# Solve with Us (Week 4)

**Machine Learning Foundations** 

Instructor: **Abhinandan Pandey** 



For what value of x, the matrix,

$$A = \begin{bmatrix} 8 & x & 0 \\ 4 & 0 & 2 \\ 12 & 6 & 0 \end{bmatrix}$$

becomes singular?



The eigenvectors of the matrix,  $\begin{bmatrix} 1 & 2 \\ 0 & 2 \end{bmatrix}$  , are written in the form

$$\begin{bmatrix} 1 \\ a \end{bmatrix}$$
 and  $\begin{bmatrix} 1 \\ b \end{bmatrix}$  . what is a+b?



If the matrix  $\begin{bmatrix} \frac{3}{5} & \frac{4}{5} \\ \frac{3}{5} & \frac{3}{5} \end{bmatrix}$ 

is orthogonal then the value of  $\, \mathcal{X} \, \mathrm{is} ? \,$ 



For the matrix, 
$$A = \begin{bmatrix} 2 & 3 \\ x & y \end{bmatrix}$$
 the eigenvalues are 4 and 8.

Calculate x+y.



Let A be the 2X2 matrix with elements  $\,a_{11}=a_{12}=a_{21}=1\,$ 

and  $a_{22}=-1$ , then the of eigenvalues of  $\mathcal{A}^{18}$  are?



The value of p such that the vector  $\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$  is an eigenvector of the matrix

$$\begin{bmatrix} 4 & 1 & 2 \\ p & 2 & 1 \\ 14 & -4 & 10 \end{bmatrix}$$
 is ?



The maximum value of 'a' such that the matrix,  $\begin{bmatrix} -3 & 0 & -2 \\ 1 & -1 & 0 \\ 0 & a & -2 \end{bmatrix}$ 

has three linearly independent real eigenvectors is



In the matrix equation Px=q, which of the following is a necessary condition for the existence of at least one solution for the unknown vector x.

- A) Augmented matrix [Pq] must have the same rank as matrix P.
- B) Vector q must have only non zero elements.
- C) Matrix P must be singular.
- D) Matrix P must be square.



Consider the following system of equations in three variables x,y and z

$$2x-y+3z=1$$

$$3x-2y+5z=2$$

$$-x-4y+z=3$$

The system of equations has



For the matrix  $\begin{bmatrix} 4 & 2 \\ 2 & 4 \end{bmatrix}$  the eigenvalue corresponding to the eigenvector

$$\begin{bmatrix} 101\\101 \end{bmatrix}$$
 is



Cayley-Hamilton theorem states that a square matrix satisfies its own characteristic equation. Consider a matrix

$$A = \begin{bmatrix} -3 & 2 \\ -1 & 0 \end{bmatrix}$$

A satisfies the relation



The eigenvalues of the following matrix are

$$\begin{bmatrix} -1 & 3 & 5 \\ -3 & -1 & 6 \\ 0 & 0 & 3 \end{bmatrix}$$



#### How was the session?



## THANK YOU!!!!