# AutoML: Hyperparameter Optimization Evolutionary Algorithms

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#### Evolutionary algorithms

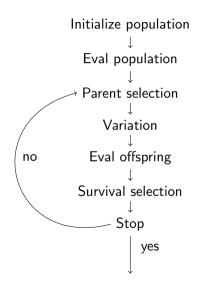
**Evolutionary algorithms** (EA) are a class of stochastic, metaheuristic optimization techniques whose mode of operation is inspired by the evolution of natural organisms.

History of evolutionary algorithms:

- **Genetic algorithms**: Use binary problem representation, therefore closest to the biological model of evolution.
- Evolution strategies: Use direct problem representation, e.g., vector of real numbers.
- **Genetic programming**: Create structures that convert an input into a fixed output (e.g. computer programs); solution candidates are represented as trees.
- **Evolutionary programming**: Similar to GP, but solution candidates are not represented by trees, but by finite state machines.

The boundaries between the terms become increasingly blurred and are often used synonymously.

# Structure of an evolutionary algorithm



#### Notation and Terminology

Symbols	EA Terminology
Solution candidate $oldsymbol{\lambda} \in oldsymbol{\Lambda}$	Chromosome of an individual
$oldsymbol{\lambda}_i$	<i>i</i> -th gene of chromosome
Set of candidates ${\mathcal P}$ with $\mu= {\mathcal P} $	Population and size
$\lambda$	Number of generated offsprings
$c: \mathbf{\Lambda}  ightarrow \mathbb{R}$	Fitness function

$$c(\pmb{\lambda}) = \widehat{GE}_{\mathcal{D}_{\mathsf{test}}}\left(\mathcal{I}(\mathcal{D}_{\mathsf{train}}, \pmb{\lambda})\right)$$

#### Notation clash:

- In EAs the objective function is often denoted f(x).
- As these symbols are used for ML already we use  $c(\lambda)$  and  $\lambda$  instead of f and x.
- Be careful: The offspring size  $\lambda$  is different from the candidate  $\lambda$  (bold symbol!).

#### Step 1: Initialize population

- ullet A evolutionary algorithm is started by generating a initial population  $\mathcal{P}=\{m{\lambda}^{(1)},...,m{\lambda}^{(\mu)}\}.$
- Usually we sample this uniformly at random.
- We could introduce problem prior knowledge via a smarter init procedure.
- This population is evaluated, i.e., the objective function is computed for every individual in the initial population.
- The initialization can have a large influence on the quality of the found solution, so many EAs employ *restarts* with new randomly generated populations.

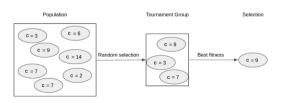
#### Step 2: Parent selection I

In the first step of an iteration,  $\lambda$  parents are chosen, who create offspring in the next step.

Possibilities for selection of parents:

- Neutral selection: choose individual with a probability  $1/\mu$ .
- Fitness-proportional selection: draw individuals with probability proportional to their fitness.

Tournament Selection: randomly select
 k individuals for a "Tournament Group".
 Of the drawn individuals, the best one
 (with the highest fitness value) is then
 chosen. Procedure is performed λ-times.



## Step 3: Variation

New individuals are now generated from the parent population. This is done by

- Recombination/Crossover: combine two parents into one offspring.
- Mutation: (locally) change an individual.

Sometimes only one operation is performed.

#### Recombination for numeric representations

Two individuals  $\lambda, \tilde{\lambda} \in \mathbb{R}^n$  in numerical representation can be recombined as follows:

- **Uniform crossover**: choose gene i with probability p of 1st parent and probability 1-p of 2nd parent.
- Intermediate recombination: new individual is created from the mean value of two parents  $\frac{1}{2}(\pmb{\lambda}+\tilde{\pmb{\lambda}})$
- Simulated Binary Crossover (SBX): generate two offspring based on

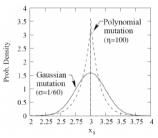
$$ar{m{\lambda}}\pmrac{1}{2}eta( ilde{m{\lambda}}-m{\lambda})$$

with  $ar{\pmb{\lambda}}=\frac{1}{2}(\pmb{\lambda}+\tilde{\pmb{\lambda}})$  and eta randomly sampled from a certain distribution.

#### Mutation for numeric representations

**Mutation:** individuals are changed, for example for  $\pmb{\lambda} \in \mathbb{R}^n$ 

- Uniform mutation: choose a random gene  $\lambda_i$  and replace it with a value uniformly distributed (within the feasible range).
- Gauss mutation:  $\tilde{\boldsymbol{\lambda}} = \boldsymbol{\lambda} \pm \sigma \mathcal{N}(0, \boldsymbol{I})$
- Polynomial mutation: polynomial distribution instead of normal distribution



Source: K. Deb, Analysing mutation schemes for real-parameter genetic algorithms, 2014

#### Recombination for bit strings

Two individuals  $\lambda, \tilde{\lambda} \in \{0,1\}^n$  encoded as bit strings can be recombined as follows:

• 1-point crossover: select crossover  $k \in \{1, ..., n-1\}$  randomly and select the first k bits from 1st parent, the last n-k bits from 2nd parent.

1	1		1
0	0		0
0	1	$\Rightarrow$	1
1	1		1
1	0		0

• Uniform crossover: select bit i with probability p of 1st parent and 1-p of 2nd parent.

## Mutation for bit strings

An individual  $\lambda \in \{0,1\}^n$  encoded as a bit string can be mutated as follows:

• **Bitflip**: for each index  $k \in \{1,...,n\}$ : bit k is flipped with probability  $p \in (0,1)$ .

1		0	
C		0	
C	$\Rightarrow$	0	
О		1	
1		1	

#### Step 4: Survival selection

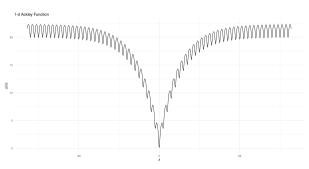
Now individuals are chosen who survive. Two common strategies are:

- $(\mu, \lambda)$ -selection: we select from the  $\lambda$  descendants the  $\mu$  best ( $\lambda \ge \mu$  necessary). But: best overall individual can get lost!
- $(\mu + \lambda)$ -selection:  $\mu$  parents and  $\lambda$  offspring are lumped together and the  $\mu$  best individuals are chosen. Best individual safely survives.

# Example of an evolutionary algorithm I

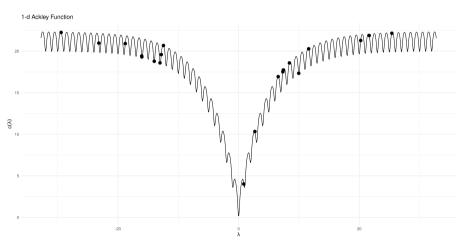
In the following, a (simple) EA is shown on the 1-dim Ackley function, optimized on  $\left[-30,30\right]$ .

Usually for the optimization of a function  $c: \mathbb{R}^n \to \mathbb{R}$  individuals are coded as real vectors  $\lambda \in \mathbb{R}^n$ , so here we use simply one real number as chromosome.



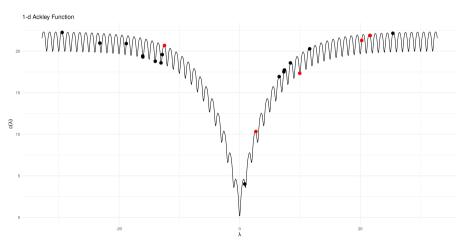
# Example of an evolutionary algorithm II

Randomly init population with size  $\mu=20$ .



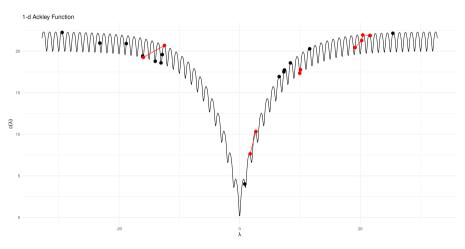
## Example of an evolutionary algorithm III

We choose  $\lambda=5$  offspring by neutral selection (red individuals).



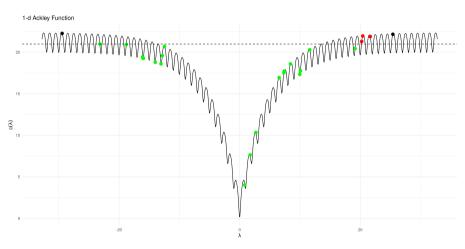
## Example of an evolutionary algorithm IV

We use a Gauss mutation with  $\sigma=2$  and do not apply a recombination.



# Example of an evolutionary algorithm V

We use a  $(\mu + \lambda)$  selection. The selected individuals are green.



# **Evolutionary Algorithms**

#### Advantages

- Conceptually simple, yet powerful enough to solve complex problems (including HPO)
- All parameter types possible in general
- Highly parallelizable (depends on  $\mu$ )
- Allows customization via specific variation operators

#### Disadvantages

- Less theory available (for realistic, complex EAs)
- Can be hard to get balance between exploration and exploitation right
- Can have quite a few control parameters, hard to set them correctly
- Customization necessary for complex problems
- Not perfectly suited for expensive problems like HPO, as quite a higher number of evaluations is usually needed for appropriate convergence / progress