4.2.18

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Question

Find the direction and normal vectors of each of the following line y = x - 2

Solution

$$y = x - 2 \tag{4.2.18.1}$$

$$\Rightarrow \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} x \\ x - 2 \end{pmatrix} = \begin{pmatrix} 0 \\ -2 \end{pmatrix} + x \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$
 (4.2.18.2)

Direction Vector

yielding

$$\mathbf{x} = \mathbf{h} + \kappa \mathbf{m} \tag{4.2.18.3}$$

where \mathbf{h} is any point on the line and

$$\mathbf{m} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \tag{4.2.18.4}$$

is the direction vector.

Normal Vector

$$\mathbf{m}^T \mathbf{n} = 0 \tag{4.2.18.5}$$

$$\mathbf{n}^T \mathbf{x} = \mathbf{n}^T \mathbf{h} + \kappa \mathbf{n}^T \mathbf{m} \tag{4.2.18.6}$$

$$\Rightarrow \mathbf{n}^T(\mathbf{x} - \mathbf{h}) = 0 \text{ or } \mathbf{n}^T \mathbf{x} = c$$
 (4.2.18.7)

for

$$c = \mathbf{n}^T \mathbf{h} \tag{4.2.18.8}$$

where

$$\mathbf{n} = \begin{pmatrix} -m \\ 1 \end{pmatrix} \tag{4.2.18.9}$$

$$\begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

is defined to be the *normal vector* of the line.

C Code - A function to find if triangle is right angled

```
#include <stdio.h>
_{
m S} | // Function to compute direction and normal vectors for a line y
      = x - 2
\frac{1}{y} // General form: x - y - 2 = 0
s // Normal vector = (a, b) = (1, -1)
a \mid //  Direction vector = (b, -a) = (-1, -1)
 void line_vectors(float *dx, float *dy, float *nx, float *ny) {
     float a = 1, b = -1; // coefficients of x - y - 2 = 0
     // Normal vector
     *nx = a;
     *ny = b;
     // Direction vector
     *dx = b;
     *dy = -a;
```

Python Code

```
import numpy as np
import matplotlib.pyplot as plt
import ctypes #included
# --- Load the C library ---
try:
   c lib = ctypes.CDLL('./line.so')
except OSError:
   print(" Error: 'line.so' not found. Compile using: gcc -
       shared -o line.so -fPIC line vectors.c")
   exit()
# Define argument and return types
c lib.line vectors.argtypes = [ctypes.POINTER(ctypes.c float),
                            ctvpes.POINTER(ctypes.c_float),
                            ctypes.POINTER(ctypes.c float),
                            ctypes.POINTER(ctypes.c float)]
c lib.line vectors.restype = None
```

Python Code

```
# --- Prepare ctypes variables ---
dx = ctypes.c_float()
dy = ctypes.c_float()
nx = ctypes.c_float()
ny = ctypes.c_float()
 # --- Call C function ---
 c_lib.line_vectors(ctypes.byref(dx), ctypes.byref(dy), ctypes.
     byref(nx), ctypes.byref(ny))
 print(f" Direction vector: ({dx.value}, {dy.value})")
 print(f" Normal vector: ({nx.value}, {ny.value})")
 | # --- Plot the line y = x - 2 ---
 x = np.linspace(-2, 6, 100)
 v = x - 2
 fig, ax = plt.subplots()
 [ax.plot(x, y, label="Line: y = x - 2", color="black")]
```

Python Code

```
# Plot direction vector
ax.arrow(P[0], P[1], dx.value, dy.value,
        head_width=0.2, color="red", length_includes_head=True,
            label="Direction Vector")
# Plot normal vector
ax.arrow(P[0], P[1], nx.value, ny.value,
        head_width=0.2, color="blue", length_includes_head=True,
            label="Normal Vector")
# Formatting
ax.set xlabel("X-axis")
ax.set ylabel("Y-axis")
ax.set title("Line y = x - 2 with Direction & Normal Vectors")
ax.legend()
ax.grid(True)
ax.set aspect("equal")
```

