Tutorial 3A: Maps, Filters, Zips

We will practice the **higher-order** functions map, filter, zip, and zipWith. The function map takes as its first argument a function $f :: a \rightarrow b$ and applies it to each element in a list, its second argument.

```
map :: (a -> b) -> [a] -> [b]
map _ [] = []
map f (x:xs) = f x : map f xs
```

The function filter takes a **property** $p :: a \rightarrow Bool$ (something that is true or false for a value of type a) and selects those elements from a list for which the property is true.

The function zip combines two lists into a list of pairs. If one list is longer than the other, the remaining elements are discarded.

```
zip :: [a] -> [b] -> [(a,b)]
zip _ [] = []
zip [] _ = []
zip (x:xs) (y:ys) = (x,y) : zip xs ys
```

The function zipWith is similar, except that instead of forming pairs, it combines the two lists with an arbitrary function.

```
zipWith :: (a -> b -> c) -> [a] -> [b] -> [c]
zipWith f _ [] = []
zipWith f [] _ = []
zipWith f (x:xs) (y:ys) = f x y : zip xs ys
```

Exercise 1: Write two versions of each of the following functions, one using **recursion** and one using **map** and **filter**.

- a) A function doubles that multiplies every number in a list by two. It may be helpful to create a function double to double a single number.
- b) A function odds that removes any even numbers from a list (use the built-in odd).
- c) A function doubleodds that doubles every odd number in a list (and removes the even numbers).

```
*Main> doubles [1..10]

[2,4,6,8,10,12,14,16,18,20]

*Main> odds [1..10]

[1,3,5,7,9]

*Main> doubleodds [1..10]

[4,8,12,16,20]
```

Exercise 2:

- a) Complete the function shorts that removes all strings longer than 5 characters from a list, using filter. Use a where-clause to define the filtering property.
- b) Complete the function squarePositives that takes all positive integers in a list and squares them. Use map and filter, with a where-clause to define any auxiliary functions you might need.
- c) Complete the function oddLengthSums that given a list of integer lists, returns for each odd-length list its sum. Use map and filter, and you may find odd, length, and sum helpful.
- d) As an optional challenge, use **sections** or **anonymous functions** to avoid the use of where-clauses in the above functions.

```
*Main> shorts ["The", "truth", "is", "that", "in", "London", "it", "is", "always", "a", "sickly", "season"]

["The", "truth", "is", "that", "in", "it", "is", "a"]

*Main> squarePositives [-3,4,1,-2,0,3]

[16,1,9]

*Main> oddLengthSums [[1],[1,2],[1,2,3],[1..4],[1..5]]

[1,6,15]
```

Exercise 3:

- a) Complete the functions remove and removeAll from Tutorial 2B again using filter . This time, if an element occurs multiple times, remove all occurrences. For removeAll , consider using the functions not and elem.
- b) Complete the function numbered that indexes the elements in a list by pairing them with numbers, counting up from 1. Use the function zip.
- c) Complete the function everyother that takes every other element from a list, starting with the first. Use numbered to count elements, filter, fst, and odd to select those pairs to keep, and map and snd to remove the indexing again.
- d) Complete the function same that takes two lists and returns a list of the positions where their elements coincide. For instance, the strings "Mary" and "Jane" have the same 2nd characters, so same should return the list [2]. Use the functions filter, map, fst, snd, zip (or numbered), and zipWith.

```
*Main> remove "Goerge" 'e'
"Gorg"

*Main> removeAll "Fitzwilliam" "Fitz"
"wllam"

*Main> numbered "days"
[(1,'d'),(2,'a'),(3,'y'),(4,'s')]

*Main> everyother "Elizabeth"
"Eiaeh"

*Main> same "Charles" "Charlotte"
[1,2,3,4,5]
```