

Assignment 1

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Download all Codes from

<https://github.com/Aashrith20/C-and-DS/tree/main/Assignment%201/codes>

Download all latex-tikz codes from

<https://github.com/Aashrith20/C-and-DS/blob/main/Assignment%201/ee18btech11035.tex>

1 PROBLEM

Consider a Sequence of 14 elements: $A = [-5, -10, 6, 3, -1, -2, 13, 4, -9, -1, 4, 12, -3, 0]$. The subsequence sum $S(i, j) = \sum_{k=i}^j A[k]$. Determine the maximum of $S(i, j)$, where $0 \leq i \leq j < 14$. (Divide and Conquer approach may be used)

2 SOLUTION

By Divide and Conquer :

Calculate mid index of array which is $(start+end)/2$. Then recursively call the function to solve the left and right subarray.

For left subarray start index is the same as previous start index but end index is mid. At each recursive call Store the returned value in a variable $leftsubarray_{max}$.

In the case of right subarray start index is $(mid + 1)$ index but end index is the same as previous end index. At each recursive call Store the returned value in a variable $rightsubarray_{max}$.

Calculating the maximum subsequence sum of whole array:

Step 1:

Calculate the maximum of subsequence sum of all the subarrays in the left subarray with ending index as mid.

$$left_{sum} = \max(S(i, mid)) \forall (start \leq i \leq mid) \quad (2.0.1)$$

Step 2:

Calculate the maximum subsequence sum of all the subarrays in the right subarray with starting index as mid+1.

$$right_{sum} = \max(S(mid + 1, i)) \forall (mid + 1 \leq i \leq end) \quad (2.0.2)$$

Calculate the $left_{sum}$ and $right_{sum}$ at each recursion call.

To get the maximum subsequence sum return $\max(leftsubarray_{sum}, rightsubarray_{sum}, left_{sum} + right_{sum})$

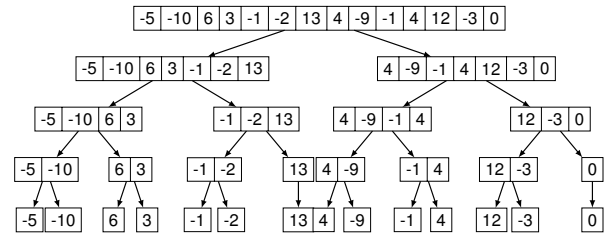


Fig. 0

3 VECTOR REPRESENTATION

$S(i, j)$ represents the sum of all elements of array from index i to j .

Let x be a vector defined as

$$\underline{x} = \begin{pmatrix} 0 & 0 & 0 & \underbrace{1 \cdots 1}_{\text{from index } i \text{ to } j} & 0 & 0 & 0 \end{pmatrix} \quad (3.0.1)$$

$S(i, j)$ can be rewritten in the vector representation as follows

$$S(i, j) = \sum_{k=i}^j A[k] \quad (3.0.2)$$

$$S(i, j) = A \underline{x}^T \quad (3.0.3)$$

4 TIME COMPLEXITY

$$T(N) = 2T(N/2) + O(N) \quad (4.0.1)$$

Solving the above recurrence relation, We get

$$T(N) = O(N \log N) \quad (4.0.2)$$