

Introduction: In this lab, we understood the concept of a more complicated signals by frequency modulation, and amplitude modulation.

Problem 3.4 in text

5. $x(t) = A \cos[2\pi(\frac{1}{b}c - \frac{1}{b}a)t] + B \cos[2\pi(\frac{1}{b}c + \frac{1}{b}a)t]$

$A = B = 1.$

(a) $A \cos[2\pi(\frac{1}{b}c - \frac{1}{b}a)t] \rightarrow \text{Re}\{A \cdot e^{j0} \cdot e^{j2\pi(\frac{1}{b}c - \frac{1}{b}a)t}\}$
 $B \cos[2\pi(\frac{1}{b}c + \frac{1}{b}a)t] \rightarrow \text{Re}\{B \cdot e^{j0} \cdot e^{j2\pi(\frac{1}{b}c + \frac{1}{b}a)t}\}$

$$x(t) = \text{Re}\{A \cdot e^{j2\pi(\frac{1}{b}c - \frac{1}{b}a)t}\} + \text{Re}\{B \cdot e^{j2\pi(\frac{1}{b}c + \frac{1}{b}a)t}\}$$

$$= \text{Re}\{(A e^{-j2\pi f_a t} + B e^{j2\pi f_a t}) \cdot e^{j2\pi f_c t}\}$$

$$\Rightarrow x(t) = \text{Re}\{z(t)\}.$$

$$\Rightarrow z(t) = (A e^{-j2\pi f_a t} + B e^{j2\pi f_a t}) \cdot e^{j2\pi f_c t}$$

(b) $z(t) = (A e^{-j2\pi f_a t} + B e^{j2\pi f_a t}) \cdot e^{j2\pi f_c t}$

$$\Rightarrow \text{Re}\{z(t)\} = ((B+A) \cos(2\pi f_a t) \cos(2\pi f_c t)) - ((B-A) \sin(2\pi f_a t) \sin(2\pi f_c t))$$

Thus, $x(t) = C \cos(2\pi f_a t) \cos(2\pi f_c t) + D \sin(2\pi f_a t) \sin(2\pi f_c t)$

where, $C = B + A$,
 $\& D = -(B - A) = A - B$.

When, $A = B = 1$,
 $x(t) = 2 \cos(2\pi f_{\Delta} t) \cos(2\pi f_{\Sigma} t)$.

(C) For $x(t)$ to be $2 \sin(2\pi f_{\Delta} t) \sin(2\pi f_{\Sigma} t)$,
 C has to be zero, and D to be 2.

Thus, $A + B = 0$, & — (1)
 $A - B = 2$. — (2)

Adding (1) & (2) —
 $\Rightarrow 2A = 2 \Rightarrow A = 1$,
 $\Rightarrow B = -1$.

So, $x(t) = \cos[2\pi(f_{\Sigma} - f_{\Delta})t] - \cos[2\pi(f_{\Sigma} + f_{\Delta})t]$

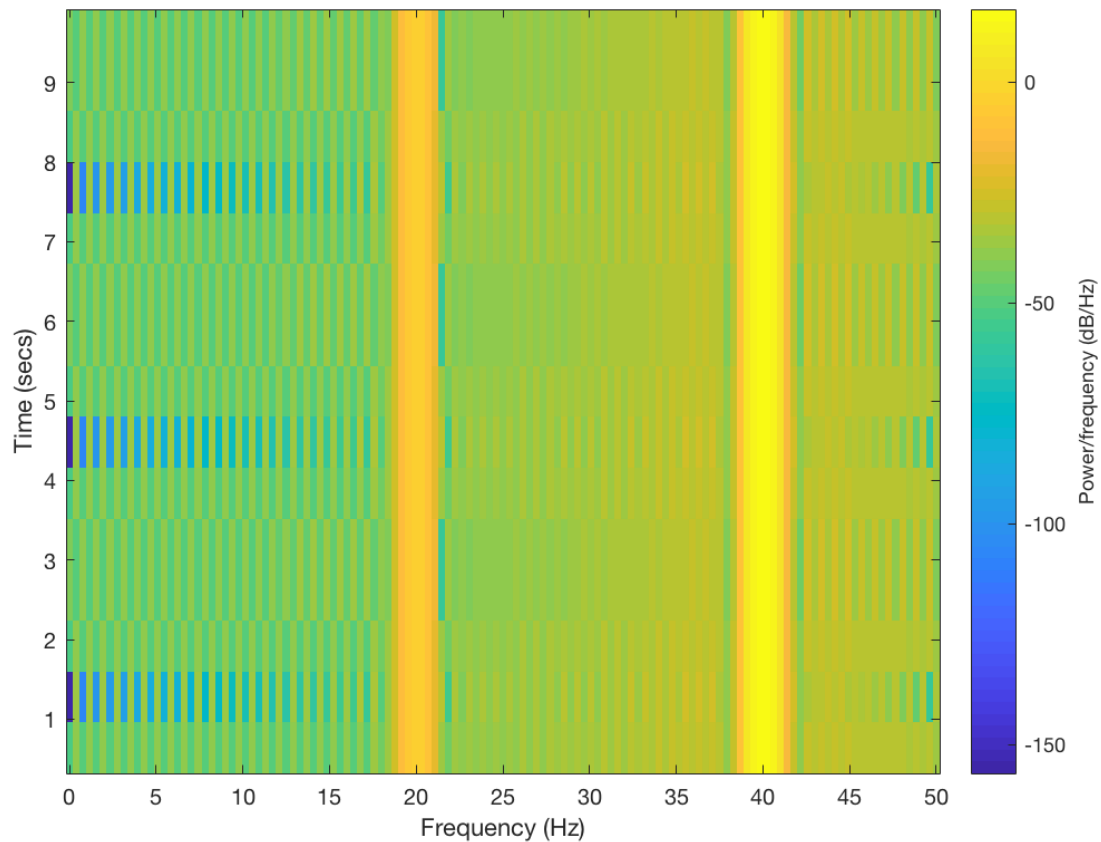
2.3 $N = 1024$;

$n = (0:N-1)$;

$w_0 = 2\pi/5$;

$x = \sin(w_0 * n) + 10 * \sin(2 * w_0 * n)$;

`spectrogram(x, 128, 64, [], 100);`



- I hear a sharp chirping sound, similar to the one's used in building alarm.
- I see a different color plot at different sample interval.

```
fsamp = 11025; % set sampling frequency
```

```
dt = 1/fsamp; % set sampling interval in seconds
```

```
dur = 1.5; % set signal duration in seconds
```

```
tt = 0:dt:dur; % create vector of time samples spaced at dt seconds
```

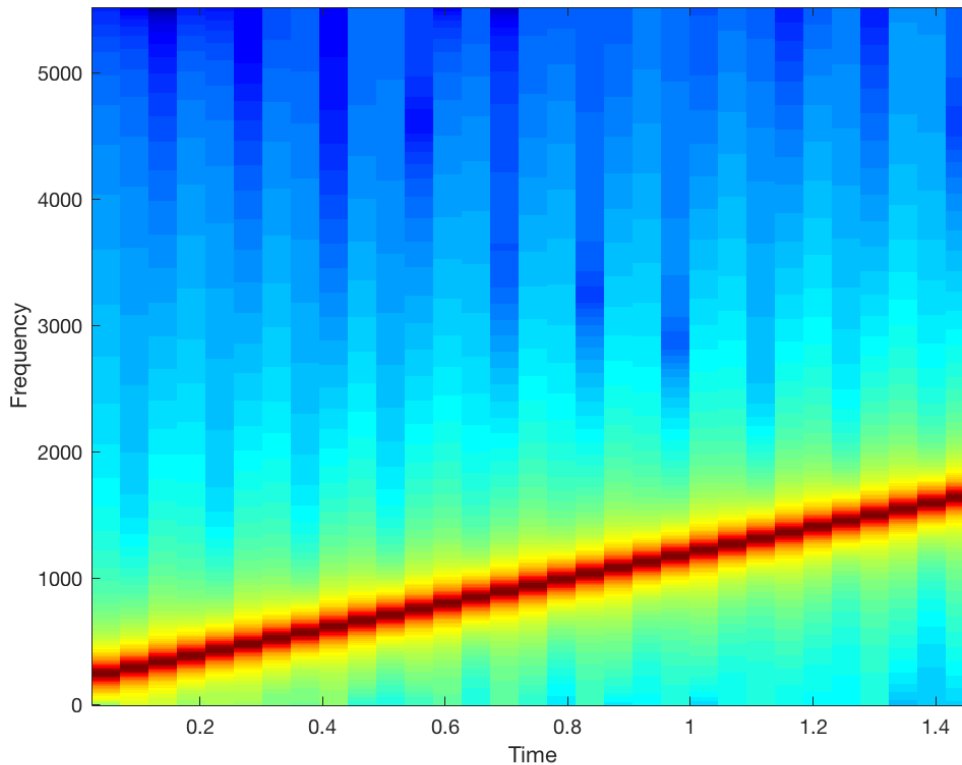
```
psi = 2*pi*(500*tt.^2 + 200*tt + 100); % set argument for chirp function
```

```
xx = 10*cos(psi); % modulate signal with cosine and amplitude cos
```

```
soundsc(xx, fsamp); % play signal
```

```
specgram(xx,1024,fsamp);% plot spectrogram
```

This sound is linear chirping sound, and is somewhat similar to the one's used in building alarm.



b. From the matlab code, the values are:

$t_n = 1.5$ sec

$A = 10$

$\mu = 2\pi * (500 * t_n.^2 + 200 * t_n + 100);$

$f_0 = 200$ Hz

$\phi = 100$

c. The range in the hertz would be from 0 to 2000 Hz.

d. The signal's frequency is linearly increasing.

```
fsamp = 11025; % set sampling frequency
```

```
dt = 1/fsamp; % set sampling interval in seconds
```

```
dur = 1.5;%set signal duration in seconds  
tt=0:dt:dur; % create vector of time samples spaced at dt seconds  
psi =2*pi* (500*tt.^2+200*tt +100); % set argument for chirp function  
xx=10*cos(psi); % modulate signal with cosine and amplitude cos  
soundsc(xx,fsamp);% play signal  
spectrogram(xx,1024,fsamp);% plot spectrogram
```

e. function [xx,tt] = mychirp (f1, f2, dur, fsamp)

%MYCHIRP generate a linear-FM chirp signal

```
xx= mychirp (f1, f2, dur, fsamp )  
f1= 400  
f2=4000  
dur=7  
fsamp= 11025  
tt=0:7
```

```
if (nargin<4)
```

```
fsamp = 11025
```

```
end
```

f. function [xx,tt] = mychirp (f1, f2, dur, fsamp)

%MYCHIRP generate a linear-FM chirp signal

```
xx= mychirp (f1, f2, dur, fsamp )  
f1= 5000  
f2=500
```

```
dur=3  
fsamp= 11025  
tt=0:3  
if (nargin<4)  
fsamp = 11025  
end
```

Yes, the frequency movement is linear.

It does chirp down.