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## EE25BTECH11026-Harsha

## **Question:**

Equations of the diagonals of the square formed by the lines x = 0, y = 0, x = 1 and y = 1 are

## **Solution:**

Let us solve the given equation theoretically and then verify the solution computationally.

According to the question,

The vertices of the square are,

$$\mathbf{a} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \mathbf{c} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad \mathbf{d} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

From the given data , we can interpret that the direction vectors of diagnols , say  $d_1$  and  $d_2$ , can be given by

$$\mathbf{d_1} = \mathbf{c} - \mathbf{a}$$
 and  $\mathbf{d_2} = \mathbf{d} - \mathbf{b}$ 

$$\therefore \mathbf{d_1} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$\mathbf{d_2} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} - \begin{pmatrix} 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

To compute the equation of the diagnols from the direction vectors, we can use the normal form of the equation, which is given by

$$\mathbf{n}^T \mathbf{r} = \mathbf{n}^T \mathbf{P}$$

where.

**n**-vector orthogonal to the direction vector

$$\mathbf{r} = \begin{pmatrix} x & y \end{pmatrix}^T$$

P=A point which lies along the vector

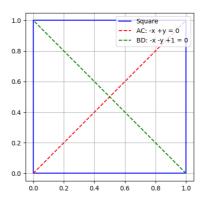
For diagnol c - a,

$$\mathbf{n} = \begin{pmatrix} -1\\1 \end{pmatrix} \quad and \quad \mathbf{P} = \begin{pmatrix} 1\\1 \end{pmatrix}$$
$$\therefore \begin{pmatrix} -1\\1 \end{pmatrix} \begin{pmatrix} x\\y \end{pmatrix} = \begin{pmatrix} -1\\1 \end{pmatrix} \begin{pmatrix} 1\\1 \end{pmatrix}$$
$$\implies y = x$$

For diagnol  $\mathbf{d} - \mathbf{b}$ ,

$$\mathbf{n} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad and \quad \mathbf{P} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
$$\therefore \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$
$$\implies x + y = 1$$

From the figure, it is clearly verified that the theoretical solution matches with the computational solution.



Plot of Square with diagonals