

gdb for CSE

Lecture - 60

(Hashmap 1)

→ Why hashing?

→ Used to reduce the time complexity of searching

→ Finding a unique index for all elements to store them ↳ hash value

→ What is hashing?

① Hash 68 2 , 761 , 494 , 567 , 869
Values = 2 1 4 7 9

③ Hash table

| | |
|---|-----|
| 0 | 761 |
| 1 | 682 |
| 2 | |
| 3 | |
| 4 | 494 |
| 5 | |
| 6 | |
| 7 | 567 |
| 8 | |
| 9 | 869 |

② $h(k) = k \bmod 10$

Hash Function

O(1)

Search(761)

→ What are hash functions?

1) Division Method

$$h(k) = k \bmod m \rightarrow \text{buckets}$$

$$m = 11$$

$$1276 \bmod 11 = 0$$

2) Mid square Method

$$h(k) = k^2 \& \text{ extract middle digits}$$

$$k = 60$$

$$k = 13$$

$$k^2 = 3600$$

$$k^2 = 169$$

3) Digit folding Method

Fold key into equal size parts.

$k_1 k_2 k_3 k_4 k_5$

$$k = 12345$$

$$12 + 34 + 5 = 51 \rightarrow \text{hash value}$$

$$12345 = 16875$$

1. Multiplication Method

$$h(k) = \text{floor}(M(KA \bmod 1))$$

eg: $k = 12345, M = 10$
 $A = 0.01$

$$K \cdot A = 123.45$$

$$KA \bmod 1 = \cancel{123} (123.45 \bmod 1) = 0.45$$

$$\hookrightarrow XM = 0.45 \times 10 = 4.5$$

$$\text{floor}(M(KA \bmod 1)) = \text{floor}(4.5) = 4$$

→ Collision :-

when 2 elements have same hash value.

→ Open hashing

Separate
Chaining

int. ki jah linkedlists ente Karayenge
 Jha bhi 2 ya 2 se jyada elements ke hash value
 same hoga to unhe ~~one~~ us hash value par ll.
 breaker adal Karayenge

→ Close hashing (Linear Probing)

$$682, 761, 494, 567, 869, \underline{634}, \underline{794}$$

1 761

2 682

3 ~~494~~

4 494

5 634

6 794

7 567

8

9 869

$$h(k) = k \bmod 10$$

$$\text{at } (h(k)+i) \bmod 10 \quad 0 \leq i \leq 9$$

$$\rightarrow h(794) = (4+0) \bmod 10 = 4$$

$$= (4+1) \bmod 10 = 5$$

$$= (4+2) \bmod 10 = 6$$

→ Close hashing (open Addressing)

- Quadratic Probing

$$h(k) = k \bmod M$$

at $(h(k) + i^2) \bmod M$ $0 \leq i \leq M$

- Double hashing

$$h_1(k) = k \bmod 5$$

$$h_2(k) = k \bmod 10$$

store at $(h_1(k) + i \cdot h_2(k)) \bmod M$

$$\Rightarrow [h(634) = h(634) + 1 \cdot h_2(634)] \bmod 10$$

$$\Rightarrow [4 + 1 \cdot 4] \bmod 10 = 8$$

⇒ Load Factor

$n \rightarrow$ no. of elements

$m \rightarrow$ no. of buckets

Load factor = $\frac{n}{m}$] → Avg entries in one bucket

⇒ Rehashing

Load factor limit = 0.75

L.F > limit

→ Increasing size of hash table & redistributing elements in it.

Q Implement hash table with closed addressing.
Separate chaining.

Ans) `#include <vector>`

#include <list>

Using namespace std;

class Hashing {

```
vector<list<int>> hashtable;
```

int buckets;

public:

Hashing (int size) :-

buckets = size;

```
 hashtable.resize(size);
```

۳

int hashvalue (int key) {

return key % buckets; //division method

3

Add key

Void add (int key)

int idx = hashValue(key);

hashtable [idx] - push_back (key);

3

//searchkey

```
list<int>::iterator search(int key) {
```

int id = hashValue(key);

return find(hashtable[idn].begin(), hashtable[idn].end(),

, key);

1

// detect key

Void delete (int key) {

```
int hashCode = hashValue(key);
```

if(search(key) = hashtable[which]) end();

```
 hashtable[addr].erase(search(key));  
cout << key << " is deleted" << endl;
```

} else {

cout << "key is not present in the hashtable";

}

}

};

```
int main () {  
    Hashing h(10);  
    h.addkey(5);  
    h.addkey(9);  
    h.addkey(3);
```

h.deletekey(3);

h.deletekey(3);

return 0;

}

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Hash Map

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⇒ Map in C++ STL

→ STL container which stores key-value pair.

→ The elements are stored in ascending / descending

→ Maps cannot have duplicate keys. order.

→ implemented through BST

A) Initialization

→ Header file required

#include <map>

→ Declaration

* By default order is ascending.
map<key datatype, value datatype> map-name

Descending order) → map<datatype1, datatype2, greater<datatype1>> map-name

→ Initialize :-

map<datatype1, datatype2> map-name = {{key1, value1},
{key2, value2}, {key3, value3}, }

→ Insertion :-

O(n) directory.insert (make_pair ("ABC", 379))

→ Printing the elements :-

• for each loop

→ key value pair

for (auto element : map1) {

key = element.first;

value = element.second;

→ **erase()**

m. erase (itr)

m. erase (key)

m. erase (start-itr, end-itr)

— $O(n)$

→ **swap()**

m1. swap(m2)

swap (m1, m2)

→ **clear()**

m. clear () → clear all elements

→ **empty()**

m. empty () → returns if empty

→ **m.size()**

→ m. max_size()

→ m.find (key) → return itr to element if present,
else it returns map.end() itr

→ **count()** → no. of occurrences of key

m.count (key) = 1

→ **upper_bound()** → returns an itr to next greater element.

→ **lower_bound()** → return itr to element if present,
else itr to next greater element.

→ begin() and end() / or begin() and rend() notes

```
#include <iostream>
#include <map>
using namespace std;
```

```
int main () {
```

```
    map<string, int> directory;
```

```
    directory["naman"] = 38769;
```

```
    directory["animesh"] = 94562;
```

```
    directory["ritu"] = 12369; // update of value already present
```

```
    for (auto element : directory) {
```

```
        cout << "Name - " << element.first << endl;
```

```
        cout << "Phone No.-" << element.second << endl;
```

```
    } cout << endl;
```

```
    directory.insert(make_pair("city", 4629)); // No change
```

```
    for (auto element : directory) {
```

```
        cout << "Name - " << element.first << endl;
```

```
        cout << "Phone No.-" << element.second << endl;
```

```
// using iterator map<string, int>::iterator itr;
```

```
for (itr = directory.begin(); itr != directory.end(); itr++) {
```

```
    cout << itr->first << " - " << itr->second << endl;
```

```
} return
```

Ques Sum of repetitive elements

You are given an integer n , representing the no. of elements.

Then you will be given n elements. You have to return the sum of repetitive elements i.e. the elements that appear more than one time

Input:

$n = 7$

Elements = {1, 1, 2, 1, 3, 3, 3}

Output: 4

The repetitive elements are 3, 1
and their sum is $1+3=4$

Soln: #include <map>

#include <vector>

using namespace std;

int main()

int n;

cin >> n;

Time

$O(n)$ { Vector <int> v;
for (int i=0; i<n; i++) {
 cin >> v[i];
 3

// sorting freq. of every
element in input array.

Space

$O(m)$ { map <int, int> m;
for (int i=0; i<n; i++) {
 m[v[i]]++;
 3

{ {1,1}, {1,2}, {1,3},
 {2,1}, {3,1}, {3,2}, {3,3} }

int sum = 0;

for (auto pair : m) {

 if (pair.second > 1) {

 sum += pair.first;

 3

// finding sum of
repetitive
elements.

return 0;

3



Unordered Map

- STL containers, store key value pair
- elements are not ordered
- Keys will be unique

Inserion } O(1)
 Deletion } implemented
 Retrieval/Search } using hashing

header file $\Rightarrow \#include <\text{Unordered map}>$

Member functions

| | |
|-------------|--------------|
| m. insert() | } O(1) avg |
| m. erase() | } O(n) worst |
| m. find() | |

Same functions as map



Multimap

- duplicate keys are allowed.

Insert

Delete $\Rightarrow O(\log N)$

Search

BST

same functions as map

same header file $\Rightarrow \#include <\text{map}>$

multimap<int, int> m;



Unordered Multimap

- elements are not ordered
- duplicate keys are allowed
- Hashing

Inserion } O(1) Avg case
 Deletion }
 Search } O(n) Worst case

header file $\Rightarrow \#include <\text{unordered_map}>$

unordered_multimap<string, int> Unmap;

Unique keys

MAP

Unordered-map

Ordered

Not ordered

Multimap

Unordered multimap.

Duplicate keys

Q4 Give Output:

multimap<int, int> m;

m.insert({1, 1});

m.insert({2, 3});

m.insert({3, 8});

start itr → m.insert({4, 9});

end itr → m.insert({5, 20})

Group []
m[5] = 25; // Line 1
m[4] = 20; // Line 2Ans

(C) compilation error; there is no [] operator in multimap.

Q23

```
auto a = equal_range(4); // returns bounds of range
of elements with key passed
for (auto it = a.first; it != a.second; it++) {
    cout << it->first << " - " << it->second << endl;
```

3

Ans

(B) 4 - 16

4 - 20

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HashMap 3 (Problem)

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Ques → Can you make the strings equal?

Given an array of strings. You can move any no. of characters from one string to any another string any no. of times. You just have to make all of them equal.

Print "Yes" if you can make every string in the array equal by using any no. of operations. otherwise print "No".

Input: ["Collegee", "oll", "Collegge"]

Output: Yes

String at 1 index can take 2 'e' from 0 index string and one 'g' from 2 index string.

Concept → ① We don't need to transfer strings by moving characters

② Each character should be present in multiple of length of array

Ans → #include <vector>

#include <unordered-map>
using namespace std;

bool canMakeEqual(vector<string> &v) {

 unordered_map<char, int> m;

 for (auto str : v) {

 for (char c : str) {

 m[c]++;

}

3

```

int n = v.size();
for (auto ele : m) {
    if (ele.second % n != 0) {
        return false;
    }
}
return true;
}

int main() {
    int n;
    cin >> n;
    Vector<string> V[n];
    for (int i = 0; i < n; i++) {
        cin >> V[i];
    }
    cout << (canMakeEqual(V) ? "Yes" : "No") << endl;
    return 0;
}

```

Q3 Check whether two strings are anagram of each other. Return true if they are else return false. An anagram of a string is another string that contains the same characters, only the order of characters can be different.
 For example, "abcd" and "dabc" are an anagram of each other.

input1: triangle
 integral

Output :- True

Methods to Solve

- (1) 2 arrays
- (2) 2 maps
- (3) 1 map

```
#include <unordered_map>
using namespace std;
```

```
bool checkAnagrams (string s1, string s2) {
    if (s1.length() != s2.length()) { return false; }
    unordered_map<int> m;
```

```
for (auto c1 : s1) {
    m[c1]++;
}
```

```
for (auto c2 : s2) {
    if (m.find(c2) == m.end()) {
        return false;
    } else {
        m[c2]--;
    }
}
```

```
for (auto el : m) {
    if (el.second != 0) {
        return false;
    }
}
```

return true;

int main

s1, s2 → enter

```
cout << (checkAnagrams (s1, s2) ? "Anagram" : "Not Anagram")
return 0;
```

}

Ques Check whether if two strings are isomorphic of each other.

Two strings are isomorphic of each other if there is a one to one mapping possible for every character of the first string to every character of the second string and all occurrences of every character in first string maps to the same character in the second string.

input 1: ~~a~~ a a b
 ~~b~~ b y

Output 1: True

Soln #include <unordered>

#include <vector>

using namespace std,

bool checkIsomorphic (String s1, String s2) {

 if (s1.length() != s2.length()) {
 return false;

}

bool checkOneToManyMapping (String s1, String s2) {

 unordered_map <char, char> m;

 for (int i = 0; i < s1.length(); i++) {

 if (m.find(s1[i]) != m.end()) {
 if (m[s1[i]] != s2[i])
 return false;

}

 } else {

 m[s1[i]] = s2[i];

}

bool S1S2 = checkOneToManyMapping (s1, s2);

bool S2S1 = checkOneToManyMapping (s2, s1);

{ Now save for loop for S2 }

[change S2, S1] in code }

return S1S2 & S2S1

3

int main() {

string S1, S2;

cin >> S1 >> S2;

cout << (checkIsAnagram(S1, S2) ? "Yes" : "No");

return 0;

3

Q → Given an array of length n and a target, return a pair where sum is equal to the target. If there is no pair present, return -1.

Input 1 : n = 7

Elements = [1, 4, 5, 11, 13, 10, 2]

Target = 13

Output 1 : [3, 6]

Method ① ↗ Nested loops

i = 0 to n

j = i + 1 to n

a[i] + a[j]

② 2 Pointer approach

array should be sorted

1 2 4 5 10 11 13
↑ ↑ ↓ ↑

O(n)

③ O(n) using map & storing previous elements.

~~Sol~~ → #include <vector>

include <map> unordered_map>
using namespace std;

int
Vector<int> targetsumpair (Vector<int> &v, int targetsum) {

unordered_map<int, int> m;

Vector<int> ans {2, -1};

for (int i = 0; i < v.size(); i++)

if (m[targetsum - v[i]] != m.end())

ans[0] = m[targetsum - v[i]];

ans[1] = ~~v[i]~~ i;

else {

m[v[i]] = i;

}

3

return ans;

}

int main() {

n → Enter

v → Enter

targetsum → Enter

Vector<int> ans = targetsumpair (v, targetsum);

cout << ans[0] << " " << ans[1];

return 0;

}

Q → Given an array arr[] of length N, find the length
of the longest subarray with a sum equal to 0.

input: n = 8

arr[] = {15, -2, 2, -8, 1, 7, 10, 23}

output: 5

Method 1 \rightarrow BF \rightarrow Nested Loops

$$(2) \quad a[l \dots r] = c$$

$$\text{prefix}_r - \text{prefix}_{l-1} = c$$

$$\text{prefix}_r = \text{prefix}_{l-1}$$

Time, Space

$O(n)$

include <vector>

include <unordered_map>

using namespace std;

```
int maxLengthZeroSumSubarray (Vector<int> &v) {
```

```
    unordered_map<int, int> m;
```

```
    int prefixc = 0;
```

```
    int maxLen = INT-MIN;
```

```
    for (int i=0; i < v.size(); i++) {
```

```
        prefixc += v[i];
```

```
        if (prefixc == 0) {
```

```
            maxlen++;
```

```
}
```

```
        if (m.find(prefixc) != m.end()) {
```

```
            maxlen = max(maxlen, i - m[prefixc]);
```

```
        } else {
```

```
            m[prefixc] = i;
```

```
}
```

```
}
```

```
        return maxlen;
```

```
}
```

```
int main() {
```

```
    vector<int> v;
```