

If I were beginning my studies, I  
would follow the advice of Plato,  
& start with mathematics  
Galileo Galilei

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$$S = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} \dots$$

Madhava (1350-1425) Kerala

$$f(x) = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} \dots$$

$$\begin{aligned} \frac{df}{dx} &= 1 - x^2 + x^4 - x^6 + \dots \\ &= \frac{1}{1+x^2} \end{aligned}$$

$$f(x) = \int \frac{1}{1+x^2} dx = \tan^{-1} x$$

$$\tan^{-1} x = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} \dots$$

$$\frac{\pi}{4} = 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} \dots$$

$P_i = \pi$  Perimeter  
W. Jones in 1706  
EULER - 1737

LEONHARD EULER

①  $e^{i\pi} + 1 = 0$  EULER

②  $V + F = E + 2$  EULER

BASEL Problem

1644

$$S = 1 + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$$

28 yrs 1738  $S = \frac{\pi^2}{6}$

$$e^{i\theta} = \cos\theta + i\sin\theta$$

GEROLAMO CARDANO (1501-1576)  
Italian

$$x^3 + px + q = 0$$

$$x = \sqrt[3]{-\frac{q}{2} + \sqrt{\frac{q^2}{4} + \frac{p^3}{27}}} + \sqrt[3]{-\frac{q}{2} - \sqrt{\frac{q^2}{4} + \frac{p^3}{27}}}$$

$$x^3 - 15x - 4 = 0$$

$$x = \sqrt[3]{2 + \sqrt{-12}} + \sqrt[3]{2 - \sqrt{-12}}$$

NIELS ABEL (1802-1829)

EVARISTE GALOIS (1811-1832)

GROUP THEORY

JAKOB BERNOULLI

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n$$

$$100 \approx 100\% \rightarrow 200$$

$$50\% / 6 \text{ mon} \rightarrow 227$$

$$25\% / 4 \text{ mon} \rightarrow 244$$

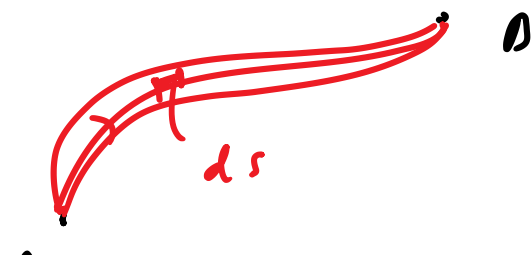
$$e = \lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n$$


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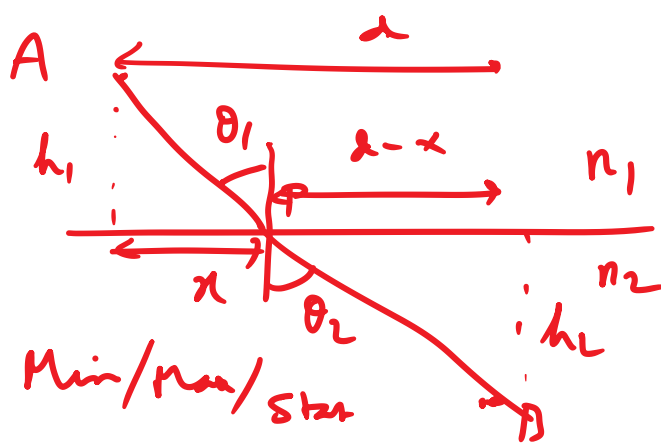
P. FERMAT

$$x^n + y^n = z^n \quad n > 2$$

Fermat's principle of least time



$$\delta \int_A^B dt = 0 \Rightarrow \delta \int_A^B \frac{ds}{v} = 0$$

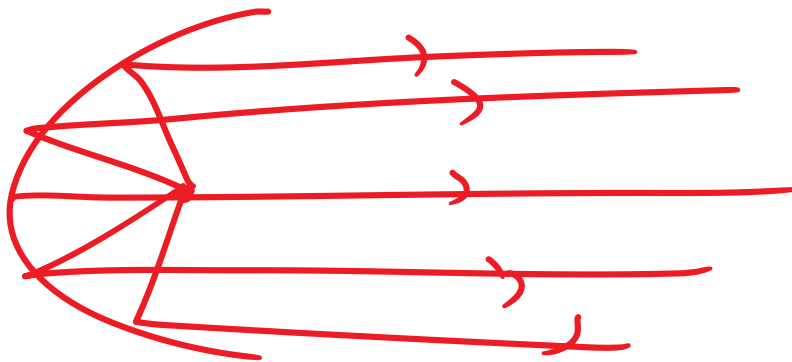
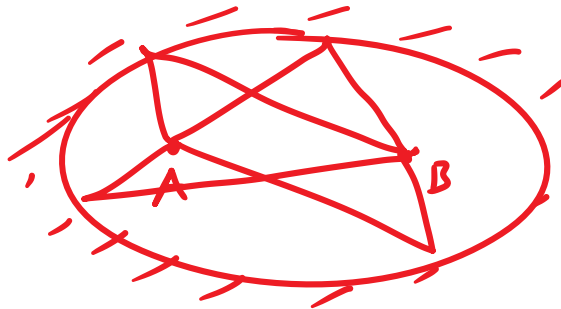


$$t = \frac{AP}{c/n_1} + \frac{PB}{c/n_2} \rightarrow \text{Min/Max/Star}$$

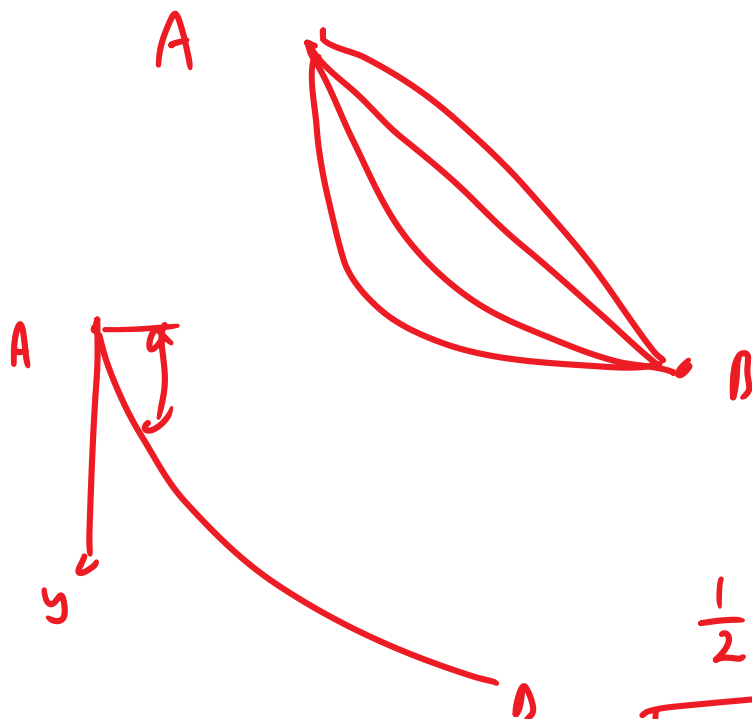
$$f(x) = n_1 \sqrt{x^2 + h_1^2} + n_2 \sqrt{(d-x)^2 + h_2^2}$$

$$\frac{df}{dx} = 0$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$



BRACHISTOCROME

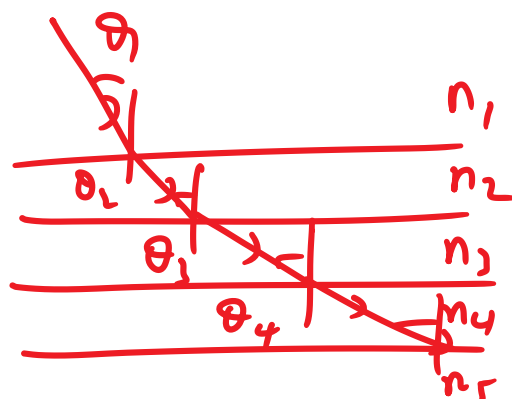


$$\frac{1}{2} m v^2 = m g y$$

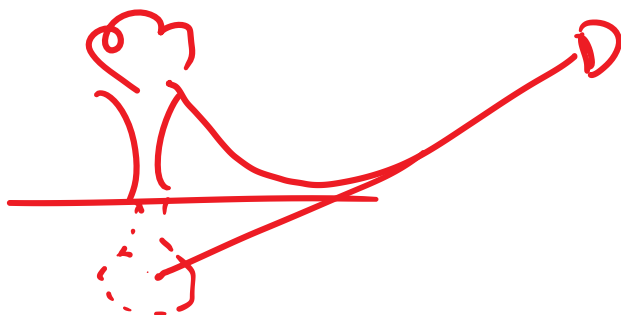
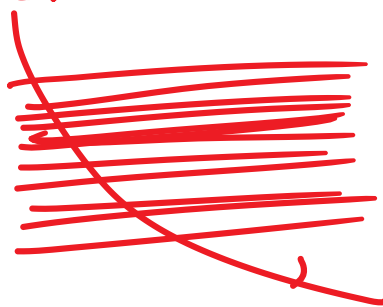
$$v(y) = \sqrt{2gy}$$

$$n(y) = c \sqrt{y}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 = n_3 \sin \theta_3 \dots$$



$$n(y) \sin \theta(y) = \text{constant}$$



$$\frac{c}{\sqrt{y}} \sin \theta(y) = G_{nr}$$

$$\frac{\sin \theta(y)}{\sqrt{y}} = G_{nr}$$

