Feedback Circuits

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0.0.1. A dc amplifier having a single-pole response with pole frequency 10Hz and unity-gain frequency of 1MHz is operated in a loop whose 0.0.3. Design a Circuit for G(s)frequency-independent feedback factor is 0.01. Find the low-frequency gain, the 3-dB frequency, and the unity-gain frequency of the closed-loop amplifier. By what factor does the pole shift?

Solution: The open-loop gain of the amplifier

$$G(s) = \frac{A_O}{1 + \frac{s}{\omega_p}} = \frac{A_O}{1 + \frac{s}{2\pi \cdot 10}}$$
 (0.0.1.1)

Given that unity gain frequency is 1MHz Replacing s with 1ω in this equation.

$$\left| \frac{A_O}{1 + \frac{J.2\pi.10^6}{2\pi.10}} \right| = 1 \tag{0.0.1.2}$$

$$|A_O| = \left| 1 + J \frac{2\pi \cdot 10^6}{2\pi \cdot 10} \right| \qquad (0.0.1.3)$$

$$A_O \approx 10^5 \tag{0.0.1.4}$$

0.0.2. Draw the bode plots of open-loop circuit **Solution:**

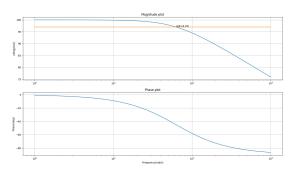


Fig. 0.0.2: Bode plots of Open-loop Transfer Function

Python code for above plot is

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codes/ee18btech11035 bode1.py

Solution: Designing G(s) Using Op-amp with DC gain of 10^5 and a pole at 10Hz.

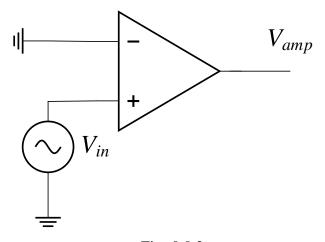


Fig. 0.0.3

(0.0.1.4) 0.0.4. Verify the gain using spice

Solution: Follow the Instructions for SPICE simulation:

spice/README.md

Netlist file for simulation:

spice/ee18btech11035 spice1.net

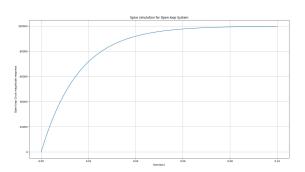


Fig. 0.0.4: Spice Simulation of Open-loop Transfer **Function**

Python code for above plot:

codes/ee18btech11035 spice1.py

0.0.5. Verification of step response of open-loop transfer function through python

Solution:

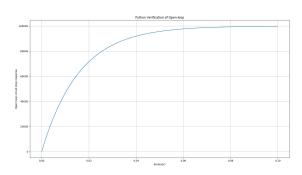


Fig. 0.0.5: Python verification of Open-loop Transfer Function

Python code for above verification is

codes/ee18btech11035 pythonverify1.py

0.0.6. Add a feedback for above circuit with a feedback factor of 0.01 an calculate closed-loop 0.0.9. Find the unity gain frequency of the closed transfer function

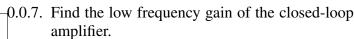
Solution: $G(s) = \frac{10^5}{1 + \frac{s}{2710}}$ and H(s) = 0.01

$$T(s) = \frac{G(s)}{1 + G(s)H(s)}$$
(0.0.6.1)

$$T = \frac{\frac{A_O}{1 + A_0 H(s)}}{1 + \frac{s}{20\pi(1 + A_0 H(s))}}$$
(0.0.6.2)

$$T(s) = \frac{99.90}{1 + \frac{s}{2\pi.10010}}$$
 (0.0.6.3)

Block diagram representation of the amplifier



Solution: As frequency is low, substituting s = 0

$$T(0) = \frac{G(0)}{1 + G(0)H(0)}$$
 (0.0.7.1)

$$=\frac{10^5}{1+10^5.(0.01)}\tag{0.0.7.2}$$

$$= 99.900 (0.0.7.3)$$

0.0.8. Find the 3-dB frequency of the closed loop amplifier

Solution:

$$T = \frac{\frac{A_O}{1 + A_0 H(s)}}{1 + \frac{s}{20\pi (1 + A_0 H(s))}}$$
(0.0.8.1)

3-dB frequency = $20\pi \cdot (1 + A_0 H(s))$

(0.0.8.2)

$$= 20\pi. \left(1 + 10^5. (0.01)\right)$$
 (0.0.8.3)

$$= 62862.8 rad/s = 10.01 kHz$$
 (0.0.8.4)

loop amplifier

Solution: Unity-gain frequency of the closed loop amplifier is obtained as follows

$$|T| = 1 \tag{0.0.9.1}$$

$$\frac{A_O}{1 + A_O H(s)} = \left| 1 + \frac{J\omega}{20\pi (1 + A_O H(s))} \right|$$
(0.0.9.2)

$$99.900 = \left| 1 + \frac{J\omega}{62862.8} \right| \tag{0.0.9.3}$$

$$\omega = 6279.649 Krad/s = 999.94 kHz$$
(0.0.9.4)

0.0.10. By what factor does the pole shift?

Solution: Open-loop pole is 10Hz and the Closed-loop pole is $20\pi \cdot (1 + A_0H(s))$

Pole-shift Factor =
$$\frac{20\pi (1 + A_O H(s))}{20\pi}$$

$$= 1 + A_O H(s) = 1001$$

$$= 0.0.10.2$$

0.0.11. Design the feedback with H(s) = 0.01**Solution:** Designing Feedback circuit:

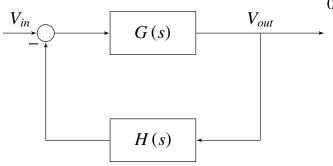


Fig. 0.0.6

As, Feedback is a constant value designing i0.0.12. Draw the Bode plots of closed-loop circuit by using simple voltage divider circuit **Solution:**

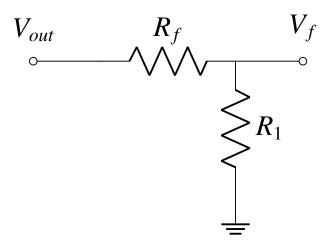


Fig. 0.0.11

$$\frac{V_f}{V_{out}} = \frac{R_1}{R_1 + R_f} = H(s) = 0.01 \quad (0.0.11.1) \cdot 0.11$$

Choosing R_1 as 10Ω and R_f as 990Ω

Overall Circuit is as follows:

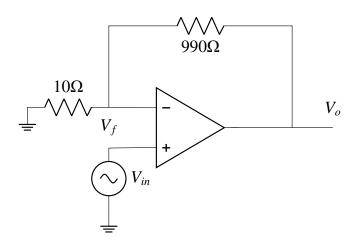


Fig. 0.0.11

Circuit	Parameter
Element	Value
Op-amp Gain	10 ⁵
Op-amp pole	10 <i>Hz</i>
R_1	10Ω
R_f	990Ω

TABLE 0.0.11

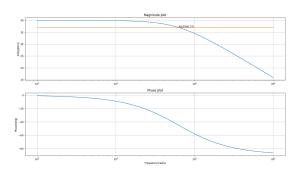


Fig. 0.0.12: Bode plots of Closed-loop Transfer Function

Python code for above plot is

(0.0.11.1)0.0.13. Verify the gain of closed loop Circuit using spice

Solution: Follow the Instructions for SPICE simulation:

spice/README.md

Netlist file for simulation:

spice/ee18btech11035 spice2.net

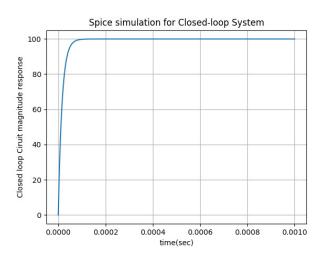


Fig. 0.0.13: Spice simulation of Closed-loop Transfer Function

Pyhton code for above plot:

codes/ee18btech11035_spice2.py

0.0.14. Verification of step response of open-loop transfer function through python **Solution:**

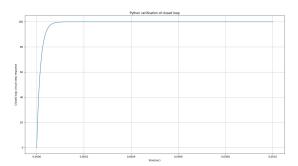


Fig. 0.0.14: Python verification of closed-loop Transfer Function

Python code for above verification is

codes/ee18btech11035_pythonverify2.py

0.0.15. Tabulating DC Gain,Bandwidth and Gain bandwidth product

Solution: Observing the fig:(0.0.2) and fig:(0.0.12) to get DC Gain and Bandwidth

	G(s)	T(s)
DC Gain	10^{5}	99.9
Band- width	20π	$20\pi.1001$
Gain	$2\pi.10^{6}$	$2\pi.10^{6}$
band-		
width		
product		

TABLE 0.0.15

Therefore, By using feedback we can get desired Gain of an amplifier while maintaining constant Gain Bandwidth product (for a first-order op-amp).