12.40

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Question

Given
$$\mathbf{M} = \begin{pmatrix} 2 & 3 & 7 \\ 6 & 4 & 7 \\ 4 & 6 & 14 \end{pmatrix}$$
. Which of the following statements is/are

correct:

- The rank of **M** is 2
- The rank of M is 3
- The rows of M are linearly independent
- The determinant of M is zero.

Theoretical Solution

Upon row reduction of matrix M to Row Echelon form (REF),

$$\begin{pmatrix} 2 & 3 & 7 \\ 6 & 4 & 7 \\ 4 & 6 & 14 \end{pmatrix} \xrightarrow{R_2 \leftarrow R_2 - 3 \times R_1} \begin{pmatrix} 2 & 3 & 7 \\ 0 & -5 & -14 \\ 0 & 0 & 0 \end{pmatrix} \tag{1}$$

 \implies (a) The rank of **M** is 2

(b) The determinant of M is 0

C Code -Finding REF of a matrix

```
#include <stdio.h>
#define ROWS 3
#define COLS 3
void row_echelon_form(double A[ROWS][COLS]) {
    int pivot_row = 0;
   for (int pivot_col = 0; pivot_col < COLS; pivot_col++) {</pre>
       int pivot = -1;
       for (int r = pivot row; r < ROWS; r++) {</pre>
           if (A[r][pivot col] != 0.0) {
               pivot = r;
               break;
       if (pivot == -1) continue;
```

C Code -Finding REF of a matrix

```
if (pivot != pivot_row) {
   for (int c = 0; c < COLS; c++) {</pre>
       double tmp = A[pivot_row][c];
       A[pivot_row][c] = A[pivot][c];
       A[pivot][c] = tmp;
for (int r = pivot_row + 1; r < ROWS; r++) {</pre>
   if (A[r][pivot_col] != 0.0) {
       double factor = A[r][pivot_col] / A[pivot_row][
           pivot col];
       for (int c = pivot_col; c < COLS; c++) {</pre>
           A[r][c] -= factor * A[pivot row][c];
}pivot row++;
if (pivot row == ROWS) break;
```

C Code -Finding REF of a matrix

```
void solve ref(double *out) {
    double A[ROWS][COLS] = {
        \{2, 3, 7\},\
        \{6, 4, 7\},\
        {4, 6, 14}
    };
    row_echelon_form(A);
    int k = 0;
    for (int i = 0; i < ROWS; i++) {</pre>
        for (int j = 0; j < COLS; j++) {</pre>
            out[k++] = A[i][j];
```

Python+C code

```
import ctypes
import sympy as sp
# Load library
lib = ctypes.CDLL("./libref_solver.so")
# Prepare result buffer (3x3 = 9 doubles)
result = (ctypes.c_double * 9)()
lib.solve ref(result)
# Convert to SymPy Matrix
ref = sp.Matrix(3, 3, result)
print("Row Echelon Form (REF):")
sp.pprint(ref)
```

Python code

```
import sympy as sp

A=sp.Matrix([[2,3,7],[6,4,7],[4,6,14]])

ref_A=A.echelon_form()
print("Row Echelon Form:")
sp.pprint(ref_A)
```