EE25BTECH11060 - V.Namaswi

## Question

Find matrix X such that

$$X \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{pmatrix} = \begin{pmatrix} -7 & -8 & -9 \\ 2 & 4 & 6 \end{pmatrix}$$

## **Solution**

Form the augmented matrix

$$\begin{pmatrix}
1 & 4 & | & -7 & -8 & -9 \\
2 & 5 & | & 2 & 4 & 6 \\
3 & 6 & | & 0 & 0 & 0
\end{pmatrix}$$
(1)

(2)

1

Replace  $R_2 \rightarrow R_2 - 2R_1$  and  $R_3 \rightarrow R_3 - 3R_1$ 

$$\begin{pmatrix}
1 & 4 & | & -7 & -8 & -9 \\
0 & -3 & | & 16 & 20 & 27 \\
0 & -6 & | & 21 & 24 & 27
\end{pmatrix}$$
(3)

Replace  $R_2 \rightarrow \frac{-1}{3}R_2$  and  $R_3 \rightarrow R_3 - 2R_2$ 

$$\begin{pmatrix}
1 & 4 & | & -7 & -8 & -9 \\
0 & 1 & | & -16/3 & -20/3 & -9 \\
0 & 0 & | & -11/3 & -16/3 & 9
\end{pmatrix}$$
(4)

Hence,

$$\mathbf{X} = \begin{pmatrix} 1 & 2 \\ -2 & 0 \end{pmatrix} \tag{5}$$

Pseudoinverse verification

Let,

$$\mathbf{A} = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{pmatrix} \tag{6}$$

$$\mathbf{B} = \begin{pmatrix} -7 & 2 \\ -8 & 4 \\ -9 & 6 \end{pmatrix} \tag{7}$$

$$\mathbf{A}^+ = \mathbf{A}^\top (\mathbf{A} \mathbf{A}^\top)^{-1} \tag{8}$$

$$= \begin{pmatrix} -17/18 & 4/9 \\ -1/9 & 1/9 \\ 13/18 & -2/9 \end{pmatrix} \tag{9}$$

$$\mathbf{X} = \mathbf{B}\mathbf{A}^{+} \tag{10}$$

$$= \begin{pmatrix} -7 & 2 \\ -8 & 4 \\ -9 & 6 \end{pmatrix} \begin{pmatrix} -17/18 & 4/9 \\ -1/9 & 1/9 \\ 13/18 & -2/9 \end{pmatrix}$$
 (11)

$$= \begin{pmatrix} 1 & 2 \\ -2 & 0 \end{pmatrix} \tag{12}$$

## Graph of 3 Planes

