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DEPARTMENT OF MATHEMATICS

Academic year 2025-2026 (Odd Semester)

Date: 12 <sup>th</sup> January 2026	Improvement CIE	Max Marks: 10+50
Time: 9:00 AM to 11:00 AM	UG	Duration: 120 minutes
Semester: III BE (CD, CI, CS, CY)		
Course Title: LINEAR ALGEBRA AND PROBABILITY THEORY		Course Code: MA231TC

Scheme and Solution

Q.No.	Answer	M																												
1	$Var(2X - 5) = 2^2 Var(X) = 4(27 - 5^2) = 8$	1+1																												
2	$\lambda = 2, P(X \geq 1) = 1 - P(X = 0) = 1 - e^{-2} = 8647$	1+1																												
3	$P(X > 1   Y = 2) = \frac{9/30}{14/30} = \frac{9}{14} = 0.6429$	1+1																												
4	$np = 9, npq = 6, p = 2/3, q = 1/3$	1+1																												
5	$P(X < 60) = 0.8413 \Rightarrow P\left(Z < \frac{60-50}{\sigma}\right) = 0.8413 \Rightarrow \frac{10}{\sigma} = 1 \Rightarrow \sigma = 10.$	1+1																												
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1a	i) $P(X \geq 1) = \frac{4}{15} + \frac{3}{15} = \frac{7}{15} = 0.4667$ ii) $E[X] = 0.8, E[X^2] = 1.95, Var(X) = 1.95 - 0.8^2 = 1.31, \sigma = \sqrt{1.31} = 1.1446$	1 4																												
1b	i) $f(y) \geq 0, \int_{-\infty}^{\infty} f(y) dy = \int_0^1 10(1-y)^9 dy = [-(1-y)^{10}]_0^1 = 1$ ii) $P(Y > 0.6) = \int_{0.6}^1 10(1-y)^9 dy = [-(1-y)^{10}]_{0.6}^1 = 0.0001$ Percentage of batches that are not acceptable is 0.01%	1+2 1 1																												
2	$\begin{array}{c ccccc} x \\ \hline y & 1 & 2 & 3 & 4 \end{array}$ Since $\sum_x \sum_y p(x, y) = 1, k = 1/54$ $\begin{array}{c cccc} x & 1 & 2 & 3 & 4 \\ \hline p_X(x) & 9/54 & 12/54 & 15/54 & 18/54 \end{array}$ $\begin{array}{c ccc} y & 1 & 2 & 3 \\ \hline p_Y(y) & 14/54 & 18/54 & 22/54 \end{array}$ $E[X] = 150k = 150/54, E[X^2] = 480/54, E[Y] = 116/54, E[Y^2] = 284/54$ $E[XY] = 320/54, Cov(X, Y) = -0.0412, \rho = -0.0473$	1 1 1 4 3																												
3	(i) $\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(x, y) dx dy = 1 \Rightarrow \int_0^1 \int_0^1 kxy dx dy = 1 \Rightarrow \frac{k}{4} = 1 \Rightarrow k = 4$ (ii) $P(X < 0.5, Y < 1) = \int_0^{0.5} \int_0^1 4xy dx dy = 1/4$ (iii) $P(X + Y > 1) = \int_0^1 \int_{1-y}^1 4xy dx dy = 2 \int_0^1 y[1 - (1-y)^2] dy = 2 \int_0^1 [2y^2 - y^3] dy$ $= 2 \left[ \frac{2y^3}{3} - \frac{y^4}{4} \right]_0^1 = \frac{5}{6}$	2 1 2 1 1+1																												
	(v) $f_Y(y) = \begin{cases} 2y, & 0 \leq y \leq 1 \\ 0, & \text{otherwise} \end{cases}$ (iv) $P(Y > 0.5) = \int_{0.5}^1 2y dy = 3/4$	2																												
4a	$n = 24, np = \mu = \frac{50}{75} = 2/3, p = 2/72$ <table border="1"> <tr> <td>Values (X):</td> <td>0</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>Frequency:</td> <td>39</td> <td>23</td> <td>12</td> <td>1</td> <td>0</td> <td>0</td> </tr> <tr> <td><math>p(x)</math></td> <td>0.5086</td> <td>0.3488</td> <td>0.1146</td> <td>0.024</td> <td>0.0036</td> <td>0.0004</td> </tr> <tr> <td>Expected Frequency</td> <td>12.2064</td> <td>8.3712</td> <td>2.7504</td> <td>0.576</td> <td>0.0864</td> <td>0.0096</td> </tr> </table>	Values (X):	0	1	2	3	4	5	Frequency:	39	23	12	1	0	0	$p(x)$	0.5086	0.3488	0.1146	0.024	0.0036	0.0004	Expected Frequency	12.2064	8.3712	2.7504	0.576	0.0864	0.0096	1+1 3 1
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38.15 26.66 8.6 1.8 0.7 0.03

	$X$ - be the number of flaws per millimeter, $\lambda = 3$	1
4b	i) $P(X = 4) = \frac{3^4 e^{-3}}{4!} = 0.1680$	1
	$Y$ - be the number of flaws per 2 millimeter, $\lambda = 6$	1
	ii) $P(Y \geq 1) = 1 - P(Y = 0) = 1 - \frac{6^0 e^{-6}}{0!} = 0.9975$	1
5a	$\mu = 10, f(x) = \frac{1}{10} e^{-10x}, F(x) = 1 - e^{-10x}$ $P(X > 60) = e^{-6} = 0.0025$ $P(30 < X < 60) = 1 - e^{-6} - (1 - e^{-3}) = 0.0473$ $P(X < x) = 0.5 \Rightarrow 1 - e^{-\frac{x}{10}} = 0.5 \Rightarrow -\frac{x}{10} = \ln 0.5 = -0.6931, x = 6.931 \text{ Minutes}$	1+1 1+1
5b	$\mu = 24, \sigma = 3.8, Z = \frac{X-24}{3.8}$ $P(X \leq 30) = P\left(Z \leq \frac{30-24}{3.8}\right) = P(Z \leq 1.58) = 0.9429$ $P(20 < X < 40) = P(-1.0526 < Z < 4.2105) = 1 - 0.1469 = 0.8531$	1 1 2