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def extended_gcd(a, b):
  # Extended Euclidean Algorithm to find modular inverse
  # It returns a tuple (g, x, y), where g is the GCD of a and b,
  # and x, y are the coefficients of the equation a * x + b * y = g
  if b == 0:
    return (a, 1, 0)
  else:
    g, x1, y1 = extended_gcd(b, a % b)
    x = y1
    y = x1 - (a // b) * y1
    return g, x, y
def mod_inverse(a, m):
  # Find the modular inverse of a under modulo m
  g, x, y = extended\_gcd(a, m)
  if g != 1:
    # Modular inverse does not exist if gcd(a, m) != 1
    return None
  else:
    return x % m
```

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def number_to_char(result):
  # Map the result of modulo to the appropriate character
  if 1 <= result <= 26:
    # Convert 1-26 to 'A'-'Z'
    return chr(result + 64) #1 -> 'A', 26 -> 'Z'
  elif 27 <= result <= 36:
    # Convert 27-36 to '0'-'9'
    return str(result - 27) # 27 -> '0', 36 -> '9'
  elif result == 37:
    # Map 37 to ' '
    return ' '
  else:
    return " # In case there's an unexpected value
def process_numbers(input_filename, output_filename):
  try:
    with open(input_filename, 'r') as file:
      # Read the entire content of the file and strip leading/trailing whitespace
      content = file.read().strip()
      # Split the content into a list of numbers (assuming they are space-separated)
      numbers = content.split()
      # Open the output file in write mode
      with open(output_filename, 'w') as output_file:
        # Process each number
         for num in numbers:
           try:
             # Convert the number to an integer and apply modulo 41
             result = int(num) % 41
```

```
# Find the modular inverse of the result modulo 41
             mod_inv = mod_inverse(result, 41)
             if mod_inv is None:
               output = '?' # If no modular inverse exists, map to '?'
             else:
               # Map the modular inverse to the appropriate character
               output = number_to_char(mod_inv)
             # Write the result to the output file
             output_file.write(output + "\n")
           except ValueError:
             print(f"Error: '{num}' is not a valid number. Skipping.")
             continue # Skip invalid numbers
    print(f"Processing complete. Results written to '{output_filename}'.")
  except FileNotFoundError:
    print(f"Error: The file '{input_filename}' was not found.")
# Example usage:
input_filename = "message.txt" # Replace with your actual input file path
output_filename = "output_results.txt" # Replace with your desired output file path
process_numbers(input_filename, output_filename)
```