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A

* RCH Algorithm.

- RCH is a stream cipher and variable key length Key algorithm.
- Encrypts one byte at a time
- The key input is a pseudorandom bit generator that produces a stream 8-bit number that is unpredictable.

① Key - Generation Algorithm:-

- A variable - length 'key' from 1 to 256 bytes is used to initialise a 256 bytes state vector $S[0]$ with elements $s[0]$ to $s[256]$.
- Initial byte LK is generated from $S[0]$ by selecting one of the 256 entries in a systematic fashion.

②

Key - Scheduling Algorithm :- The entries of S are set equal to the values from 0-255 in ascending order, a temporary vector T is created. If length of total key K is 256 bytes all the K is assigned to T .

Main Formula.

```
for i = 0 to 255
    j = ((j + s[i]) + T[i]) % 256
    swap(s[i], s[j]);
```

Here s is the state vector, T is the temporary vector and j is element which will be swapped.

After the s -array is completely changed then the following algorithm is used.

while true:-

```
i = (i+1) mod 256
j = ((j + s[i]) mod 256)
swap(s[i], s[j])
t = (s[i] + s[j]) mod 256
R = s[t]
```

Then it continues with encryption using the new K_e array and s vector.

* A5/1 stream cipher.

→ A5/1 is a stream cipher used to provide privacy in GSM cellular telephone standards.

→ Uses three LFSR's (linear-feedback shift register).

→ A register is clocked if its clocking bit agrees with the clocking bit of at least one of the other two registers.

→ LFSR (1) → 19-bits feedback polynomial

$$x^{19} + x^{18} + x^{17} + x^{14} + 1$$

Clocking bit $\rightarrow 18$

Tapped bits $\rightarrow 13, 16, 14, 18$

→ LFSR (2) → 22 bits feedback polynomial

$$x^{22} + x^{21} + 1$$

Clocking bit $\rightarrow 10$.

Tapped bits $\rightarrow 20, 21$

→ LFSR (3) → 23 bits

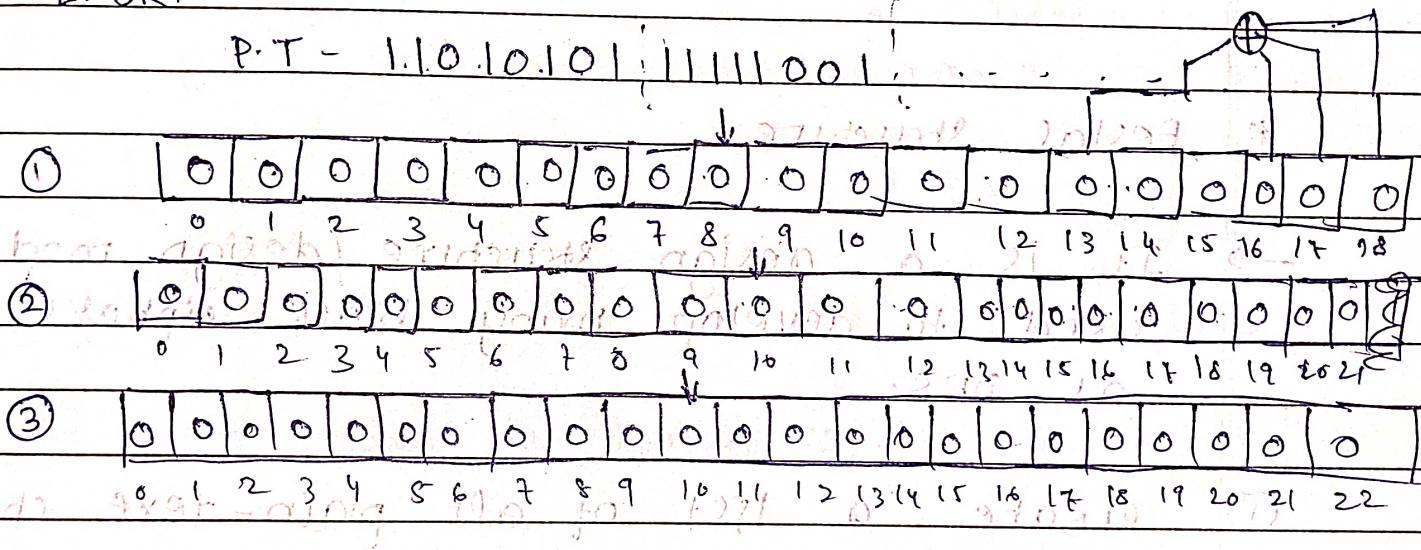
Feedback polynomial

$$x^{23} + x^{22} + x^{21} + x^8 + 1$$

Clocking bit = 8

Tapped bit = 7, 20, 21, 22

- The Keystream generator produces an infinite sequence of pseudorandom bits that are XORed with the plain-text.
 - Keystream generator is initialised with a secret key and a public frame number.
 - The Keystream generator produces a keystream bit by clocking each LFSR in turn and XORing the selected outbits from each LFSR.



Majority = maj(A[8], B[10], C[10])

Key bit (Every iteration) = A[18] ⊕ B[22] ⊕ C[22]

* Block cipher

- A block cipher takes a block of plaintext bits and generates a block of cipher text bits generally of same size.
- Avoid very small block size. Taking smaller size will reduce the possible block permutations.
- Multiple of 8-bit is the perfect size.

* Festal Structure

- It is a design structure/design model used to develop many block ciphers such as DES.
- ① Create a list of all plain-text characters.
 - ② Convert the plain text to ASCII and then 8-bit binary format.
 - ③ Divide the binary plain text string into two halves, L₁ and R₁ or R₁.
 - ④ Generate a random binary keys (K₁ and K₂) of length equal to half the length of plain text for two rounds.

$$F_1 = \text{XOR}(R_1, K_1)$$

$$F_2 = \text{XOR}(R_2, K_2)$$

$$R_2 = \text{XOR}(F_1, L_1)$$

$$L_2 = R_1$$

$$R_3 = \text{XOR}(F_2, L_2)$$

$$L_3 = R_2$$

* AES (Advanced Encryption Standard)

- A block cipher.
- The key-size can be [128 | 192 | 256] bits
- Encrypts data in blocks of 128 bits.

No. of rounds depend on the length of key.

- ① 128 bit key → 10 rounds
- ② 192 bit key → 12 rounds
- ③ 256 bit key → 14 rounds.

Plain Text

Pre round
Transform

Round 1

Round 2

Round 3

Round N

Cipher Text
(128 bit)

K_0

K_1

K_2

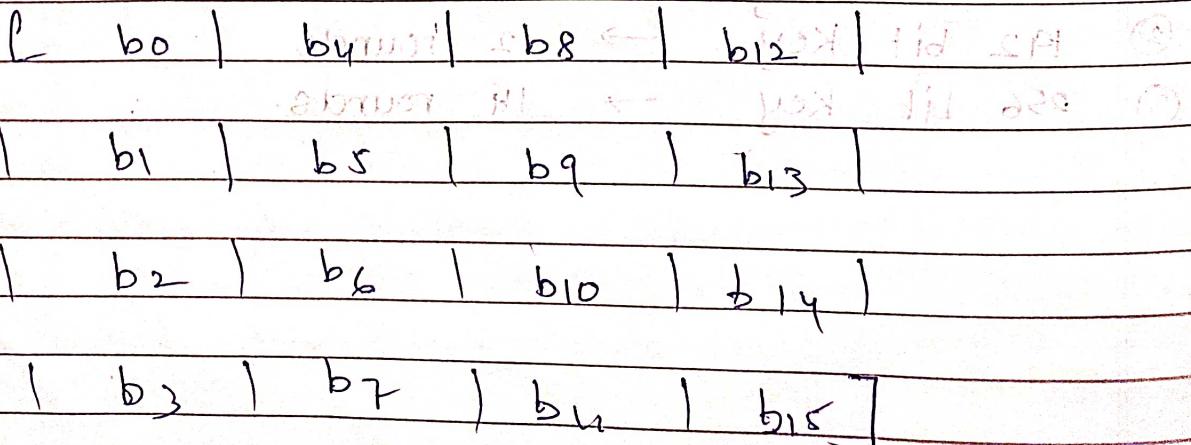
K_3

K_N

Key Expansion

Encryption:

AES considers 16 byte



Each round comprised of 4 steps

- ① SubBytes :- Each byte is substituted with another byte. Performed using a lookup table also called the S-Box.
- ② Shift Rows :- Each row is shifted a particular no. of times.
- ③ Mix Columns :- Each column is multiplied with a specific matrix. (Matrix Multiplication)
- ④ Add Round Key :- Resultant output of previous stage is XORed with corresponding round key.

Decryption

- Add Round Keys
- Inverse Mix Columns
- Inverse Shift Rows
- Inverse SubBytes.

* DES (Data Encryption Standard)

- Uses 16 round Feistel structure
- Block size of 64 bits
- Effective Key length of 56 bits

Plain text

(64-bit input) K_1 (48 bit)

Round 1

Round 2

Round 16

Final Permutation

64-bit Cipher Text

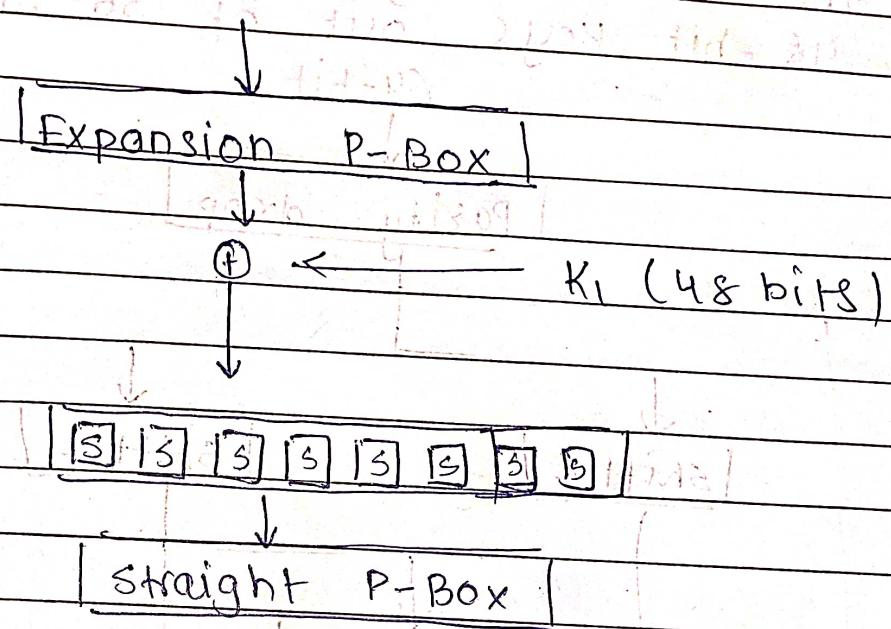
K_2 (48 bit)

K_{16} (48 bit)

56-bit
Cipher Key.

① Round function.

→ The heart of this cipher is the DES function. The DES function applies a 48-bit key to the right-most 32-bits and produces a 32-bit output.



→ Expansion Permutation Box : Expands the current 32-bit input to 48-bit input

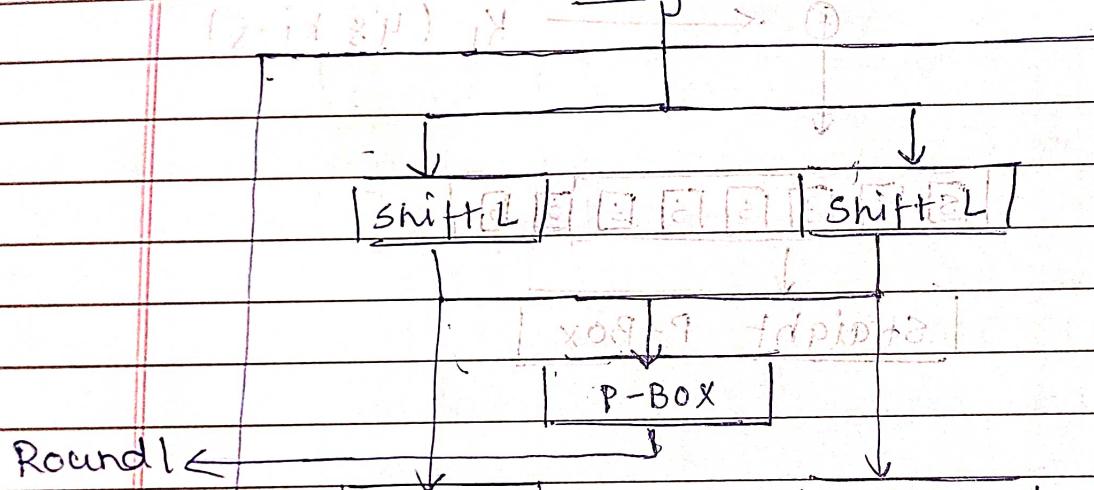
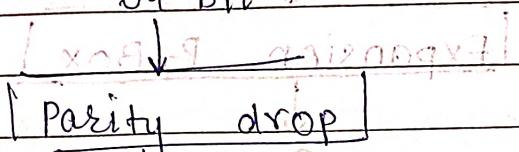
→ XOR (Whitener) → XOR operation is performed on the expanded right section and round key.

→ Substitution Boxes : The S-boxes carry out confusion. DES uses 8 S-boxes each with a 6-bit input and a 4-bit output.

→ straight permutation.

(2) Key generation

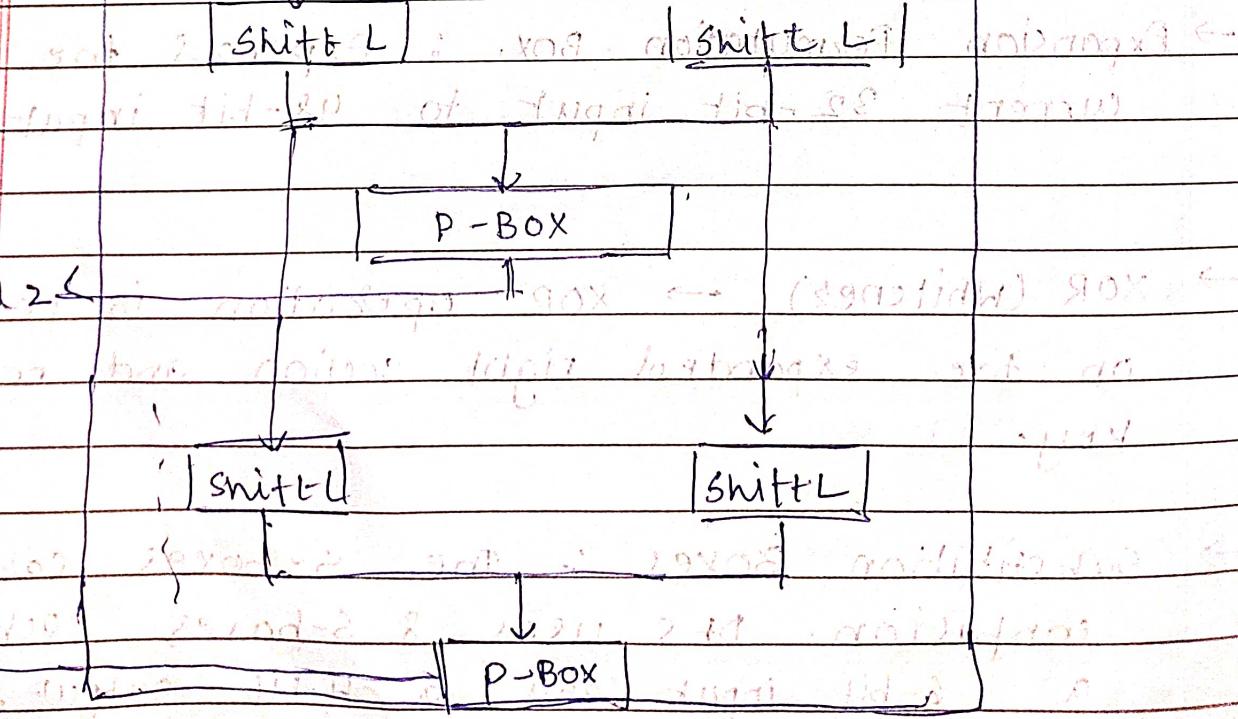
→ The round key generator generates 16-48-bit keys out of 56-bit cipher key.



Round 1

Round 2

Round 3



③ DES Analysis

- a) Avalanche Effect : A small change in plaintext result in the very great change in the cipher text.
- b) Completeness :- Each bit of ciphertext depends on many bits of plain text.

*

* Shared Key-Gen using Diffie-Hellman key exchange protocol.

→ Used to establish a shared secret that can be used for secret communication while exchanging data over a public network using the elliptic curve.

Person 1 Person 2

Public Keys - P, G Public Keys - P, G

Private Key - a Private Key - b

Key generated -

$$n = G^a \bmod P$$

Key generated -

$$y = G^b \bmod P$$

Key received = y

Key received = n

Generated secret key

$$\text{key} = K_a = y^a \bmod P$$

Generated secret

$$\text{key} = K_b = n^b \bmod P$$

Now $K_a = K_b$

Steps.

① Person 1 and Person 2 get public numbers

$$P = 23, G = 9.$$

② Person 1 selected a private key $a = 4$ and person 2 selected private key $b = 3$

$$\begin{aligned} \text{Person 1} &= 9^4 \bmod 23 = 6 \\ \text{Person 2} &= 9^3 \bmod 23 = 16 \end{aligned}$$

Person 1 receives $y = 16$

Person 2 receives $n = 6$.

$$\text{Person 1} = K_a = y^a \bmod P$$

$$\text{Person 2} = K_b = 6^3 \bmod 23 = 9$$

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- * Asymmetric Key Cryptography
- Needs two keys. Public key is used to encrypt (or code) a message and anyone can receive it.
- The other key allows you to decode / decrypt the message and is kept private.

* Advantages - No need for secure key exchange b/w Alice and Bob.

- Example - A client sends its public key to the server and requests for some data.
- The server encrypts the data using client's public key and sends the encrypted data.
- Client receives this data and decrypts it.

Applications

- ① SSL Protocol
- ② SSH protocol.
- ③ Digital Signatures.

* Digital Signature:

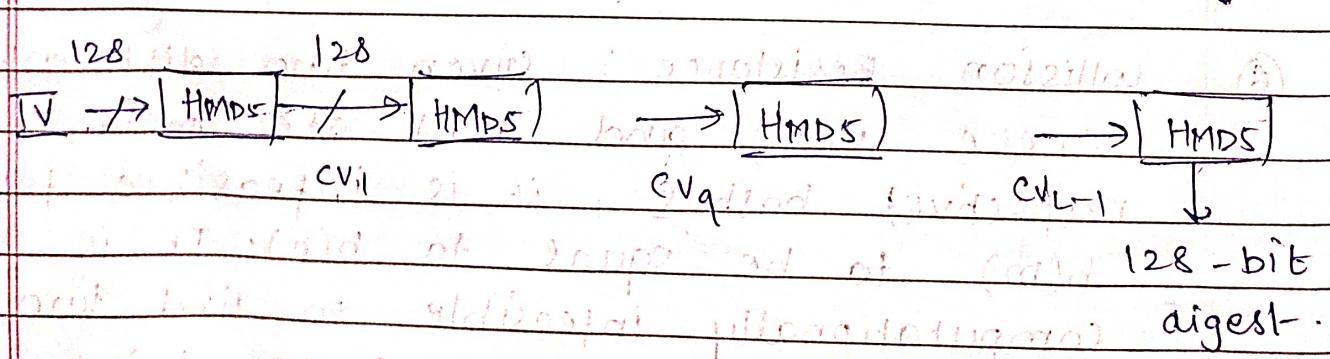
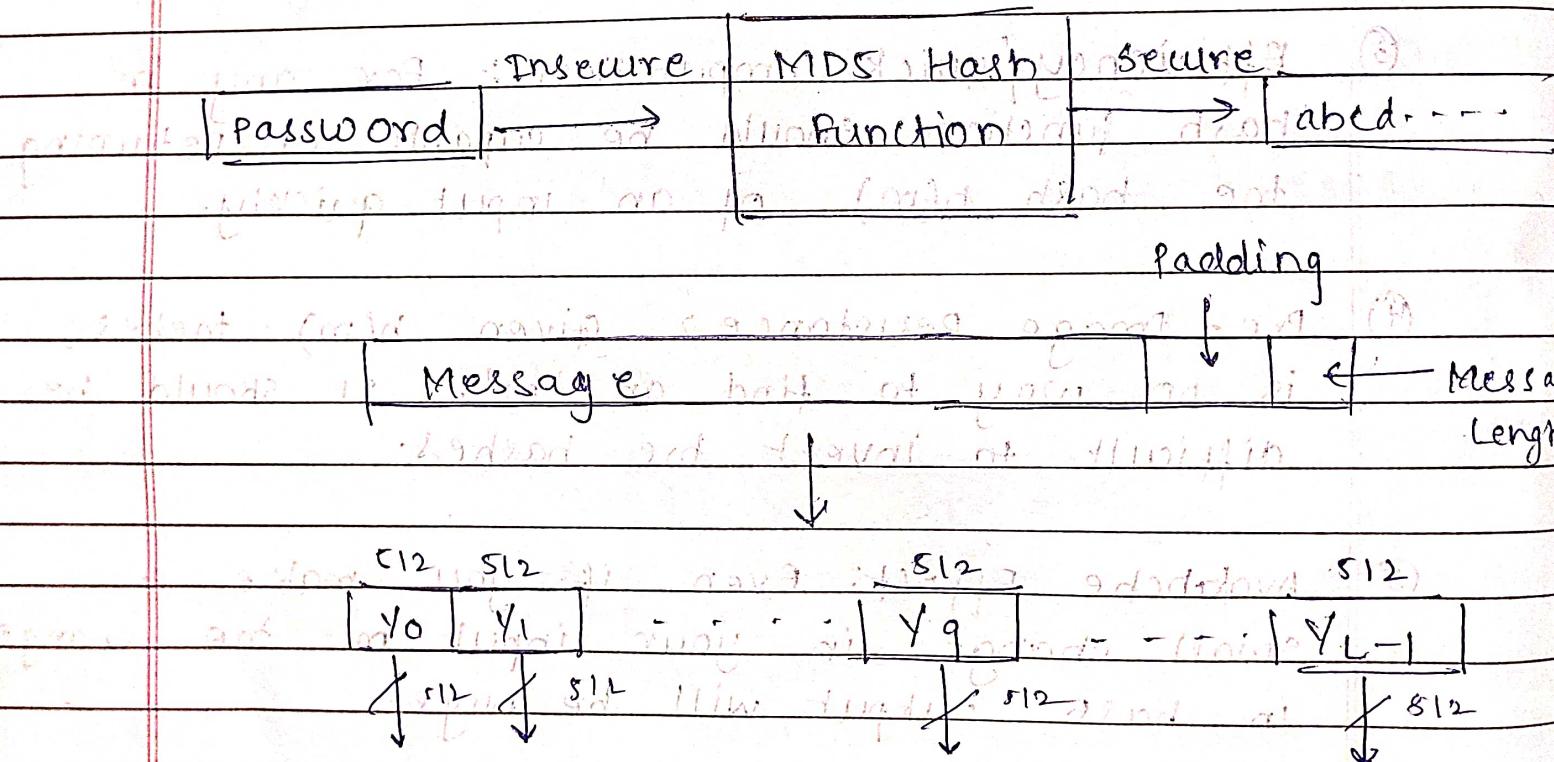
- Result of encrypting the Hash of the data to be exchanged.
- A mathematical scheme for verifying the authenticity of digital messages and documents.
- A valid digital signature gives a recipient reason to believe that the message was created by a known sender, that sender cannot deny having sent that message (denial of origin)
- A hash of a document is created using a mathematical algorithm. This hash is specific to this particular document; even the slightest change would result in a different hash.
- Encrypted using signer's private key. The encrypted hash and the signer's public key are combined into a digital signature which is appended to the document.

* Properties of a Good Cryptographic Function.

- ① Deterministic: No matter how many times you pass a particular input ' m ' through a hash function you will always get the same result $h(m)$.
- ② Compression: For any size input ' m ', output length of $h(m)$ should be small.
- ③ Efficiency/Quick Computation: For any ' m ' hash function should be capable of returning the hash $h(m)$ of an input quickly.
- ④ Pre-Image Resistance: Given $h(m)$, there is no way to find an m . It should be difficult to invert the hashes.
- ⑤ Avalanche Effect: Even if you make a small change in your input ' m ' the changes in hash output will be huge.
- ⑥ Collision Resistance: Given two different where $n(m)$ and $h(n)$ are their respective hashes, it is infeasible for $h(m)$ to be equal to $h(n)$. It is computationally infeasible to find two values that hash the same thing.

* MDS - (Message-Digest) 5)

- processes input data in 512-bit blocks.
- MDS generated message digest of 128 bits.
- used as an encryption or fingerprint function for a file.



- ① Append Padding Bits : Bits are padded to make length of original message equal to 64-bit less than exact multiple of 512.
→ Padding is single 1 followed by 0s.
- Padding is always added when length of original message is 64 bit less than exact multiple (of) 512.
- ② Append Length : calculate original length of the message (excluding padding bits) and add it to the end of the message as a 64-bit value.
- ③ Form Input Block : Divide input message into blocks of 512-bit each & divide into 16 sub-blocks.
→ Each sub-block contains 32-bits.
- ④ Initialize chaining variables.

word A : 01 01 23 45 67 89 00 00 00 00 00 00 00 00 00 00

word B : 89 AB CD EF .

word C : FE DC BA 98 .

word D : 76 43 54 32 10 01 .

word E : 0A 0B 0C 0D 0E 0F 0G 0H 0I 0J 0K 0L 0M 0N 0O 0P

⑤ Process message in 16-word blocks.

$$b = b + ((a + \text{AUX FUN}(B, C, D) + M[i] + T[k]) \ll s)$$

(3) and (4) will be carried 16 bits at a time

$$(1 - 16) \text{ bits} \quad \text{and } F(B, C, D) = (B \oplus C) \parallel (C \oplus D)$$

(17 - 32)

$$G(B, C, D) = (B \oplus D) \parallel (C \oplus D)$$

(33 - 48)

$$H(B, C, D) = B \oplus C ? D$$

(49 - 64)

$$I(B, C, D) = e? (B \parallel \neg D)$$

→ A added to 32-bit output

→ same steps as 1 to 16 should follow

→ M[i] is added to output

→ +[k] is added to output

→ circular left shifts by s-bits

→ variable b is added to output

→ resultant output becomes input for next round.

→ T[k] is an array of constant derived from sin value containing 64 elements

where each element is 32-bit.

* SHA - 1

- Processes input data in 512-bit blocks (16 32-bit words) and generates a 160-bit (5 words of 32-bit hash value called message-digest).
- Considered Insecure since PF2005.

Steps:

Env [H1-HW] \rightarrow Env [A1-AW] \leftarrow Env

① Append Padding Bits.

→ Same as MD5.

② Append of Length

$(1 \text{ bit}) \parallel (32 \text{ bits}) \leftarrow (00-1) \parallel (0H-1S)$

$\leftarrow (0H-1S) \parallel (00-1P) \leftarrow (00-1P) \parallel (00-1A) \parallel (00-1B)$

③ Forming Input Block

→ same as MD5.

④ Initialising chaining Variables

→ same as MD5.

(5) consists of 4 rounds with each round consisting of 20 steps (total 80)

$a' = e + \text{Process}(P+t, S^e(a) + W[t]) + K[t]$

Each round takes a 32-bit block of registers a, b, c, d, e and a constant $K[t]$

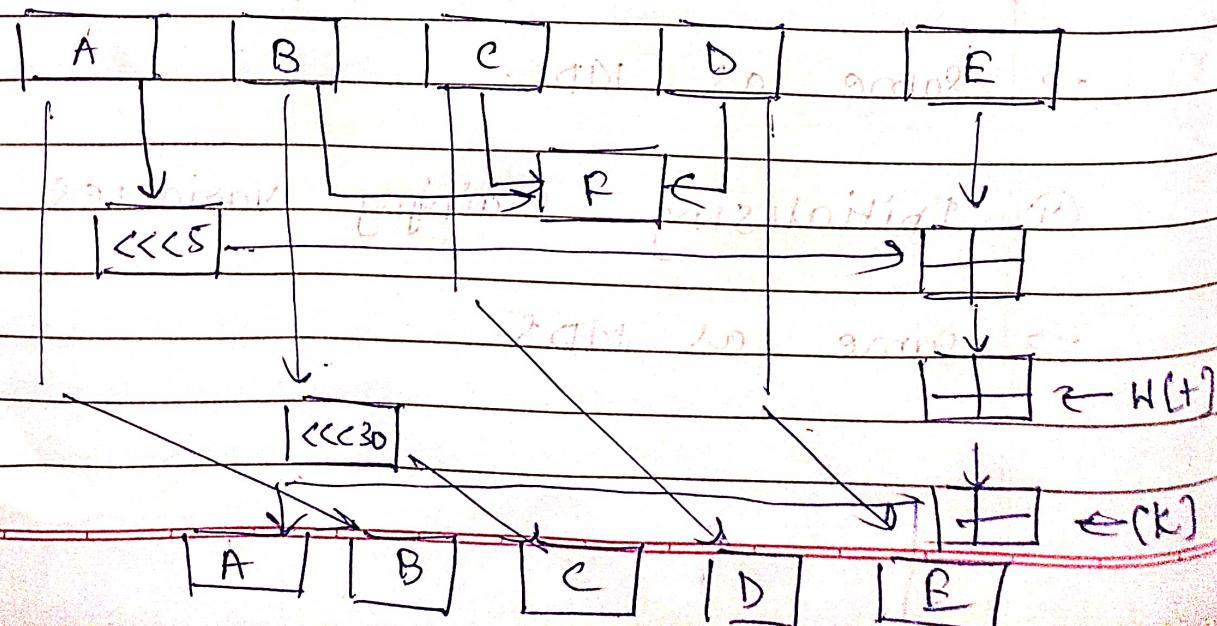
$t = 0, 1, \dots, 79$ and $80, 81, \dots, 119$ for each round.

$$W[t] = S^1(W[t-16] \oplus W[t-14] \oplus \dots \oplus W[t-8] \oplus W[t-3])$$

S^1 denotes circular left shift by 1

Round

- 1 (1-20) $\rightarrow (b \oplus e) \parallel (a \oplus d)$
- 2 (21-40) $\rightarrow b \oplus c \oplus d \oplus e$
- 3 (41-60) $\rightarrow (b \oplus c) \oplus (b \oplus d) \parallel (c \oplus d)$
- 4 (61-80) $\rightarrow (b \oplus c \oplus d \oplus e)$



Difference in MD5 and SHA-1

MD5 = 128 bits
SHA-1 = 160 bits

Message Digest Information 128 bits vs 160 bits

Operations to break 2^{128} vs 2^{160}

from MD5 to SHA-1

If 2 meg MD to SHA-1 2^{60} vs 2^{80}

are same

Hardware for SHA-1 is faster than MD5

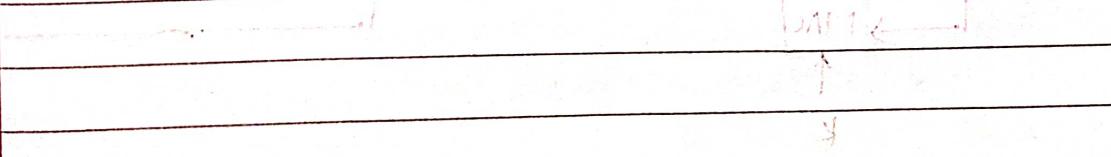
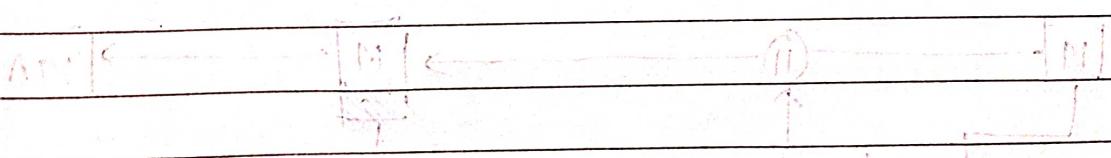
Software speed of SHA-1 is slower than MD5

Software complexity of SHA-1 is higher than MD5

Attacks have been attempted to break

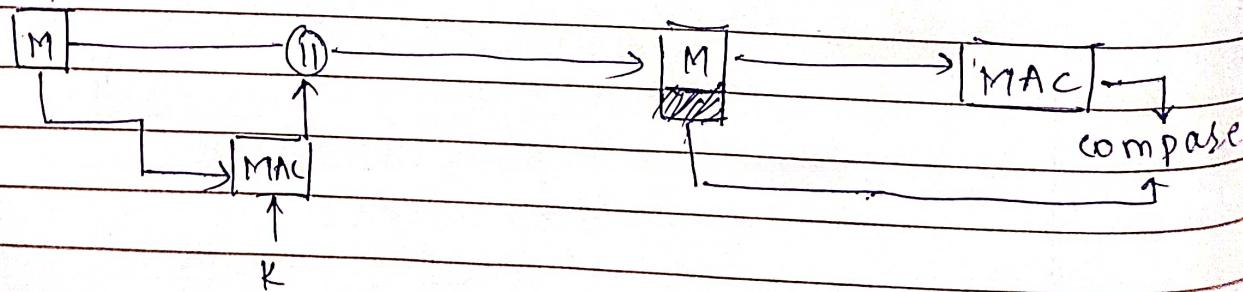
No claim of compromise some argue No claim.

Attack extent not claimed



* MAC (Message Authentication Code)

- MACs allow the message and the digest to be sent over insecure channel.
- Involves shared symmetric key between Alice and Bob.
- Also known as cryptographic checksum involving the use of secret key to generate small fixed-size block of data.
- When A has a message to send to B, calculates the MAC as a function of the message $MAC = C(M, K)$ which is appended to the original message.
- Receiver also generates the code and compares it with what he/she received thus ensuring the originality of the msg.



* Types of MAC.

- ① MAC without encryption: This model can provide authentication but not confidentiality so anyone can see the message.
- ② Internal Server Error code: Sender encrypts the content before sending it through network for confidentiality thus provides both.
- ③ External Error code: First apply MAC on the encrypted message 'c' and compare it with received MAC value on the receiver's side and then decrypt 'c' if they both are same. else we simply discard the content received.

