

# AI1103-Assignment 3

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Python codes :

<https://github.com/Aayush-2492/Assignments/tree/main/Assignment3/code>

Latex codes :

<https://github.com/Aayush-2492/Assignments/tree/main/Assignment3>

Let B denote the event that out of last three coins, only one shows tail.

$$P(B) = \frac{3}{8} \quad (0.0.3)$$

Since tossing a coin and rolling a dice are independent events,

$$P((X_i = k) \cdot (Y = l)) = P(X_i = k) \cdot P(Y = l) \quad (0.0.4)$$

$k \in \{0, 1\}$  and  $l \in \{1, 2, 3, 4, 5, 6\}$ .

Let A denote the event that the score is 2.

Clearly,

$$P(A) = P(Y = 2|X_1 = 0) \cdot P(X_1 = 0) + P(B|X_1 = 1) \cdot P(X_1 = 1) \quad (0.0.5)$$

$$= P((X_1 = 0) \cdot (Y = 2)) + P((X_1 = 1) \cdot B) \quad (0.0.6)$$

$$= P(X_1 = 0) \cdot P(Y = 2) + P(X_1 = 1) \cdot P(B) \quad (0.0.7)$$

$$= \frac{1}{2} \cdot \frac{1}{6} + \frac{1}{2} \cdot \frac{3}{8} \quad (0.0.8)$$

$$= \frac{13}{48} \quad (0.0.9)$$

We have to find  $P(X_1 = 0|A)$

$$P(X_1 = 0|A) = \frac{P(A \cdot (X_1 = 0))}{P(A)} \quad (0.0.10)$$

$$= \frac{P(X_1 = 0) \cdot P(Y = 2)}{P(A)} \quad (0.0.11)$$

$$= \frac{\frac{1}{2} \cdot \frac{1}{6}}{\frac{13}{48}} \quad (0.0.12)$$

$$= \frac{4}{13} \quad (0.0.13)$$

$$= 0.31 \quad (0.0.14)$$

## QUESTION 29

Raju has four fair coins and one fair dice. At first Raju tosses a coin. If the coin shows head then he rolls the dice and the number that dice shows is taken as his score. If the coin shows tail then he tosses three more coins and the total number of tails shown (including the first one) is taken as his score. If Raju tells that his score is 2 then the probability that he rolled the dice is (up to two decimal places):

## SOLUTION

Let  $X_i$  denote the random variable function for the  $i$ th coin  $i \in \{1, 2, 3, 4\}$ .

$X_i \in (0, 1)$  where 0 represents head and 1 represents tail  $i \in \{1, 2, 3, 4\}$ .

	Head	Tail
$X_i = k$	0	1

$$P(X_i = k) = \frac{1}{2} \quad (0.0.1)$$

$k \in \{0, 1\}$  and  $i \in \{1, 2, 3, 4\}$ .

Let  $Y$  denote the random variable function for the dice.

$Y \in (1, 2, 3, 4, 5, 6)$  where 1 represents dice showing 1 and so on.

Dice number	1	2	3	4	5	6
$Y = k$	1	2	3	4	5	6

$$P(Y = k) = \frac{1}{6} \quad (0.0.2)$$

$k \in \{1, 2, 3, 4, 5, 6\}$ .

**Therefore, required probability = 0.31**