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Hands-ON 3

Q1 function $x = f(n)$

$x = 1;$

for $i = 1 : n$

for $j = 1 : n$

$x = x + 1;$

Find the runtime of the algorithm mathematically.

Ans The outer loop runs from 1 to n , and for each iteration of the outer loop, the inner loop also runs from 1 to n .

analyzing the number of iterations:

For $i = 1$, the inner loop runs n times.

$i = 2$, the inner loop runs n times.

\vdots

$i = n$, the inner loop runs n times.

The total number of iterations of both loops :

$$\sum (i=1 \text{ to } n) \sum$$

The total number of iterations of both loops :-

$$\Rightarrow \sum_{i=1}^n \sum_{j=1}^n 1$$

$$\Rightarrow \left[\sum_{j=1}^n 1 = n \right] \Rightarrow$$

$$\Rightarrow \sum_{i=1}^n n \Rightarrow n \sum_{i=1}^n 1$$

$$\Rightarrow n \times n = n^2$$

The runtime of the algorithm is $O(n^2)$.