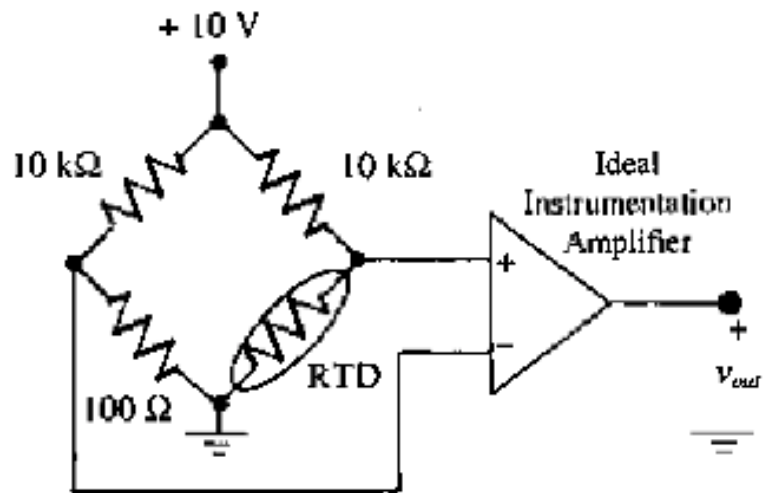
- a) 1  $\Omega$                       b) 2  $\Omega$                       c) 4  $\Omega$                       d) 5  $\Omega$

53) The Q factor of the coil at an angular frequency of 1000 rad/s is

(GATE IN 2010)

- a) 1                      b) 2                      c) 4                      d) 5

Consider a temperature measurement scheme shown in the adjoining figure. It uses an RTD whose resistance at 0°C is 100  $\Omega$  and temperature coefficient of resistance ( $\alpha$ ) is 0.00392 /°C.



- 54) The differential gain of the instrumentation amplifier to achieve a voltage sensitivity of  $10\text{ mV}/^\circ\text{C}$  at  $0^\circ\text{C}$ , should be approximately (GATE IN 2010)
- a) 13.41                      b) 26.02                      c) 57.53                      d) 90.14
- 55) The RTD is placed in a hot water bath of temperature  $100^\circ\text{C}$ . Based on the gain calculated in Q.54, the error in the measured value of the temperature due to bridge nonlinearity is (GATE IN 2010)
- a)  $-0.1^\circ\text{C}$                       b)  $0.4^\circ\text{C}$                       c)  $0.9^\circ\text{C}$                       d)  $+1.2^\circ\text{C}$

56) 25 persons are in a room. 15 of them play hockey, 17 of them play football and 10 of them play both hockey and football. Then the number of persons playing neither hockey nor football is:  
(GATE IN 2010)

- a) 2                                      b) 17                                      c) 13                                      d) 3

57) Choose the most appropriate word from the options given below to complete the following sentence:  
**If we manage to \_\_\_\_\_ our natural resources, we would leave a better planet for our children.**  
(GATE IN 2010)

- a) uphold  
b) restrain  
c) cherish  
d) conserve

58) The question below consists of a pair of related words followed by four pairs of words. Select the pair that best expresses the relation in the original pair.  
**Unemployed : Worker**  
(GATE IN 2010)

- a) fallow : land  
b) unaware : sleeper  
c) wit : jester  
d) renovated : house

59) Which of the following options is the closest in meaning to the word below:  
**Circuitous**  
(GATE IN 2010)

- a) cyclic  
b) indirect  
c) confusing  
d) crooked

60) Choose the most appropriate word from the options given below to complete the following sentence:  
**His rather casual remarks on politics \_\_\_\_\_ his lack of seriousness about the subject.**  
(GATE IN 2010)

- a) masked                                      b) belied                                      c) betrayed                                      d) suppressed

61) Hari (H), Gita (G), Irfan (I) and Saira (S) are siblings (i.e. brothers and sisters). All were born on 1<sup>st</sup> January. The age difference between any two successive siblings (that is born one after another) is less than 3 years. Given the following facts:

- Hari's age + Gita's age > Irfan's age + Saira's age.
- The age difference between Gita and Saira is 1 year. However, Gita is not the oldest and Saira is not the youngest.
- There are no twins.

In what order were they born (oldest first)?

(GATE IN 2010)

- a) HSIH                      b) SGHI                      c) IGSB                      d) IHSG

62) 5 skilled workers can build a wall in 20 days; 8 semi-skilled workers can build a wall in 25 days; 10 unskilled workers can build a wall in 30 days. If a team has 2 skilled, 6 semi-skilled and 5 unskilled workers, how long will it take to build the wall? (GATE IN 2010)

- a) 20 days                      b) 18 days                      c) 16 days                      d) 15 days

63) **Modern warfare has changed from large scale clashes of armies to suppression of civilian populations. Chemical agents that do their work silently appear to be suited to such warfare; and regrettably, there exist people in military establishments who think that chemical agents are useful tools for their cause.**

Which of the following statements best sums up the meaning of the above passage:

(GATE IN 2010)

- a) Modern warfare has resulted in civil strife.  
 b) Chemical agents are useful in modern warfare.  
 c) Use of chemical agents in warfare would be undesirable.  
 d) People in military establishments like to use chemical agents in war.

64) Given digits 2, 2, 3, 3, 3, 4, 4, 4, 4 how many distinct 4-digit numbers greater than 3000 can be formed? (GATE IN 2010)

- a) 50                      b) 51                      c) 52                      d) 54

65) If  $137 + 276 = 435$  how much is  $731 + 672$ ? (GATE IN 2010)

- a) 534                      b) 1403                      c) 1623                      d) 1513

**END OF THE QUESTION PAPER**