



### Research Topic (3)

#### Title: Constant-Harvest Model

Write research on:

Ordinary Differential Equations "ODE" is a tool to model different engineering, physical and biological systems. Let's apply one of these methods to solve a very important problem in the field of **population of fishery**.

**Constant-Harvest Model.** A model that describes the population of a fishery "P" in which harvesting takes place at a constant rate "H" is given by

$$\frac{dP}{dt} = kP - h,$$

where k and h are positive constants. This equation is called Constant-Harvest Model.

The research should include:

- 1- Introduction about Ordinary differential equation.
- 2- List essential equations to solve initial value problem using Laplace transform
- 3- Discuss the constant –Harvest Model and explain the meaning of each term in the equation.
- 4- Solve the Constant-Harvest Model, Solve the DE subject to  $P(0) = P_0$
- 5- Describe the behavior of the population  $P(t)$  for increasing time in the three cases:
  - A)  $P(0) > h/k$
  - B)  $P(0) = h/k$
  - C)  $P(0) < h/k$
- 6- Use results from part **B** to determine whether the fish population will ever go to extinct in finite time, that is, whether there exists a time  $T > 0$  such that  $P(T) = 0$ . If the population goes to extinct, then find T.
- 7- Graph  $P(t)$  versus time t. Your graph must show the three cases mentioned in question number 5.
- 8- Conclusion
- 9- References

**NB:**

The form of the research should follow the following rules:

- a. Writing using Microsoft Word.
- b. using Time New Roman font.
- c. 14 Font size for text and 16 Bold for the title.
- d. single space between the lines.
- e. Page margins are 2.5 cm from top, bottom, right and left.
- f. The number of pages is not less than 5 or The number of words is not less than 400.
- h. English language formulation should be correct and sound.
- i. Clarity of texts, pictures or drawings.

*With My Best Wishes,  
Prof. Ali Elnaem.  
Dr. M. Abdel-Aziz*