QUEUING THEOREY

S.No		QUESTION	ANSWER
	Model 1		
1	At what average rate must a clerk at a supermarket work in order to ensure a probability of 0.90 so that the customer will not have to spend more than 12 min.? It is assumed that there is only one counter at which customers arrive in a Poisson fashion at an average rate of 15 per hour The length of service by the clerk has an exponential distribution		
2	Consider a self-service store with one cashier. Assume Poisson arrivals and exponential service times .Suppose that an average nine customers arrive every 5 min. and that the cashier can serve 10 in 5 min. Find:		
	(a) aver	rage number of customers in the system	
	(b) prob	pability of having more than 10 customers in the system, and	
	(c) prob	pability that a customer has to queue for more than 2 min.	
		recan be speed up to 12 in 5 min. by using a different cash register, what will be of this on the quantities (a), (b) and (c)	
3	Customer arrive at a box office window, being manned by a single individual, according to a Poisson input process with a mean rate of 30 per hour The time required to serve a customer has an exponential distribution with a mean of 90 seconds Find the average time spent by a customer. Also determine the average number of customers in the system and the average queue length		
4	The mean rate of arrival of planes at an airport during the peak period is 20 per hour, and the actual number of arrivals in any hour follows a Poisson distribution The airport can land 60 planes per hour on an average, in good weather, and 30 planes per hour in bad weather The actual number landing in anyhour follows Poisson distribution with these respective averages. When there is congestion, the planes are forced to fly over the field in the stack awaiting the landing of other planes that arrived earlier		
		wmanyplaneswouldbeflying overthe field in the stack, on an average, in good ther conditions and in bad weather conditions?	
	(b) Hov	vlong would aplane be in the stack and in the process of landing in good and ad weather?	
5	A repair shop, attended by a single mechanic, has an average of four customers an hour who bring small appliances for repair The mechanics inspects them for defects and for this he takes six min. on an average. Arrivals are Poisson and service rate has an exponential distribution. You are required to:		
	(a) Find	the proportion of time during which there is no customer in the shop	
	(b) Find	the probability of finding at least one customer in the shop	
	(c) Calo	culate the average number of customers in the system	
	(d) Find	I the average time spent by a customer in the shop including service	

6	Inabank, cheques are cashed at a single 'teller' counter. Customers arrive at the counterina Poisson manner at an average rate of 30 customers per hour. The teller takes, on an average, a minute and a half to cash a cheque The service time has been shown to be exponentially distributed			
	(a) Calculate the % of time the teller is busy			
	(b) Calculate the average time a customer is expected to spend in the system.			
7	In a tool crib manned by a single assistant, operators arrive at the tool crib at the rate of 10 per hour. Each operator needs 3 min, on an average, to be served. Find out the loss of production due to the time lost in waiting for an operator in a shift of 8 hours, if the rate of production is 100 units per shift			
8	Trucks arrival at a factory for collecting finished goods that are supposed to be transported to distant markets. As and when they come they are required to join a waiting line and are served on first come, first served basis Trucks arrive at the rate of 10 per hour whereas the loading rate is 15 per hour It is also given that arrivals are Poisson and loading is exponentially distributed. Transporters have complained that their trucks have to wait for nearly 12 mins at the plant. Examine whether the complaint is justified Also determine the probability that the loaders are idle in the above problem.			
9	Onanaverage96patientper24hourdayrequiretheserviceofanemergencyclinic. Alsoonan average, apatientrequires 10min. ofactive attention. Assume that the facility can handle only one emergency at a time. Suppose that it costs the clinic Rs 100 per patient treated to obtain an average servicing time of 10 min. and that each min. of decreases in this average time would cost Rs 10 per patient treated, how much would have to be budgeted by the clinic to decreases the average size of the queue from 4/3 patients to 1/2 patient?			
10	Inaservicedepartmentmannedbyoneserver,onanaverageonecustomerarrivesevery10min. It has been found out that each customer requires 6 min. to be served Find out			
	(a) Average queue length			
	(b) Average time spent in the system			
	(c) Probability that there would be two customers in the queue			
11	A fertilizer company distributes its product by trucks that are loaded at its only loading station. Both, company trucks and contractor's trucks are used for this purpose. It was found that on an average, every 5 min. one truck arrived and the average loading time was 3 min. Out of these trucks 40% belong to the contractors. Making suitable assumptions, determine			
	(a) The probability that a truck has to wait			
	(b) The waiting time of a truck that waits			
	(c) The expected waiting time of contractor's trucks per day			
12	People arrive at a paying counter in a bank at the rate of 12 per hour according to a Poisson process and average time that a person is at the counter is 2 minutes with exponential distribution. (i) What is the probability that an customer on arrival will find that the clerk at counter is busy? (ii) The bank has decided to open another counter if a customer waits for 3 or more minutes at the counter. Find the average arrival rate so that the bank will open another counter			
13	Customers arrive at a one window drive in bank according to a Poisson distribution with mean of 10 per hour. Service time per customer is exponential with a mean of 5 min. The space in front of the			

	window, including that for the serviced car, can accommodate a maximum of 3 cars The other cars can wait outside this space			
		What is the probability that an arriving customer can drive directly to the space in		
	, ,	front of the window?		
		What is the probability that an arriving customer will have to wait outside the indicated space?		
	(c)	How long is an arriving customer expected to wait before starting service?		
14	A maintenance service facility has Poisson distribution arrival rates, negative exponential service times, and operates on a first come, first served queue discipline. Breakdowns occur on an average of three per day. The maintenance crew can service, on an average, six machines per day, Find the:			
	(a)	Utilization factor of the service facility		
	(b)	Mean waiting time in the system		
	(c)	Mean number machines in the system		
	(d)	Mean waiting time of machines in the queue		
	(e)	Probability of finding 2 machines in the system		
15	between one ar follows an expo	rsarrive at abooth following a Poisson distribution with an average time of 5 min. rival and the next the time taken for a telephone call is on an average 3 min. and it onential distribution. What is the probability that the booth is busy? How many more be established to reduce the total time spent to less than or equal to half of the present e?		
16	Inafactory, the machine breakdown on an average rate of 10 machines perhours. The idletime cost of a machine is estimated to be 20 per hour. The factory works 8 hours a day. The factory manager is considering 2 mechanics for repairing the machines. The first mechanic A takes about 5 min. on an average, to repair a machine and demands wages of Rs 10 per hour The second mechanic B takes about 4 min. in repairing a machine and demands wages at the rate of Rs 15 per hour. Assuming that the rate of machine breakdown is Poisson Distributed and the repair rate is exponentially distributed, which of the two mechanics should be engaged?			
17	mean 30 minute average of 12 sc	nanic finds that the time required to repair a scooter is exponentially distributed with es. The arrival rate of scooters for repair is approximately Poisson distribution with the cootersper8hoursday. Find the expected time for which the mechanic is idle in aday. oterson an average is therein the system? Also find the probability that a customer		
	Model 2			
18	service time co	2 hours, in a day (08:00 to 10:00 am), trains arrive at the yard every 20 min. but the ontinues to remain 36 min. then calculate, for this period The probability that the yard is empty, and		
	, ,	Theaveragenumber of trains in the system, on the assumption that the line capacity of the yard is only limited to 4 trains.		

19	At a railway station, only one train is handled at a time the railway yard is sufficient only for two trains to wait while the other is given a signal to leave the station. Trains arrive at the station at an average rate of 6 per hour and the railway station can handle them on an average 12 per hour. Assuming Poisson arrivals and exponential service distribution, find the steady state probabilities for the various number of trains in the system. Also find the average waiting time of a new train arriving at the yard.	
20	Assume that good trains are coming in a yard at the rate of 30 trains per day and suppose that the Inter arrival times follow an exponential distribution. The service time for each train is assumed to be exponential with an average of 36 min. If the yard can admit 9 trains at a time (there being 10 lies, one of which is reserved for shunting purpose), calculate the probability that the yard is empty and find the average queue length.	
21	Patients arrive at a clinic according to Poisson distribution at the rate of 30 patients per hour. The waiting room does not accommodate more than 14 patients. The examination time per patient is exponential with mean rate of 20 per hour. (i) Find effective arrival rate at clinic	
	(ii) What is the probability that an arriving patient will not wait. Will he find a vacant seat in the room?(iii) What is the expected waiting time until a patient is discharged from the clinic?	
22	A petrol station has a single pump and space for not more than 3 cars (2 waiting, 1 being served) A car arriving when the space is filled to capacity goes elsewhere for petrol. Cars arriving to a Poisson distribution at a mean rate of one every 8 minutes. This service time has an exponential distribution with a mean of 4 minutes. The owner has the opportunity of renting an adjacent piece of land which would provide space for an additional car to wait. (He can not build another pump) The rent will be Rs. 2000 per month. The expected net profit from each customer is Rs 2 and the station is open 10 hours every day. Would it be profitable to rent the additional space?	