

# CS341

# Artificial Intelligence

## Lecture 6

---

**DR. HEBA MOHSEN**

# Heuristic Search

---

- On the average they improve the quality of the paths that are explored.
- Using Heuristics, we can hope to get good ( though possibly non-optimal ) solutions
- There are good general purpose heuristics that are useful in a wide variety of problem domains.
- Special purpose heuristics exploit domain specific knowledge
- Heuristic search uses **Heuristic Function**: This is a function that maps from problem state descriptions to measures of desirability, usually represented as numbers.

# Best-first search

---

Idea: use an **evaluation function**  $f(n)$  for each node

- $f(n)$  provides an estimate for the total cost.
- Expand the node  $n$  with smallest  $f(n)$ .

Implementation:

Order the nodes in fringe increasing order of cost.

Special cases:

- greedy best-first search
- $A^*$  search

# Heuristics for 8-puzzle

---

These heuristics were obtained by relaxing constraints ...

**h1:** The number of misplaced tiles (squares with number).

**h2:** The sum of the distances of the tiles from their goal positions.

# Heuristics for 8-puzzle I

- The number of **misplaced tiles** (not including the blank)

Current  
State

1	2	3
4	5	6
7		8

Goal  
State

1	2	3
4	5	6
7	8	

In this case, only “8” is misplaced, so the heuristic function evaluates to 1.

In other words, the heuristic is *telling* us, that it *thinks* a solution might be available in just 1 more move.

1	2	3
4	5	6
7	8	8

N	N	N
N	N	N
N	Y	

Notation:  $h(n)$        $h(\text{current state}) = 1$

# Heuristics for 8-puzzle II

- The **Manhattan Distance** (not including the blank)

Current State

3	2	8
4	5	6
7	1	

Goal State

1	2	3
4	5	6
7	8	

In this case, only the “3”, “8” and “1” tiles are misplaced, by 2, 3, and 3 squares respectively, so the heuristic function evaluates to 8.

In other words, the heuristic is *telling us*, that it *thinks* a solution is available in just 8 more moves.

3	→	<u>3</u>

2 spaces

	←	8
	↓	
	<u>8</u>	

3 spaces

<u>1</u>	←	
	↑	
	1	

3 spaces

Total 8

Notation:  $h(n)$

$h(\text{current state}) = 8$

# A\* Search

(with systematic checking of repeated states)

---

## 8-Puzzle with $h_1()$

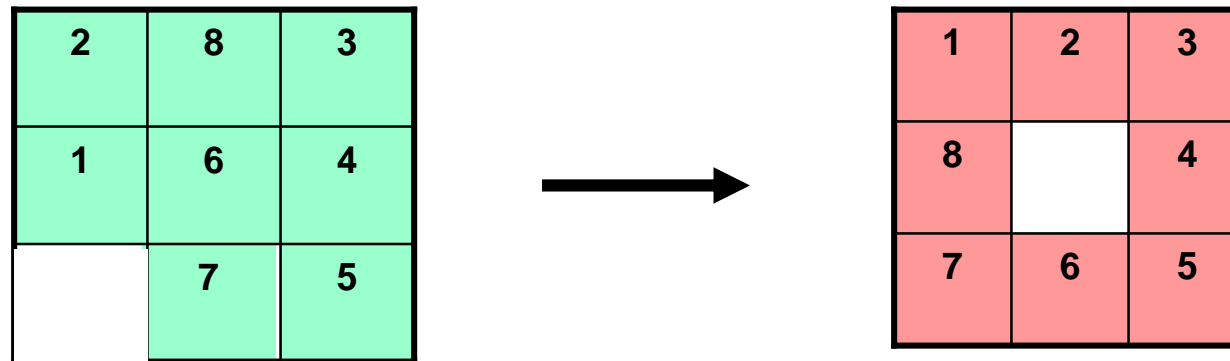
$h_1()$ : the number of misplaced tiles

# 8-Puzzle Problem

---

Solve the following 8-puzzle problem using A\* search algorithm as search strategy and the following function  $f(n)$  as heuristic:  $f(n)=g(n)+h(n)$

- $h(n)$ : the number of misplaced tiles
- $g(n)$ : the number of steps from the initial state





# A\* Search

(with systematic checking of repeated states)

---

## 8-Puzzle with h2()

h2(): Manhattan Distance

# 8-Puzzle Problem

---

Solve the following 8-puzzle problem using A\* search algorithm as search strategy and the following function  $f(n)$  as heuristic:  $f(n)=g(n)+h(n)$

- $h(n)$ : the Manhattan Distance
- $g(n)$ : the number of steps from the initial state

2	8	3
1	6	4
	7	5



1	2	3
8		4
7	6	5