

## Binary Trees

⇒ What is a Tree data structure:-

- Non-linear data structures stores hierarchical data.
- elements are stored at different levels.
- elements are called nodes → which are connected / linked together to represent hierarchy.

⇒ Terminology

- Root

- Child Node

- Parent Node

- Sibling Nodes → (E, F)

~~External Node~~

- Leaf Node → have no child nodes (E, F, G, D)

- No. of Edges → link b/w 2 nodes

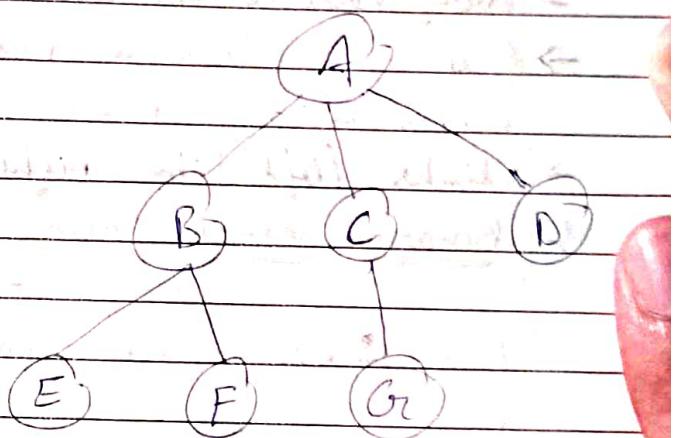
- Level → no. of edges from root nodes

- Height → Max. no. of edges b/w a leaf node and root ~~node~~ node.

- size → no. of nodes in a tree

if  $n$  nodes →  $n-1$  edges

- subtree → tree which is a child of a node

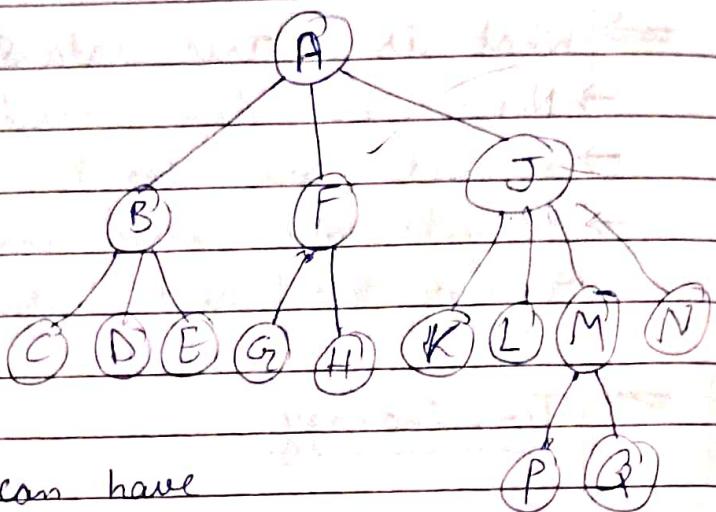


→ Binary Tree is said to be extended binary tree for 2-ary tree if each node has either 0 or 2 children. Nodes having 2 children is internal Node and is represented by circle. Node having 0 child is external and represented by square.

## (\*) Types of trees

### 1. Generic Trees

A node can have any no. of child nodes.



### 2. Binary Trees

→ every node contain data

→ tree in which a node can have maximum 2 child nodes.

→ 2 links (left child, Right child)

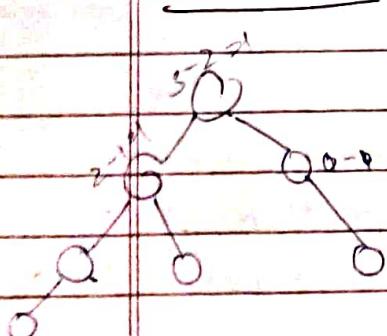
### 3. Binary Search trees (BST)

→ BT in which all nodes in left subtree will have value less than root node value.

All nodes in right subtree will have value more than root node value.

### 4. AVL Trees → Self Balancing tree

→ diff. b/w heights of left Sub tree and right subtree can be 1, 0, -1.



## (\*) Implementation of Node Class:-

Node	left	Data	Right
------	------	------	-------

Stores the address of left & right child nodes respectively.

\* if any child does not exist, pointer will point to NULL.

```
struct Node {
public:
```

```
    int value;
    Node* left;
    Node* right;
```

```
Node (int v) {
```

```
    value = v;
```

```
    left = right = NULL;
```

```
};
```

```
int main () {
```

```
    Node* root = new Node(2);
```

```
    root->left = new Node(1);
```

```
    root->right = new Node(3);
```

```
    cout << root->value << endl;
```

```
    cout << root->left->value
```

```
};
```

```
cout << root->right->value
```

```
}
```



## Traversals

① DFS (Depth First search)

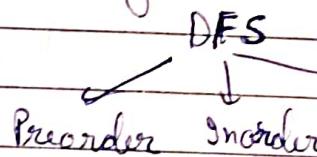
→ travel along the height.

① Preorder

(i) Visit the Root Node

(ii) left subtree

(iii) Right subtree



Void preorderTraversal (Node\* rootNode) {

```
if (rootNode == NULL) {
```

```
    return;
```

```
}
```

```
cout << rootNode->value << " ";
```

```
preorderTraversal (rootNode->left);
```

```
preorderTraversal (rootNode->right);
```

```
}
```

## (2) Inorder

- (i) Visit left subtree }
- (ii) Root node } recursively
- (iii) Visit right subtree }

Void InorderTraversal (Node\* rootNode) {

```
if (rootNode == NULL) { // base case
    return;
}
```

// recursive call

InorderTraversal (rootNode → left);

cout << rootNode → Value << " ";

InorderTraversal (rootNode → right);

}

## (3) Postorder

- (i) Visit left subtree }
- (ii) Right subtree } recursively
- (iii) Root Node }

Void Postorder (Node\* rootNode) {

```
if (rootNode == NULL) {
    return;
}
```

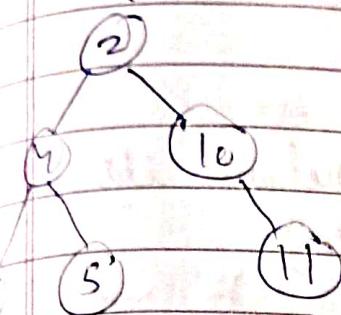
Postorder (rootNode → left);

Postorder (rootNode → right);

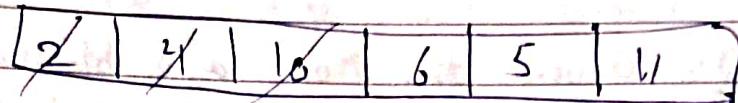
cout << rootNode → value << " ";

}

② Levelorder → Breadth first Traversal



Use Queues data structure



Fk kaata or 2 Ghusaye

```
#include <queue>
```

```
Class Node {
```

```
}
```

```
Void LevelorderTraversal (Node* rootNode) {
```

```
    if (rootNode == NULL) {  
        return;  
    }
```

```
    queue < Node*> q;  
    q.push(rootNode)
```

```
    while (!q.empty()) {
```

```
        int nodesAtCurrentLevel = q.size();
```

```
        while (nodesAtCurrentLevel--) {
```

```
            Node* currNode = q.front();
```

```
            q.pop()
```

```
            cout << currNode->value << " ";
```

```
            if (currNode->left) {
```

```
                q.push(currNode->left);
```

```
            }
```

```
            if (currNode->right) {
```

```
                q.push(currNode->right);
```

```
            }
```

3 Count < end;

Q. Given the root of a binary tree, return its maximum depth. (No. of Nodes Top to bottom)

Sol. int maxDepth(Node\* root){

```
if (root == NULL) {  
    return 0;  
}
```

```
int leftDepth = maxDepth(root->left);  
int rightDepth = maxDepth(root->right);  
return (max(leftDepth, rightDepth) + 1);
```

Q. Given the root of a binary tree, return the no. of leafnodes present in it.

Sol. int leafNodes(Node\* root){

```
if (root == NULL) {  
    return 0;  
}
```

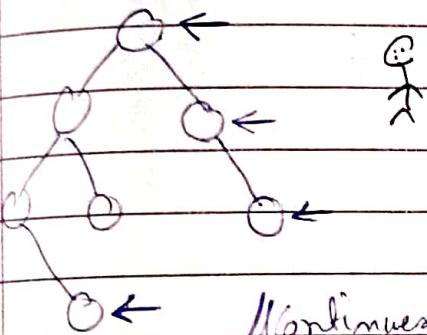
```
if (root->left == NULL && root->right == NULL) {  
    return 1;  
}
```

```
int leftSubtreeLeafnodes = LeafNodes (root->left);
int rightSubtreeLeafnodes = LeafNodes (root->right);
```

```
return leftSubtreeLeafnodes + rightSubtreeLeafnodes;
```

}

Q Given the root of a binary tree, imagine yourself standing on the right side of it, return the values of the nodes you can see from top to bottom.



Solv Class Node{

};

```
vector<int> rightViewBinaryTree (Node* root) {
```

```
    vector<int> ans;
```

```
    if (root == NULL) {
```

```
        return ans;
```

}

```
queue<Node*> q;
```

```
q.push(root);
```

```
while (!q.empty()) {
```

```
    int nodesAtCurrlvel = q.size();
```

```
    while (nodesAtCurrlvel) {
```

```
        Node* currNode = q.front();
```

```
        q.pop();
```

```

if (node->curlevel == 1) {
    ans.push_back (currnode->value);
}

```

{}

```

if (currnode->left) {

```

```

    q.push (currnode->left);
}

```

{}

```

if (currnode->right) {

```

```

    q.push (currnode->right);
}

```

{}

```

node->curlevel--;

```

```

}
@

```

{}

```

return ans;
}

```

```

int main () {

```

```

    Node* rootNode = new Node(2);

```

```

    ;
}

```

```

Vector< int > ans = rightViewBinaryTree (rootNode);

```

```

for (auto i : ans) {

```

```

    cout << i << " ";
}

```

```

cout << endl;
}

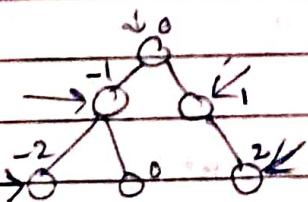
```

```

return 0;
}

```

Q33 Print the top view of a binary tree.



queue - Pair (Node, column)

Map - Column → Value

Col of Left child → Col of Parent - 1

Col of Right child → Col of Parent + 1

```
#include <vector>
#include <queue>
#include <map>
using namespace std;
```

## Class Node

33

~~vector <int> TopViewBinaryTree(Node\* root) {~~

Vector<int> ans;

if (root == NULL) {

return ans;

queue < pair < Node\*, int > > q;

q. push (make-pair (root, 0));

```
map<int,int>m;
```

while (!q.empty()) {

int nodesatcurrlevel = q.size();

while (nodesatcurlevel --) {

pair<Node\*, int> p = q.front();

Node \* currNode = p.first;

int currColumn = p.second;

g. bob( );

if (m.find(CurrNode) == m.end()) {  
 m[CurrColumn] = CurrNode -> value;

if (currNode->left) {

q. push(make\_pair(currNode,  $\rightarrow$  left, curr column))

if (currNode->right) {

q. push (make-pair (currNode → right,  
currColumn + 1))

```

    3
    5
for (auto it : m) {
    ans.push_back(it.second);
}

```

int main () {

```

Node* rootNode = new Node(2);

```

```

Vector<int> ans = TopView Binary Tree (rootNode);

```

```

for (auto i : ans) {

```

```

cout << i << " ";

```

```

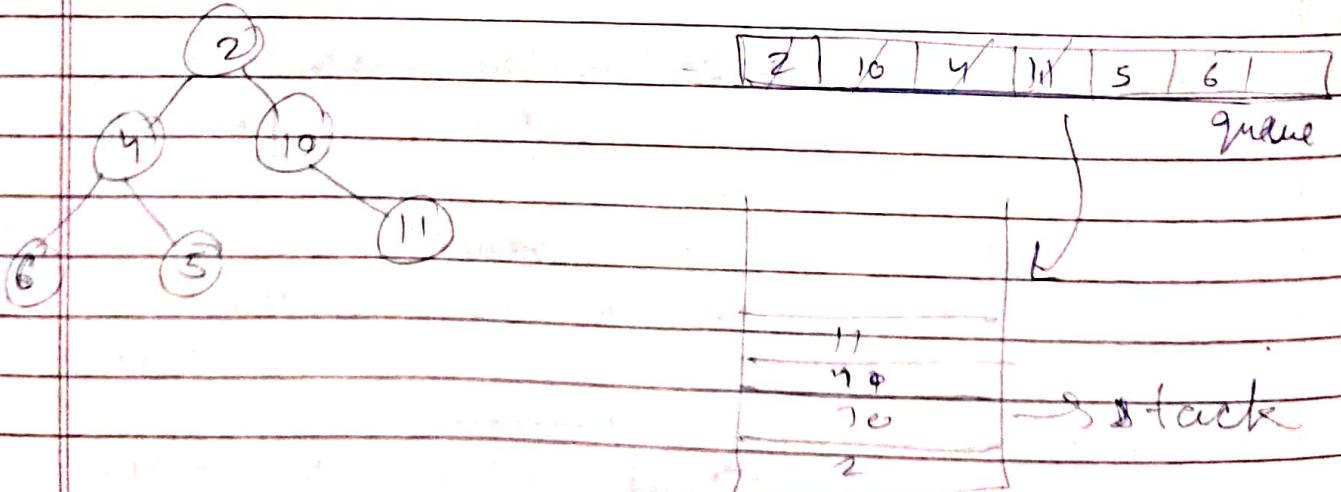
} cout << endl;
return 0;
}

```

(H.W)

Q4 Given a binary tree, print the bottom view from left to right. A node is included in the bottom view if it can be seen when we look at the tree from the bottom.

Q5 Print the level order in reverse manner i.e. print the last row first and then the rows below.



```
#include <vector>
#include <queue>
#include <stack>
using namespace std;
```

```
Vector<int> reverseLevelOrder (Node* root) {
```

```
    Vector<int> ans;
```

```
    if (root == NULL) {
```

```
        return ans;
```

```
}
```

```
queue<Node*> q;
```

```
stack<int> s;
```

```
q.push (root);
```

```
while (!q.empty ()) {
```

```
    int NodesatCurrentLevel = q.size();
```

```
    while (NodesatCurrentLevel--) {
```

```
        Node* currNode = q.front();
```

```
        q.pop();
```

```
s.push (currNode);
```

```
        if (currNode->right) {
```

```
            q.push (currNode->right);
```

```
}
```

```
        if (currNode->left) {
```

```
            q.push (currNode->left);
```

```
}
```

```
}
```

```
    while (!s.empty ()) {
```

```
        ans.push_back (s.top());
```

```
s.pop();
```

return ans;

}

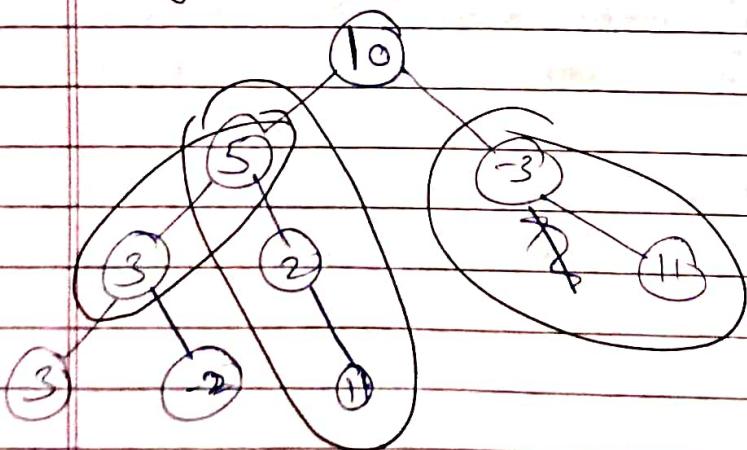
int main() {

```
Vector<int> ans = reverseLevelOrder(rootNode);
for(auto i: ans)
    cout << ans << " ";
cout << endl;
return 0;
}
```

## Lecture 7.2

### Interview Problems on Binary Trees.

- Q1** Given the root of a binary tree and an integer target sum, return the no. of paths where the sum of the values along the path equals target sum. The path does not need to start or end at the root or a leaf, but it must go downwards (i.e. traveling only from parent nodes to child nodes).



Soln

### Class Solution {

public:

```
int pathSumHelper(TreeNode* root, int targetSum,
                   int currSum, unordered_map<long int, int> pathCount);
```

```
if (root == NULL) {
```

```
    return 0;
```

```
}
```

```
currSum += root->value;
```

```
int ansCount = pathCount[currSum - targetSum];
```

```
pathCount[currSum]++;
```

```
ansCount += pathSumHelper(root->left, targetSum,
```

```
currSum, pathCount)
```

```
+ pathSumHelper(root->right, targetSum,
```

```
currSum, pathCount);
```

```
pathCount[currSum]--; // while Backtracking
```

```
return ansCount;
```

```
}
```

```
int pathSum(TreeNode* root, int targetSum) {
```

```
unordered_map<long int, int> pathCount;
```

```
pathCount[0] = 1;
```

```
return pathSumHelper(root, targetSum, 0, pathCount);
```

```
}
```

Q2 Given the root of a binary tree, return the maximum path sum of any non-empty path.

Ans 1. left child

2. Right child

3. both left & right child

4. only Root node

$$\maxSum = (\text{left maxSum} + \text{right maxSum} + \text{rootVal})$$

$$\max(\maxSum, \uparrow)$$

return root  $\rightarrow$  val + maxc(leftmaxSum, rightmaxSum);

Sol. 2 Class Solution {

public:

int maxSumPathHelper(TreeNode\* root, int & maxSum);

T.C, S.C

O(N)

if (root == NULL) {  
 return 0;

}

int leftmaxSum = max(0, maxSumPathHelper(root  $\rightarrow$  left,  
maxSum));

int rightmaxSum = max(0, maxSumPathHelper(root  $\rightarrow$  right,  
maxSum));

maxSum = max(maxSum, root  $\rightarrow$  val + leftmaxSum + rightmaxSum);

return (root  $\rightarrow$  val + maxc(leftmaxSum, rightmaxSum));

}

Q int maxPathSum(TreeNode\* root) {

int maxSum = INT\_MIN;

maxSumPathHelper(root, maxSum);

return maxSum;

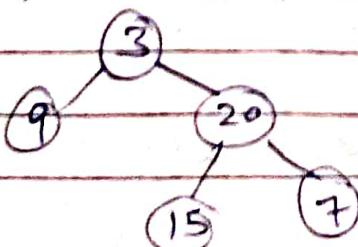
}

};

Q 3- Given two integer arrays preorder and inorder where preorder is the preorder traversal of a binary tree and inorder is the inorder traversal of the same tree, construct and return the binary tree.

input: preorder = [3, 9, 20, 15, 7], inorder [9, 3, 15, 20, 7]

output: [3, 9, 20, null, null, 15, 7]



Sol1- Class Solution {public:

```
TreeNode* buildTreeHelper(vector<int> &preorder, int prestart,
                           int preend, vector<int> &inorder,
                           int instart, int inend,
                           unordered_map<int, int> &inmap) {
```

```
    if (prestart > preend || instart > inend) {
```

```
        return NULL; // handling the leaf nodes.
```

{}

```
    TreeNode* rootNode = new TreeNode (preorder[prestart])
```

```
    int rootInorderIndex = inmap[rootNode->val];
```

```
    int leftSubtreeSize = rootInorderIndex - instart;
```

```
    rootNode->left = buildTreeHelper (preorder, prestart + 1,
                                       prestart + leftSubtreeSize, inorder, instart,
                                       rootInorderIndex rootInorderIndex - 1, inmap);
```

```
    rootNode->right = buildTreeHelper (preorder, prestart + leftSubtreeSize + 1, preend, inorder,
                                         rootInorderIndex + 1, inend, inmap);
```

```
    return rootNode;
```

{}

```
TreeNode* buildTree (vector<int> &preorder, vector<int> &inorder)
```

```
    unordered_map<int, int> inmap;
```

```
    for (int i=0; i<inorder.size(); i++) {
```

```
        inmap[inorder[i]] = i;
```

{}

a

```
    return buildTreeHelper (preorder, 0, preorder.size() - 1,
                           inorder, 0, inorder.size() - 1, inmap);
```

{

};

## Construct BT From

T.C =  $O(N)$   
S.S =  $O(N)$

FREEMIND

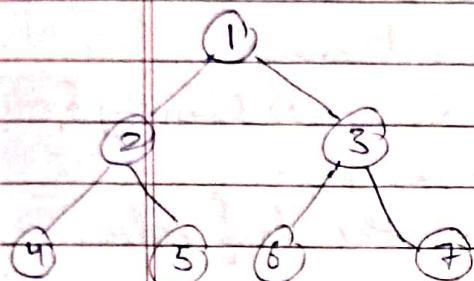
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Preorder and Postorder

Input:- Preorder = [1, 2, 4, 5, 3, 6, 7], Postorder = [4, 5, 2, 6, 7, 3, 1]

Output:-



Posttree: Post start,

Left Child  
Index

Right Subtree

left child index + 1,

Post end - 1

Preorder: Prestart Prestart + 1 [Prestart + leftSubtreeSize + 1, Prestart + leftSubtreeElements + 1, Preend]  
leftChildIndex - poststart + 1

Sol:- Class Solution :-

public:

TreeNode\* ConstructFromPrePostHelper (vector<int> & preorder,  
int prestart, int preend, vector<int> & postorder,  
int poststart, int postend, Unordered\_map<  
<int, int> & postmap>) {

if (prestart > preend || poststart > postend) {  
return NULL;

}

TreeNode\* rootNode = new TreeNode (preorder[prestart]);  
if (prestart == preend) {  
return rootNode;

}

int leftchildVal = preorder[prestart + 1];

int leftchildIndex = postmap[leftchildVal];

int leftSubtreeSize = leftchildIndex - prestart + 1;

rootNode->left = ConstructFromPrePostHelper (&

(preorder, prestart + 1, prestart + leftSubtreeSize, postorder, poststart,  
leftchildIndex, postmap));

`rootNode -> right = constructFromPrePostHelper (preorder,  
prestart + leftSubtreeSize + 1, preend, postorder, leftchildIndex + 1,  
postend - 1, postmap);`

`return rootNode;`

③

`TreeNode* constructFromPrePost (vector<int>& preorder,  
vector<int>& postorder) {  
unordered_map<int, int> postmap;  
for (int i = 0; i < postorder.size(); i++) {  
postmap[postorder[i]] = i;`

?

`return constructFromPrePostHelper (preorder, 0,  
preorder.size() - 1, postorder, 0, postorder.size() - 1,  
postmap);`

?

3;

A

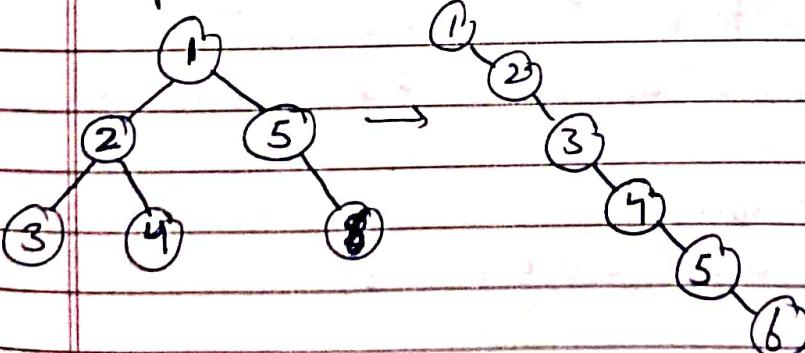
Flatten Binary Tree to linked list:

① The ll should use the same tree Node class where the right child pointer points to the next node in the list and the left child pointer is always null.

② The "linked-list" should be in the same order as a pre-order traversal of the binary tree.

input:- root = [1, 2, 5, 3, 4, null, 6]

output:- 1 → 2 → 3 → 4 → 5 → 6



```

{ if (root == NULL) return; // base case
  flatten (root -> right)
  flatten (root -> left) // recursive call
  root -> right = last;
  root -> left = NULL;
  last = root; // self work
  return;
}
  
```

T.C, S.C → O(N)

Ans 3 Class Solution {

public:

TreeNode\* lastNode = NULL;

Void flatten(TreeNode\* root){

if (root == NULL) {

return;

}

flatten(root-&gt;right);

flatten(root-&gt;left);

root-&gt;right = lastNode;

root-&gt;left = NULL;

lastNode = root;

return;

}

};

Amount of time for binary tree to be infected.

G3 You are given the root of a binary tree with unique values, and an integer start. At minute 0, an infection starts from the node with value start. Each minute a node becomes infected if:

- The node is currently uninfected.

- The node is adjacent to an infected node.

Return the no. of minutes needed for the entire tree to be infected.

input:- root = [1, 2, 5, 3, 4, null, 6]

output:- [1, null, 2, null, 3, null, 4, null, 5, null, 6]

## Solve: Class Solution {

public:

```
int calculateTime(TreeNode* startNode, unordered_map<  
    TreeNode*, TreeNode*> &parent)
```

```
unordered_set<TreeNode*> infected;
```

```
queue<TreeNode*> q;
```

```
q.push(startNode);
```

```
infected.insert(startNode);
```

```
int time = 0;
```

```
while (!q.empty()) {
```

```
    int currLevelNodes = q.size();
```

```
    bool infectFlag = false;
```

```
    while (currLevelNodes--) {
```

```
        TreeNode* currNode = q.front();
```

```
        q.pop();
```

```
        if (currNode->left && !infected.count((currNode->left))) {
```

```
            infectFlag = true;
```

```
            infected.insert(currNode->left);
```

```
            q.push(currNode->left);
```

```
        if (currNode->right && !infected.count((currNode->right))) {
```

```
            infectFlag = true;
```

```
            infected.insert((currNode->right));
```

```
            q.push(currNode->right);
```

```
if (parent[currNode] && !infected.count(parent[currNode]))  
    infectFlag = true;  
infected.insert(parent[currNode]);  
q.push(parent[currNode]);
```

3

if (infectFlag) time++;

3

return time;

```
TreeNode* makeParent(TreeNode* root, unordered_map<TreeNode*, TreeNode*>  
    &parent, int start) {
```

queue < TreeNode \* > q;

q. push (root);

```
TreeNode* startNode;
```

```
while(!q.empty()) {
```

TreeNode\* curNode = q.front();

q.pop();

if ( $\text{currNode} \rightarrow \text{val} == \text{start}$ ) {

startNode = currNode;

3

if ( $\text{currNode} \rightarrow \text{left}$ ) {     $\text{parent}[\text{currNode} \rightarrow \text{left}] = \text{currNode};$

q.push([currNode->left]);

3 if ( $\text{currNode} \rightarrow \text{right}$ ) { parent [ $\text{currNode} \rightarrow \text{right}$ ] =  $\text{currNode}$ ;

q.push(CurrNode→right);

3

3 return startNode;

3

int amountOfTime(TreeNode \*root, int start) {

unordered\_map<TreeNode\*, TreeNode\*> parent;

TreeNode\* startNode = makeParent(root, parent, start);

```
return calculateTime(startNode, parent);
```