Q1. Given an integer array arr and an integer k, return true if it is possible to divide the vector into k non-empty subsets with equal sum.

```
Input: arr = [1,3,2,2] k = 2
   Output: true
Ans:
public class PartitionArrayIntoKSubsets {
  public static boolean canPartitionKSubsets(int[] arr, int k) {
     int sum = 0;
     for (int num : arr) {
        sum += num;
     }
     if (k \le 0 || sum \% k != 0) {
        return false; // Invalid input
     int targetSum = sum / k;
     boolean[] visited = new boolean[arr.length];
     return backtrack(arr, k, 0, 0, targetSum, visited);
  }
  private static boolean backtrack(int[] arr, int k, int currentSum, int startIndex, int targetSum,
boolean[] visited) {
     if (k == 0) {
        return true; // All subsets found
     }
     if (currentSum == targetSum) {
        return backtrack(arr, k - 1, 0, 0, targetSum, visited);
     }
     for (int i = startIndex; i < arr.length; i++) {
        if (!visited[i] && currentSum + arr[i] <= targetSum) {
          visited[i] = true;
          if (backtrack(arr, k, currentSum + arr[i], i + 1, targetSum, visited)) {
             return true;
          visited[i] = false;
        }
     }
```

```
return false;
  }
  public static void main(String[] args) {
     // Example usage
     int[] arr = {4, 3, 2, 3, 5, 2, 1};
     int k = 4;
     boolean result = canPartitionKSubsets(arr, k);
     System.out.println("Can partition into " + k + " subsets: " + result);
  }
}
   Q2. Given an integer array arr, print all the possible permutations of the given array.
   Note: The array will only contain non repeating elements.
   Input 1: arr = [1, 2, 3]
   Output1: [[1,2,3], [1,3,2], [2,1,3], [2,3,1], [3,1,2], [3,2,1]]
Ans:
import java.util.ArrayList;
import java.util.List;
public class Permutations {
  public static List<List<Integer>> permute(int[] nums) {
     List<List<Integer>> result = new ArrayList<>();
     List<Integer> currentPermutation = new ArrayList<>();
     boolean[] used = new boolean[nums.length];
     backtrack(nums, result, currentPermutation, used);
     return result;
  }
  private static void backtrack(int[] nums, List<List<Integer>> result, List<Integer>
currentPermutation, boolean[] used) {
     if (currentPermutation.size() == nums.length) {
        result.add(new ArrayList<>(currentPermutation));
        return;
     }
```

```
for (int i = 0; i < nums.length; i++) {
       if (!used[i]) {
          // Choose
          used[i] = true;
          currentPermutation.add(nums[i]);
          // Explore
          backtrack(nums, result, currentPermutation, used);
          // Unchoose
          used[i] = false;
          currentPermutation.remove(currentPermutation.size() - 1);
       }
     }
  }
  public static void main(String[] args) {
     // Example usage
     int[] nums = \{1, 2, 3\};
     List<List<Integer>> permutations = permute(nums);
     System.out.println("All permutations:");
     for (List<Integer> permutation : permutations) {
        System.out.println(permutation);
     }
  }
}
```

Q3. Given a collection of numbers, nums, that might contain duplicates, return all possible unique permutations in any order.

Example 1:

```
Input: nums = [1,1,2]
Output:
[[1,1,2], [1,2,1], [2,1,1]]
```

Ans:

```
import java.util.ArrayList;
import java.util.Arrays;
import java.util.List;
```

```
public class UniquePermutations {
  public static List<List<Integer>> permuteUnique(int[] nums) {
     List<List<Integer>> result = new ArrayList<>();
     List<Integer> currentPermutation = new ArrayList<>();
     boolean[] used = new boolean[nums.length];
     Arrays.sort(nums); // Sort the array to handle duplicates
     backtrack(nums, result, currentPermutation, used);
     return result;
  }
  private static void backtrack(int[] nums, List<List<Integer>> result, List<Integer>
currentPermutation, boolean[] used) {
     if (currentPermutation.size() == nums.length) {
       result.add(new ArrayList<>(currentPermutation));
       return;
     }
     for (int i = 0; i < nums.length; i++) {
       // Skip duplicates at the same level of recursion
       if (used[i] || (i > 0 && nums[i] == nums[i - 1] && !used[i - 1])) {
          continue;
       }
       // Choose
       used[i] = true;
       currentPermutation.add(nums[i]);
       // Explore
       backtrack(nums, result, currentPermutation, used);
       // Unchoose
       used[i] = false;
       currentPermutation.remove(currentPermutation.size() - 1);
    }
  }
  public static void main(String[] args) {
     // Example usage
     int[] nums = \{1, 1, 2\};
     List<List<Integer>> permutations = permuteUnique(nums);
```

```
System.out.println("All unique permutations:");
     for (List<Integer> permutation : permutations) {
       System.out.println(permutation);
     }
  }
}
  Q4. Check if the product of some subset of an array is equal to the target value.
  Input: n = 5, target = 16
  Array = [23254]
  Here the target will be equal to 2x2x4 = 16
  Output: YES
Ans:
public class SubsetProduct {
  public static boolean isSubsetProduct(int[] nums, int target) {
     return backtrack(nums, target, 1, 0);
  }
  private static boolean backtrack(int[] nums, int target, long currentProduct, int index) {
     if (currentProduct == target) {
       return true; // Subset found with the target product
     }
     for (int i = index; i < nums.length; i++) {
       // Choose
       currentProduct *= nums[i];
       // Explore
       if (backtrack(nums, target, currentProduct, i + 1)) {
          return true; // Found a subset with the target product
       }
       // Unchoose
       currentProduct /= nums[i];
     }
     return false;
```

}

```
public static void main(String[] args) {
    // Example usage
    int[] nums = {2, 3, 5};
    int target = 30;

    boolean result = isSubsetProduct(nums, target);
    System.out.println("Subset with product equal to " + target + ": " + result);
}
```

Input: n = 4 Output: 2

Q5. The n-queens puzzle is the problem of placing n queens on an n x n chessboard such that no two queens attack each other. Given an integer n, return the number of distinct solutions to the n-queens puzzle.

```
Ans:
public class NQueens {
  public static int totalNQueens(int n) {
     int[] placement = new int[n];
     int[] result = new int[1];
     solveNQueens(n, 0, placement, result);
     return result[0];
  }
  private static void solveNQueens(int n, int row, int[] placement, int[] result) {
     if (row == n) {
       // All queens are placed successfully, increment the result count
       result[0]++;
       return;
     }
     for (int col = 0; col < n; col++) \{
       if (isValid(row, col, placement)) {
          placement[row] = col;
          solveNQueens(n, row + 1, placement, result);
       }
     }
  }
```

```
private static boolean isValid(int row, int col, int[] placement) {
     for (int i = 0; i < row; i++) {
        // Check if there is a queen in the same column or diagonals
        if (placement[i] == col || Math.abs(placement[i] - col) == Math.abs(i - row)) {
          return false;
        }
     }
     return true;
  }
  public static void main(String[] args) {
     // Example usage
     int n = 4;
     int result = totalNQueens(n);
     System.out.println("Total distinct solutions for " + n + "-Queens puzzle: " + result);
  }
}
```