Task name: Majority element

Task number: 2

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Non-recursive algorithm

pseudocode

```
function find_majority_element(arr, n):
    count[n]
    for i = 0 to n-1 do
        count[i] = 0
    majority = -1
    max_count = 0
    for i = 0 to n-1 do
        count[arr[i]] = count[arr[i]] + 1
        if count[arr[i]] > max_count then
            majority = arr[i]
            max_count = count[arr[i]]
    if max_count > n/2 then
        return majority
    else:
        return -1

function main():
    arr = [3, 3, 4, 2, 4, 4, 2, 4, 4]
    n = size of arr
    majority_element = find_majority_element(arr, n)
    if majority_element != -1 then
        print "The majority element is ", majority_element
    else:
        print "There is no majority element in the array"
    return 0
```

Analysis

1. `int count[n];` - Time complexity is O(1)

2. `for (int i = 0; i < n; i++) { count[i] = 0; }` - Time complexity is O(n)

3. `int majority = -1;` - Time complexity is O(1)

4. `int max_count = 0;` - Time complexity is O(1)

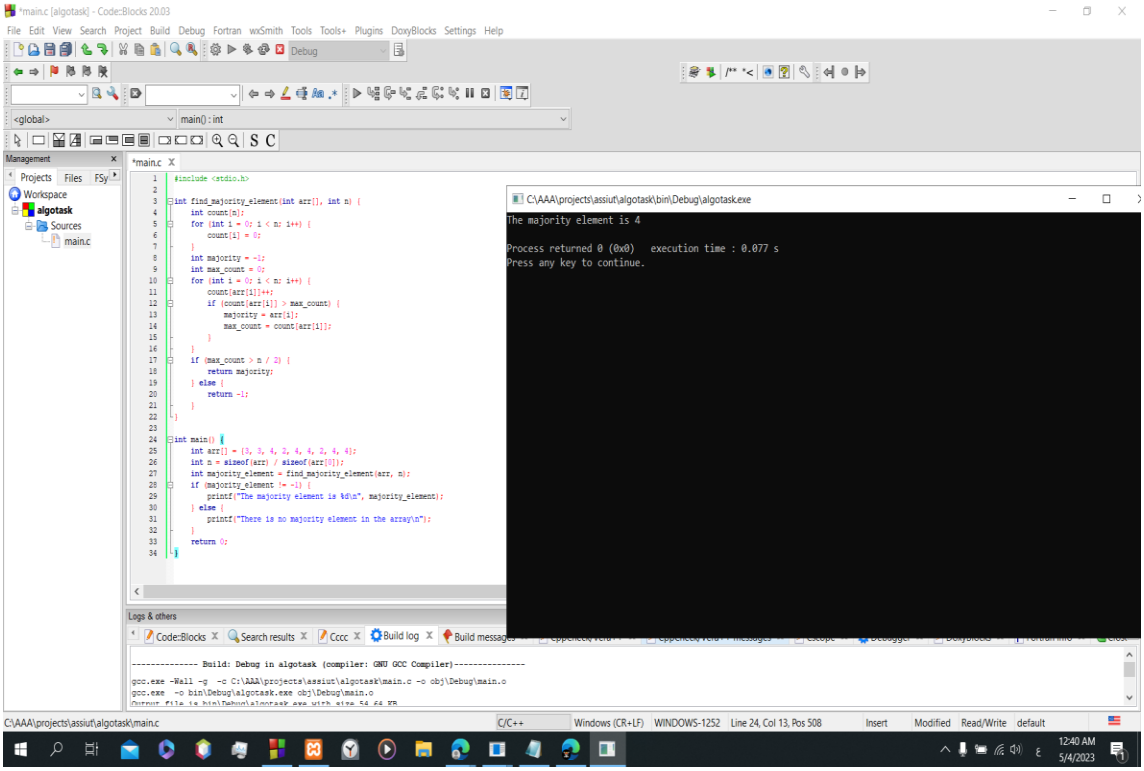
5. `for (int i = 0; i < n; i++) { count[arr[i]]++; ... }` - Time complexity is O(n)

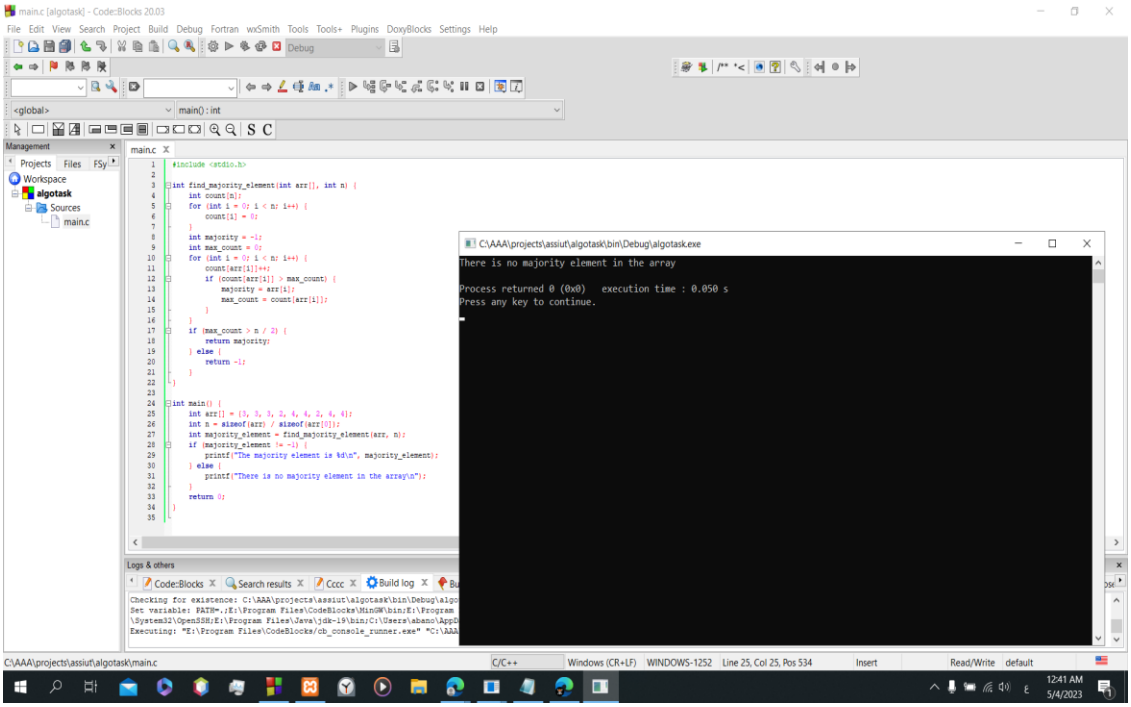
6. `if (count[arr[i]] > max_count) { majority = arr[i]; max_count = count[arr[i]]; }` - Time complexity is O(1)

7. `if (max_count > n / 2) { return majority; } else { return -1; }` - Time complexity is O(1)

The time complexity of the `find_majority_element` function is O(n)

Output


*main.c [algotask] - Code::Blocks 20.03
C:\AAA\projects\assiut\algotask\bin\Debug\algotask.exe
The majority element is 4
Process returned 0 (0x0) execution time : 0.077 s
Press any key to continue.


main.c [algotask] - Code::Blocks 20.03
C:\AAA\projects\assiut\algotask\bin\Debug\algotask.exe
There is no majority element in the array
Process returned 0 (0x0) execution time : 0.050 s
Press any key to continue.

Recursive algorithm

Pseudocode

```
FUNCTION findMajorityElement(array[], size)
   IF size equals 1 THEN(
      RETURN array[0]
    )
   SET mid to size divided by 2
   SET leftMajority to findMajorityElement(array, mid)
   SET rightMajority to findMajorityElement(array + mid, size - mid)
   IF leftMajority equals rightMajority THEN(
      RETURN leftMajority
)
   SET leftCount to 0
   SET rightCount to 0
   FOR i from 0 to size-1 DO(
      IF array[i] equals leftMajority THEN
         INCREMENT leftCount by 1
      ELSEIF array[i] equals rightMajority THEN
         INCREMENT rightCount by 1

  )
   IF leftCount is greater than size divided by 2 THEN
      RETURN leftMajority
   ELSEIF rightCount is greater than size divided by 2 THEN
      RETURN rightMajority
   ELSE
      RETURN -1
END FUNCTION
```

main()

DECLARE arr as an array of integers with values {3, 3, 4, 2, 4, 4, 2, 4, 4}

DECLARE size as the length of arr divided by the length of the first element of arr

SET majorityElement to the result of calling findMajorityElement with arguments arr and size

PRINT "The majority element of the array is: " concatenated with majorityElement

Analysis

1. `if (size == 1) { return array[0]; }` - Time complexity is O(1).

2. `int mid = size / 2;` - Time complexity is O(1)

3. `int leftMajority = findMajorityElement(array, mid);` - Time complexity is T(n/2), where T is the time complexity of the function and n is the size of the array.

4. `int rightMajority = findMajorityElement(array + mid, size - mid);` - Time complexity is T(n/2), where T is the time complexity of the function and n is the size of the array

5. `if (leftMajority == rightMajority) { return leftMajority; }` - Time complexity is O(1).

6. `int leftCount = 0, rightCount = 0;` - Time complexity is O(1).

7. `for (int i = 0; i < size; i++) { ... }` - Time complexity is O(n).

8. `if (leftCount > size/2) { return leftMajority; }` - Time complexity is O(1).

9. `else if (rightCount > size/2) { return rightMajority; }` - Time complexity is O(1).

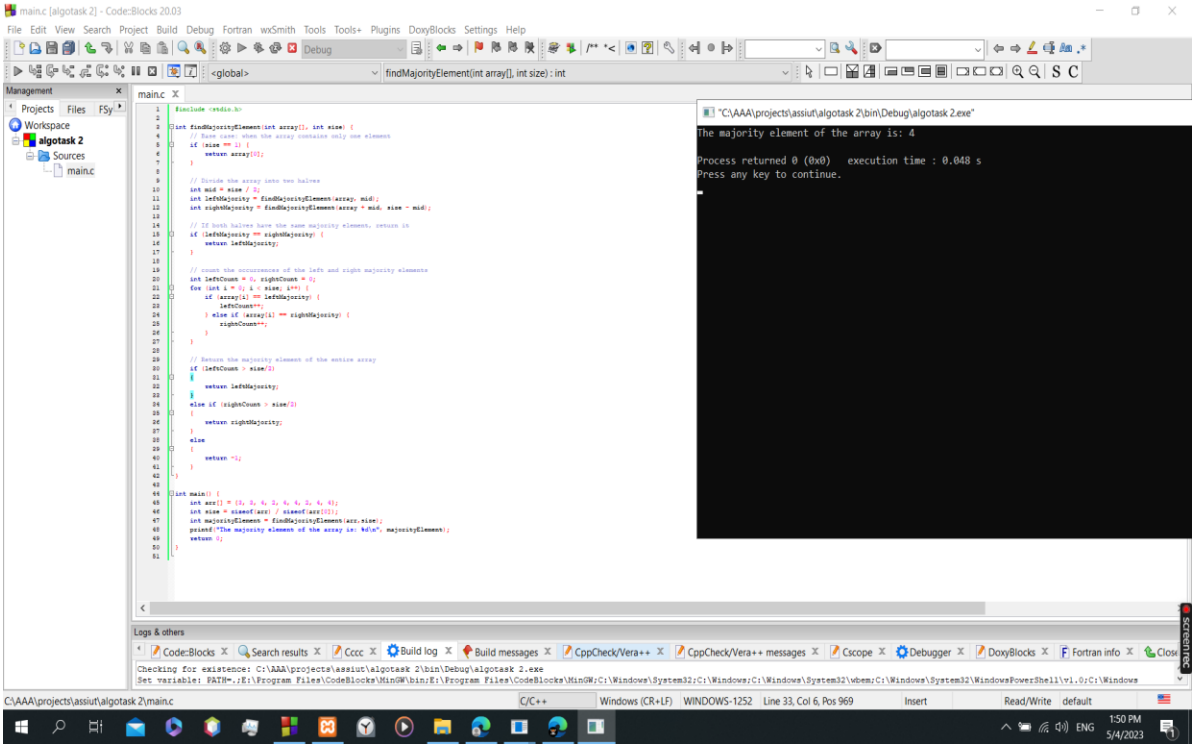
10. `else { return -1; }` - Time complexity is O(1).

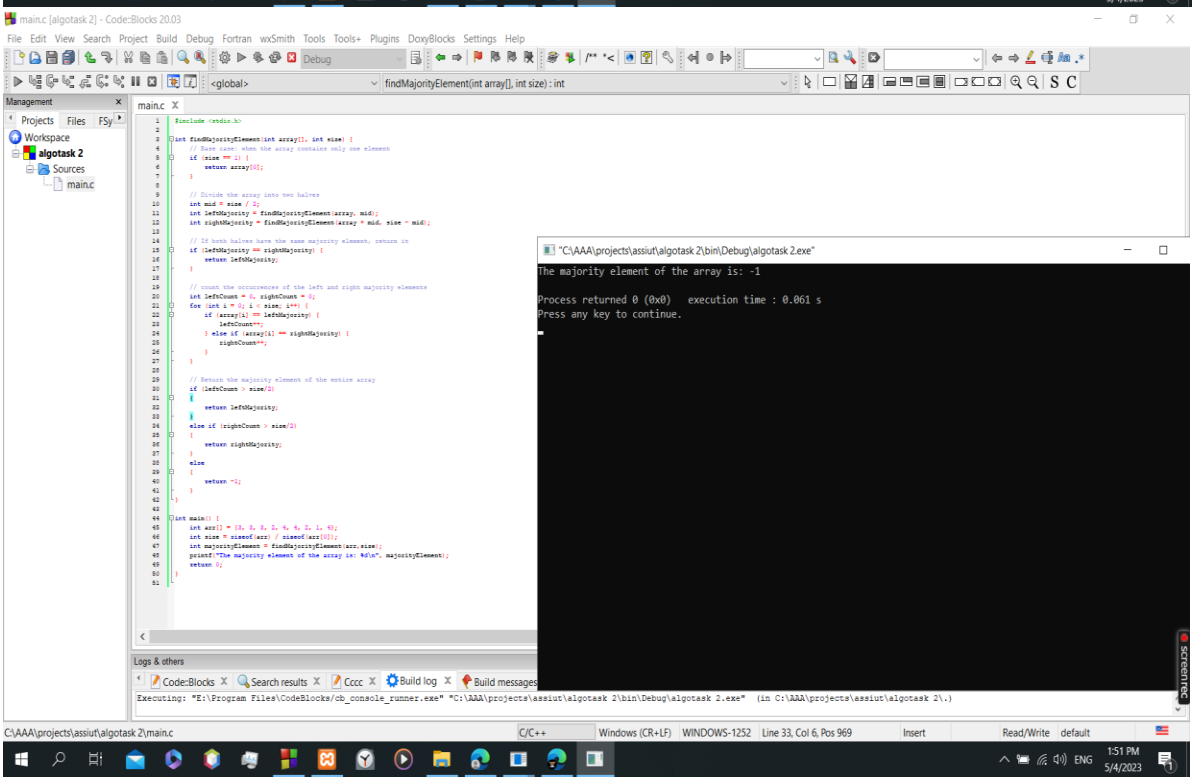
the time complexity of the `findMajorityElement` function:

is O(n log n) in the worst case, where n is the size of the array.

is O(n) in the best case.

Output


"C:\AAA\projects\assiut\algotask 2\bin\Debug\algotask 2.exe"
The majority element of the array is: 4
Process returned 0 (0x0) execution time : 0.048 s
Press any key to continue.


"C:\AAA\projects\assiut\algotask 2\bin\Debug\algotask 2.exe"
The majority element of the array is: -1
Process returned 0 (0x0) execution time : 0.061 s
Press any key to continue.

Comparison

Here's a comparison table between the two codes:

	Non recursive algorithm	Recursive algorithm
Time Complexity	O(n)	O(n log n)
Best Case	O(n)	O(1)
Worst Case	O(n^2)	O(n log n)
Average Case	O(n^2)	O(n log n)
Space Complexity	O(n)	O(log n)
Strengths	Works well for uniformly distributed data	Works well for arbitrary data
Weaknesses	can be a problem for very large input sizes.	May take longer on average

Overall, recursive algorithm is better in terms of performance but requires more space due to the recursive calls. Non recursive algorithm is simpler and easier to read but has poor performance.