2.8.37

EE25BTECH11047 - RAVULA SHASHANK REDDY

September 14, 2025

Question: If $|\mathbf{a} \times \mathbf{b}|^2 + (\mathbf{a}^T \mathbf{b})^2 = 144$ and $||\mathbf{a}|| = 4$, then $||\mathbf{b}||$ is equal to

Solution:

We know that

$$|\mathbf{a} \times \mathbf{b}|^2 + (\mathbf{a}^T \mathbf{b})^2 = ||\mathbf{a}||^2 ||\mathbf{b}||^2$$
 (1)

Given:

$$|\mathbf{a} \times \mathbf{b}|^2 + (\mathbf{a}^T \mathbf{b})^2 = 144, \tag{2}$$

$$\|\mathbf{a}\| = 4,\tag{3}$$

$$144 = \|\mathbf{a}\|^2 \|\mathbf{b}\|^2 \tag{4}$$

$$144 = 4^2 ||\mathbf{b}||^2 \tag{5}$$

$$144 = 16||\mathbf{b}||^2 \tag{6}$$

$$\|\mathbf{b}\|^2 = \frac{144}{16} = 9 \tag{7}$$

$$\|\mathbf{b}\| = 3. \tag{8}$$