Support Vector Machines

Nipun Batra June 16, 2020

IIT Gandhinagar

Non-Linearly Separable Data

Data not separate in $\mathbb R$

Can we still use SVM?

Yes!

How? Project data to a higher dimensional space.

Projection/Transformation Function

$$\phi: \mathbb{R}^d \to \mathbb{R}^D$$

where, *d* = original dimension D = new dimensionIn our example:

$$d = 1; D = 2$$

Linear SVM:

Maximize

$$L(\alpha) = \sum_{i=1}^{N} \alpha_i - \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_i \alpha_j y_i y_j \overline{x_i}. \overline{x_j}$$

such that constraints are satisfied.

Transformation (ϕ)



$$L(\alpha) = \sum_{i=1}^{N} \alpha_i - \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} \alpha_i \alpha_j y_i y_j \phi(\overline{x_i}).\phi(\overline{x_j})$$

Steps

1. Compute $\phi(x)$ for each point

$$\phi: \mathbb{R}^d \to \mathbb{R}^D$$

- 2. Computer dot products over \mathbb{R}^d space
- Q. If D >> dBoth steps are expensive!

Kernel Trick