Multi-criteria Optimization

Practical Applications

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Practical Applications in Machine Learning I

ROC Optimization: Balance true positive and false positive rates

- Typically unbalanced classification tasks with unspecified costs.
- Could also use other ROC metrics, e.g., positive predicted value or false discovery rate.

Efficient Models: Balance predictive performance with prediction time, energy consumption and/or model size.

- Time: Models in production need to predict fast.
- Size / Energy consumption: Models should be deployed on a mobile/edge device and not use much power.

Sparse Models: Balance *predictive performance* and *number of used features*, either for cost efficiency, but often also for interpretability.

Fair Models: Balance predictive performance and fairness.

- Model has to be fair regarding subgroups in the data, e.g. gender.
- Many different approaches to quantify fairness exist.

ROC Optimization - Setup

Again, we want to train a *spam detector* on the popular Spam dataset¹.

- Learning algorithm: SVM with RBF kernel.
- Hyperparameters to optimize:

$$\begin{array}{ccc} \text{cost} & [2^{-15}, 2^{15}] \\ & \gamma & [2^{-15}, 2^{15}] \\ \text{Threshold} \; t & [0, 1] \end{array}$$

Objective: minimize false positive rate

(FPR) and *maximize* true positive rate (TPR), evaluated through 5-fold CV

- Optimizer: Multi-criteria Bayesian optimization:
 - ParEGO with $\rho = 0.05$, s = 100000.
 - Acquisition function u: Confidence Bound with $\alpha = 2$.
 - ▶ Budget: 100 evaluations
- Tuning is conducted on a training holdout and all hyperparameter configurations on the estimated Pareto front are validated on an outer validation set.

The threshold $t\ \mbox{could}$ be separately optimized post-hoc.

https://archive.ics.uci.edu/ml/datasets/spambase

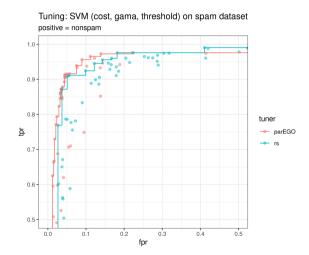
ROC Optimization - Result I

We notice:

- Compared to random search: Many ParEGO evaluations are on the Pareto front.
- The Pareto front of *ParEGO* dominates most points from the random search.
- The dominated hypervolume to the reference point (0,1) is:

ParEGO: 0.965 random search:

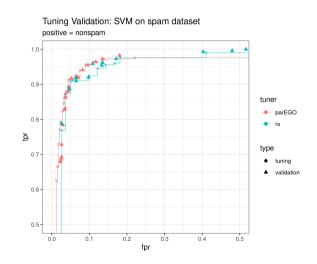
0.959



ROC Optimization - Result II

We validate the configurations on the estimated Pareto front on a holdout:

- The performance on the validation set varies slightly.
- The TPR got slightly better but the FPR got slightly worse.
- On the validation set, some configurations get dominated by others.

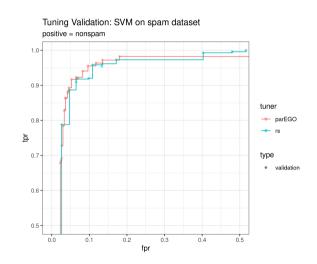


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- On the validation set, some configurations get dominated by others.
- The dominated hypervolume of the validation set is:

ParEGO: 0.960 random search: 0.961



Efficient Models - Overview

- "Efficiency" can be:
 - Memory consumption of the model
 - ► Training or prediction time
 - Number of features needed
 - Energy consumption for prediction
- Some hyperparameters have a strong impact on the efficiency of a model, e.g.,
 - Number of trees in random forests or gradient tree boosting,
 - ▶ Number, size and type of layers in neural networks,
 - L1 regularization penalties,
- Other hyperparameters might have no influence on efficiency.
- Typical scenario: Optimize jointly over multiple algorithms of varying efficiency.

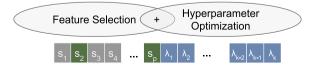
Efficient Models - Example: Feature Selection I

Goal of *feature selection*: Identify an informative feature subset with only a small drop in predictive performance compared to all features.

Find optimal hyperparameter setting $oldsymbol{\lambda}$ and minimal feature subset s

$$\min_{\boldsymbol{\lambda} \in \boldsymbol{\Lambda}, s \in \{0,1\}^p} \left(\widehat{GE} \left(\mathcal{I}(\mathcal{D}, \boldsymbol{\lambda}, s) \right), \frac{1}{p} \sum_{i=1}^p s_i \right)$$

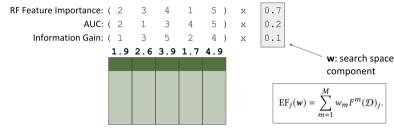
- Problem: Feature selection and hyperparameter tuning are usually two separate steps.
- Solution: Identify an informative subset of features and a good hyperparameter configuration simultaneously.



Efficient Models - Example: Feature Selection II

Idea: Multi-Objective Hyperparameter Tuning and Feature Selection using Filter Ensembles [Binder et al. 2020]:

• Pre-calculate multiple ranked feature filter values .



- New joint hyperparameter vector: ${m \lambda}=(ilde{{m \lambda}},w_1,\ldots,w_p, au)$
 - Hyperparameters of learner: $\hat{\lambda}$
 - Weight of each feature filter value vector: (w_1, \ldots, w_p)
 - Fraction of features to keep τ

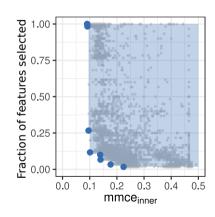
Efficient Models - Example: Feature Selection III

Combined feature selection and hyperparameter optimization on Sonar dataset².

- Learning algorithm: SVM with RBF kernel.
- Hyperparameters to optimize:

$$egin{array}{ccc} \mathsf{cost} & [2^{-10}, 2^{10}] \ \gamma & [2^{-10}, 2^{10}] \ (w_1, \dots, w_p) & [0, 1]^p \ & au & [0, 1]^p \end{array}$$

- Objective: minimize *misclassification* and *fraction of* features selected
- Optimizer: ParEGO with random forest surrogate, LCB acquisition function, 15 batch proposals, budget: 2000 evaluations



²Only the tuning error is shown here

Efficient Models - Example: FLOPS

Goal: Optimize prediction accuracy and number of floating point operations (FLOPs) [Wang et al. 2019].

Data: Image Classification on CIFAR-10.

Learner: DenseNet - Densely Connected Convolutional Network [Huang et al. 2018].

- Composed out of 4 dense blocks.
- A dense block consists of multiple convolutional layers where the inputs for each layer are all feature maps of all preceding layers in the block.
- Dense blocks are connected via convolutional and max pooling layer.

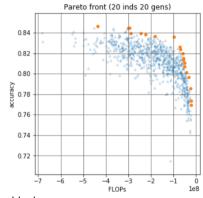
Training: 300 Epochs with a batch size of 128 and initial learning rate of 0.1.

Efficient Models - Example: FLOPS

- Objective: accuracy vs. FLOPS (floating point operations, per observation)
- Search Space:

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growth rate (k) [8,32] layers in first block [4,6] layers in second block [4,12] layers in third block [4,24] layers in fourth block [4,16]
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• Tuner: Particle Swarm Optimization with a population size of 20 and 400 evaluations.

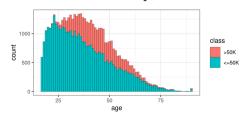


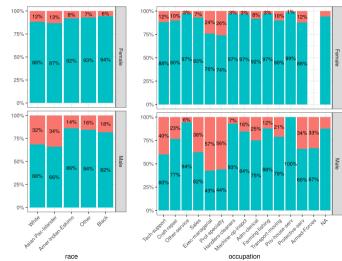
The growth rate is the number of output feature maps in each layer of a block

Fair Models - The Adult dataset

Dataset: Adult

- Source: US Census database, 1994, https://www.openml.org/d/1590.
- 48842 observations
- Target: binary, income above 50k
- 14 features: age, education, hours.per.week, marital.status, native.country, occupation, race, relationship, sex, ...





Fair Models - Setup I

A fair model for income prediction on binarized target.

- Learner: eXtreme Gradient Boosting
- Hyperparameters to optimize:

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\begin{array}{ccc} & \text{eta} & [0.01,0.2] \\ & \text{gamma} & [2^{-7},2^6] \\ & \text{max\_depth} & \{2,\dots,20\} \\ & \text{colsample\_bytree} & [0.5,1] \\ & \text{colsample\_bylevel} & [0.5,1] \\ & \text{lambda} & [2^{-10},2^{10}] \\ & \text{alpha} & [2^{-10},2^{10}] \\ & \text{subsample} & [0.5,1] \\ \end{array}
```

• Objective: minimize misclassification error and unfairness

Fair Models - Setup II

- Careful: Usually this data would be used to model the relation between person characteristics and income, then to discuss and study by careful inference - to figure out if something like e.g. a "gender pay gap" exists.
- Here, in our toy example we pretend now that we would like to create a automatic
 "assignment algorithm" for salary maybe not totally unrealistic nowadays? In such a
 scenario, biasing the prediction by incorporating fairness might be of interest.
- Here, a simplified proxy for fairness is defined as the absolute difference in F1-Scores between female (f) and male (m) population (low is good):

$$L_{\mathsf{fair}} := |L_{\mathsf{F1}}(y_f, \hat{f}(\mathbf{x}_f)) - L_{\mathsf{F1}}(y_m, \hat{f}(\mathbf{x}_m))|$$

Fair Models - Results

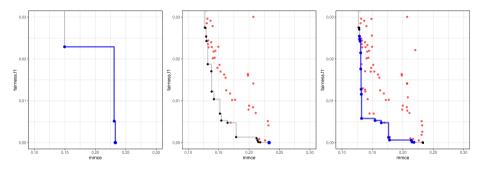


Figure: Pareto fronts after 20, 70 and 120 tuning iterations.

- Optimizer: ParEGO with random forest surrogate and restricted range of projections to [0.1, 0.9] (No interest in very unfair or bad configurations).
- Here, the hyperparameters actually have an effect on the defined fairness measure.
- However, this is often not the case or not enough to ensure a fair model.