```
import cvxpy as cp
import numpy as np
from itertools import product
```

Data of the Problem

```
shipping_cost = np.array([[1,3,2],[3,2,2]]).reshape(2,3)
production_cost = np.array([11,10]).reshape(2,1)
given_demand = np.array([[100,150,120],[120,180,150],[150,200,180]]).reshape(3,3)
selling_price = np.array([[16,16]]).reshape(2,1)
produce = np.array([100,200]).reshape(2,1)
produce_limit = np.array([300,300]).reshape(2,1)
senario = 27
senario_prob = (1/senario)*(np.ones((senario,1)))
```

Senario generation of the demand

```
senario = given_demand.T
senario_comb = []
index = np.arange(0,3)
index_permute = product(index,repeat=3)
for i in index_permute:
    temp_array =[]
    for j in range(0,3):
        temp_array.append(float(senario[j,:][i[j]]))
    senario_comb.append(temp_array)
all_demand = np.array(senario_comb).reshape(27,3)
```

Question 1.3 Solve large scale problem combining all senarios into one problem

Large scale problem solution

```
produce = cp.Variable(shape=(2,1))
sell = cp.Variable(shape=(54,3))
salvage = cp.Variable(shape=(54,1))
produce_limit = np.array([300,300]).reshape(2,1)
ls_constraints_senario = []
```

```
for index,demand in enumerate(all demand):
    i = index*2
    ls_constraints_senario.append(cp.sum(sell[i:i+2,:],axis=1,keepdims=True) +salvage[i:i+2,
    ls constraints senario.append(cp.sum(sell[i:i+2,:],axis=0,keepdims=True) <= demand.resha
ls_constraints = [produce>=0,produce<=produce_limit,sell>= np.zeros_like(sell),salvage>= np.
ls_constraints.extend(ls_constraints_senario)
ls objective = cp.Minimize((production cost.T@produce)-(16/27)*cp.sum(sell,keepdims=True) +
ls_problem = cp.Problem(ls_objective, ls_constraints)
ls problem.solve()
→ -1609.999997418313
print("----Large Scale formulation results----")
print("Optimal Production plan ", produce.value)
print("Optimal Value of the Problem", ls problem.value)
→ ----Large Scale formulation results----
     Optimal Production plan [[120.00000002]
      [299.9999999]]
     Optimal Value of the Problem -1609.9999997418313
```

Expected value of demand

```
expected_demand = np.mean(all_demand,axis=0)

produce = cp.Variable(shape=(2,1))
sell = cp.Variable(shape=(2,3))
salvage = cp.Variable(shape=(2,1))
produce_limit = np.array([300,300]).reshape(2,1)

ed_constraints_senario = []
ed_constraints_senario.append(cp.sum(sell,axis=1,keepdims=True) +salvage <= produce)
ed_constraints_senario.append(cp.sum(sell,axis=0,keepdims=True) <= expected_demand.reshape(1)

ed_constraints = [produce>=0,produce<=produce_limit,sell>= np.zeros_like(sell),salvage>= np.
ed_constraints.extend(ed_constraints_senario)

ed_objective = cp.Minimize((production_cost.T@produce)-(16)*cp.sum(sell,keepdims=True) + (1)
ed_problem = cp.Problem(ed_objective, ed_constraints)
ed_problem.solve()
```

Q-1.4

Solving problem treating each demand individually

```
produce over scenario = []
objective_over_scenario = []
for demand in all_demand:
    produce = cp.Variable(shape=(2,1))
    sell = cp.Variable(shape=(2,3))
    salvage = cp.Variable(shape=(2,1))
    produce limit = np.array([300,300]).reshape(2,1)
    constraints_senario = []
    constraints_senario.append(cp.sum(sell,axis=1,keepdims=True) +salvage <= produce)</pre>
    constraints_senario.append(cp.sum(sell,axis=0,keepdims=True) <= demand.reshape(1,-1))</pre>
    constraints = [produce>=0,produce<=produce_limit,sell>= np.zeros_like(sell),salvage>= np.zeros_like(sell)
    constraints.extend(constraints_senario)
    objective = cp.Minimize((production_cost.T@produce)-(16)*cp.sum(sell,keepdims=True) + (1
    problem = cp.Problem(objective, constraints)
    problem.solve()
    produce_over_scenario.append(produce.value)
    objective_over_scenario.append(problem.value)
```

Calculating value of perfect information

```
produce_over_scenario = np.array(produce_over_scenario).reshape(27,2)
objective_over_scenario = np.array(objective_over_scenario).reshape(27,1)
value_of_perfect_info = ls_problem.value - np.mean(objective_over_scenario)
print("Value of value of perfect information ",value_of_perfect_info)
→ Value of value of perfect information 159.9999967386409
```

Q 1.5

Solve the scenario formulation with nonanticipativity constraints.

```
produce = cp.Variable(shape=(2,27))
    sell = cp.Variable(shape=(54,3))
    salvage = cp.Variable(shape=(54,1))
    produce_limit = (np.array([300,300]).reshape(2,1))
    produce_limit_ext = np.repeat([produce_limit],27,axis=0).reshape(2,27)
    na_constraints = []
    # Nonanticipativity constraints
    for index,demand in enumerate(all demand):
        na_constraints.append(cp.reshape(produce[:,index],shape=(2,1))==(1/27)*cp.sum(produce,ax)
    for index,demand in enumerate(all_demand):
        i = index*2
        na_constraints.append(cp.sum(sell[i:i+2,:],axis=1,keepdims=True) +salvage[i:i+2,:] <= cr</pre>
        na_constraints.append(cp.sum(sell[i:i+2,:],axis=0,keepdims=True) <= demand.reshape(1,-1)</pre>
    constraints = [produce>=0,produce<=produce_limit,sell>= np.zeros_like(sell),salvage>= np.zer
    na_constraints.extend(constraints)
    na_{objective} = cp.Minimize((1/27)*cp.sum(production_cost.T@produce)-(16/27)*cp.sum(sell,keep.sum(sell))
    na_problem = cp.Problem(na_objective, na_constraints)
    na_problem.solve()
    → -1609.9999999266336
    print("---- Results using nonanticipativity ----")
    print("\nOptimal Production plan using",produce.value)
https://colab.research.google.com/drive/1MvKIKLC_J8BR9rSyAlhJ_VbcBXRu1yK9#scrollTo=5cguQ-H-tUJA&printMode=true
```

Q-1.6

Solve the problem by the cutting plane method in the basic version (Benders decomposition)

```
def solve_second_stage_problem(produce,demand,shipping_cost):
    sell = cp.Variable(shape=(2,3))
    salvage = cp.Variable(shape=(2,1))

    objective = cp.Minimize(-16*cp.sum(sell,keepdims=True) + cp.trace((((shipping_cost@(sell constraints = [cp.sum(sell,axis=1,keepdims=True) + salvage <= produce,cp.sum(sell,axis=0, problem = cp.Problem(objective, constraints)
    problem.solve()
    return problem

def solve_master_problem(produce,produce_limit,g_ks,alpha_ks):
    production_cost = np.array([11,10]).reshape(2,1)
    produce = cp.Variable(shape=(2,1),name="produce")
    v = cp.Variable(shape=(1,1),name="value")
    constraints = []
    for i in range(0,len(g_ks)):</pre>
```

```
constraints.append(np.array(g_ks[i]).T@produce+np.array(alpha_ks[i])<=v)</pre>
    constraints.extend([produce>=0,v>=-100000,produce<=produce_limit])</pre>
    objective = cp.Minimize(production_cost.T@produce + v)
    problem = cp.Problem(objective, constraints)
    problem.solve()
    return problem
produce = np.array([100,200]).reshape(2,1) # Initial Guess
g ks = []
alpha_ks = []
objctive values = [np.nan]
epsilon = 10**(-4)
iter = 0
while True:
    # Solve Second stage problem for each demand and store its duals and objective values
    duals = []
    objs= []
    for demand in all demand:
        second_stage_sol = solve_second_stage_problem(produce,demand,shipping_cost)
        temp_dual = second_stage_sol.constraints[0].dual_value
                                                                  # Take the duals of 1st cor
        temp_obj = second_stage_sol.value
                                                                  # Take the objective value
        # Store duals and objective values for each senario
        duals.append(temp dual)
        objs.append(temp_obj)
    # Reshaping the values
    duals = np.array(duals).reshape(-1,2)
    objs = np.array(objs).reshape(-1,1)
    g_ks_temp = (-senario_prob.T@duals).T
    alpha_ks_temp = senario_prob.T@objs - g_ks_temp.T@produce
    g_ks.append(g_ks_temp)
    alpha_ks.append(alpha_ks_temp)
    first_stage_sol = solve_master_problem(produce,produce_limit,g_ks,alpha_ks)
    obj value = first stage sol.value
    new_produce = first_stage_sol.var_dict["produce"].value
    new_limit = first_stage_sol.var_dict["value"].value
```

```
if np.abs(obj_value - objctive_values[-1])<= epsilon:</pre>
      print("Terminating condition satisfied !")
      break
   else:
      pass
   objctive_values.append(obj_value)
   produce,limit = new_produce,new_limit # swap the values
   iter = iter+1
   print(f"\n-----")
   print(f"\nproduction is {produce}")
   print(f"\nobjctive value is {first_stage_sol.value}\n")
\rightarrow
    ------Iteration no. 1-----
    production is [[300.00000004]
     [299.99999992]]
    objctive value is -2351.895943550797
    -----Iteration no. 2-----
    production is [[149.00805118]
     [299.9999992]]
    objctive value is -1784.2447749212179
    -----Iteration no. 3-----
    production is [[112.70470909]
     [300.00000003]]
    objctive value is -1647.7631011106232
    -----Iteration no. 4-----
    production is [[125.23365091]
     [299.99999495]]
    objctive value is -1618.5289057328064
    -----Iteration no. 5-----
    production is [[119.99999869]
     [299.9999991]]
    objctive value is -1609.9999959895367
```

```
Terminating condition satisfied !
```

```
print("---- Results using Bender Decompostion ----")
print(f"\nproduction is {produce}")
print(f"\nobjctive value is {first_stage_sol.value}\n")

---- Results using Bender Decompostion ----
production is [[119.9999869]
      [299.9999991]]

objctive value is -1609.9999957406962
```

Q-1.7 (Solve the problem by the multicut method)

```
def solve_master_problem_ml(produce,g_ks,alpha_ks,senario_prob,production_cost,produce_limit
    produce = cp.Variable(shape=(2,1),name="produce")
    v = cp.Variable(shape=(len(senario prob),1),name="value")
    constraints = []
    for i in range(0,len(g ks)):
        for j in range(0,len(g_ks[i])):
            constraints.append(np.array([g_ks[i][j]])@produce+np.array([alpha_ks[i][j]])<=v[</pre>
    constraints.extend([produce>=0,v>=-100000,produce<=produce_limit])</pre>
    objective = cp.Minimize(production_cost.T@produce + senario_prob.T@v)
    problem = cp.Problem(objective, constraints)
    problem.solve()
    return problem
g_ks = []
alpha_ks = []
senario = 27
objctive_values = [np.nan]
epsilon = 10**(-4)
iter = 0
while True:
```

Solve Second stage problem for each demand and store its duals and objective values

```
duals = []
   objs= []
   for demand in all_demand:
       second_stage_sol = solve_second_stage_problem(produce,demand,shipping_cost)
       temp dual = second_stage_sol.constraints[0].dual_value
                                                              # Take the duals of 1st cor
       temp_obj = second_stage_sol.value
                                                              # Take the objective value
       # Store duals and objective values for each senario
       duals.append(temp dual)
       objs.append(temp obj)
    # Reshaping the values
   duals = np.array(duals).reshape(-1,2)
   objs = np.array(objs).reshape(-1,1)
   gks batch = []
   alpha ks batch = []
   for i in range(0, senario):
       gks_batch.append(-duals[i])
       alpha_ks_batch.append(objs[i]+duals[i].T@produce)
   g_ks.append(gks_batch)
   alpha ks.append(alpha ks batch)
   first_stage_sol = solve_master_problem_ml(produce,g_ks,alpha_ks,senario_prob,production_
   obj value = first stage sol.value
   new_produce = first_stage_sol.var_dict["produce"].value
   new limit = first stage sol.var dict["value"].value
   if np.abs(obj value - objctive values[-1])<= epsilon:
       print("Terminating condition satisfied !")
       break
   else:
       pass
   objctive_values.append(obj_value)
   produce,limit = new produce,new limit # swap the values
   iter = iter+1
   print(f"\n-----")
   print(f"\nproduction is {produce}")
   print(f"\nobjctive value is {first stage sol.value}\n")
→
     ------Iteration no. 1-----
    production is [[299.9999989]
```

```
[299.9999999]]
     objctive value is -1727.7034315843757
     -----Iteration no. 2-----
     production is [[120.00000283]
      [299.9999952]]
     objctive value is -1609.9999916085671
     Terminating condition satisfied !
print("---- Results using Multicut Method----")
print(f"\nproduction is {produce}")
print(f"\nobjctive value is {first_stage_sol.value}\n")
---- Results using Multicut Method----
     production is [[120.00000172]
      [299.9999982]]
     objctive value is -1609.9999916636561
                                    + Code
                                               + Text
Start coding or generate with AI.
```

https://colab.research.google.com/drive/1MvKlKLC_J8BR9rSyAlhJ_VbcBXRu1yK9#scrollTo=5cguQ-H-tUJA&printMode=true