```
In [ ]: import numpy as np
        class FuzzySet:
            def __init__(self, iterable: any):
                self.f_set = set(iterable)
                self.f_list = list(iterable)
                self.f_len = len(iterable)
                for elem in self.f set:
                    if not isinstance(elem, tuple):
                         raise TypeError("No tuples in the fuzzy set")
                    if not isinstance(elem[1], float):
                         raise ValueError("Probabilities not assigned to elements")
            def __or__(self, other):
                # fuzzy set union
                if len(self.f_set) != len(other.f_set):
                     raise ValueError("Length of the sets is different")
                f_set = [x for x in self.f_set]
                other = [x for x in other.f_set]
                return FuzzySet([f_set[i] if f_set[i][1] > other[i][1] else other[i] for i
            def __and__(self, other):
                # fuzzy set intersection
                if len(self.f_set) != len(other.f_set):
                     raise ValueError("Length of the sets is different")
                f_set = [x for x in self.f_set]
                other = [x for x in other.f_set]
                return FuzzySet([f_set[i] if f_set[i][1] < other[i][1] else other[i] for i</pre>
            def __invert__(self):
                f_set = [x for x in self.f_set]
                for indx, elem in enumerate(f_set):
                     f_{set[indx]} = (elem[0], float(round(1 - elem[1], 2)))
                return FuzzySet(f_set)
            def __sub__(self, other):
                if len(self) != len(other):
                     raise ValueError("Length of the sets is different")
                return self & ~other
            def __mul__(self, other):
                 if len(self) != len(other):
                    raise ValueError("Length of the sets is different")
                return FuzzySet([(self[i][0], self[i][1] * other[i][1]) for i in range(lend
            def __mod__(self, other):
                # cartesian product
                print(f'The size of the relation will be: {len(self)}x{len(other)} ')
                mx = self
                mi = other
                tmp = [[] for i in range(len(mx))]
                i = 0
                for x in mx:
                    for y in mi:
                        tmp[i].append(min(x[1], y[1]))
                    i += 1
                return np.array(tmp)
```

```
@staticmethod
                def max min(array1: np.ndarray, array2: np.ndarray):
                                tmp = np.zeros((array1.shape[0], array2.shape[1]))
                                t = list()
                                for i in range(len(array1)):
                                                 for j in range(len(array2[0])):
                                                                 for k in range(len(array2)):
                                                                                  t.append(round(min(array1[i][k], array2[k][j]), 2))
                                                                 tmp[i][j] = max(t)
                                                                 t.clear()
                                return tmp
                def __len__(self):
                                self.f_len = sum([1 for i in self.f_set])
                                return self.f_len
                def __str__(self):
                                return f'{[x for x in self.f_set]}'
                def __getitem__(self, item):
                                return self.f_list[item]
                def __iter__(self):
                                for i in range(len(self)):
                                                 yield self[i]
a = FuzzySet({('x1', 0.5), ('x2', 0.7), ('x3', 0.0)})
b = FuzzySet({('x1', 0.8), ('x2', 0.2), ('x3', 1.0)})
c = FuzzySet({('x', 0.3), ('y', 0.3), ('z', 0.5)})
x = FuzzySet({('a', 0.5), ('b', 0.3), ('c', 0.7)})
y = FuzzySet({('a', 0.6), ('b', 0.4)})
print(f'a -> {a}')
print(f'b -> {b}')
print(f'Fuzzy union: \n{a | b}')
print(f'Fuzzy intersection: \n{a & b}')
print(f'Fuzzy inversion of b: \n{~b}')
print(f"Fuzzy inversion of a: \n {~a}")
print(f'Fuzzy Subtraction: \n{a - b}')
r = np.array([[0.6, 0.6, 0.8, 0.9], [0.1, 0.2, 0.9, 0.8], [0.9, 0.3, 0.4, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.8], [0.9, 0.
s = np.array([[0.1, 0.2, 0.7, 0.9], [1.0, 1.0, 0.4, 0.6], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.6], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.5, 0.9], [0.0, 0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9], [0.0, 0.0, 0.9
print(f"Max Min: of \n{r} \nand \n{s}\n:\n\n")
print(FuzzySet.max_min(r, s))
```

```
a \rightarrow [('x1', 0.5), ('x3', 0.0), ('x2', 0.7)]
b -> [('x1', 0.8), ('x2', 0.2), ('x3', 1.0)]
Fuzzy union:
[('x1', 0.8), ('x2', 0.2), ('x3', 1.0)]
Fuzzy intersection:
[('x1', 0.5), ('x3', 0.0), ('x2', 0.7)]
Fuzzy inversion of b:
[('x1', 0.2), ('x3', 0.0), ('x2', 0.8)]
Fuzzy inversion of a:
 [('x1', 0.5), ('x2', 0.3), ('x3', 1.0)]
Fuzzy Subtraction:
[('x1', 0.2), ('x3', 0.0), ('x2', 0.7)]
Max Min: of
[[0.6 0.6 0.8 0.9]
[0.1 0.2 0.9 0.8]
[0.9 0.3 0.4 0.8]
[0.9 0.8 0.1 0.2]]
and
[[0.1 0.2 0.7 0.9]
[1. 1. 0.4 0.6]
[0. 0. 0.5 0.9]
[0.9 1. 0.8 0.2]]
[[0.9 0.9 0.8 0.8]
[0.8 0.8 0.8 0.9]
[0.8 0.8 0.8 0.9]
 [0.8 0.8 0.7 0.9]]
```