#### 4.3.13

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#### Question

Equations of the diagonals of the square formed by the lines x=0, y=0, x=1 and y=1 are \_\_\_\_\_\_.

#### Theoretical Solution

According to the question,
The vertices of the square are,

$$\mathbf{a} = \begin{pmatrix} 0 \\ 0 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \quad \mathbf{c} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad \mathbf{d} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

#### Equation

To compute the equation of the diagonals , we can use the normal form of the equation, which is given by

 $\mathbf{n}^T \mathbf{x} = \mathbf{0}$  for the lines passing through the origin

 $\mathbf{n}^T \mathbf{x} = 1$  for the lines not passing through the origin

where,

**n**-vector orthogonal to the direction vector

$$\mathbf{x} = \begin{pmatrix} x & y \end{pmatrix}^T$$

#### Theoretical Solution

For diagonal  $\mathbf{c} - \mathbf{a}$ , as it passes through the origin,

$$\therefore \mathbf{n}^T \mathbf{x} = 0$$

By substituting the vector through which it passes through,

$$\mathbf{n}^T \begin{pmatrix} 1 \\ 1 \end{pmatrix} = 0$$

we get

$$\mathbf{n} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$\therefore \text{ The equation of line is } \begin{pmatrix} -1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = 0$$

#### Theoretical Solution

But, for diagonal  $\mathbf{d} - \mathbf{b}$ , as the diagonal doesn't pass through the origin,

$$\mathbf{n}^T \mathbf{x} = 1$$

As we know that the diagonal  $\mathbf{d} - \mathbf{b}$  pass through the vectors  $\begin{pmatrix} 1 & 0 \end{pmatrix}^T$  and  $\begin{pmatrix} 0 & 1 \end{pmatrix}^T$ , we can say that  $\mathbf{n}$  would be  $\begin{pmatrix} 1 & 1 \end{pmatrix}^T$ 

$$\therefore$$
 The equation of line is  $\begin{pmatrix} 1 & 1 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = 1$ 

## C Code -Finding Equations of diagonals of a square

```
#include <stdio.h>
void diagonal equations (double vertices [4] [2], double n1 [2],
    double *c1, double n2[2], double *c2) {
   // A, B, C, D are the vertices
   double *A = vertices[0];
   double *B = vertices[1]:
   double *C = vertices[2];
   double *D = vertices[3];
   // Diagonal AC
   double dx1 = C[0] - A[0];
   double dy1 = C[1] - A[1];
   n1[0] = dy1;
   n1[1] = -dx1;
    *c1 = n1[0]*A[0] + n1[1]*A[1];
```

# C Code -Finding Equations of diagonals of a square

```
// Diagonal BD
double dx2 = D[0] - B[0];
double dy2 = D[1] - B[1];
n2[0] = dy2;
n2[1] = -dx2;
*c2 = n2[0]*B[0] + n2[1]*B[1];
}
```

```
import ctypes
import numpy as np
import matplotlib as mp
mp.use("TkAgg")
import matplotlib.pyplot as plt
# Load C shared library
lib = ctypes.CDLL("./libdiagonals.so")
# Define argument types for the function
lib.diagonal equations.argtypes = [
   (ctypes.c double * 2) * 4,
   ctvpes.POINTER(ctypes.c_double),
   ctypes.POINTER(ctypes.c double),
   ctypes.POINTER(ctypes.c_double),
   ctypes.POINTER(ctypes.c double)
```

```
# Define square vertices
vertices = [(0.0,0.0), (1.0,0.0), (1.0,1.0), (0.0,1.0)]
vert_array = ((ctypes.c_double*2)*4)(*[(ctypes.c_double*2)(*v)
    for v in vertices])
# Output containers
n1 = (ctypes.c_double*2)()
c1 = ctypes.c_double()
n2 = (ctypes.c_double*2)()
c2 = ctypes.c_double()
# Call C function
lib.diagonal_equations(vert_array, n1, ctypes.byref(c1), n2,
    ctypes.byref(c2))
n1 = np.array([n1[0], n1[1]])
n2 = np.array([n2[0], n2[1]])
```

```
# Convert to Cartesian equation: ax + by + d = 0
def cartesian_eq(n, c):
   a, b = n
   d = -c
   eq = []
   if a != 0:
       eq.append(f''\{a\}x'')
    if b = 0:
       sign = "+" if b > 0 and eq else ""
       eq.append(f"{sign}{b}y")
    if d != 0:
       sign = "+" if d > 0 and eq else ""
       eq.append(f"{sign}{d}")
   return " ".join(eq) + " = 0"
eq1 = cartesian eq(n1, c1.value)
eq2 = cartesian eq(n2, c2.value)
```

```
= {c1.value}")
print("Diagonal BD (normal form):", f"[{n2[0]} {n2[1]}] [x y]^T
    = \{c2.value\}"\}
 # ---- PI.OT ----
 A, B, C, D = vertices
| square x = [A[0], B[0], C[0], D[0], A[0] |
 square y = [A[1], B[1], C[1], D[1], A[1]]
plt.plot(square x, square y, 'b-', label='Square')
 # Plot diagonals
plt.plot([A[0], C[0]], [A[1], C[1]], 'r--', label=eq1)
plt.plot([B[0], D[0]], [B[1], D[1]], 'g--', label=eq2)
```

```
import matplotlib as mp
mp.use("TkAgg")
import numpy as np
import matplotlib.pyplot as plt
def line_equation_normal(point1, point2):
   """Returns line equation in normal form: n^T x = c
      where n is the normal vector and x = [x \ y]^T.""
   x1, y1 = point1
   x2, y2 = point2
   # Direction vector
   dx, dy = x2 - x1, y2 - y1
   # Normal vector
   n = np.array([dy, -dx])
   # Constant term
   c = n @ np.array([x1, y1])
   return n, c
```

```
def diagonals of square(vertices):
   Given 4 vertices of a square (in order), compute equations of
        diagonals.
   A, B, C, D = vertices
   # Diagonals are AC and BD
   line1 = line_equation_normal(A, C)
   line2 = line_equation_normal(B, D)
   return line1, line2
def format_normal_form(n, c):
   """Format equation in normal form."""
   return f''[{n[0]} {n[1]}] [x y]^T = {c}''
```

```
def format_cartesian(n, c):
    """Convert n^T x = c into Cartesian form ax + by + d = 0
    where n = [a \ b]."""
    a, b = n
    d = -c
    terms = []
    if a != 0:
        terms.append(f''\{'' \text{ if a == 1 else '-' if a == -1 else a}\}x
            ")
    if b != 0:
        sign = "+" if b > 0 and terms else ""
        terms.append(f''\{sign\}\{''' if abs(b) == 1 else b\}y'' if b
            not in [1, -1] else f''\{sign\}\{'y' \text{ if } b == 1 \text{ else } '-y'\}''
    if d != 0:
        sign = "+" if d > 0 and terms else ""
        terms.append(f"{sign}{d}")
    return " ".join(terms) + " = 0"
```

```
def plot_square_and_diagonals(vertices, line1, line2):
"""Plot square and its diagonals with Cartesian equations on
   the plot."""
A, B, C, D = vertices
square_x = [A[0], B[0], C[0], D[0], A[0]]
square_y = [A[1], B[1], C[1], D[1], A[1]]
plt.plot(square_x, square_y, 'b-', label='Square')
# Plot diagonals
plt.plot([A[0], C[0]], [A[1], C[1]], 'r--', label='Diagonal
   AC')
plt.plot([B[0], D[0]], [B[1], D[1]], 'g--', label='Diagonal
   BD')
# Equations in Cartesian form for plot
eq1 = format cartesian(*line1)
eq2 = format cartesian(*line2)
```

```
# Midpoints of diagonals
  mid AC = ((A[0]+C[0])/2, (A[1]+C[1])/2)
  mid BD = ((B[0]+D[0])/2, (B[1]+D[1])/2)
  # Place texts
  plt.text(mid_AC[0]+0.05, mid_AC[1]+0.05, eq1, color='red',
      fontsize=10, ha='left')
  plt.text(mid BD[0]-0.15, mid BD[1]-0.1, eq2, color='green',
      fontsize=10, ha='right')
  plt.gca().set aspect('equal', adjustable='box')
  plt.legend(loc="upper right")
  plt.grid(True)
  plt.savefig("/home/user/Matrix/Matgeo assignments/4.3.13/figs
      /Figure 1")
  plt.show()
```

```
vertices = [(0,0), (1,0), (1,1), (0,1)]
# Compute diagonal equations
line1, line2 = diagonals of square(vertices)
# Print normal forms
print("Diagonal AC equation (normal form):", format normal form(*
    line1))
print("Diagonal BD equation (normal form):", format normal form(*
    line2))
# Plot with Cartesian equations
plot_square_and_diagonals(vertices, line1, line2)
```

Figure: Plot of square and its diagonals

