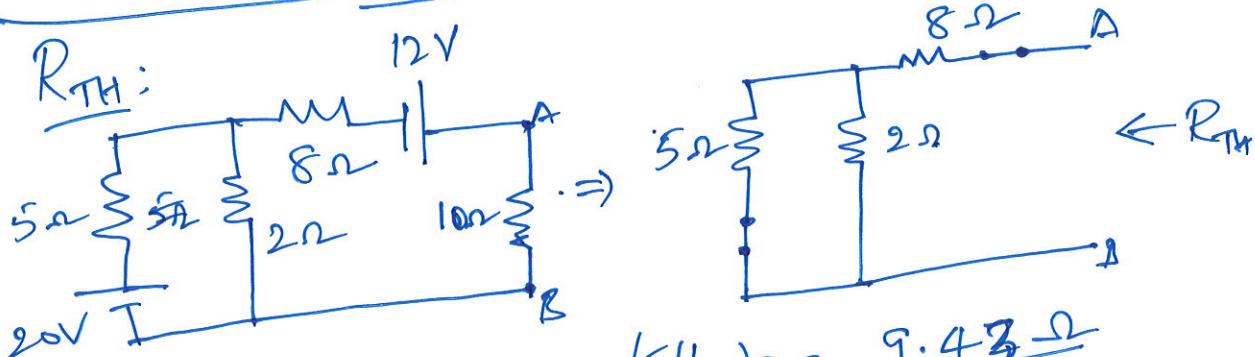
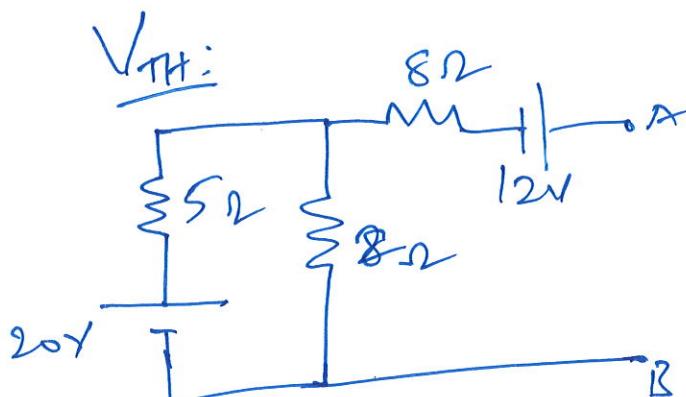


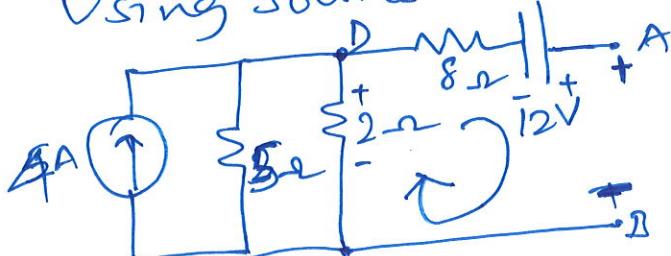
SOLUTIONS1 & 2Fig. 1Thevenin's Equivalent :

$$R_{TH} = 8\Omega + \left(\frac{5}{12}\right)\Omega = 9.43\Omega$$



$$I_{2\Omega} = \frac{4 \times 5}{2+5} = 2.86A$$

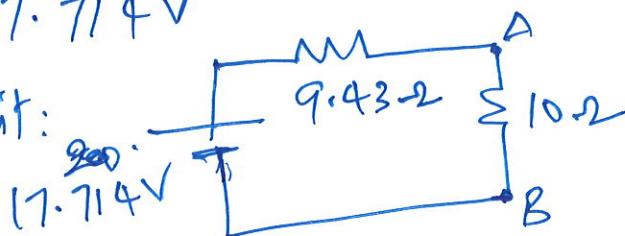
Using source transformation

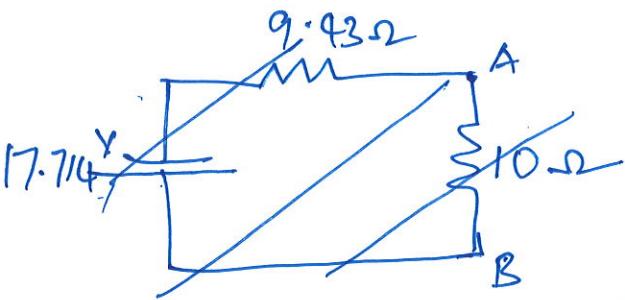
Apply KVL in loop ABDA $12 - V_{AB} + 2 \times 2.86 = 0$

$$V_{AB} = +17.714V = V_{TH}$$

$$V_{TH} = V_{AB} = +17.714V$$

Equivalent circuit:





$$I_L = \frac{17.714}{9.43 + 10} = 9.117 \text{ mA}$$

$$V_L = \frac{17.714 \times 10}{19.43} = 9.117 \text{ V}$$

As $R_L \neq R_{TH}$, maximum power is transferred.

Maximum power is transferred when $R_L = R_{TH}$

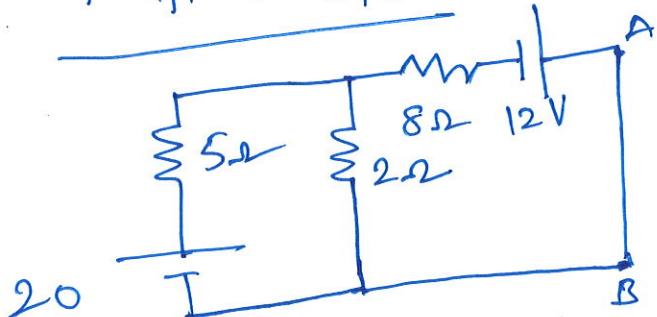
$$P_{\max} = V_L \Big|_{R_L=R_{TH}} \cdot I_L \Big|_{R_L=R_{TH}} = \frac{V_{TH}}{2} \cdot \frac{V_{TH}}{2R_{TH}} = \frac{V_{TH}^2}{4R_{TH}}$$

$$\underline{P_{\max} = 8.32 \text{ W}}$$

Norton Equivalent :

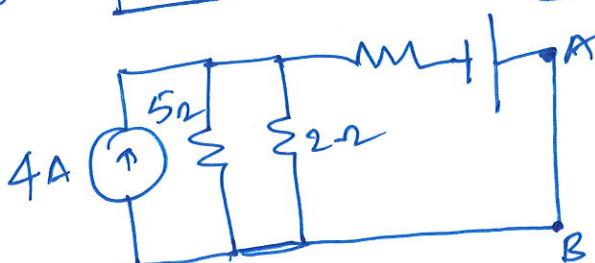
$$R_N = R_{TH} = 9.43 \Omega$$

To find I_N :



using source transformation

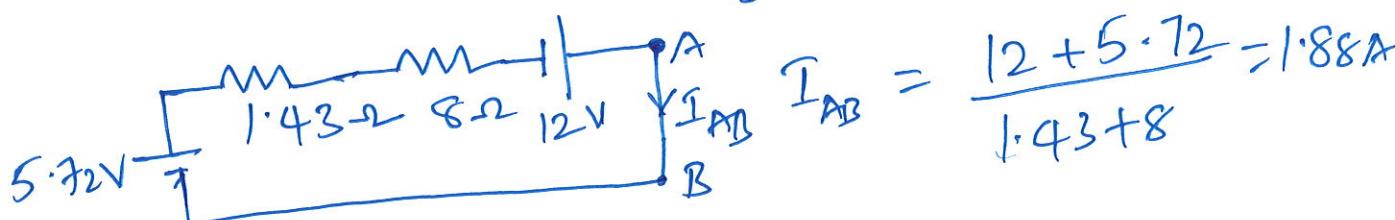
$$I_S = \frac{20}{5} = 4 \text{ A}$$



$$5//2 = 1.43 \Omega$$

Using Source Transformation

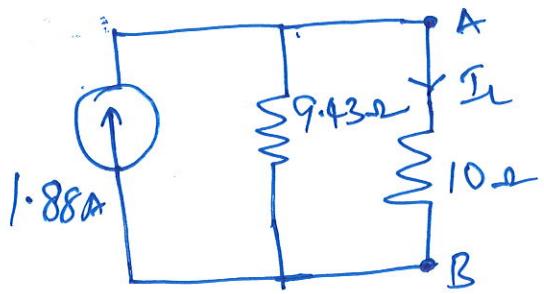
$$V_S = 4 \times 1.43 = 5.72 \text{ V}$$



$$I_{AB} = \frac{12 + 5.72}{1.43 + 8} = 1.88 \text{ A}$$

$$I_N = I_{AB} = 1.88 \text{ A}$$

(3)



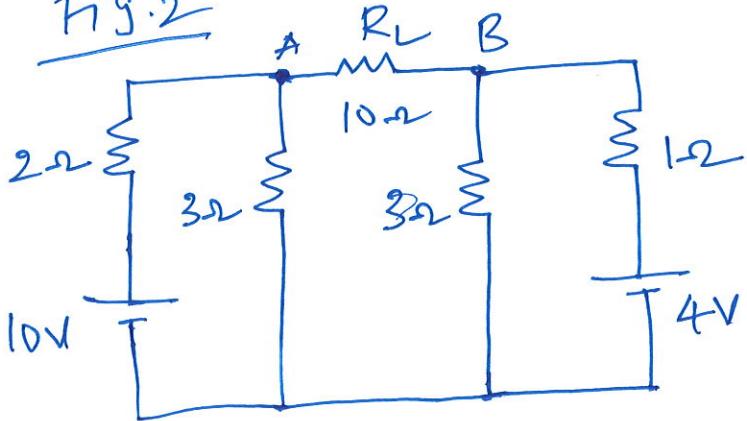
$$I_L = \frac{1.88 \times 9.43}{10 + 9.43} \approx 912 \text{ mA}$$

$$V_L = 9.12 \text{ V}$$

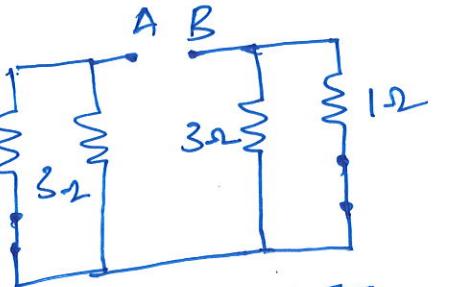
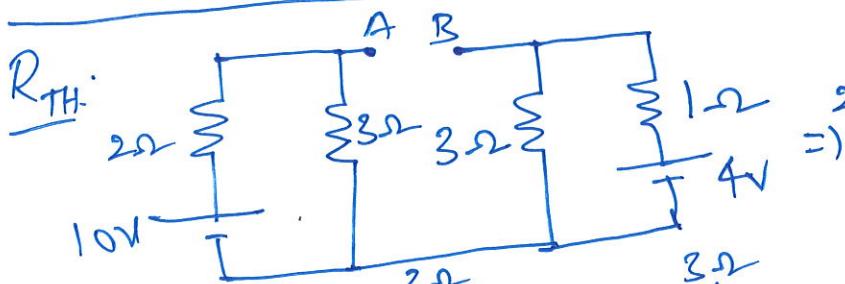
$$P_L = I_L \cdot V_L = 8.32 \text{ W}$$

(small errors are due to rounding off)

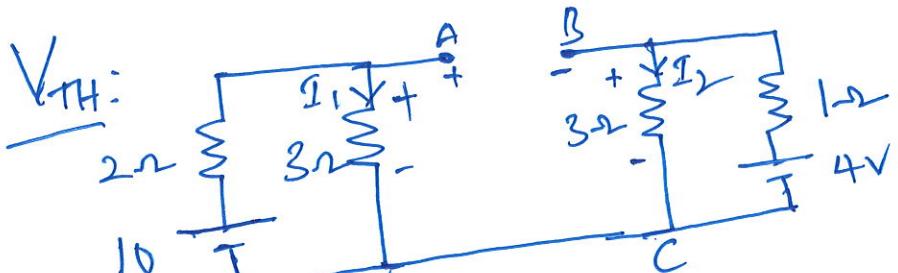
Fig. 2



THEVENIN'S EQUIVALENT:



$$R_{AB} = 1.95 \Omega \quad R_{TH} = R_{AB} = 1.95 \Omega$$



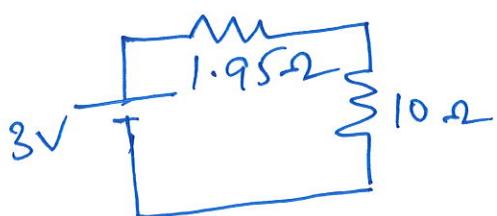
$$I_1 = \frac{10}{5} = 2 \text{ A} \quad I_2 = \frac{4}{4} = 1 \text{ A}$$

(4)

Applying KVL in the loop ABCA,

$$V_{AB} = 3 \times 2 - 3 \times 1 = 3V$$

$$V_{TH} = V_{AB} = 3V$$



$$V_L = \frac{3 \times 10}{10 + 1.95} = 2.51V$$

$$I_L = \frac{V_L}{R_L} = 0.251A$$

$$P_L = V_L \cdot I_L = 0.63W$$

Power delivered to load is maximum when $R_L = R_{TH}$

$$\text{for } R_L = R_{TH}, V_L = \frac{V_{TH}}{R_L + R_{TH}} = \frac{V_{TH}}{2} = 1.5V$$

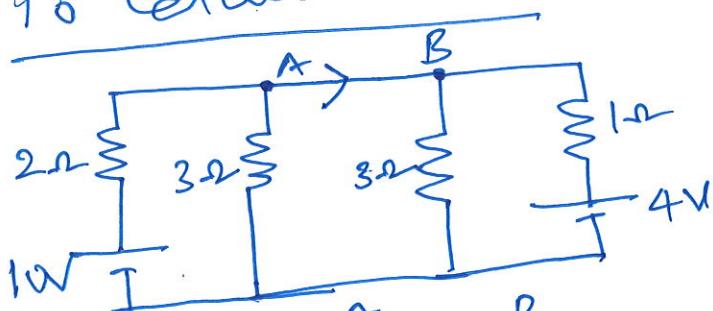
$$I_L \text{ for } R_L = R_{TH} : I_L = \frac{V_{TH}}{R_L} = \frac{1.5}{1.95} = 0.77A$$

$$\underline{\underline{P_{LMAX} = 1.154W}}$$

NORTON's EQUIVALENT :

$$R_N = R_{TH} = 1.95\Omega$$

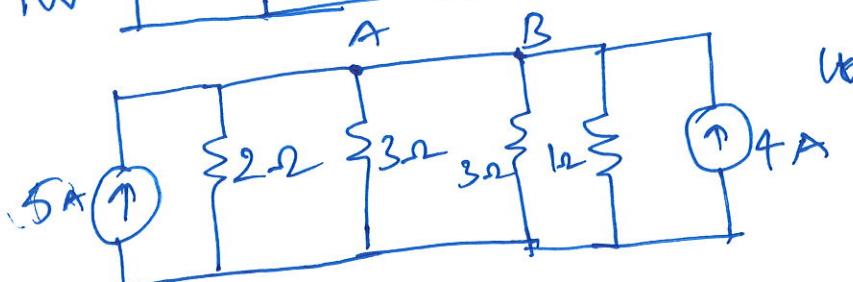
To calculate I_N :



Using Source transformation

$$I_{S1} = \frac{10}{2} = 5A$$

$$I_{S2} = \frac{4}{1} = 4A$$



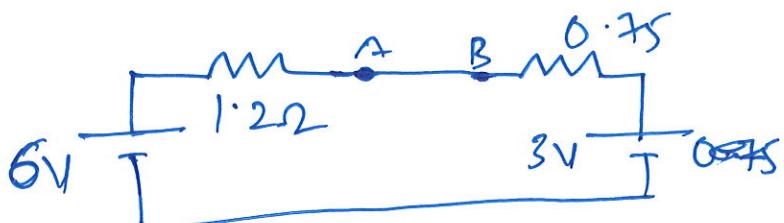
$$2//3 = 1.2\Omega$$

$$3//1 = 0.75\Omega$$

(5)

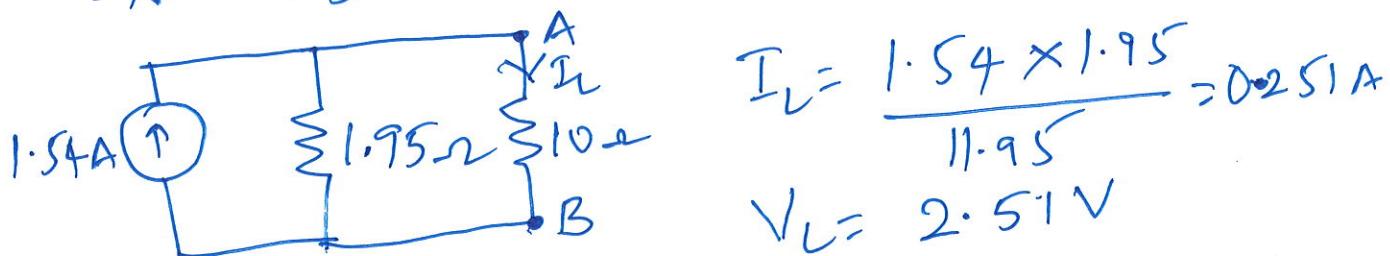
Using Source transformation,

$$V_{S1} = 5A \times 1.2 = 6V \quad V_{S2} = 4A \times 0.75 = 3V$$



$$I_{AB} = \frac{6-3}{1.95} = 1.54A$$

$$I_N = I_{AB} = 1.54A$$

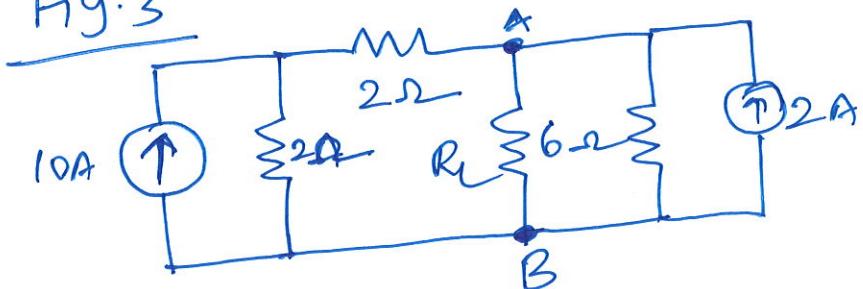


$$I_L = \frac{1.54 \times 1.95}{11.95} = 0.251A$$

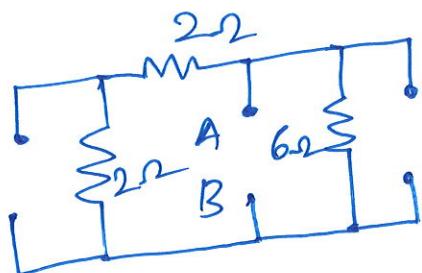
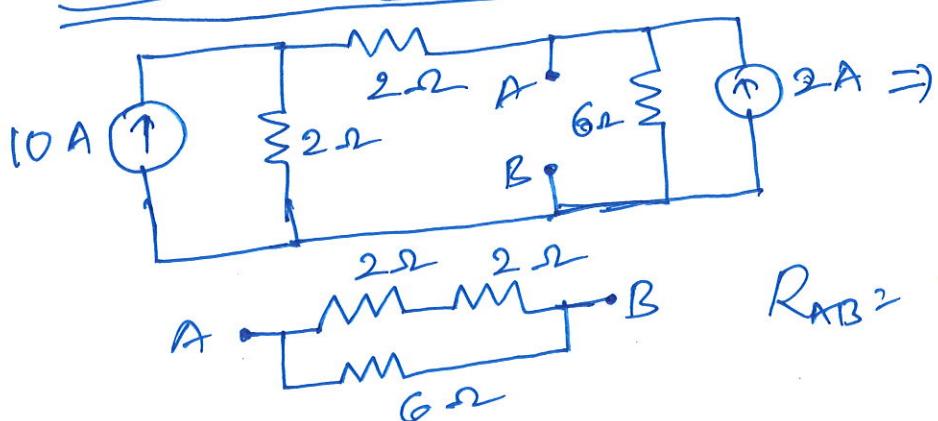
$$V_L = 2.51V$$

$$P_L = V_L \cdot I_L = \underline{\underline{0.63W}}$$

Fig. 3



THEVENIN'S EQUIVALENT



$$R_{AB} = 4//6 = 2.4\Omega$$

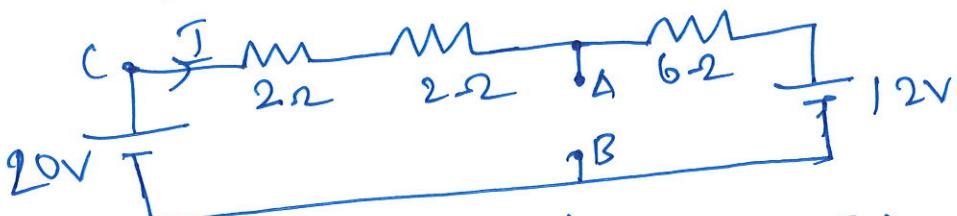
$$R_{TH} = R_{AB} = 2.4\Omega$$

(6)

To find V_{TH} :

Using Source transformation,

$$V_{S_1} = 10 \times 2 = 20V \quad V_{S_2} = 2 \times 6 = 12V$$

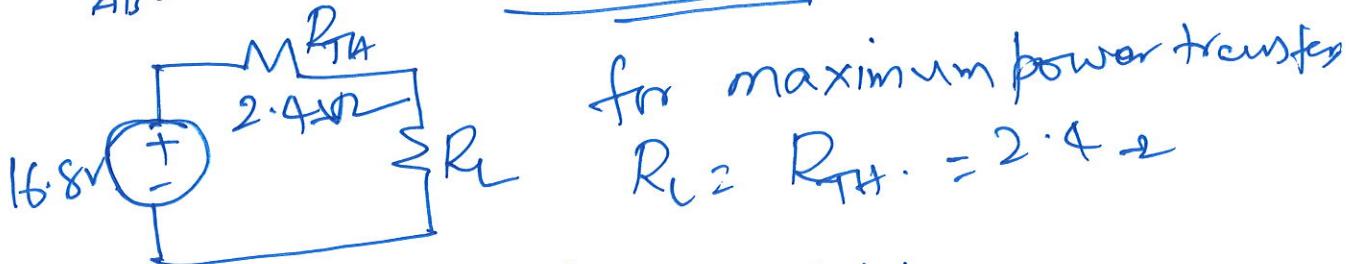


$$I = \frac{20 - 12}{2 + 2 + 6} = 0.8A$$

Applying KVL for the loop ABCA,

$$20 - I(2+2) = V_{AD} = 20 - 0.8 \times 4 = 16.8V$$

$$V_{AD} = 16.8V \quad V_{TH} = \underline{V_{AB}} = 16.8V$$



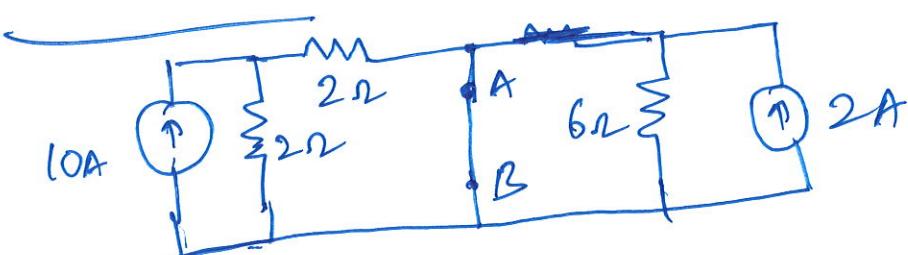
$$V_L = \frac{16.8 \times 2.4}{2.4 + 2.4} = 8.4V$$

$$I_L = \frac{8.4}{2.4} = 3.5A \quad P_L = \underline{\underline{28.04W}}$$

Norton's Equivalent:

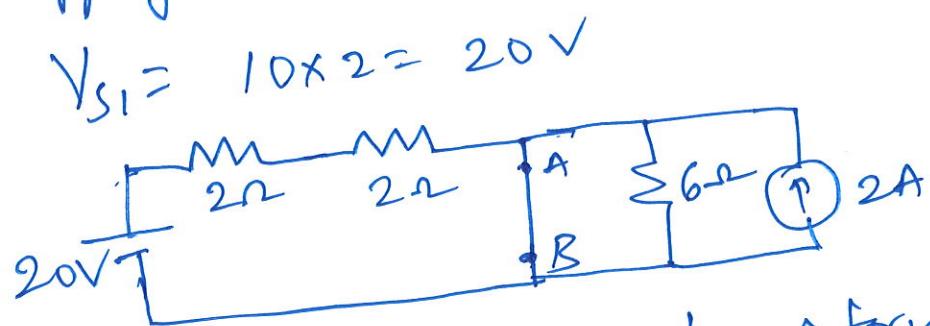
$$R_N = R_{TH} = 2.4\Omega$$

To find I_N :

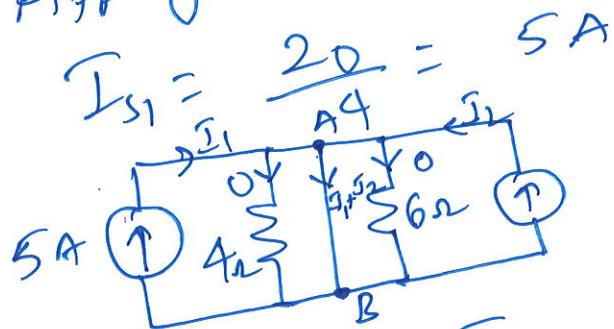


(7)

Applying Source transformation,

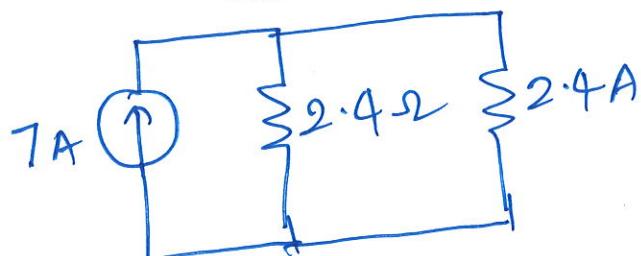


Applying source transformation,



$$I_1 + I_2 = 7A$$

$$I_{AB} = 7A = I_N$$

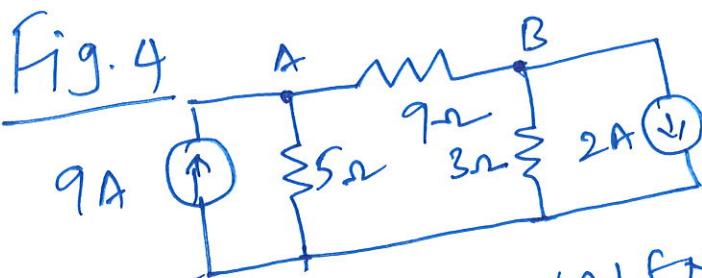


$$I_L = \frac{7 \times 2.4}{4.8} = 3.5A$$

$$V_L = I_L R_L = 8.4V$$

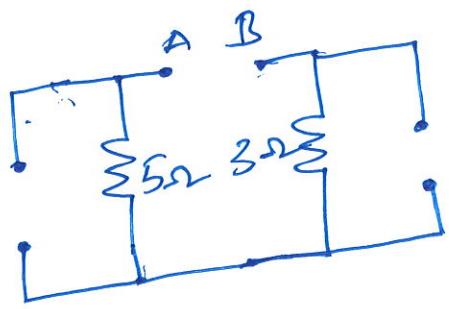
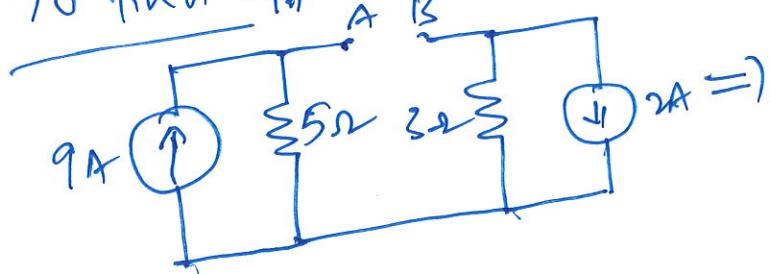
$$P_V = 29.4W$$

Fig. 4



THEVENIN'S EQUIVALENT CIRCUIT :

To find R_{TH} :

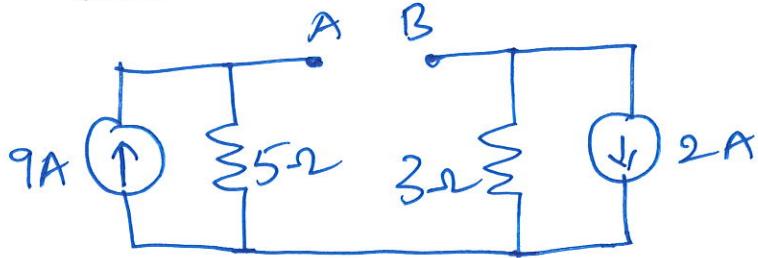


(8)

$$R_{AB} = 8\Omega$$

$$R_{TH} = R_{AB} = \underline{8\Omega}$$

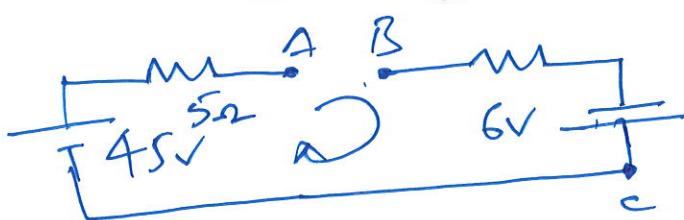
To find V_{TH} :



Using Source transformation

$$V_{S_1} = 9 \times 5 = 45V$$

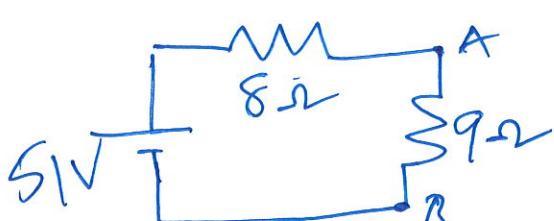
$$V_{S_2} = 2 \times 3 = 6V$$



Applying KVL for the loop A(BCA)

$$45 - V_{AB} + 6 = 0 \quad V_{AB} = \underline{51V}$$

$$V_{TH} = V_{AB} = \underline{51V}$$



$$V_L = \frac{51 \times 9}{9+8} = 27V$$

$$I_L = 27/9 = 3A$$

$$P_L = V_L I_L = 81W$$

P_L is maximum when $R_L = R_{TH}$

$$\text{Then } P_{L,\max} = \frac{V_L \cdot R_L}{R_L + R_{TH}} \Bigg|_{R_L=R_{TH}} \cdot \frac{V_L}{R_L + R_{TH}} \Bigg|_{R_L=R_{TH}}$$

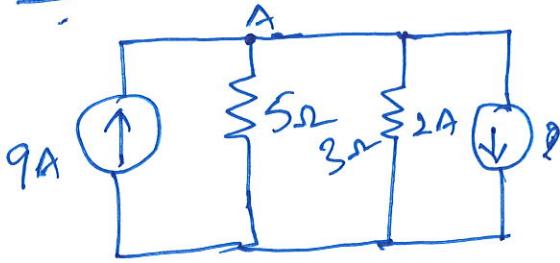
$$= 25 \cdot 5 \times \frac{25 \cdot 5}{25+8} = \underline{\underline{81.28W}}$$

NORTON's EQUIVALENT

$$R_N = R_{TH} = 8\Omega$$

To find I_N :

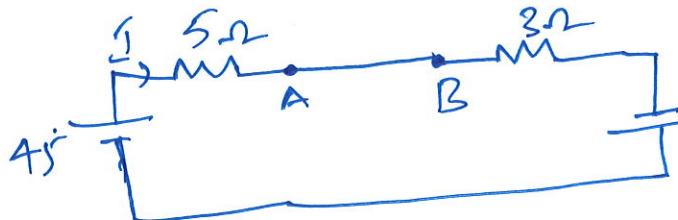
(9)



Using Source transformation

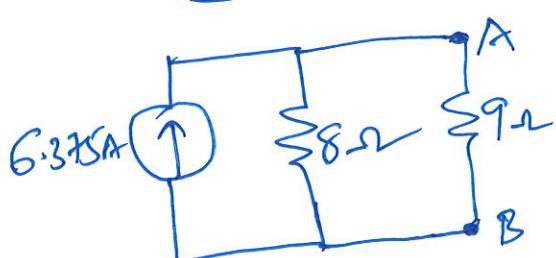
$$V_{S_1} = 9 \times 5 = 45V$$

$$V_{S_2} = 2 \times 3 = 6V$$



$$I = \frac{45 + 6}{8} = 6.375A$$

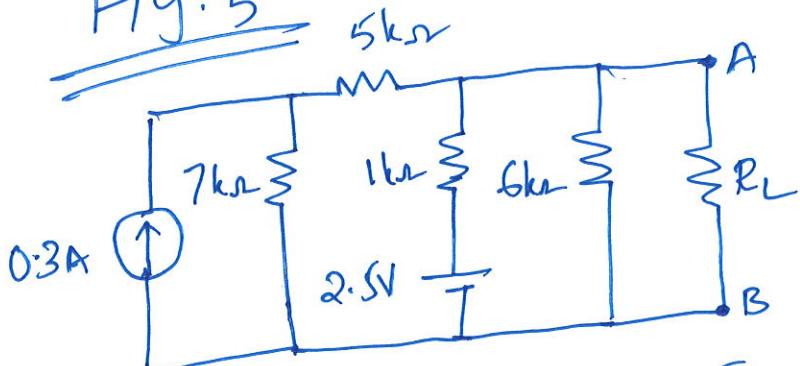
$$I_N = 6.375A$$



$$I_L = \frac{6.375 \times 8}{8 + 9} = 3A$$

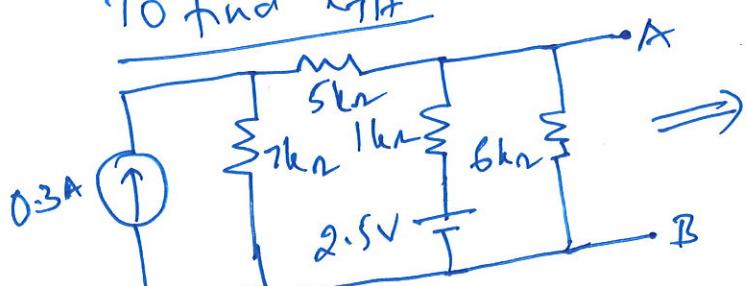
$$V_L = I_L \cdot R_L = 3 \times 9 = 27V$$

Fig. 5

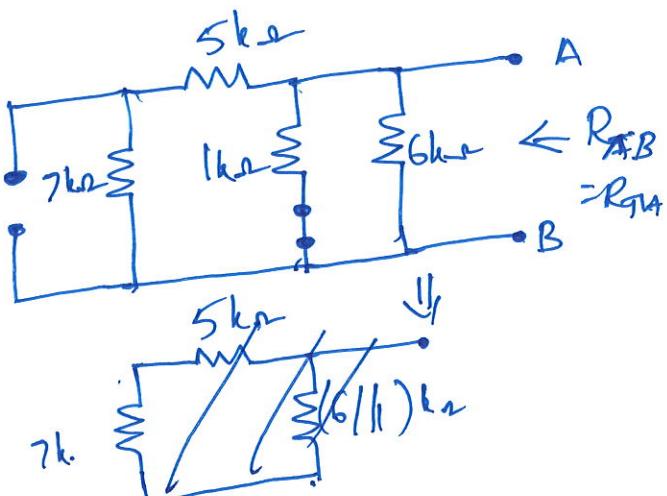


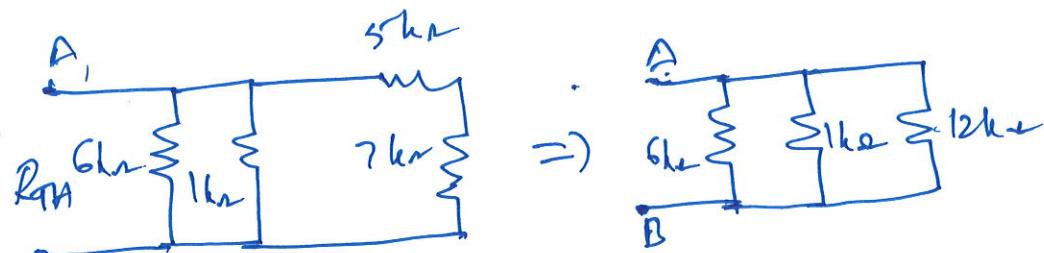
THEVININ'S EQUIVALENT

To find R_{TH}



$$6k \parallel 1k = 857\text{ }\Omega$$

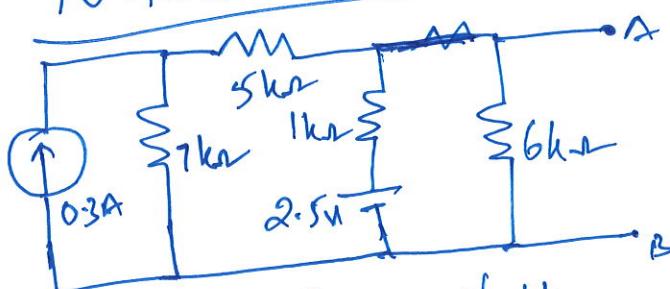




$$R_{AB} = (6\text{k}\Omega \parallel 1\text{k}\Omega \parallel 7\text{k}\Omega) = 800\text{\Omega}$$

$$R_{TH} = R_{AB} = 800\text{\Omega}$$

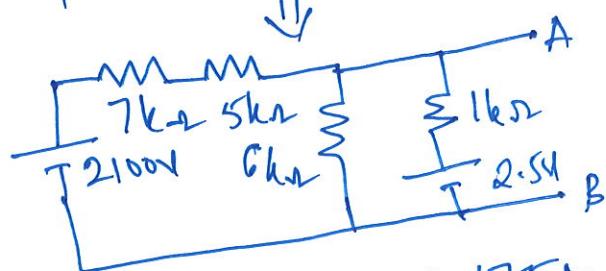
To find V_{TH}



$$V_{TH} = V_{AD} = V_{6\text{k}\Omega} = \text{Voltage across } 2.5\text{V source and } 1\text{k}\Omega.$$

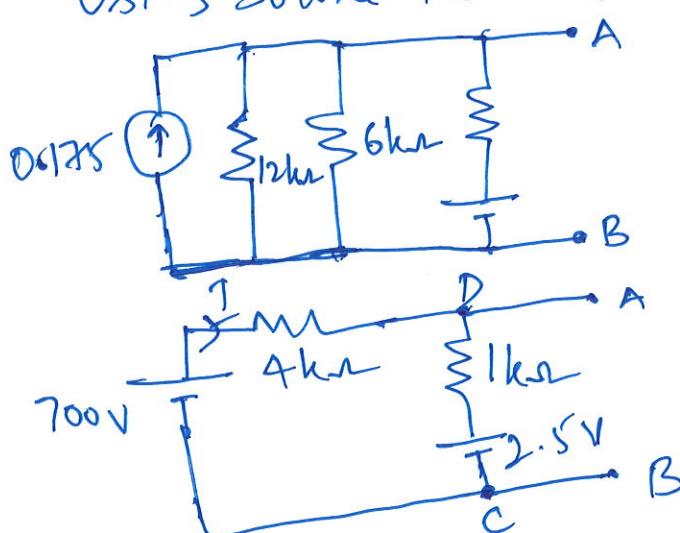
Using Source Transformation

$$V_{S1} = 0.3 \times 7\text{k} = 2100\text{V}$$



$$I_{S1} = \frac{2100\text{V}}{12\text{k}\Omega} = 0.175\text{A}$$

Using Source transform;



$$12\text{k}\Omega \parallel 6\text{k}\Omega = 4\text{k}\Omega$$

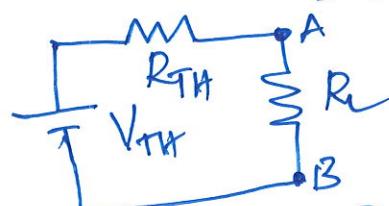
$$\text{Using Source transformation, } V_{S1} = 0.175 \times 4\text{k}\Omega = 700\text{V}$$

$$I = \frac{700 - 2.5}{5\text{k}\Omega} = 0.1395\text{A}$$

Applying KVL for loop

$$V_{TH} = V_{AB} = 142\text{V}$$

$$ABCDA, V_{AB} = 0.1395 \times 1 \times 10^3 + 2.5 = 142\text{V}$$



Maximum power is transferred when $R_L = R_{TH}$.

$$\text{Thus, } R_L = 800\text{\Omega}$$

(10)

(11)

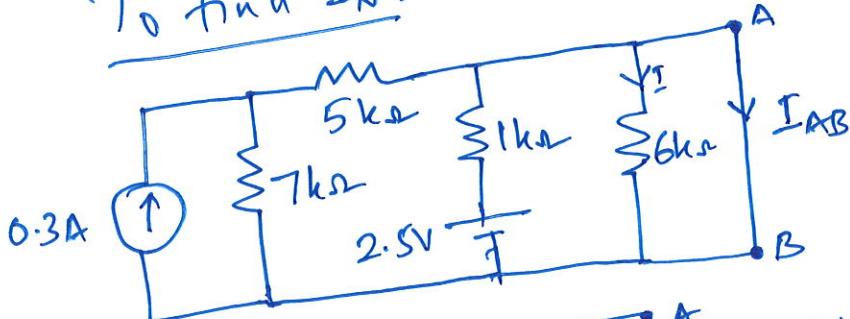
$$I_L = \frac{V_{TH}}{R_{TH} + R_L} = \frac{142}{800 + 800} = \underline{\underline{88.75 \text{ mA}}}$$

$$V_L = I_L R_L = \underline{\underline{71 \text{ V}}} \quad P_L = V_L I_L = \underline{\underline{6.3 \text{ W}}}$$

NORTON'S EQUIVALENT

$$R_N = R_{TH} = 800 \Omega$$

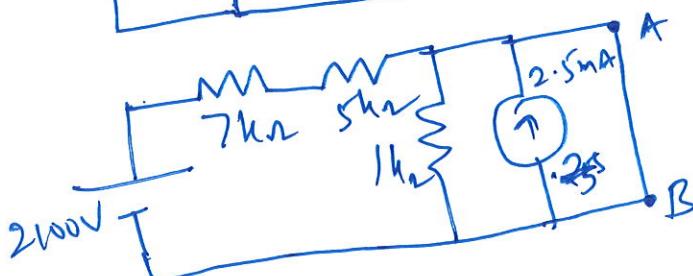
To find I_N :



Using Source transformation

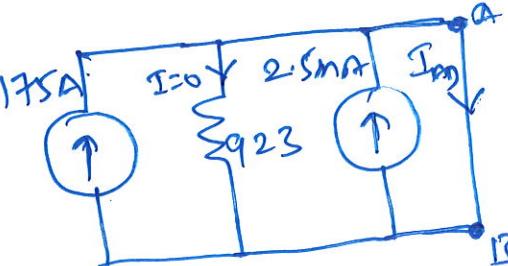
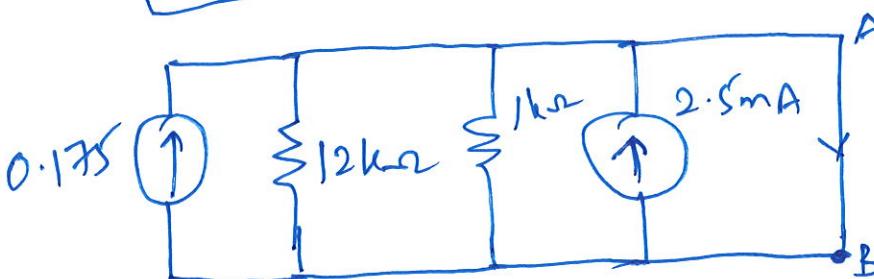
$$I_{S1} = \frac{2.5 \text{ V}}{1 \text{ k}\Omega} = 2.5 \text{ mA}$$

$$V_{S1} = 0.3 \times 7 \text{ k} = 2100 \text{ V}$$



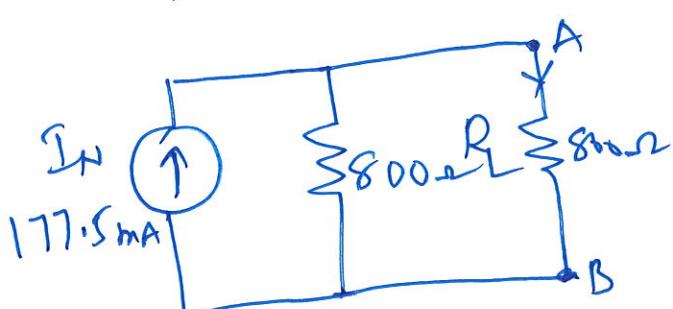
Using Source transformation,

$$\Rightarrow I_{S1} = \frac{2100}{12 \text{ k}} = 0.175 \text{ A}$$



$$I_{AB} = 0.175 \text{ A} + 2.5 \text{ mA} = \underline{\underline{177.5 \text{ mA}}}$$

$$I_N = I_{AB} = \underline{\underline{177.5 \text{ mA}}}$$



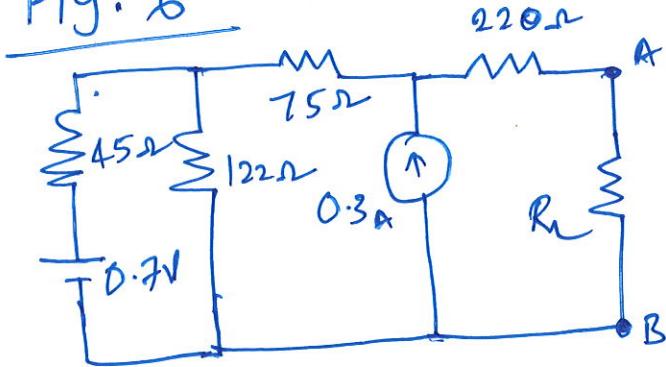
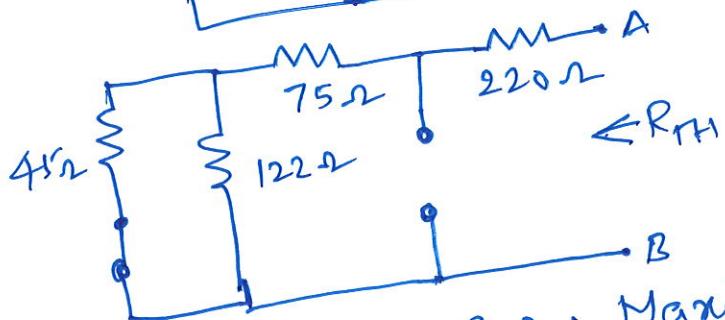
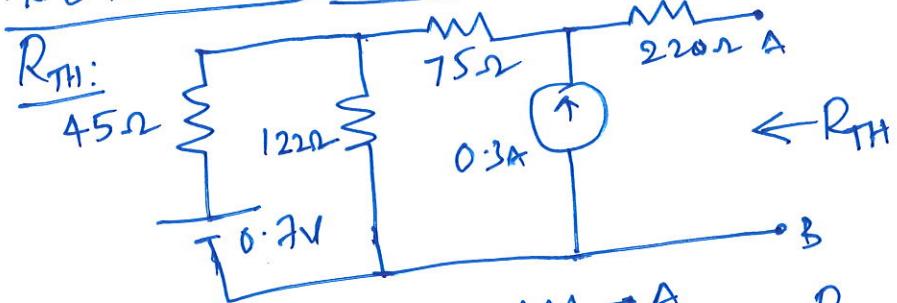
$$I_L = \frac{177.5 \text{ mA} \times 800}{800 + 800} = 88.75 \text{ mA}$$

$$V_L = 71 \text{ V}$$

$$P_L = V_L I_L = \underline{\underline{6.3 \text{ W}}}$$

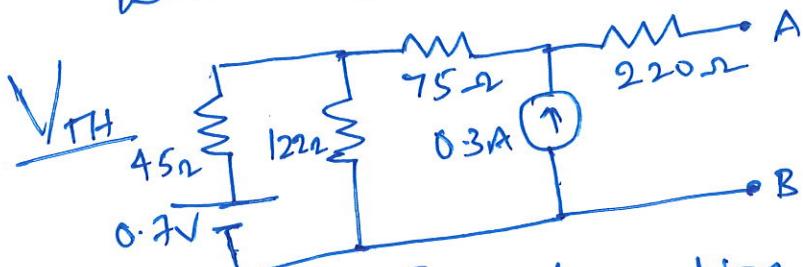
(2)

Fig. 6

THEVENIN'S EQUIVALENT :

$$R_{AB} = 220 + 75 + (45 \parallel 122) \\ = 323 \Omega$$

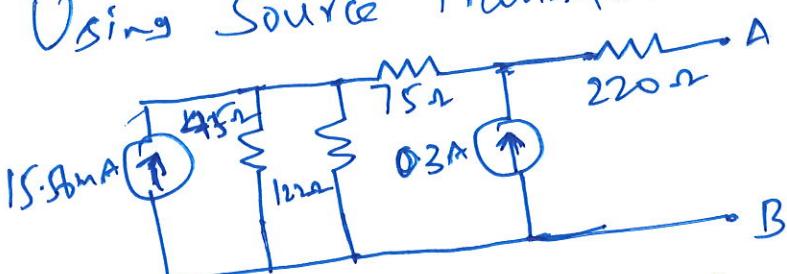
$R_{TH} = R_{AB} = \underline{323 \Omega}$. Maximum power transferred
when $R_L = \underline{R_{TH}}$. $R_L = \underline{323 \Omega}$



Using Source Transformation

$$I_{S1} = \frac{0.7V}{45\Omega} = 15.56mA$$

$$45 \parallel 122 = 33\Omega$$



Using Source transformation,

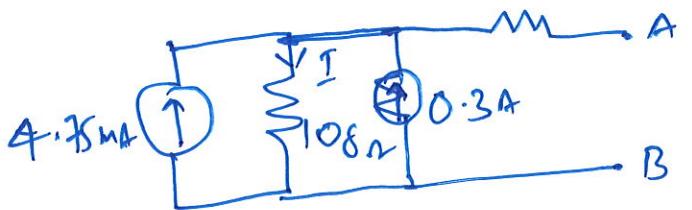
$$V_{S1} = 15.56mA \times 33 = \underline{0.513V}$$



Using Source transformation,

$$I_S = \frac{0.513}{33+75} = 4.75 \text{ mA}$$

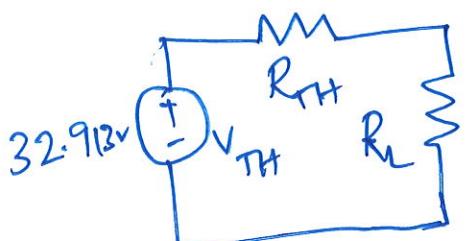
$$R_S = 108 \Omega$$



$$I = 0.3 + 4.75 \text{ mA} \\ = 30.475 \text{ mA}$$

$$V_{AB} = I \times 108 \Omega = \underline{32.913V}$$

$$V_{TH} = V_{AB} = 32.913V$$



$$R_{TH} = R_L = 323 \Omega$$

$$I_L = \frac{V_{TH}}{R_{TH} + R_L} = 50.95 \text{ mA}$$

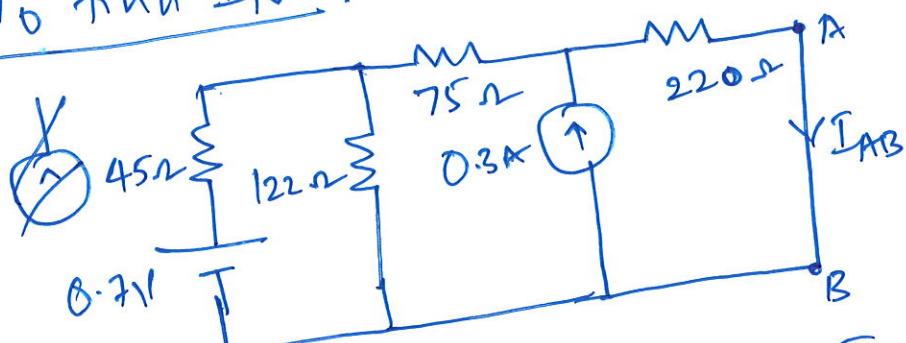
$$V_L = I_L \cdot R_L = 16.4565V$$

$$P_L = V_L \cdot I_L = \underline{0.8384 \text{ W}}$$

Norton's EQUIVALENT

$$R_N = R_{TH} = 323 \Omega$$

To find I_N :



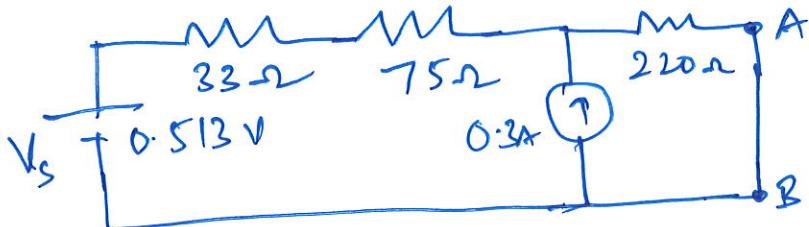
$$\text{Using Source transformation, } I_{S1} = \frac{0.7V}{45\Omega} = 15.56 \text{ mA}$$

$$45 \parallel 122 = 33 \Omega$$

$$R_{S1} = 33 \Omega \quad I_{S1} = 15.56 \text{ mA}$$

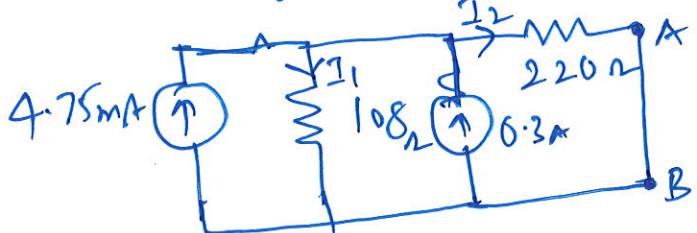
$$\text{Using Source transformation, } V_{S1} = I_{S1} R_{S1} = \underline{0.513V}$$

(14)



Using Source transformation, $R_S = 33 + 75 = 108\Omega$

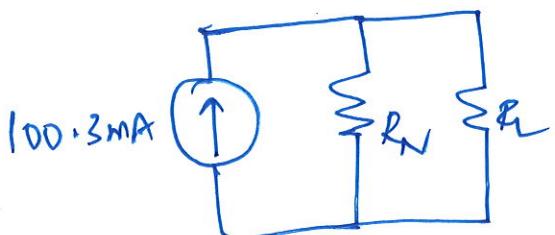
$$I_S = \frac{V_s}{R_S} = 4.75 \text{ mA}$$



$$I_2 = \frac{(0.3 + 4.75 \times 10^{-3}) \times 108}{108 + 220}$$

$$\approx 100.3 \text{ mA}$$

$$I_V = I_{AB} = I_2 = 100.3 \text{ mA}$$



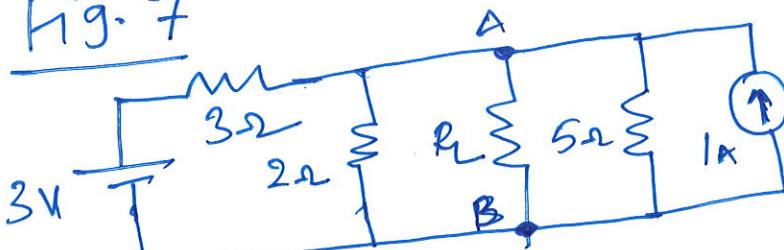
$$R_N = R_L = 330\Omega$$

$$I_L = \frac{50.17 \text{ mA}}{16.56 \text{ V}}$$

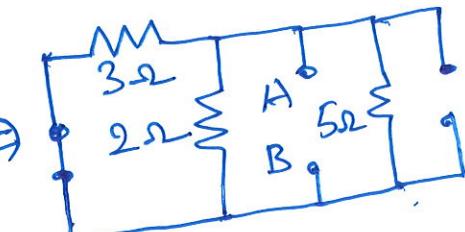
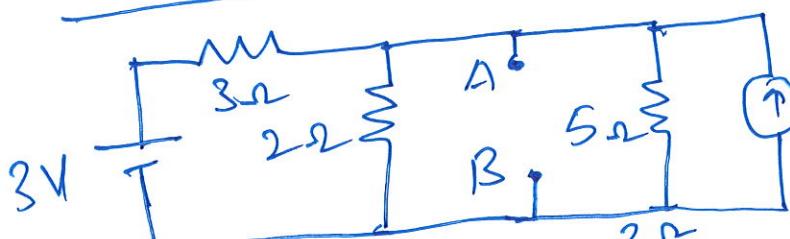
$$P_L = 0.83 \text{ mW}$$

(Small differences are due to rounding off errors)

Fig. 7



THEVENIN'S EQUIVALENT :



$$R_{AB} = 0.97\Omega$$

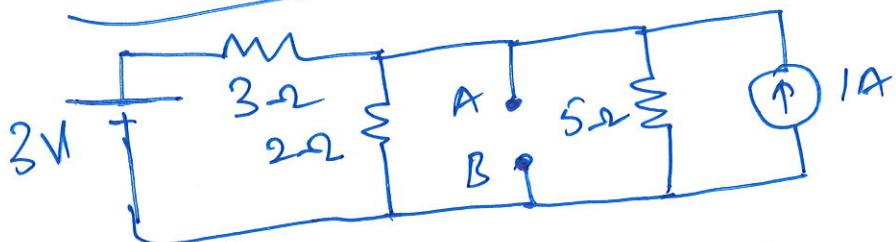
(15)

$$R_{TH} = R_{AB} = 0.97 \Omega$$

Maximum power is transferred when

$$R_L = R_{TH} \quad \text{Thus, } R_L = 0.97 \Omega$$

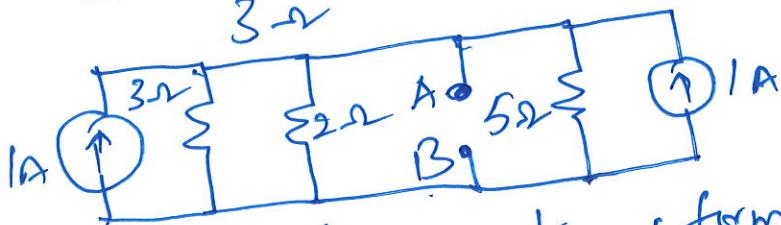
To find V_{TH} :



Using Source transformation,

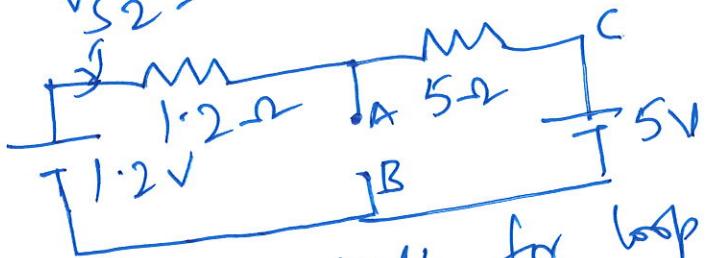
$$I_{S1} = \frac{3V}{3\Omega} = 1A$$

$$3 \parallel 2 = 1.2 \Omega$$



Using Source transformation, $V_{S1} = 1 \times 1.2 = 1.2V$

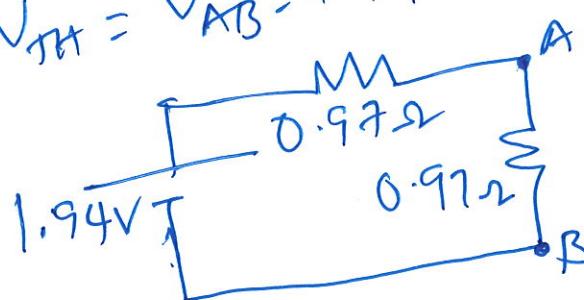
$$V_{S2} = 1 \times 5 = 5V$$



$$I = \frac{1.2 - 5}{1.2 + 5} = -0.613A$$

Applying KVL for loop ABCA, $V_{AB} = -5 \times 0.613 + 5 = 1.94V$

$$V_{TH} = V_{AB} = 1.94V$$



$$I_L = \frac{1.94}{2 \times 0.97} = 1A$$

$$V_L = 0.97V$$

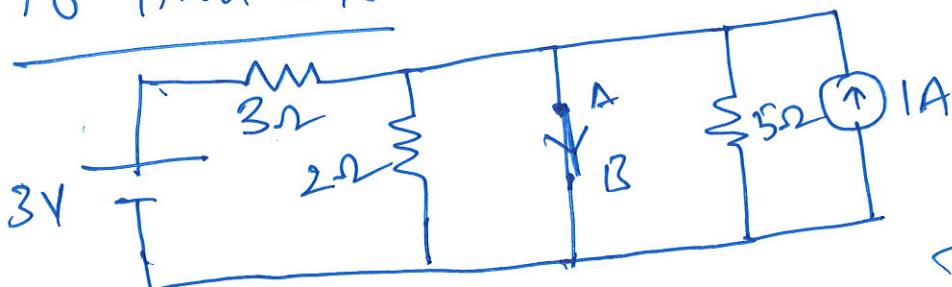
$$P_L = V_L \cdot I_L = \underline{\underline{0.97W}}$$

(16)

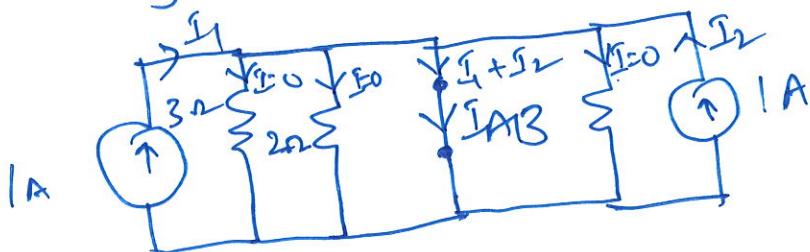
Norton's EQUIVALENT

$$R_N = R_{TH} = \cancel{0.72\Omega} \quad 0.97\Omega$$

To find I_N :

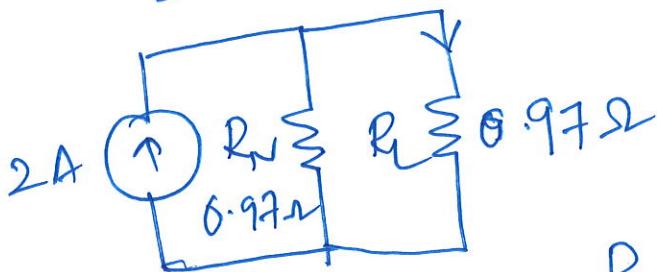


Using Source transformation: $I_{S1} = \frac{3V}{3\Omega} = 1A$



$$I_{AB} = I_1 + I_2 = 2A$$

$$I_N = I_{AB} = 2A$$



$$I_L = \frac{2 \times 0.97}{0.97 + 0.97} = 1A$$

$$V_L = I_L \cdot R_L = 0.97V$$

$$P_L = V_L \cdot I_L = \underline{\underline{0.97W}}$$