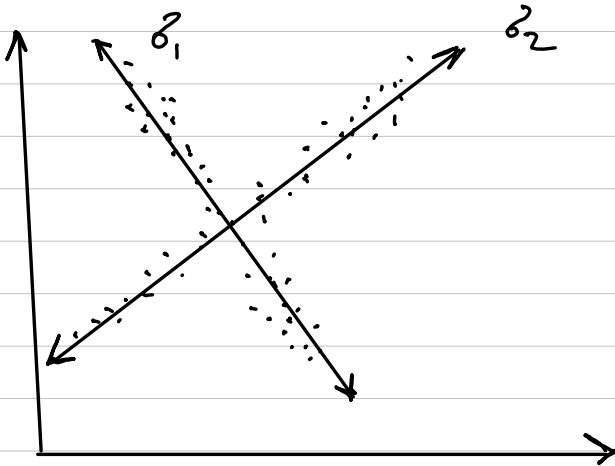


ICA

Independent Component Analysis

- Technique used to separate mixed signals
- Used in signal processing → ① Audio
② Image
- Used for feature extraction
- Unsupervised learning technique

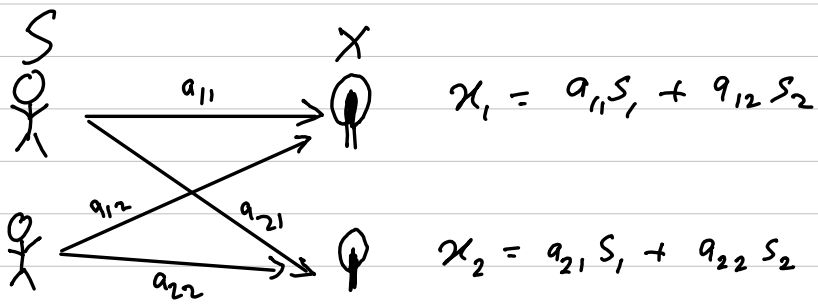


- Blind source separation technique

Cocktail Party Problem

There are n people in room & n microphones
Voice of the people is recorded in the microphones.

Goal is to separate out the voices of people



We have X and need to calculate S

Here we are assuming that the n people are all statistically independent

This is the main assumption that allows us to solve PCA

Mathematical expressions \rightarrow

$$X_1(t) = a_{11}S_1(t) + a_{12}S_2(t)$$

$$X_2(t) = a_{21}S_1(t) + a_{22}S_2(t)$$

$a_{ij} \rightarrow$ Mixing coefficients

Unknowns \rightarrow $a_{ij} \rightarrow 4$
 $X_i(t) \rightarrow 2$ } 6 unknowns

2 constraints (equations)

We cannot solve directly.

In Matrix form

$$X = AS \quad - (1)$$

$$\therefore S = A^{-1}X \quad - (2)$$

ICA calculates S from X

So we need to find a transformation matrix A such that A maximizes the independence of hidden components

Given N distinct linear combinations of N elements, determine the original N elements

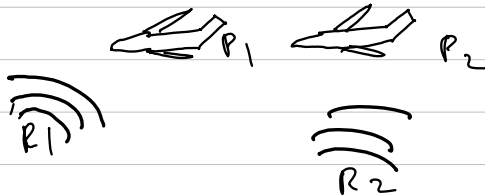
Assumptions in ICA \rightarrow

- 1) Original signals are statically independent
- 2) Each source exhibits non-gaussian distributions

Applications \rightarrow

- ① separation of mixed signals
 - ② used for feature extraction
 - ③ Radar detection \rightarrow
- } ML

example there are many planes & many radars
How can we find out which plane is detected

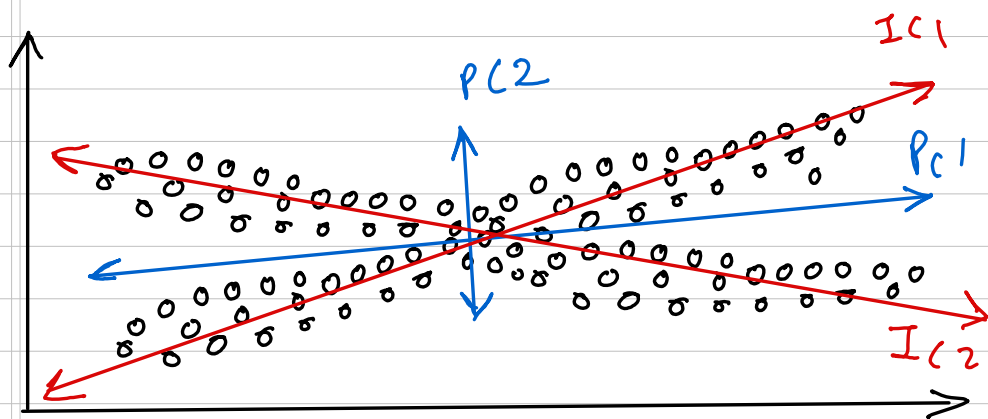


- ④ EEG activity

Disadvantages →

- ① ICA is used to separate linear mixtures
- ② If mixture is not linear, then ICA fails
- ③ ICA is computationally expensive
- ④ Convergence issues

ICA	PCA
Identifies independent sources	Identifies direction of maximum variance
Non Gaussian data	Gaussian data
Extract independent sources	Reduce dimensionality of data to avoid overfitting
May or may not be orthogonal, but are statistically independent	Orthogonal components Not necessarily independent
Separate information	Compress information



The direction of maximum variance is the one which gives most quality of data

Independent components are the directions of spread of the data