Matgeo Presentation - Problem 1.9.10

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Problem Statement

Given two points

$$\mathbf{A} = \begin{pmatrix} 0 \\ 6 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ -2 \end{pmatrix}.$$

find the distance between them.

Verify results using:

C implementation

Python (ctypes + numpy)

Visualization with matplotlib

solution

solution:

Let
$$\mathbf{A} = \begin{pmatrix} 0 \\ 6 \end{pmatrix}$$
, $\mathbf{B} = \begin{pmatrix} 0 \\ -2 \end{pmatrix}$. (0.1)

The distance between **A** and **B** is $d(\mathbf{A}, \mathbf{B}) = \|\mathbf{A} - \mathbf{B}\|_2$. (0.2)

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 0 \\ 6 \end{pmatrix} - \begin{pmatrix} 0 \\ -2 \end{pmatrix} = \begin{pmatrix} 0 \\ 8 \end{pmatrix}. \tag{0.3}$$

solution

$$\|\mathbf{A} - \mathbf{B}\|_2 = \sqrt{(\mathbf{A} - \mathbf{B})^T (\mathbf{A} - \mathbf{B})}.$$
 (0.4)

$$=\sqrt{\begin{pmatrix}0 & 8\end{pmatrix}\begin{pmatrix}0 \\ 8\end{pmatrix}}=\sqrt{0^2+8^2}=\sqrt{64}.$$
 (0.5)

conclusion: The distance between **A** and **B** is = 8. (0.6)

C Source Code: points.c

```
#include <stdio.h>
#include <math.h>
double distance(int x1, int y1, int x2, int y2) {
   return sqrt((x1-x2)*(x1-x2) + (y1-y2)*(y1-y2));
}
void get_points(int *points) {
   points[0] = 0; points[1] = 6; // A
   points[2] = 0; points[3] = -2; // B
```

Python Script: solve.py

```
import ctypes
# Load shared library
lib = ctypes.CDLL("./libpoints.so")
\# Define argument and return types
lib.distance.argtypes=[ctypes.c_int,ctypes.c_int,ctypes.c_int
lib.distance.restype = ctypes.c_double
lib.get_points.argtypes = [ctypes.POINTER(ctypes.c_int)]
lib.get_points.restype = None
# Prepare array for points
points = (ctypes.c_int * 4)()
lib.get_points(points)
x1, y1, x2, y2 = points
print(f"Point A = (\{x1\}, \{y1\})")
print(f"Point B = (\{x2\}, \{y2\})")
\# Get distance
dist = lib.distance(x1, y1, x2, y2)
print(f"Distance between A and B = {dist}")
```

Python Script: plot.py

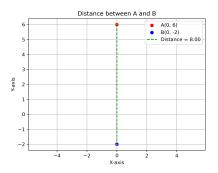
```
import numpy as np
import matplotlib.pyplot as plt
# Points
A = np.array([0, 6])
B = np.array([0, -2])
# Distance using numpy
dist = np.linalg.norm(A - B)
# Plotting
plt.scatter(A[0], A[1], color="red", label=f"A{tuple(A)}")
plt.scatter(B[0], B[1], color="blue", label=f"B{tuple(B)}")
plt.plot([A[0], B[0]], [A[1], B[1]],
         color="green", linestyle="--",
         label=f"Distance = {dist:.2f}")
```

Python Script: plot.py

```
plt.xlabel("X-axis")
plt.ylabel("Y-axis")
plt.title("Distance between A and B")
plt.legend()
plt.grid(True)
plt.axis("equal")

plt.savefig("points_plot.png", dpi=300)
plt.show()
```

Result Plot



Distance
$$= 8.00$$
 (0.7)