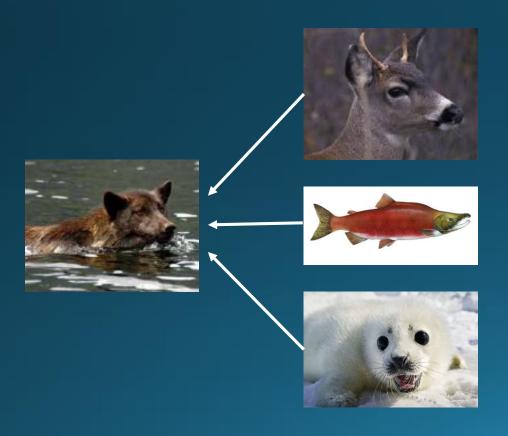
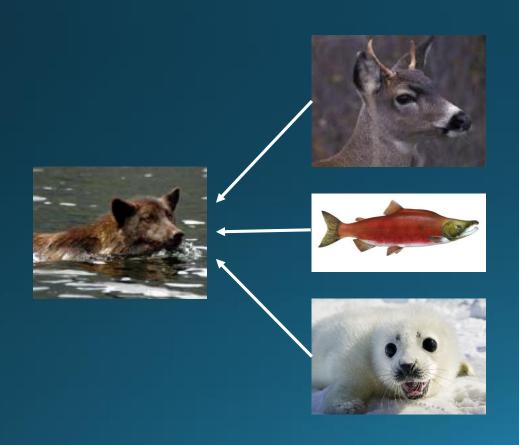
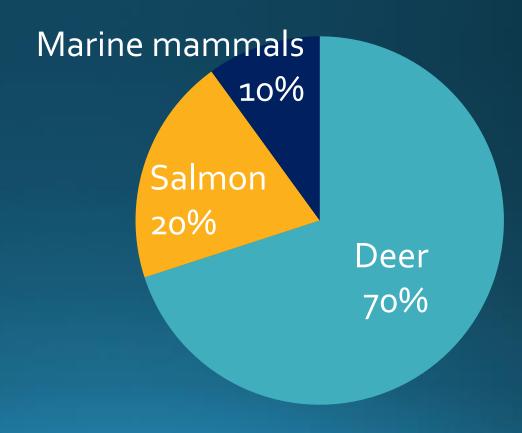
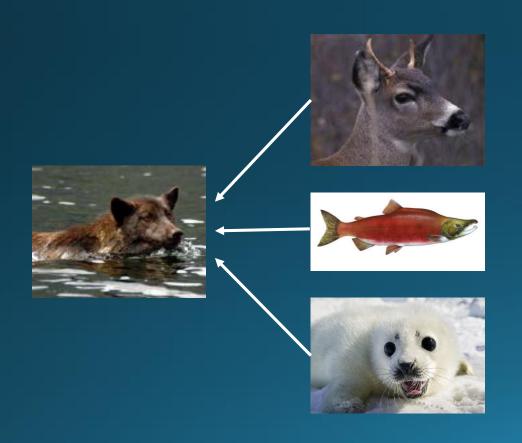
MixSIAR: Advanced stable isotope mixing models in R

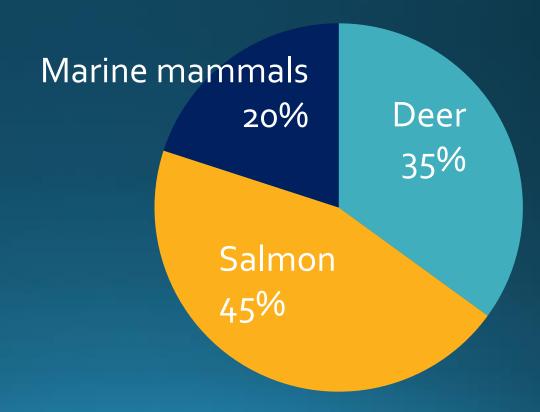
Brian Stock, Brice Semmens, Eric Ward, Jonathan Moore, Andrew Parnell, Andrew Jackson, Donald Phillips, Stuart Bearhop, Richard Inger





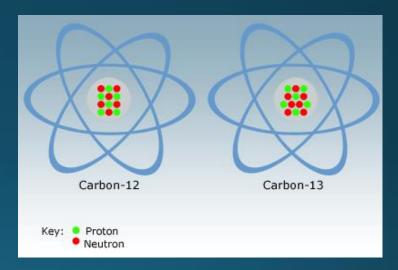






What are stable isotopes?

- Elemental variants (extra neutrons) that do not decay
 - ¹²C, ¹³C
 - ¹⁴N, ¹⁵N
 - ¹⁶O, ¹⁸O
 - 32**S**, 34**S**



What are stable isotopes?

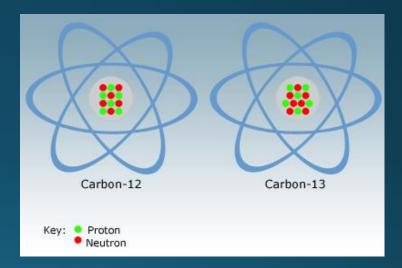
- Elemental variants (extra neutrons) that do not decay

```
• ^{12}C, ^{13}C \delta^{13}C
```

•
$$^{14}N$$
, ^{15}N $\delta^{15}N$

•
16
O, 18 O δ^{18} O

•
$$3^2$$
S, 3^4 S δ^{34} S



Why are stable isotopes useful?

Why are stable isotopes useful?

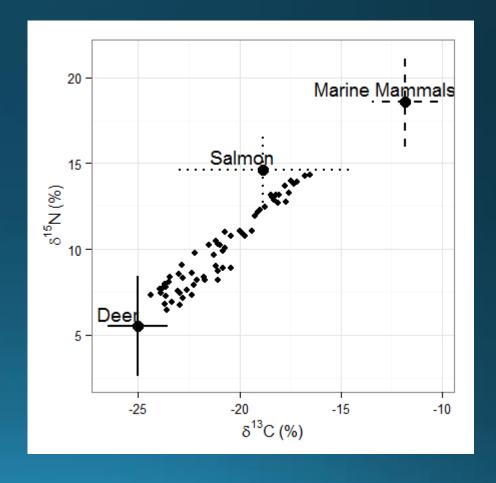
Principle #1

Variation exists

Why are stable isotopes useful?

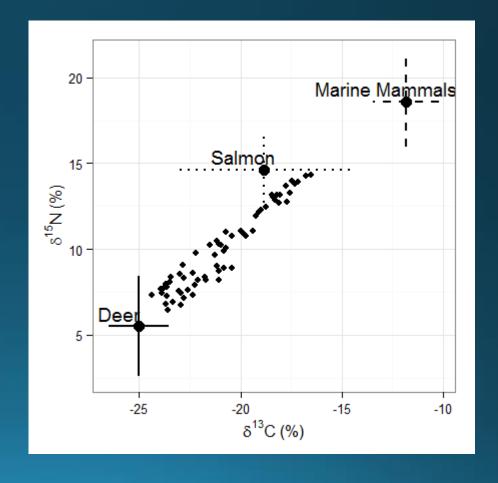
Principle #1

Variation exists



Why are stable isotopes useful?

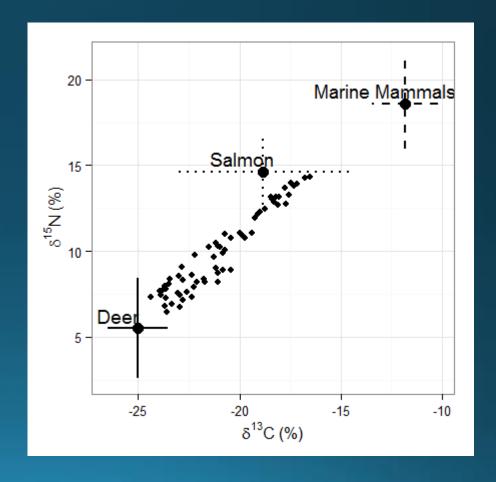
Principle #2
"You are what you eat"



Why are stable isotopes useful?

Variation exists

- + "You are what you eat"
- Closer you are to a source,the more of it you're eating



Linear mixing model:

Diet = ?



Linear mixing model:

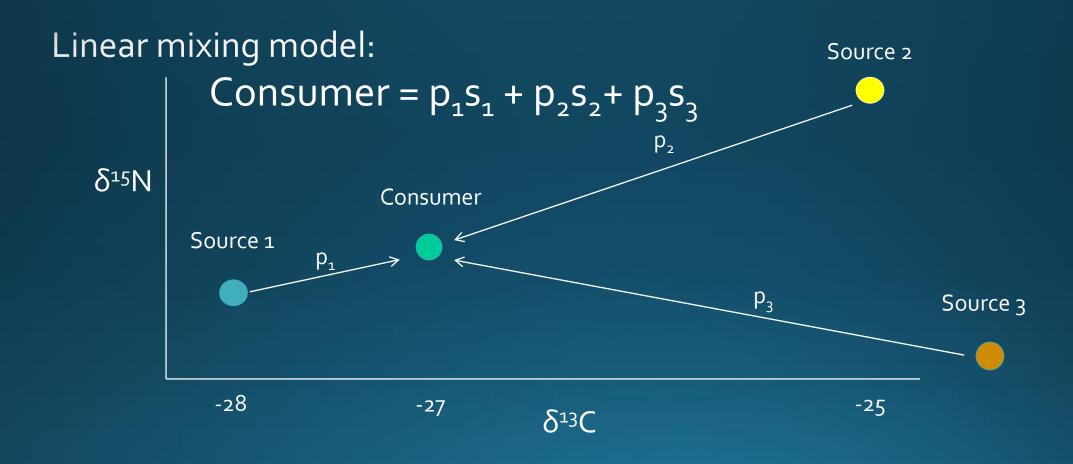
Consumer =
$$p_1 * s_1 + p_2 * s_2$$
 $(p_1 + p_2 = 1)$

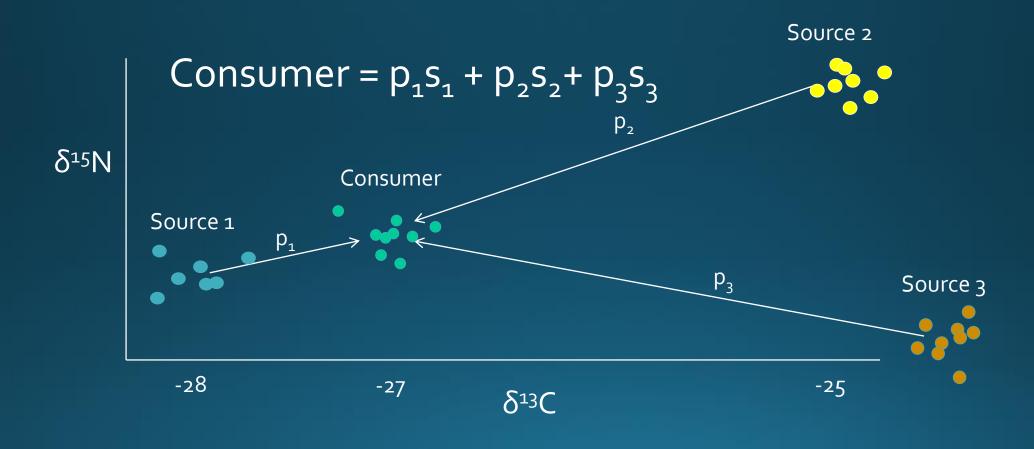


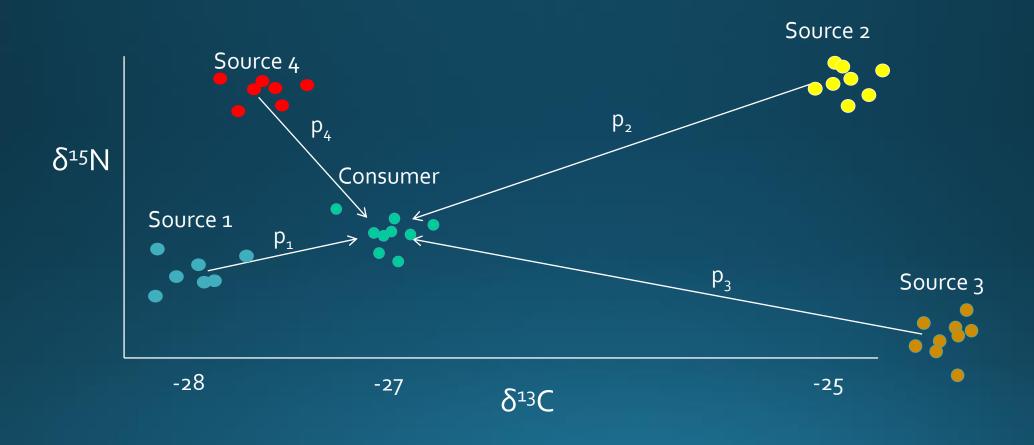
Linear mixing model:

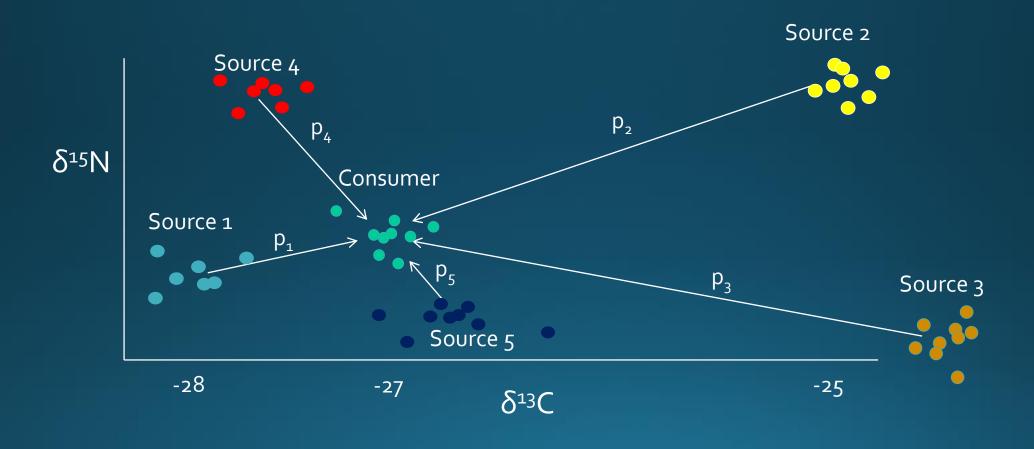
Consumer =
$$2/3 s_1 + 1/3 s_2$$











LETTER

Incorporating uncertainty and prior information into stable isotope mixing models

Moore and Semmens (2008)

MixSIR

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MixSIR

TECHNICAL COMMENT

Erroneous behaviour of MixSIR, a recently published Bayesian isotope mixing model: a discussion of Moore & Semmens (2008)

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SIAR

Semmens et al. (2009)

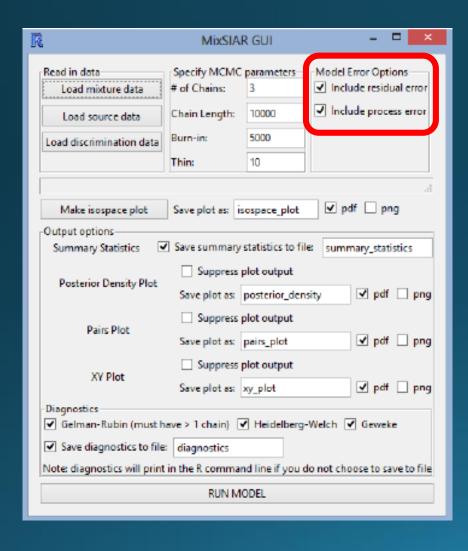




Source Partitioning Using Stable Isotopes: Coping with Too Much Variation

Andrew C. Parnell¹, Richard Inger², Stuart Bearhop², Andrew L. Jackson³*

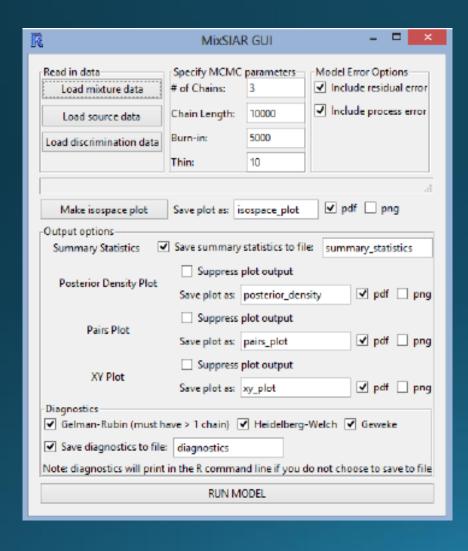
MixSIAR software



MixSIR SIAR

Written in R and JAGS (open source)
Incorporates recent advances in
mixing model methods

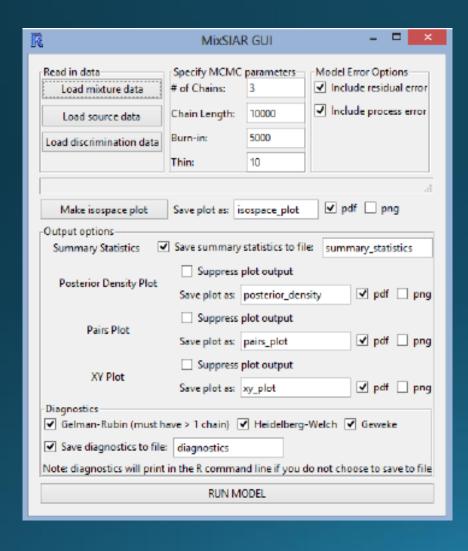
MixSIAR software



Incorporates recent advances in mixing model methods:

- Addresses variability in source and discrimination values
 - 1. Hierarchical structure
- Addresses variation in mixture populations:
 - 2. Random effects
 - 3. Fixed effects
 - 4. Continuous effects

MixSIAR software



Incorporates recent advances in mixing model methods:

- Addresses variability in source and discrimination values
 - 1. Hierarchical structure
- Addresses variation in mixture populations:
 - 2. Fixed effects
 - 3. Random effects
 - 4. Continuous effects

Source and discrimination variability

Consumer =
$$\sum_{k} p_k (s_k + c_k)$$

p - proportion of diet

s - source

c - discrimination

Source and discrimination variability

Consumer =
$$\sum_{k} p_k (s_k + c_k)$$

$$s_k \sim N(\mu_k, \omega_k^2)$$

p - proportion of diet

s - source

c - discrimination

Source and discrimination variability

Consumer =
$$\sum_{k} p_k (s_k + c_k)$$

$$s_k \sim N(\mu_k, \omega_k^2)$$

 $c_k \sim N(\lambda_k, \tau_k^2)$

p - proportion of diet

s - source

c - discrimination

Consumer variability

Previously:

p = [20%, 50%, 20% 10%]

Assumes that all consumers have the same diet

Consumer variability

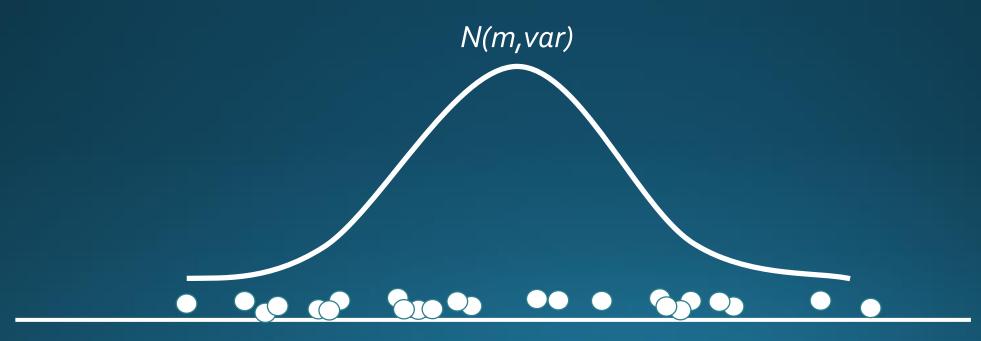
Previously:

p = [20%, 50%, 20% 10%]

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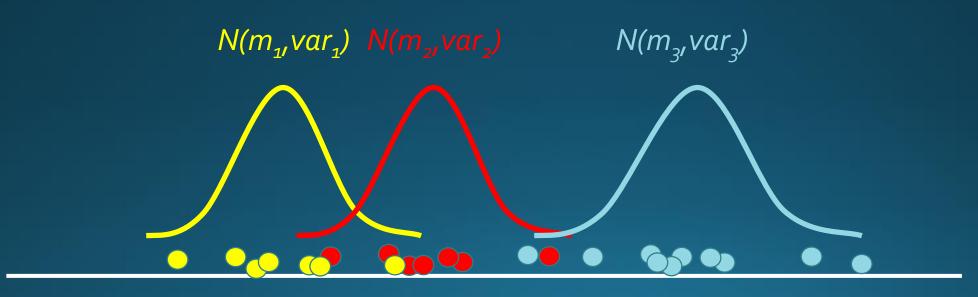
- Random effects
- Fixed effects
- Continuous effects





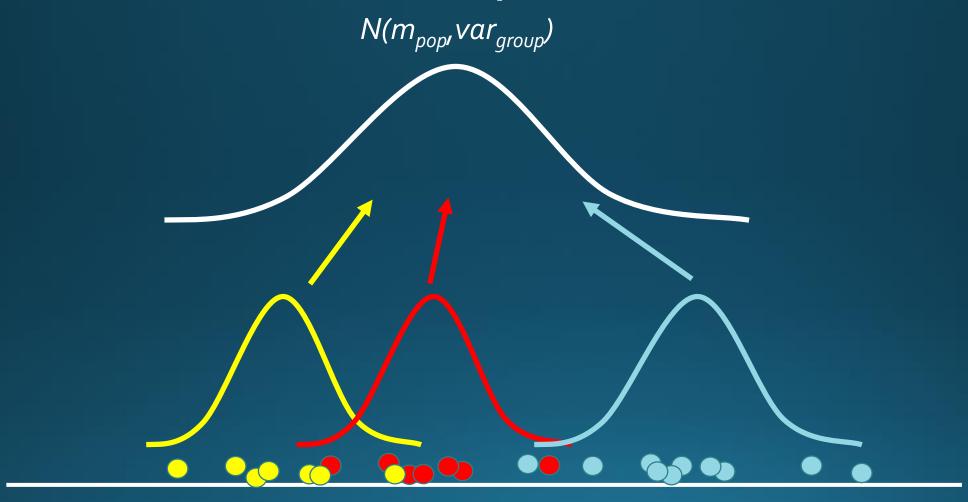
Consumer δ^{13} C



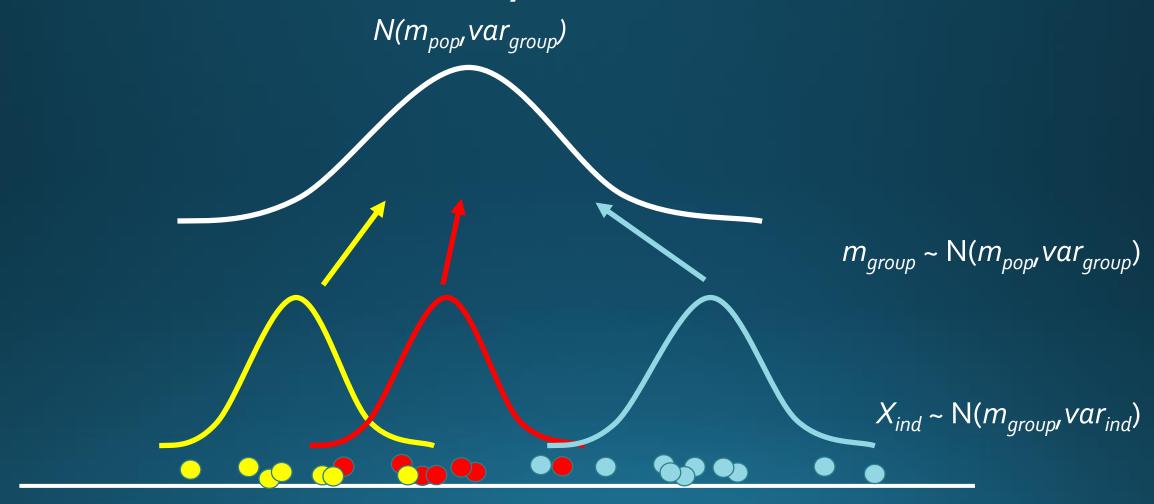


Consumer δ^{13} C

Consumer variability: random effects

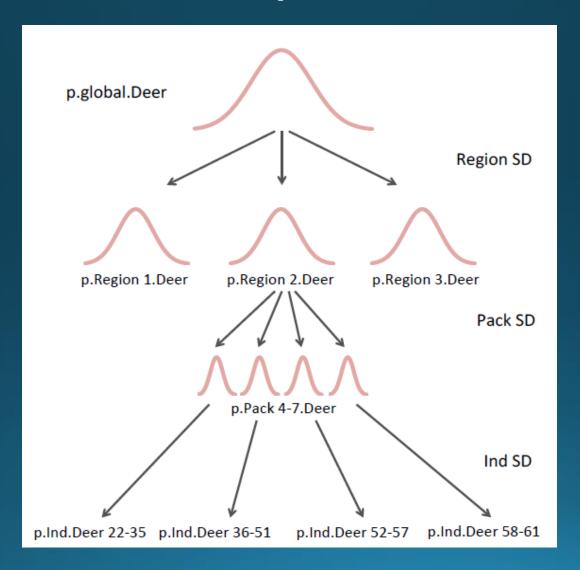


Consumer variability: random effects



Consumer δ^{13} C

Consumer variability: random effects



Consumer variability: continuous effects

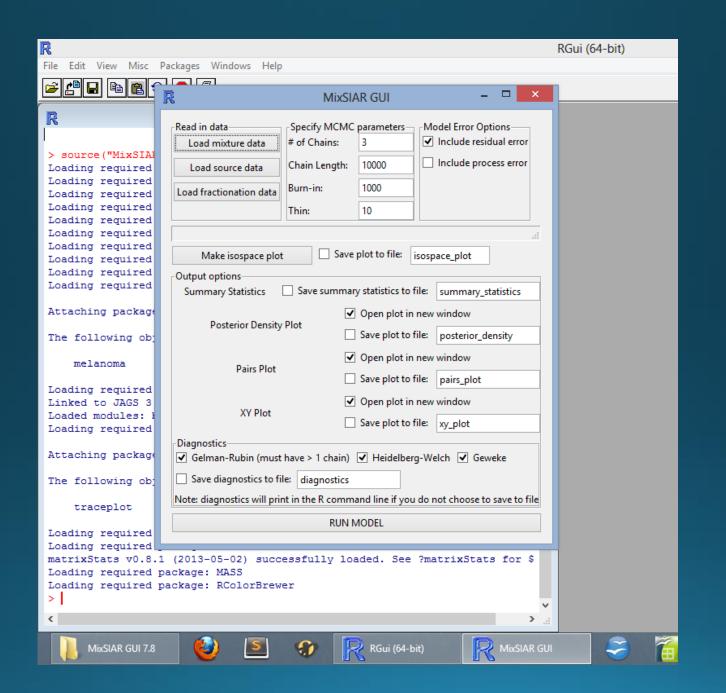


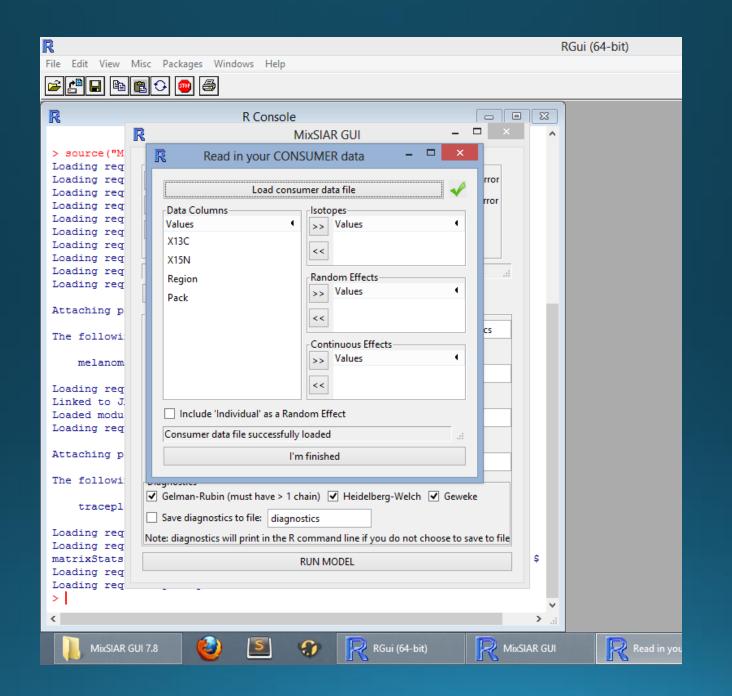
Consumer variability: continuous effects

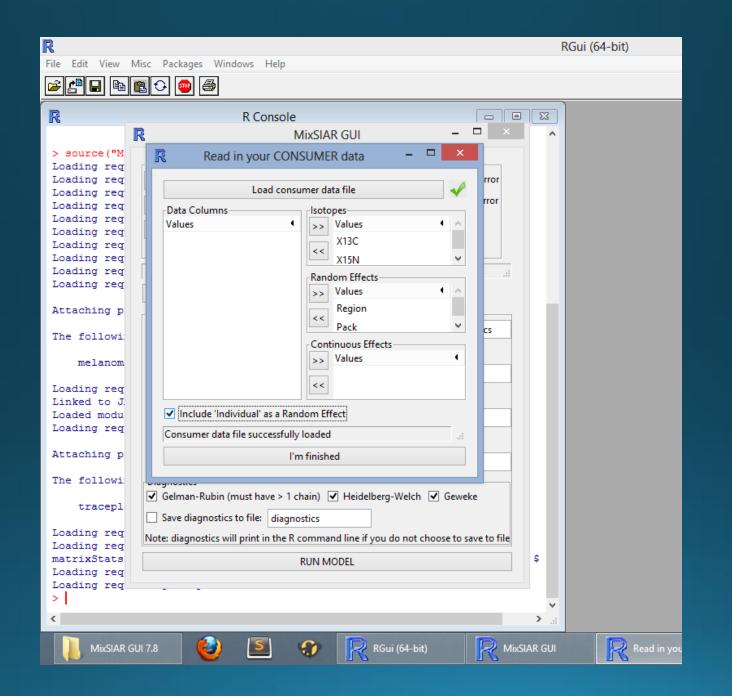


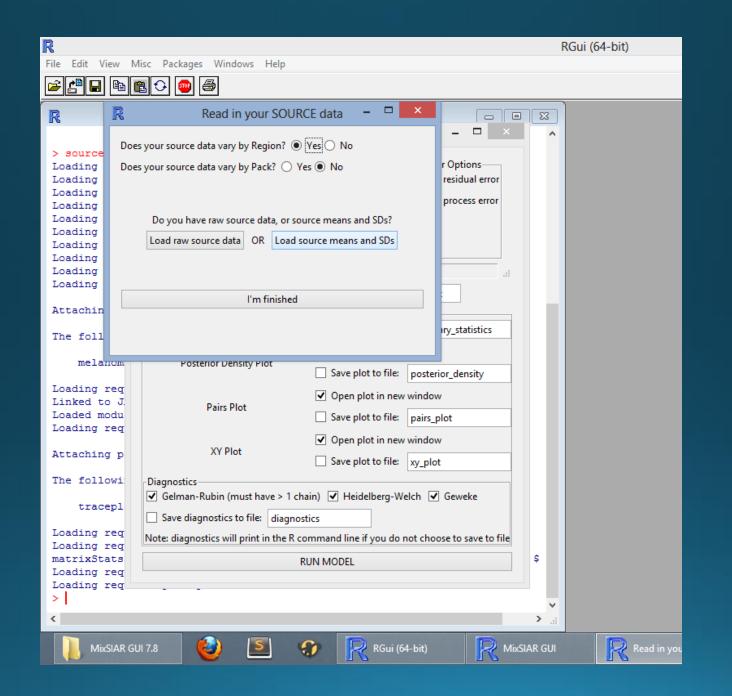
$$\delta_c = p_1 \cdot p_1 + p_2 \cdot p_2 + \dots + p_i \cdot p_i$$

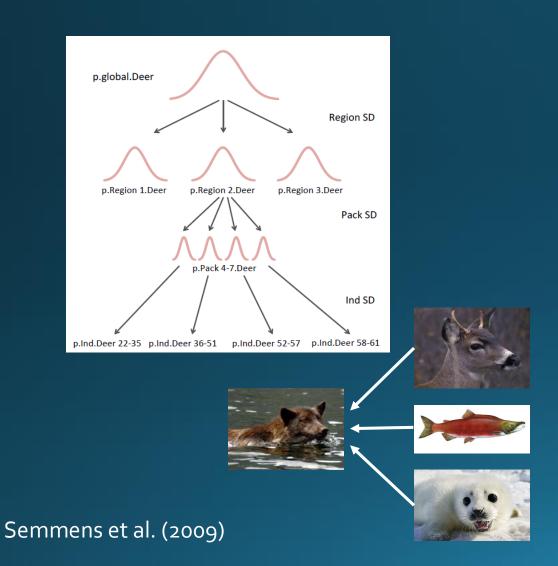
$$p_1 = B_0 + B_1 * Predictor_c$$

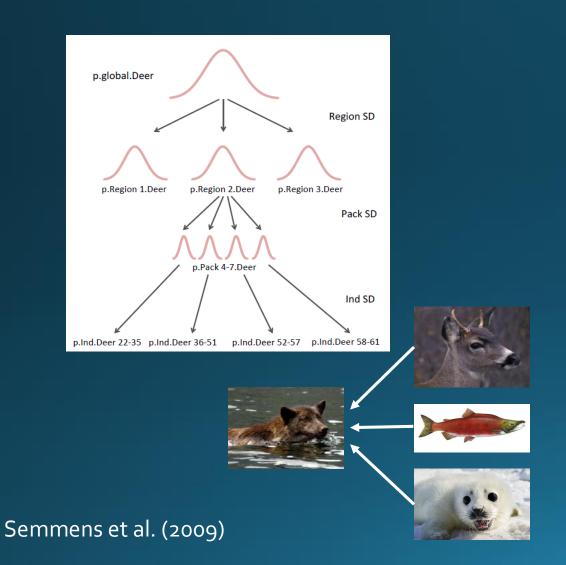


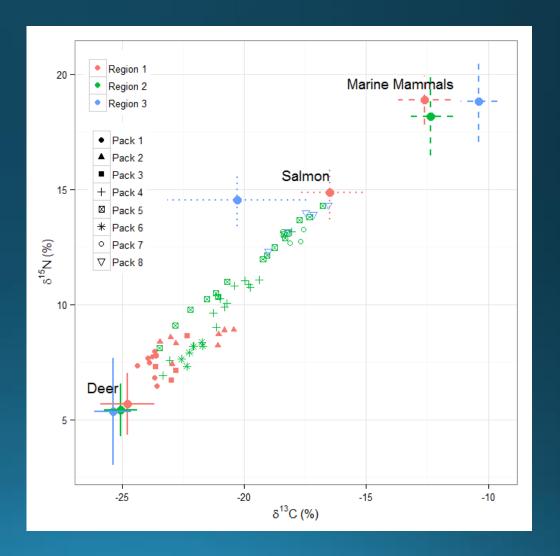


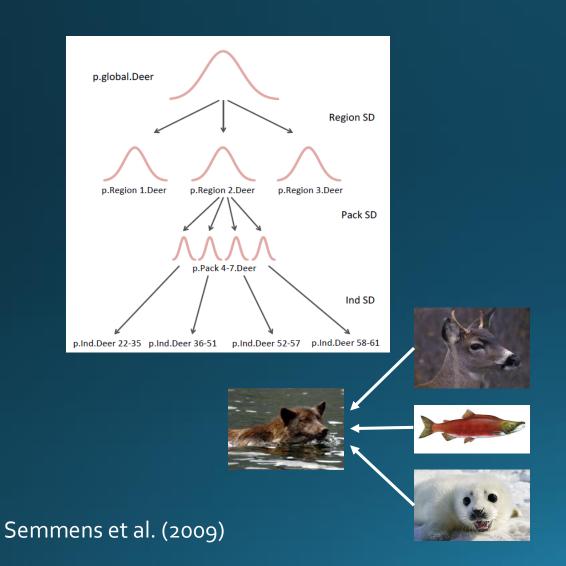


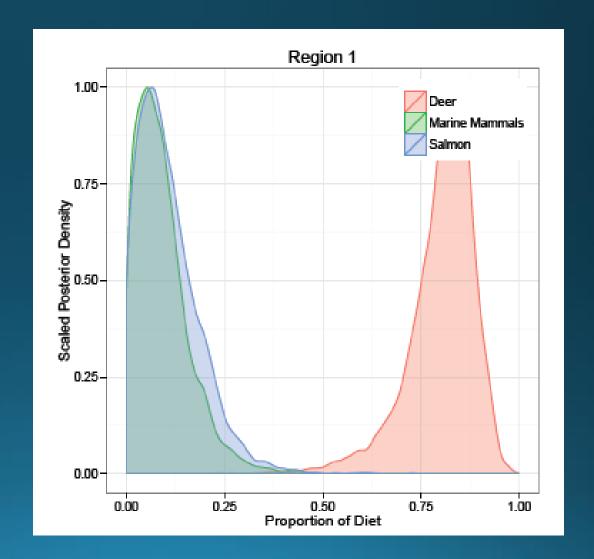


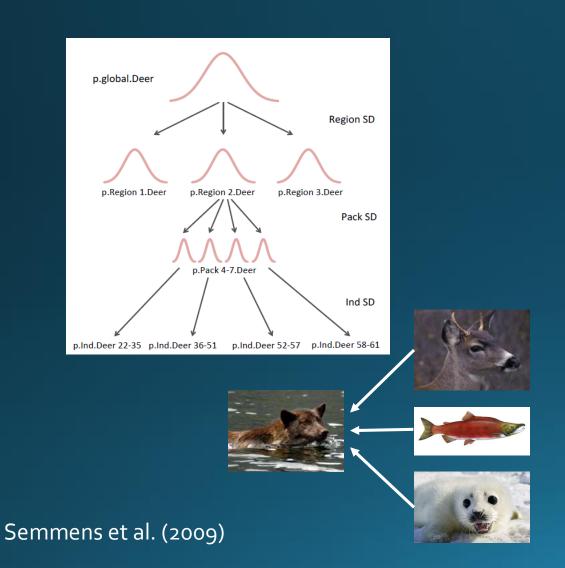


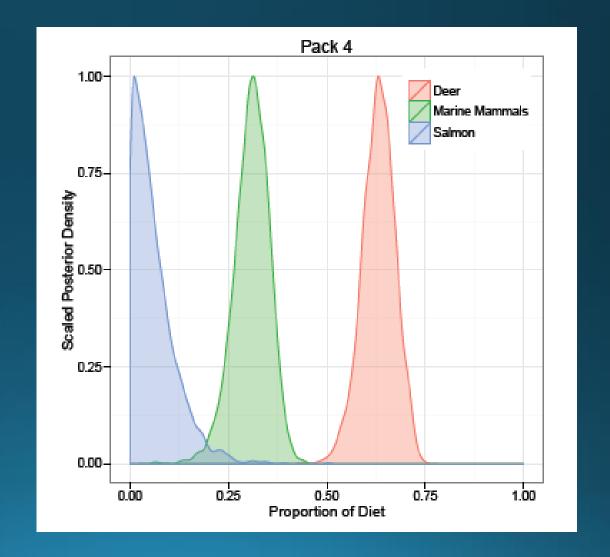


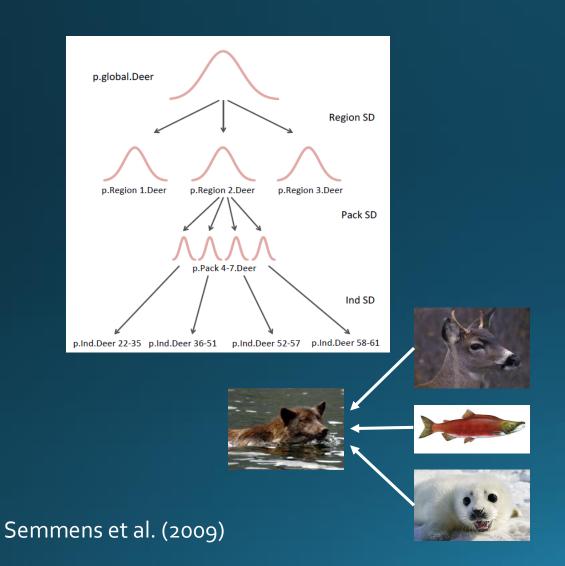


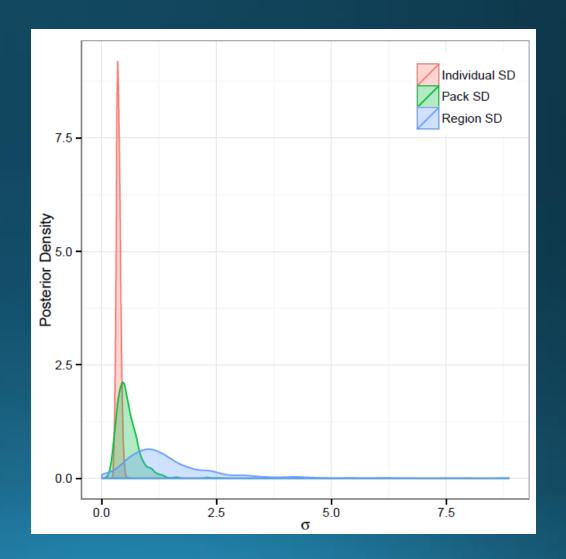




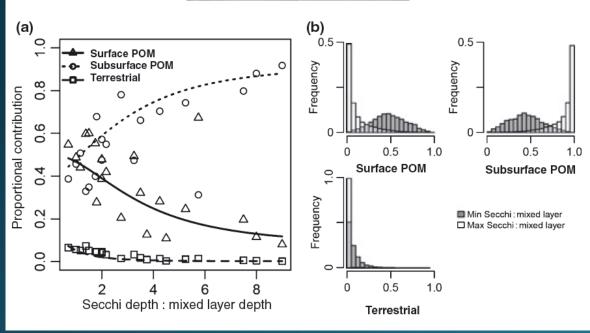




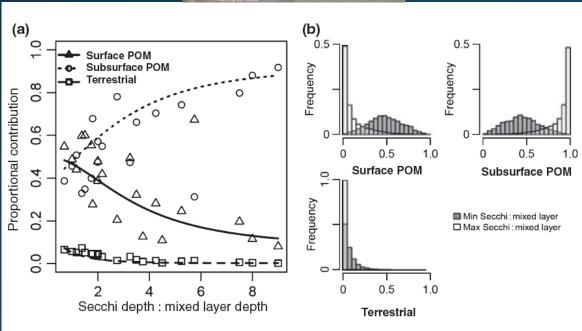


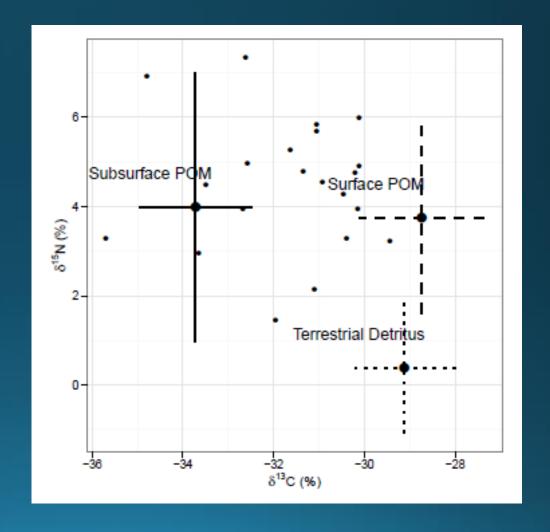




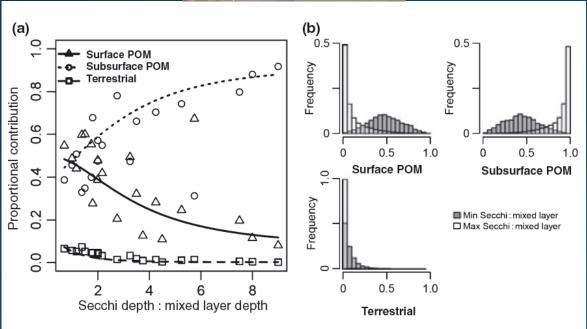


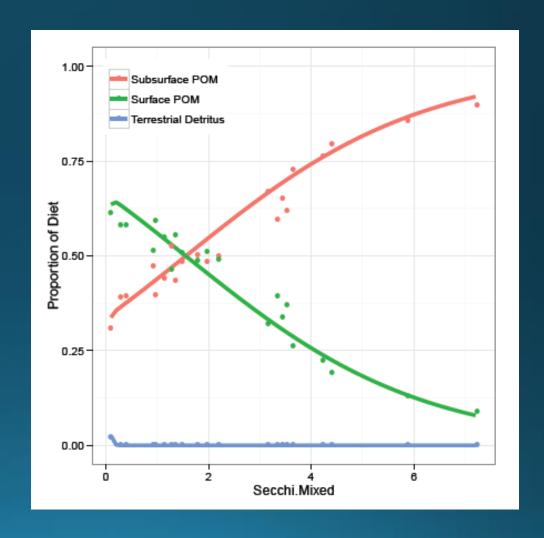




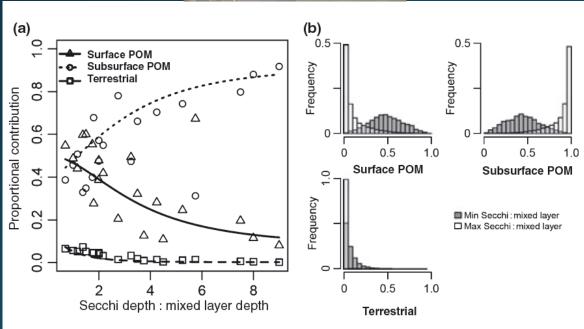


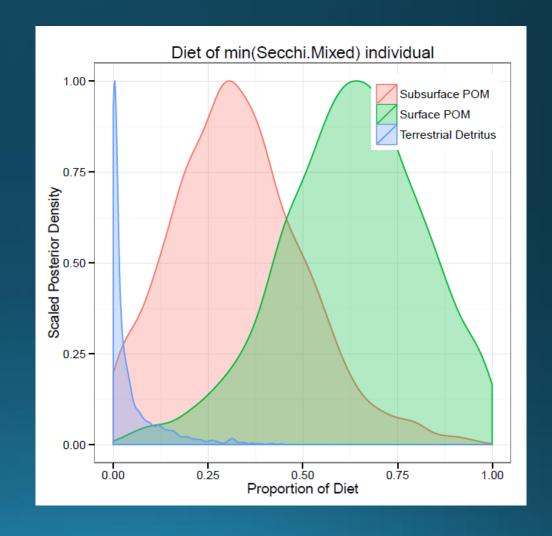




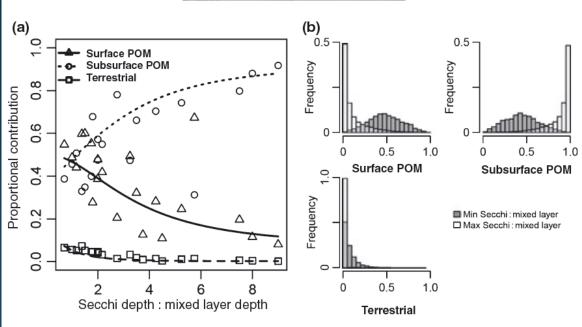


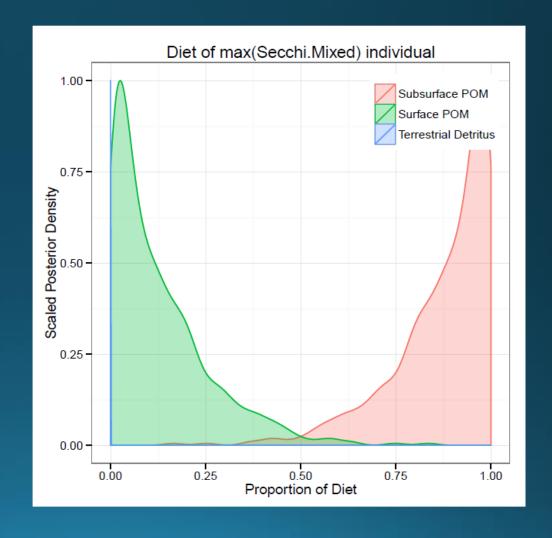




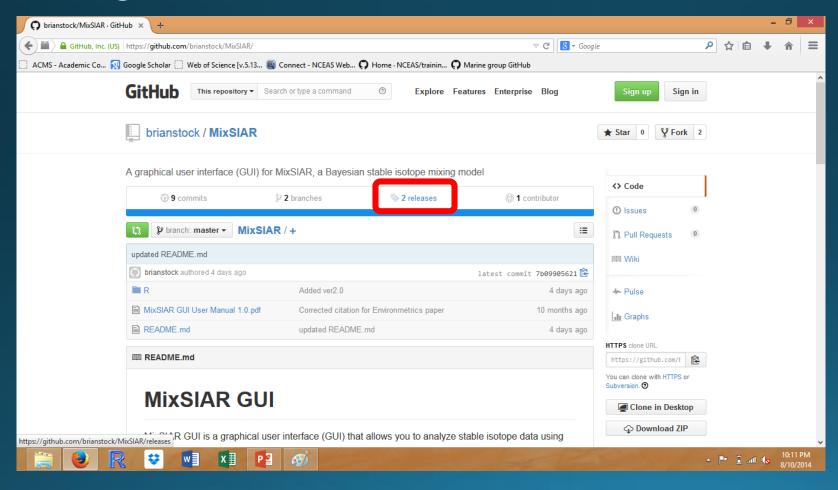








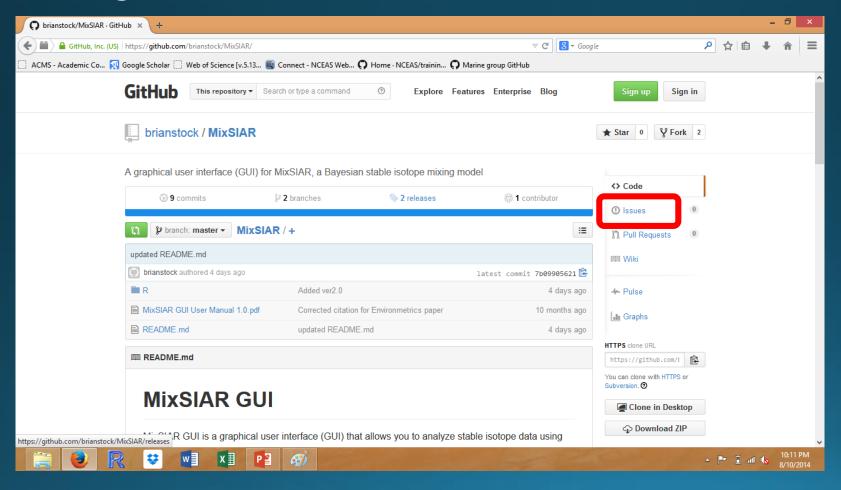
www.github.com/brianstock/MixSIAR



Releases

- Download code

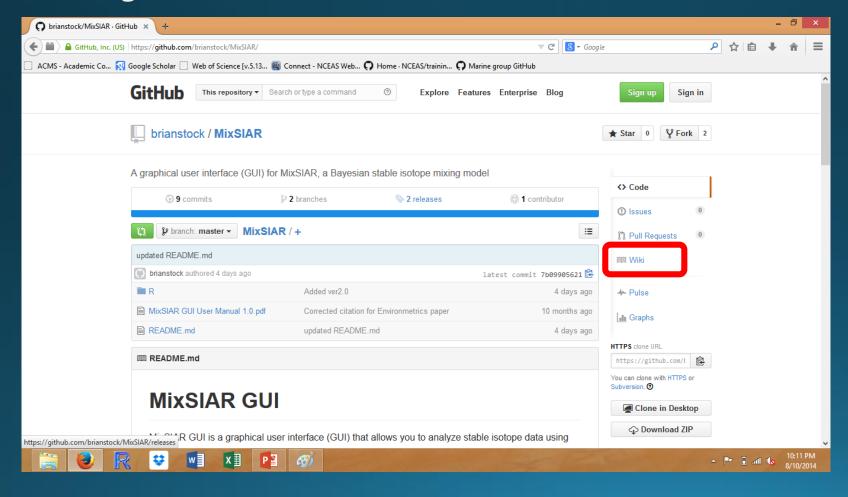
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Issues

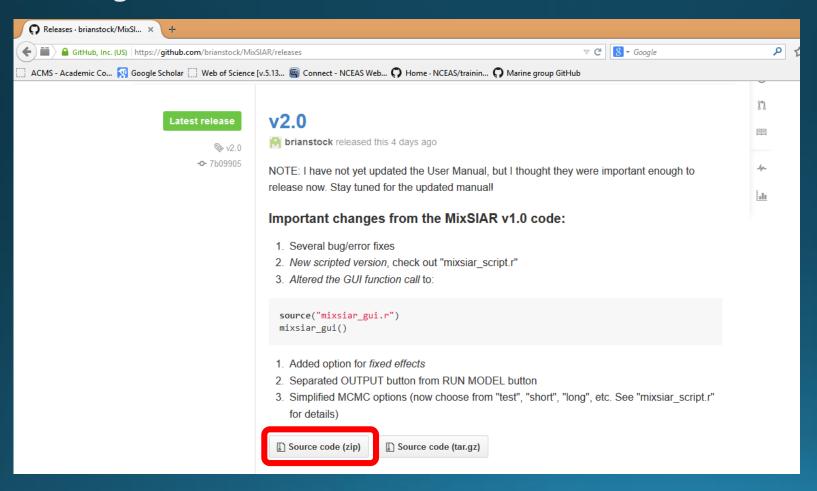
- Report bugs
- Ask questions
- Suggest changes

www.github.com/brianstock/MixSIAR



Wiki - FAQ

www.github.com/brianstock/MixSIAR/releases



Acknowledgements

MixSIAR team:

- Brice Semmens (SIO)
- Eric Ward (NWFSC)
- Jon Moore (Simon Fraser)
- Don Phillips (EPA)
- Andrew Parnell (University College Dublin)
- Andrew Jackson (Trinity College Dublin)
- Richard Inger (Exeter)
- Stuart Bearhop (Exeter)

Funding:

CAPAM (CIMEC, NOAA)



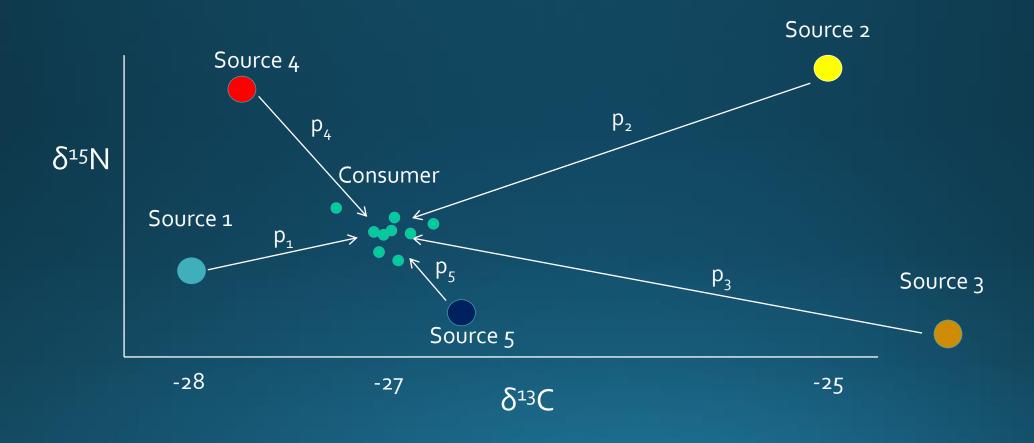
FAQ

- How many isotopes/tracers can I use?
- How many sources and effects can I include?
- Can MixSIAR handle missing data?
- What's the difference between MixSIR and SIAR? IsoSource?
- What are the model assumptions? Are they valid?
- What about normality?
- How do I compare models using DIC?
- What's the best way to model individuals?

Model assumptions

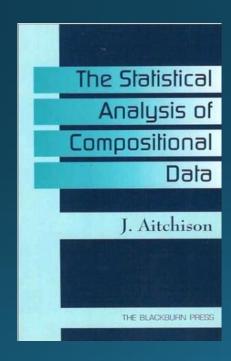
- All diet sources are included in the model
- Discrimination correctly estimated
- Isotopes are uncorrelated
- Sources are sampled across tissue turnover period

What about IsoSource?



Proportions are not normal!

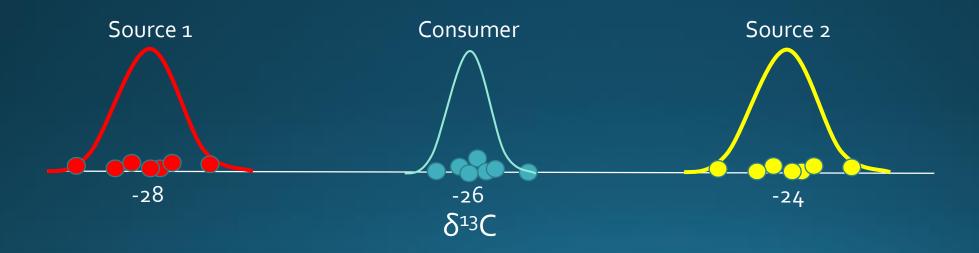
 Use the ILR (inverse log ratio) transform for compositions



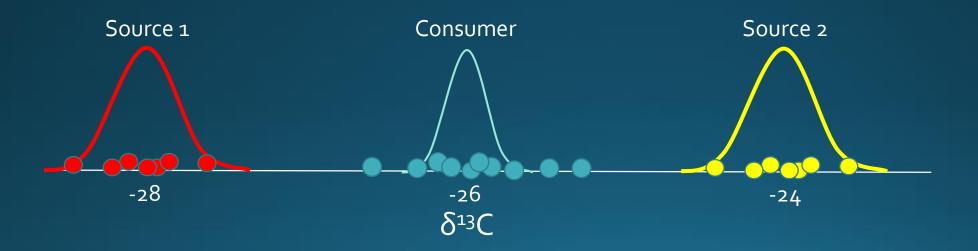
Aitchison (1986) Egozcue et al. (2010)



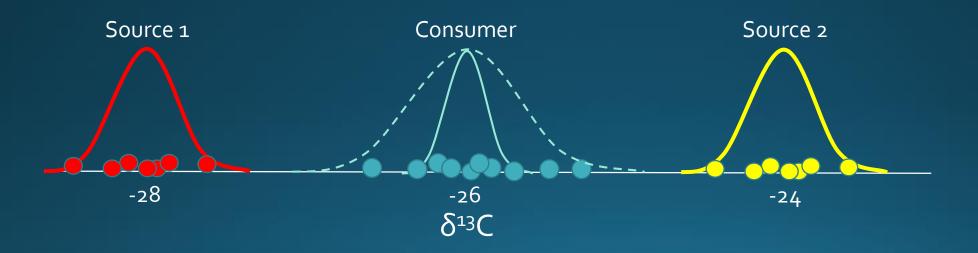
MixSIR $\sigma^2_{process}$ Medium variance



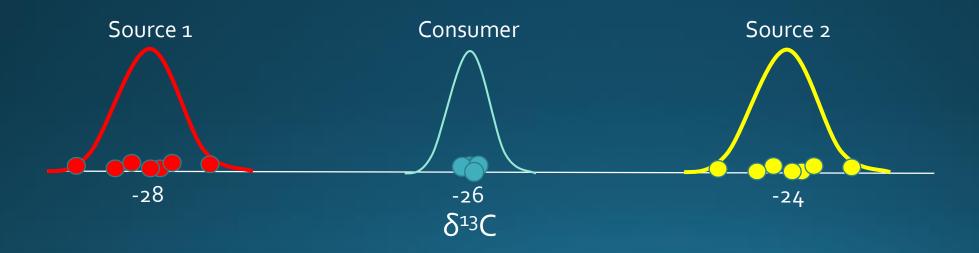
MixSIR $\sigma^2_{process}$ High variance



SIAR $\sigma^2_{process} + \sigma^2_{resid}$ High variance

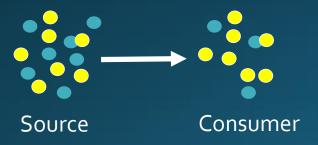


SIAR $\sigma^2_{process} + \sigma^2_{resid}$ Low variance



- Trophic enrichment factor (TEF)
- Trophic discrimination factor (TDF)

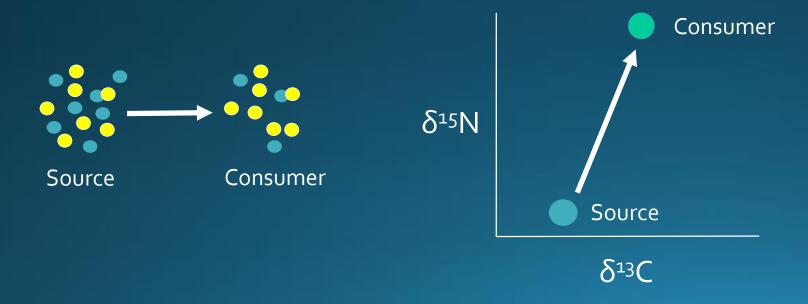
- Trophic enrichment factor (TEF)
- Trophic discrimination factor (TDF)



- Trophic enrichment factor (TEF)
- Trophic discrimination factor (TDF)



- Trophic enrichment factor (TEF)
- Trophic discrimination factor (TDF)



$$X_{ij} = \frac{\sum_{k=1}^{K} p_k q_{jk}}{\sum_{k=1}^{K} p_k q_{jk}}$$

$$c_{jk} \sim N\left(\lambda_{jk}, \tau_{jk}^2\right)$$

Concentration dependence