

model

December 25, 2024

1 The OperationsResearch fall-2024 problem

1.1 Summary

The goal of project is to minimize the revenue of a factory which is producing metal alloys and sends them to markets using containers. we have some limitations in different levels of problem which you can see in project doc.

1.2 Pyomo formulation

We begin by importing the Pyomo package and creating a model abstract object:

```
[ ]: from pyomo.environ import *
infinity = float('inf')
model = AbstractModel(name='OR1')
```

The sets *Ore*, *Alloys*, *Metals*, *Factories*, *Depots* and *Markets* are declared abstractly using the `Set` component:

```
[ ]: model.Ore = Set()
model.Alloys = Set()
model.Metals = Set()
model.Factories = Set()
model.Depots = Set()
model.Markets = Set()
```

Similarly, we add parameters, the model parameters are defined abstractly using the `Param` component:

```
[ ]: M = 999999999
epsilon = 1e-9
discount_percentage = 0.05

model.min_buy_fac = Param(model.Factories, within=NonNegativeReals, default=0.0)
model.max_buy_fac = Param(model.Factories, within=NonNegativeReals,
    ↪ default=infinity)
model.discount_margin = Param(model.Factories, within=NonNegativeReals,
    ↪ default=infinity)
model.contract_cost = Param(model.Factories, within= NonNegativeReals)
model.A_comb_min = Param(model.Metals, within=NonNegativeReals, default=0.0)
```

```

model.A_comb_max = Param(model.Metals, within=NonNegativeReals,
    ↪default=infinity)
model.B_comb_min = Param(model.Metals, within=NonNegativeReals, default=0.0)
model.B_comb_max = Param(model.Metals, within=NonNegativeReals,
    ↪default=infinity)
model.price_of_alloy_fac = Param(model.Factories, model.Alloys,
    ↪within=NonNegativeReals)
model.Max_ore = Param(model.Ore, within=NonNegativeReals)
model.Ore_cost = Param(model.Ore, within=NonNegativeReals)
model.Ore_combination = Param(model.Ore, model.Metals, within=NonNegativeReals)
model.container_cap = Param(within= NonNegativeIntegers)
model.Container_min_to_be_sent_depot = Param(model.Factories, model.Depots,
    ↪within=NonNegativeIntegers)
model.Container_Max_to_be_sent_depot = Param(model.Factories, model.Depots,
    ↪within=NonNegativeIntegers)
model.Container_cost_to_be_sent_depot = Param(model.Factories, model.Depots ,
    ↪within=NonNegativeReals)
model.depots_min_to_receive = Param(model.Depots, within=NonNegativeIntegers)
model.depots_Max_to_receive = Param(model.Depots, within=NonNegativeIntegers)
model.Container_min_to_be_sent_market = Param(model.Depots, model.Markets,
    ↪within= NonNegativeIntegers)
model.Container_Max_to_be_sent_market = Param(model.Depots, model.Markets,
    ↪within= NonNegativeIntegers)
model.Container_cost_to_be_sent_market = Param(model.Depots ,model.Markets,
    ↪within= NonNegativeReals)
model.Max_market_demand = Param(model.Markets,model.Alloys, within=
    ↪NonNegativeReals)
model.Market_price = Param(model.Markets , model.Alloys , within=
    ↪NonNegativeReals)

```

The `within` option here is used in these parameter declarations to define expected properties of the parameters. This information is used to perform error checks on the data that is used to initialize the parameter components.

The `Var` component is used to define the decision variables: the binary is $\{0,1\}$ to be clear.

```

[ ]: model.Z = Var(model.Ore,model.Alloys, within=NonNegativeReals)
model.F = Var(model.Ore,model.Alloys, within=NonNegativeReals)
model.A = Var(model.Ore,model.Alloys, within=NonNegativeReals)
model.C = Var(model.Ore,model.Alloys, within=NonNegativeReals)
model.U = Var(model.Alloys,within=NonNegativeReals)
model.t = Var(model.Alloys,model.Factories,model.Depots,
    ↪within=NonNegativeReals)
model.Extracted_ore = Var(model.Ore,within=NonNegativeReals) # defined as S in
    ↪report
model.h = Var(model.Factories,within= Binary)
model.B = Var(model.Factories, model.Depots, within=NonNegativeIntegers)

```

```

model.g = Var(model.Alloys, model.Depots, model.Markets,
    ↪within=NonNegativeReals)
model.G = Var(model.Depots, model.Markets, within= NonNegativeIntegers)
model.l = Var(model.Depots, model.Markets, within= Binary)
model.d = Var([1,2], within= Binary)
model.R = Var(model.Alloys,[1,2], within= NonNegativeReals, initialize=0)

```

Rule functions are used to define constraint expressions in the Constraint component: here we have rule for maximum extraction of Ore:

```

[ ]: def Max_extracted_ore_rule(model,i):
    return model.Extracted_ore[i] <= model.Max_ore[i]
model.Max_extracted_ore_limit = Constraint(model.
    ↪Ore,rule=Max_extracted_ore_rule)

```

Rule for Alloy weight limit(alloy weight is sum of metals weights in it):

```

[ ]: def Alloy_sum_rule(model,j):
    return model.U[j] == sum(model.Z[i,j] for i in model.Ore)+\
        sum(model.C[i,j] for i in model.Ore)+\
        sum(model.A[i,j] for i in model.Ore)+\
        sum(model.F[i,j] for i in model.Ore)
model.Alloy_sum_limit = Constraint(model.Alloys,rule=Alloy_sum_rule)

```

Rule for Metals in alloys(should be less than (or equal to) extracted metals from Ore):

```

[ ]: def Metal_sum_rule_Z(model,i):
    return sum(model.Z[i,j] for j in model.Alloys) <= model.
    ↪Extracted_ore[i]*model.Ore_combination[i,'Zinc']
model.Metal_sum_limit_Z = Constraint(model.Ore,rule=Metal_sum_rule_Z)

```

```

[ ]: def Metal_sum_rule_F(model,i):
    return sum(model.F[i,j] for j in model.Alloys) <= model.
    ↪Extracted_ore[i]*model.Ore_combination[i,'Iron']
model.Metal_sum_limit_F = Constraint(model.Ore,rule=Metal_sum_rule_F)

```

```

[ ]: def Metal_sum_rule_C(model,i):
    return sum(model.C[i,j] for j in model.Alloys) <= model.
    ↪Extracted_ore[i]*model.Ore_combination[i,'Copper']
model.Metal_sum_limit_C = Constraint(model.Ore,rule=Metal_sum_rule_C)

```

```

[ ]: def Metal_sum_rule_A(model,i):
    return sum(model.A[i,j] for j in model.Alloys) <= model.
    ↪Extracted_ore[i]*model.Ore_combination[i,'Aluminum']
model.Metal_sum_limit_A = Constraint(model.Ore,rule=Metal_sum_rule_A)

```

Rule for limitation of percentage of Metals in Alloys(f is bottom limit and t is top limit):

```
[ ]: def Metal_in_alloy_rule_A_Z_f(model):
    value = sum(model.Z[i, 'A'] for i in model.Ore)
    return model.A_comb_min['Zinc']*model.U['A']<=value
model.Metal_in_alloy_limit_A_Z_f = Constraint(rule=Metal_in_alloy_rule_A_Z_f)
def Metal_in_alloy_rule_A_Z_t(model):
    value = sum(model.Z[i, 'A'] for i in model.Ore)
    return value<=model.A_comb_max['Zinc']*model.U['A']
model.Metal_in_alloy_limit_A_Z_t = Constraint(rule=Metal_in_alloy_rule_A_Z_t)
```

```
[ ]: def Metal_in_alloy_rule_A_C_f(model):
    value = sum(model.C[i, 'A'] for i in model.Ore)
    return model.A_comb_min['Copper']*model.U['A']<=value
model.Metal_in_alloy_limit_A_C_f = Constraint(rule=Metal_in_alloy_rule_A_C_f)
def Metal_in_alloy_rule_A_C_t(model):
    value = sum(model.C[i, 'A'] for i in model.Ore)
    return value<=model.A_comb_max['Copper']*model.U['A']
model.Metal_in_alloy_limit_A_C_t = Constraint(rule=Metal_in_alloy_rule_A_C_t)
```

```
[ ]: def Metal_in_alloy_rule_A_A_f(model):
    value = sum(model.A[i, 'A'] for i in model.Ore)
    return model.A_comb_min['Aluminum']*model.U['A']<=value
model.Metal_in_alloy_limit_A_A_f = Constraint(rule=Metal_in_alloy_rule_A_A_f)
def Metal_in_alloy_rule_A_A_t(model):
    value = sum(model.A[i, 'A'] for i in model.Ore)
    return value<=model.A_comb_max['Aluminum']*model.U['A']
model.Metal_in_alloy_limit_A_A_t = Constraint(rule=Metal_in_alloy_rule_A_A_t)
```

```
[ ]: def Metal_in_alloy_rule_A_F_f(model):
    value = sum(model.F[i, 'A'] for i in model.Ore)
    return model.A_comb_min['Iron']*model.U['A']<=value
model.Metal_in_alloy_limit_A_F_f = Constraint(rule=Metal_in_alloy_rule_A_F_f)
def Metal_in_alloy_rule_A_F_t(model):
    value = sum(model.F[i, 'A'] for i in model.Ore)
    return value<=model.A_comb_max['Iron']*model.U['A']
model.Metal_in_alloy_limit_A_F_t = Constraint(rule=Metal_in_alloy_rule_A_F_t)
```

```
[ ]: def Metal_in_alloy_rule_B_Z_f(model):
    value = sum(model.Z[i, 'B'] for i in model.Ore)
    return model.B_comb_min['Zinc']*model.U['B']<=value
model.Metal_in_alloy_limit_B_Z_f = Constraint(rule=Metal_in_alloy_rule_B_Z_f)
def Metal_in_alloy_rule_B_Z_t(model):
    value = sum(model.Z[i, 'B'] for i in model.Ore)
    return value<=model.B_comb_max['Zinc']*model.U['B']
model.Metal_in_alloy_limit_B_Z_t = Constraint(rule=Metal_in_alloy_rule_B_Z_t)
```

```
[ ]: def Metal_in_alloy_rule_B_C_f(model):
    value = sum(model.C[i, 'B'] for i in model.Ore)
```

```

    return model.B_comb_min['Copper']*model.U['B']<=value
model.Metal_in_alloy_limit_B_C_f = Constraint(rule=Metal_in_alloy_rule_B_C_f)
def Metal_in_alloy_rule_B_C_t(model):
    value = sum(model.C[i,'B'] for i in model.Ore)
    return value<=model.B_comb_max['Copper']*model.U['B']
model.Metal_in_alloy_limit_B_C_t = Constraint(rule=Metal_in_alloy_rule_B_C_t)

```

```

[ ]: def Metal_in_alloy_rule_B_A_f(model):
    value = sum(model.A[i,'B'] for i in model.Ore)
    return model.B_comb_min['Aluminum']*model.U['B']<=value
model.Metal_in_alloy_limit_B_A_f = Constraint(rule=Metal_in_alloy_rule_B_A_f)
def Metal_in_alloy_rule_B_A_t(model):
    value = sum(model.A[i,'B'] for i in model.Ore)
    return value<=model.B_comb_max['Aluminum']*model.U['B']
model.Metal_in_alloy_limit_B_A_t = Constraint(rule=Metal_in_alloy_rule_B_A_t)

```

```

[ ]: def Metal_in_alloy_rule_B_F_f(model):
    value = sum(model.F[i,'B'] for i in model.Ore)
    return model.B_comb_min['Iron']*model.U['B']<=value
model.Metal_in_alloy_limit_B_F_f = Constraint(rule=Metal_in_alloy_rule_B_F_f)
def Metal_in_alloy_rule_B_F_t(model):
    value = sum(model.F[i,'B'] for i in model.Ore)
    return value<=model.B_comb_max['Iron']*model.U['B']
model.Metal_in_alloy_limit_B_F_t = Constraint(rule=Metal_in_alloy_rule_B_F_t)

```

Rule for amount of exported alloy from main Factory, it should be less than(or equal to):

```

[ ]: def Export_from_main_fac_rule(model,i):
    return model.U[i] >= sum(model.t[i,'Main',k] for k in model.Depots)
model.Export_from_main_fac_limit = Constraint(model.
    ↪Alloys,rule=Export_from_main_fac_rule)

```

Rule of Limits of buying from factories:

```

[ ]: def buy_from_fac_rule_f(model,i):
    value = sum(sum(model.t[j,i,k] for k in model.Depots)\
                    for j in model.Alloys)
    return model.min_buy_fac[i]*model.h[i]<=value
model.buy_from_fac_limit_f= Constraint([1,2],rule=buy_from_fac_rule_f)
def buy_from_fac_rule_t(model,i):
    value = sum(sum(model.t[j,i,k] for k in model.Depots)\
                    for j in model.Alloys)
    return value<=model.max_buy_fac[i]*model.h[i]
model.buy_from_fac_limit_t= Constraint([1,2],rule=buy_from_fac_rule_t)

```

Rule of limit for Alloys in one container from Factory to Depot:

```
[ ]: def container_rule(model,i,j):
    return sum(model.t[a,i,j] for a in model.Alloys) <= model.B[i,j]*model.
    ↪container_cap
model.container_limit = Constraint(model.Factories, model.Depots,
    ↪rule=container_rule)
```

Rule of limit for transporting from fac to depots No1.:

```
[ ]: def transportation_rule_t(model,i,j):
    return model.B[i,j]<= model.Container_Max_to_be_sent_depot[i,j]*model.h[i]
model.transportation_limit_t = Constraint(model.Factories,model.Depots, rule=
    ↪transportation_rule_t)
def transportation_rule_f(model,i,j):
    return model.Container_min_to_be_sent_depot[i,j]*model.h[i]<=model.B[i,j]
model.transportation_limit_f = Constraint(model.Factories,model.Depots, rule=
    ↪transportation_rule_f)
```

Rule of limit for transporting from fac to depots No2.:

```
[ ]: def transportation_rule2(model,j):
    return inequality(model.depots_min_to_receive[j],sum(model.B[i,j] for i in
    ↪model.Factories),\
                    model.depots_Max_to_receive[j])
model.transportation_limit2 = Constraint(model.Depots,rule=
    ↪transportation_rule2)
```

Rule of limit for transporting from depots to markets:

```
[ ]: def transp_from_dep_to_marker_rule(model,i,k):
    return sum(model.t[i,j,k] for j in model.Factories) >= sum(model.g[i,k,l]
    ↪for l in model.Markets)
model.transp_from_dep_to_marker_limit = Constraint(model.Alloys,model.Depots,\
    ↪rule=
    ↪transp_from_dep_to_marker_rule)
```

Rule of limits for Alloys in containers transporting from depots to markets:

```
[ ]: def container_rule2(model,i,j):
    return sum(model.g[l,i,j] for l in model.Alloys) <= model.G[i,j]*model.
    ↪container_cap
model.container_limit2 = Constraint(model.Depots, model.Markets,
    ↪rule=container_rule2)
```

Limit for containers to be sent to markets:

```
[ ]: def market_sell_rule_f(model,i,j):
    return model.Container_min_to_be_sent_market[i,j]*model.l[i,j]<=model.G[i,j]
model.market_sell_limit_f = Constraint(model.Depots,model.Markets, rule=
    ↪market_sell_rule_f)
```

```
def market_sell_rule_t(model,i,j):
    return model.G[i,j]<=model.Container_min_to_be_sent_market[i,j]*model.l[i,j]
model.market_sell_limit_t = Constraint(model.Depots,model.Markets, rule=
↪market_sell_rule_t)
```

Here we have maximum market demands rule:

```
[ ]: def max_market_demand_rule(model,k,i):
    return sum(model.g[i,j,k] for j in model.Depots) <= model.
↪Max_market_demand[k,i]
model.max_market_demand_limit = Constraint(model.Markets, model.Alloys, rule=
↪max_market_demand_rule)
```

The Objective component is used to define the revenue objective. This component uses a rule function to construct the objective expression:

sense = maximize means we want to maximize the revenue.

```
[ ]: def revenue_rule(model):
    return sum(sum(model.Market_price[m,j]*sum(model.g[j,k,m] for k in model.
↪Depots) for j in model.Alloys) for m in model.Markets)-\
    sum(model.Extracted_ore[i]*model.Ore_cost[i] for i in model.Ore)-\
    sum(sum(model.price_of_alloy_fac[u,j]*sum(model.t[j,u,k] for k in
↪model.Depots) for j in model.Alloys) for u in model.Factories)-\
    sum(model.h[u]*model.contract_cost[u] for u in model.Factories)-\
    sum(sum(model.Container_cost_to_be_sent_depot[i,j]*model.B[i,j] for
↪j in model.Depots) for i in model.Factories)-\
    sum(sum(model.G[i,j]*model.Container_cost_to_be_sent_market[i,j] for
↪j in model.Markets) for i in model.Depots)
```

```
[ ]: model.revenue = Objective(rule=revenue_rule, sense=maximize)
```

here is added constraints and adjusted revenue for part B:

```
[ ]: def discount_rule_1(model,u):
    return sum(sum(model.t[j,u,k] for j in model.Alloys) for k in model.
↪Depots)+epsilon <= model.d[u]*model.discount_margin[u] +\
    ↪ model.discount_margin[u]

def discount_rule_2(model,u):
    return sum(sum(model.t[j,u,k] for j in model.Alloys) for k in model.Depots)
↪>= model.discount_margin[u]*model.d[u]

def discount_rule_3(model,u,j):
    return sum(model.t[j,u,k] for k in model.Depots) >= model.R[j,u]

def discount_rule_4(model,u):
    return sum(model.R[j,u] for j in model.Alloys) <= model.d[u]*M
```

```

def revenue_rule_discount_added(model):
    return sum(sum(model.Market_price[m,j]*sum(model.g[j,k,m] for k in model.
↳Depots) for j in model.Alloys) for m in model.Markets)-\
        sum(model.Extracted_ore[i]*model.Ore_cost[i] for i in model.Ore)-\
        sum(sum(model.price_of_alloy_fac[u,j]*sum(model.t[j,u,k] for k in
↳model.Depots) for j in model.Alloys) for u in model.Factories)-\
        sum(model.h[u]*model.contract_cost[u] for u in model.Factories)-\
        sum(sum(model.Container_cost_to_be_sent_depot[i,j]*model.B[i,j] for
↳j in model.Depots) for i in model.Factories)-\
        sum(sum(model.G[i,j]*model.Container_cost_to_be_sent_market[i,j] for
↳j in model.Markets) for i in model.Depots)+\
        sum(sum(discount_percentage*model.R[j,u]*model.
↳price_of_alloy_fac[u,j] for u in [1,2]) for j in model.Alloys)

def apply_discount_rule():
    model.discount_limit_1 = Constraint([1,2],rule=discount_rule_1)
    model.discount_limit_2 = Constraint([1,2],rule=discount_rule_2)
    model.discount_limit_3 = Constraint([1,2],model.Alloys,rule=discount_rule_3)
    model.discount_limit_4 = Constraint([1,2],rule=discount_rule_4)
    model.revenue = Objective(rule=revenue_rule_discount_added, sense=maximize)

```

1.3 model data

since we have made an abstract model, we can add the data after creating model, to see the data we are feeding the model

execute command below or have a look at params.dat:

```
[6]: !cat params.dat
```

```

set Alloys:=
    A
    B;

param: Factories:          min_buy_fac  discount_margin  max_buy_fac
contract_cost:=
    1          2000          2500          5000          120
    2          2500          3000          6000          90
    Main       0            .            .            0    ;

param: Depots:             depots_min_to_receive  depots_Max_to_receive :=
    Tehran                20                      65
    Isfahan                30                      70    ;

param container_cap:= 100;

set Markets:=

```


Mashhad
Kerman
Ahvaz
Tabriz ;

param: Metals:	A_comb_min	A_comb_max	B_comb_min	B_comb_max :=
Iron	0	0.25	0.45	0.70
Aluminum	0.55	1	0	0.70
Zinc	0	0.8	0	1
Copper	0	1	0.35	1 ;

param: Ore:	Max_ore	Ore_cost :=
1	560	45
2	1000	65
3	1440	70 ;

param Ore_combination:	Iron	Aluminum	Zinc	Copper :=
1	.05	.35	.25	.30
2	.20	.30	.15	.25
3	.05	.25	.65	.05 ;

param Container_min_to_be_sent_depot:	Tehran	Isfahan :=
Main	5	5
1	10	10
2	5	5 ;

param Container_Max_to_be_sent_depot:	Tehran	Isfahan :=
Main	20	20
1	30	30
2	25	15 ;

param Container_cost_to_be_sent_depot:	Tehran	Isfahan :=
Main	200	230
1	180	210
2	240	220 ;

param Container_min_to_be_sent_market:	Mashhad	Kerman	Ahvaz	Tabriz :=
Tehran	3	6	10	5
Isfahan	4	5	5	10 ;

```

param Container_Max_to_be_sent_market:
      Mashhad      Kerman      Ahvaz      Tabriz :=
Tehran      7      12      18      15
Isfahan      6      14      20      20 ;

```

```

param Container_cost_to_be_sent_market:
      Mashhad      Kerman      Ahvaz      Tabriz :=
Tehran      110      85      120      100
Isfahan      100      100      110      90 ;

```

```

param Max_market_demand:
      A      B :=
Mashhad      600      400
Kerman      800      1200
Ahvaz      1500      1500
Tabriz      1400      1100 ;

```

```

param Market_price:
      A      B :=
Mashhad      520      700
Kerman      540      690
Ahvaz      490      730
Tabriz      500      710 ;

```

```

param price_of_alloy_fac:
      A      B :=
1      375      520
2      390      540
Main      0      0 ;

```

1.4 Solution

To get the result of a problem, you can execute the command below:

make sure to replace `-problem-number` with correct number, use problem-dict.

results are also saved in `results.yaml`

```
[2]: !python model_runner.py -problem-number
```

this is problem-dictionary

```

{      '-a': ' ',      '-b': ' ',      '-c': ' ',      '-d': ' ',      '-e': ' ',
'-f': ' ',      '-g': ' ',      '-h': ' ',      '-i': ' ' {

```

for example you can execute the code below to see results of problem :

1.4.1 Problem A

```
[7]: !python model_runner.py -a
```

results for problem: -a

Problem:

- Name: unknown
- Lower bound: 1593740.3030303
- Upper bound: 1593740.3030303
- Number of objectives: 1
- Number of constraints: 97
- Number of variables: 82
- Number of nonzeros: 304
- Sense: maximize

Solver:

- Status: ok
- Termination condition: optimal
- Statistics:
 - Branch and bound:
 - Number of bounded subproblems: 39
 - Number of created subproblems: 39
 - Error rc: 0
 - Time: 0.010610103607177734

Solution:

- number of solutions: 0
- number of solutions displayed: 0

Model OR1

Variables:

Z : Size=6, Index=Ore*Alloys							
Key	: Lower	: Value		: Upper	: Fixed	: Stale	: Domain
(1, 'A')	: 0	:	140.0	: None	: False	: False	:
NonNegativeReals							
(1, 'B')	: 0	:	0.0	: None	: False	: False	:
NonNegativeReals							
(2, 'A')	: 0	:	150.0	: None	: False	: False	:
NonNegativeReals							
(2, 'B')	: 0	:	0.0	: None	: False	: False	:
NonNegativeReals							
(3, 'A')	: 0	: 225.69696969697	:	: None	: False	: False	:
NonNegativeReals							
(3, 'B')	: 0	: 133.333333333333	:	: None	: False	: False	:
NonNegativeReals							
F : Size=6, Index=Ore*Alloys							

```

Key      : Lower : Value : Upper : Fixed : Stale : Domain
(1, 'A') :      0 :   0.0 :  None : False : False : NonNegativeReals
(1, 'B') :      0 :  28.0 :  None : False : False : NonNegativeReals
(2, 'A') :      0 :   0.0 :  None : False : False : NonNegativeReals
(2, 'B') :      0 : 200.0 :  None : False : False : NonNegativeReals
(3, 'A') :      0 :   0.0 :  None : False : False : NonNegativeReals
(3, 'B') :      0 :  72.0 :  None : False : False : NonNegativeReals
A : Size=6, Index=Ore*Alloys
Key      : Lower : Value : Upper : Fixed : Stale : Domain
(1, 'A') :      0 : 196.0 :  None : False : False : NonNegativeReals
(1, 'B') :      0 :   0.0 :  None : False : False : NonNegativeReals
(2, 'A') :      0 : 300.0 :  None : False : False : NonNegativeReals
(2, 'B') :      0 :   0.0 :  None : False : False : NonNegativeReals
(3, 'A') :      0 : 360.0 :  None : False : False : NonNegativeReals
(3, 'B') :      0 :   0.0 :  None : False : False : NonNegativeReals
C : Size=6, Index=Ore*Alloys
Key      : Lower : Value : Upper : Fixed : Stale : Domain
(1, 'A') :      0 :           0.0 :  None : False : False :
NonNegativeReals
(1, 'B') :      0 :          168.0 :  None : False : False :
NonNegativeReals
(2, 'A') :      0 : 184.6666666666667 :  None : False : False :
NonNegativeReals
(2, 'B') :      0 : 65.33333333333333 :  None : False : False :
NonNegativeReals
(3, 'A') :      0 :           0.0 :  None : False : False :
NonNegativeReals
(3, 'B') :      0 :           0.0 :  None : False : False :
NonNegativeReals
U : Size=2, Index=Alloys
Key : Lower : Value : Upper : Fixed : Stale : Domain
A :      0 : 1556.36363636364 :  None : False : False :
NonNegativeReals
B :      0 : 666.6666666666667 :  None : False : False :
NonNegativeReals
t : Size=12, Index=Alloys*Factories*Depots
Key      : Lower : Value : Upper : Fixed :
Stale : Domain
('A', 1, 'Isfahan') :      0 :           0.0 :  None : False :
False : NonNegativeReals
('A', 1, 'Tehran') :      0 :           0.0 :  None : False :
False : NonNegativeReals
('A', 2, 'Isfahan') :      0 :           0.0 :  None : False :
False : NonNegativeReals
('A', 2, 'Tehran') :      0 :           0.0 :  None : False :
False : NonNegativeReals
('A', 'Main', 'Isfahan') :      0 : 1256.36363636364 :  None : False :
False : NonNegativeReals

```

```

('A', 'Main', 'Tehran') :      0 :      300.0 :  None : False :
False : NonNegativeReals
('B', 1, 'Isfahan') :      0 : 676.969696969697 :  None : False :
False : NonNegativeReals
('B', 1, 'Tehran') :      0 :      1900.0 :  None : False :
False : NonNegativeReals
('B', 2, 'Isfahan') :      0 :      0.0 :  None : False :
False : NonNegativeReals
('B', 2, 'Tehran') :      0 :      0.0 :  None : False :
False : NonNegativeReals
('B', 'Main', 'Isfahan') :      0 : 466.666666666667 :  None : False :
False : NonNegativeReals
('B', 'Main', 'Tehran') :      0 :      200.0 :  None : False :
False : NonNegativeReals
  Extracted_ore : Size=3, Index=Ore
    Key : Lower : Value : Upper : Fixed : Stale : Domain
      1 :      0 : 560.0 :  None : False : False : NonNegativeReals
      2 :      0 : 1000.0 :  None : False : False : NonNegativeReals
      3 :      0 : 1440.0 :  None : False : False : NonNegativeReals
  h : Size=3, Index=Factories
    Key : Lower : Value : Upper : Fixed : Stale : Domain
      1 :      0 : 1.0 :      1 : False : False : Binary
      2 :      0 : 0.0 :      1 : False : False : Binary
    Main :      0 : 1.0 :      1 : False : False : Binary
  B : Size=6, Index=Factories*Depots
    Key : Lower : Value : Upper : Fixed : Stale : Domain
    (1, 'Isfahan') :      0 : 12.0 :  None : False : False :
NonNegativeIntegers
    (1, 'Tehran') :      0 : 19.0 :  None : False : False :
NonNegativeIntegers
    (2, 'Isfahan') :      0 : 0.0 :  None : False : False :
NonNegativeIntegers
    (2, 'Tehran') :      0 : 0.0 :  None : False : False :
NonNegativeIntegers
    ('Main', 'Isfahan') :      0 : 18.0 :  None : False : False :
NonNegativeIntegers
    ('Main', 'Tehran') :      0 : 5.0 :  None : False : False :
NonNegativeIntegers
  g : Size=16, Index=Alloys*Depots*Markets
    Key : Lower : Value : Upper : Fixed :
    Stale : Domain
    ('A', 'Isfahan', 'Ahvaz') :      0 :      0.0 :  None : False :
False : NonNegativeReals
    ('A', 'Isfahan', 'Kerman') :      0 :      500.0 :  None : False :
False : NonNegativeReals
    ('A', 'Isfahan', 'Mashhad') :      0 : 356.363636363636 :  None : False :
False : NonNegativeReals
    ('A', 'Isfahan', 'Tabriz') :      0 :      400.0 :  None : False :

```

```

False : NonNegativeReals
      ('A', 'Tehran', 'Ahvaz') :      0 :      0.0 : None : False :
False : NonNegativeReals
      ('A', 'Tehran', 'Kerman') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('A', 'Tehran', 'Mashhad') :      0 :      0.0 : None : False :
False : NonNegativeReals
      ('A', 'Tehran', 'Tabriz') :      0 :      0.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Ahvaz') :      0 :      500.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Kerman') :      0 :      0.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Mashhad') :      0 : 43.636363636363637 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Tabriz') :      0 :      600.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Ahvaz') :      0 :     1000.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Kerman') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Mashhad') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Tabriz') :      0 :      500.0 : None : False :
False : NonNegativeReals
      G : Size=8, Index=Depots*Markets
          Key : Lower : Value : Upper : Fixed : Stale : Domain
          ('Isfahan', 'Ahvaz') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Kerman') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Mashhad') :      0 :   4.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Tabriz') :      0 :  10.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Ahvaz') :      0 :  10.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Kerman') :      0 :   6.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Mashhad') :      0 :   3.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Tabriz') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
      l : Size=8, Index=Depots*Markets
          Key : Lower : Value : Upper : Fixed : Stale : Domain
          ('Isfahan', 'Ahvaz') :      0 :   1.0 :      1 : False : False : Binary
          ('Isfahan', 'Kerman') :      0 :   1.0 :      1 : False : False : Binary
          ('Isfahan', 'Mashhad') :      0 :   1.0 :      1 : False : False : Binary

```

```

('Isfahan', 'Tabriz') :      0 :   1.0 :      1 : False : False : Binary
('Tehran', 'Ahvaz') :      0 :   1.0 :      1 : False : False : Binary
('Tehran', 'Kerman') :      0 :   1.0 :      1 : False : False : Binary
('Tehran', 'Mashhad') :     0 :   1.0 :      1 : False : False : Binary
('Tehran', 'Tabriz') :      0 :   1.0 :      1 : False : False : Binary
d : Size=2, Index={1, 2}
  Key : Lower : Value : Upper : Fixed : Stale : Domain
    1 :      0 : None :      1 : False : True  : Binary
    2 :      0 : None :      1 : False : True  : Binary
R : Size=4, Index=Alloys*{1, 2}
  Key      : Lower : Value : Upper : Fixed : Stale : Domain
  ('A', 1) :      0 :      0 : None : False : True  : NonNegativeReals
  ('A', 2) :      0 :      0 : None : False : True  : NonNegativeReals
  ('B', 1) :      0 :      0 : None : False : True  : NonNegativeReals
  ('B', 2) :      0 :      0 : None : False : True  : NonNegativeReals

```

Objectives:

```

revenue : Size=1, Index=None, Active=True
  Key : Active : Value
  None : True : 1593740.3030303027

```

Constraints:

```

Max_extracted_ore_limit : Size=3
  Key : Lower : Body : Upper
    1 : None : 560.0 : 560
    2 : None : 1000.0 : 1000
    3 : None : 1440.0 : 1440
Alloy_sum_limit : Size=2
  Key : Lower : Body : Upper
    A : None : 2.9558577807620168e-12 : 0.0
    B : None : 6.821210263296962e-13 : 0.0
Metal_sum_limit_Z : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 0.0 : 0.0
    3 : None : -576.969696969697 : 0.0
Metal_sum_limit_F : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 0.0 : 0.0
    3 : None : 0.0 : 0.0
Metal_sum_limit_C : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 2.984279490192421e-13 : 0.0
    3 : None : -72.0 : 0.0
Metal_sum_limit_A : Size=3
  Key : Lower : Body : Upper

```

```

1 : None : 0.0 : 0.0
2 : None : 0.0 : 0.0
3 : None : 0.0 : 0.0
Metal_in_alloy_limit_A_Z_f : Size=1
Key : Lower : Body : Upper
None : None : -515.69696969697 : 0.0
Metal_in_alloy_limit_A_Z_t : Size=1
Key : Lower : Body : Upper
None : None : -729.393939393942 : 0.0
Metal_in_alloy_limit_A_C_f : Size=1
Key : Lower : Body : Upper
None : None : -184.666666666667 : 0.0
Metal_in_alloy_limit_A_C_t : Size=1
Key : Lower : Body : Upper
None : None : -1371.696969696973 : 0.0
Metal_in_alloy_limit_A_A_f : Size=1
Key : Lower : Body : Upper
None : None : 2.0463630789890885e-12 : 0.0
Metal_in_alloy_limit_A_A_t : Size=1
Key : Lower : Body : Upper
None : None : -700.3636363636399 : 0.0
Metal_in_alloy_limit_A_F_f : Size=1
Key : Lower : Body : Upper
None : None : 0.0 : 0.0
Metal_in_alloy_limit_A_F_t : Size=1
Key : Lower : Body : Upper
None : None : -389.09090909091 : 0.0
Metal_in_alloy_limit_B_Z_f : Size=1
Key : Lower : Body : Upper
None : None : -133.333333333333 : 0.0
Metal_in_alloy_limit_B_Z_t : Size=1
Key : Lower : Body : Upper
None : None : -533.333333333339 : 0.0
Metal_in_alloy_limit_B_C_f : Size=1
Key : Lower : Body : Upper
None : None : 1.1368683772161603e-13 : 0.0
Metal_in_alloy_limit_B_C_t : Size=1
Key : Lower : Body : Upper
None : None : -433.333333333336 : 0.0
Metal_in_alloy_limit_B_A_f : Size=1
Key : Lower : Body : Upper
None : None : 0.0 : 0.0
Metal_in_alloy_limit_B_A_t : Size=1
Key : Lower : Body : Upper
None : None : -466.6666666666686 : 0.0
Metal_in_alloy_limit_B_F_f : Size=1
Key : Lower : Body : Upper
None : None : 1.7053025658242404e-13 : 0.0

```



```

Metal_in_alloy_limit_B_F_t : Size=1
  Key : Lower : Body : Upper
  None : None : -166.66666666666686 : 0.0
Export_from_main_fac_limit : Size=2
  Key : Lower : Body : Upper
  A : None : 0.0 : 0.0
  B : None : 5.684341886080802e-14 : 0.0
buy_from_fac_limit_f : Size=2
  Key : Lower : Body : Upper
  1 : None : -576.969696969697 : 0.0
  2 : None : 0.0 : 0.0
buy_from_fac_limit_t : Size=2
  Key : Lower : Body : Upper
  1 : None : -2423.030303030303 : 0.0
  2 : None : 0.0 : 0.0
container_limit : Size=6
  Key : Lower : Body : Upper
  (1, 'Isfahan') : None : -523.030303030303 : 0.0
  (1, 'Tehran') : None : 0.0 : 0.0
  (2, 'Isfahan') : None : 0.0 : 0.0
  (2, 'Tehran') : None : 0.0 : 0.0
  ('Main', 'Isfahan') : None : -76.96969696969308 : 0.0
  ('Main', 'Tehran') : None : 0.0 : 0.0
transportation_limit_t : Size=6
  Key : Lower : Body : Upper
  (1, 'Isfahan') : None : -18.0 : 0.0
  (1, 'Tehran') : None : -11.0 : 0.0
  (2, 'Isfahan') : None : 0.0 : 0.0
  (2, 'Tehran') : None : 0.0 : 0.0
  ('Main', 'Isfahan') : None : -2.0 : 0.0
  ('Main', 'Tehran') : None : -15.0 : 0.0
transportation_limit_f : Size=6
  Key : Lower : Body : Upper
  (1, 'Isfahan') : None : -2.0 : 0.0
  (1, 'Tehran') : None : -9.0 : 0.0
  (2, 'Isfahan') : None : 0.0 : 0.0
  (2, 'Tehran') : None : 0.0 : 0.0
  ('Main', 'Isfahan') : None : -13.0 : 0.0
  ('Main', 'Tehran') : None : 0.0 : 0.0
transportation_limit2 : Size=2
  Key : Lower : Body : Upper
  Isfahan : 30.0 : 30.0 : 70.0
  Tehran : 20.0 : 24.0 : 65.0
transp_from_dep_to_market_limit : Size=4
  Key : Lower : Body : Upper
  ('A', 'Isfahan') : None : -3.865352482534945e-12 : 0.0
  ('A', 'Tehran') : None : 0.0 : 0.0
  ('B', 'Isfahan') : None : -2.2737367544323206e-13 : 0.0

```

```

        ('B', 'Tehran') : None : 0.0 : 0.0
container_limit2 : Size=8
    Key : Lower : Body : Upper
        ('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
        ('Isfahan', 'Kerman') : None : 0.0 : 0.0
        ('Isfahan', 'Mashhad') : None : -3.268496584496461e-13 : 0.0
        ('Isfahan', 'Tabriz') : None : 0.0 : 0.0
        ('Tehran', 'Ahvaz') : None : 0.0 : 0.0
        ('Tehran', 'Kerman') : None : 0.0 : 0.0
        ('Tehran', 'Mashhad') : None : 0.0 : 0.0
        ('Tehran', 'Tabriz') : None : 0.0 : 0.0
market_sell_limit_f : Size=8
    Key : Lower : Body : Upper
        ('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
        ('Isfahan', 'Kerman') : None : 0.0 : 0.0
        ('Isfahan', 'Mashhad') : None : 0.0 : 0.0
        ('Isfahan', 'Tabriz') : None : 0.0 : 0.0
        ('Tehran', 'Ahvaz') : None : 0.0 : 0.0
        ('Tehran', 'Kerman') : None : 0.0 : 0.0
        ('Tehran', 'Mashhad') : None : 0.0 : 0.0
        ('Tehran', 'Tabriz') : None : 0.0 : 0.0
market_sell_limit_t : Size=8
    Key : Lower : Body : Upper
        ('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
        ('Isfahan', 'Kerman') : None : 0.0 : 0.0
        ('Isfahan', 'Mashhad') : None : 0.0 : 0.0
        ('Isfahan', 'Tabriz') : None : 0.0 : 0.0
        ('Tehran', 'Ahvaz') : None : 0.0 : 0.0
        ('Tehran', 'Kerman') : None : 0.0 : 0.0
        ('Tehran', 'Mashhad') : None : 0.0 : 0.0
        ('Tehran', 'Tabriz') : None : 0.0 : 0.0
max_market_demand_limit : Size=8
    Key : Lower : Body : Upper
        ('Ahvaz', 'A') : None : 0.0 : 1500.0
        ('Ahvaz', 'B') : None : 1500.0 : 1500.0
        ('Kerman', 'A') : None : 800.0 : 800.0
        ('Kerman', 'B') : None : 300.0 : 1200.0
        ('Mashhad', 'A') : None : 356.3636363636363 : 600.0
        ('Mashhad', 'B') : None : 343.6363636363637 : 400.0
        ('Tabriz', 'A') : None : 400.0 : 1400.0
        ('Tabriz', 'B') : None : 1100.0 : 1100.0
results saved in results.yaml

```

1.4.2 Problem B

```
[8]: !python model_runner.py -b
```

```
results for problem: -b
```

WARNING: Implicitly replacing the Component attribute revenue (type=<class 'pyomo.core.base.objective.ScalarObjective'>) on block OR1 with a new Component (type=<class 'pyomo.core.base.objective.ScalarObjective'>). This is usually indicative of a modelling error. To avoid this warning, use block.del_component() and block.add_component().

Problem:

- Name: unknown
 - Lower bound: 1593740.3030303
 - Upper bound: 1593740.3030303
 - Number of objectives: 1
 - Number of constraints: 97
 - Number of variables: 82
 - Number of nonzeros: 304
 - Sense: maximize

Solver:

- Status: ok
 - Termination condition: optimal
 - Statistics:
 - Branch and bound:
 - Number of bounded subproblems: 39
 - Number of created subproblems: 39
 - Error rc: 0
 - Time: 0.009909868240356445

Solution:

- number of solutions: 0
 - number of solutions displayed: 0

Model OR1

Variables:

Z : Size=6, Index=Ore*Alloys							
	Key	: Lower	: Value		: Upper	: Fixed	: Stale : Domain
	(1, 'A')	: 0	:	140.0	: None	: False	: False :
NonNegativeReals	(1, 'B')	: 0	:	0.0	: None	: False	: False :
NonNegativeReals	(2, 'A')	: 0	:	150.0	: None	: False	: False :
NonNegativeReals	(2, 'B')	: 0	:	0.0	: None	: False	: False :
NonNegativeReals	(3, 'A')	: 0	: 225.69696969697	:	: None	: False	: False :
NonNegativeReals	(3, 'B')	: 0	: 133.333333333333	:	: None	: False	: False :
NonNegativeReals							
F : Size=6, Index=Ore*Alloys							
	Key	: Lower	: Value	: Upper	: Fixed	: Stale	: Domain
	(1, 'A')	: 0	: 0.0	: None	: False	: False	: NonNegativeReals

```

(1, 'B') :      0 : 28.0 : None : False : False : NonNegativeReals
(2, 'A') :      0 :  0.0 : None : False : False : NonNegativeReals
(2, 'B') :      0 : 200.0 : None : False : False : NonNegativeReals
(3, 'A') :      0 :  0.0 : None : False : False : NonNegativeReals
(3, 'B') :      0 : 72.0 : None : False : False : NonNegativeReals
A : Size=6, Index=Ore*Alloys
  Key      : Lower : Value : Upper : Fixed : Stale : Domain
(1, 'A') :      0 : 196.0 : None : False : False : NonNegativeReals
(1, 'B') :      0 :  0.0 : None : False : False : NonNegativeReals
(2, 'A') :      0 : 300.0 : None : False : False : NonNegativeReals
(2, 'B') :      0 :  0.0 : None : False : False : NonNegativeReals
(3, 'A') :      0 : 360.0 : None : False : False : NonNegativeReals
(3, 'B') :      0 :  0.0 : None : False : False : NonNegativeReals
C : Size=6, Index=Ore*Alloys
  Key      : Lower : Value : Upper : Fixed : Stale : Domain
(1, 'A') :      0 :      : 0.0 : None : False : False :
NonNegativeReals
(1, 'B') :      0 :      : 168.0 : None : False : False :
NonNegativeReals
(2, 'A') :      0 : 184.6666666666667 : None : False : False :
NonNegativeReals
(2, 'B') :      0 : 65.33333333333333 : None : False : False :
NonNegativeReals
(3, 'A') :      0 :      : 0.0 : None : False : False :
NonNegativeReals
(3, 'B') :      0 :      : 0.0 : None : False : False :
NonNegativeReals
U : Size=2, Index=Alloys
  Key : Lower : Value : Upper : Fixed : Stale : Domain
  A :      0 : 1556.36363636364 : None : False : False :
NonNegativeReals
  B :      0 : 666.6666666666667 : None : False : False :
NonNegativeReals
t : Size=12, Index=Alloys*Factories*Depots
  Key      : Lower : Value : Upper : Fixed :
Stale : Domain
('A', 1, 'Isfahan') :      0 :      : 0.0 : None : False :
False : NonNegativeReals
('A', 1, 'Tehran') :      0 :      : 0.0 : None : False :
False : NonNegativeReals
('A', 2, 'Isfahan') :      0 :      : 0.0 : None : False :
False : NonNegativeReals
('A', 2, 'Tehran') :      0 :      : 0.0 : None : False :
False : NonNegativeReals
('A', 'Main', 'Isfahan') :      0 : 1256.36363636364 : None : False :
False : NonNegativeReals
('A', 'Main', 'Tehran') :      0 :      : 300.0 : None : False :
False : NonNegativeReals

```

```

                ('B', 1, 'Isfahan') :      0 : 676.969696969697 : None : False :
False : NonNegativeReals
                ('B', 1, 'Tehran') :      0 :           1900.0 : None : False :
False : NonNegativeReals
                ('B', 2, 'Isfahan') :      0 :           0.0 : None : False :
False : NonNegativeReals
                ('B', 2, 'Tehran') :      0 :           0.0 : None : False :
False : NonNegativeReals
                ('B', 'Main', 'Isfahan') :    0 : 466.666666666667 : None : False :
False : NonNegativeReals
                ('B', 'Main', 'Tehran') :    0 :           200.0 : None : False :
False : NonNegativeReals
    Extracted_ore : Size=3, Index=0re
        Key : Lower : Value : Upper : Fixed : Stale : Domain
            1 :      0 : 560.0 : None : False : False : NonNegativeReals
            2 :      0 : 1000.0 : None : False : False : NonNegativeReals
            3 :      0 : 1440.0 : None : False : False : NonNegativeReals
    h : Size=3, Index=Factories
        Key : Lower : Value : Upper : Fixed : Stale : Domain
            1 :      0 : 1.0 :      1 : False : False : Binary
            2 :      0 : 0.0 :      1 : False : False : Binary
        Main :      0 : 1.0 :      1 : False : False : Binary
    B : Size=6, Index=Factories*Depots
        Key
            : Lower : Value : Upper : Fixed : Stale : Domain
        (1, 'Isfahan') :      0 : 12.0 : None : False : False :
NonNegativeIntegers
        (1, 'Tehran') :      0 : 19.0 : None : False : False :
NonNegativeIntegers
        (2, 'Isfahan') :      0 : 0.0 : None : False : False :
NonNegativeIntegers
        (2, 'Tehran') :      0 : 0.0 : None : False : False :
NonNegativeIntegers
        ('Main', 'Isfahan') :      0 : 18.0 : None : False : False :
NonNegativeIntegers
        ('Main', 'Tehran') :      0 : 5.0 : None : False : False :
NonNegativeIntegers
    g : Size=16, Index=Alloys*Depots*Markets
        Key
            : Lower : Value
        : Upper : Fixed :
Stale : Domain
        ('A', 'Isfahan', 'Ahvaz') :      0 :           0.0 : None : False :
False : NonNegativeReals
        ('A', 'Isfahan', 'Kerman') :      0 :           500.0 : None : False :
False : NonNegativeReals
        ('A', 'Isfahan', 'Mashhad') :      0 : 356.363636363636 : None : False :
False : NonNegativeReals
        ('A', 'Isfahan', 'Tabriz') :      0 :           400.0 : None : False :
False : NonNegativeReals
        ('A', 'Tehran', 'Ahvaz') :      0 :           0.0 : None : False :

```

```

False : NonNegativeReals
      ('A', 'Tehran', 'Kerman') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('A', 'Tehran', 'Mashhad') :      0 :       0.0 : None : False :
False : NonNegativeReals
      ('A', 'Tehran', 'Tabriz') :      0 :       0.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Ahvaz') :      0 :      500.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Kerman') :      0 :       0.0 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Mashhad') :      0 : 43.6363636363637 : None : False :
False : NonNegativeReals
      ('B', 'Isfahan', 'Tabriz') :      0 :      600.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Ahvaz') :      0 :     1000.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Kerman') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Mashhad') :      0 :      300.0 : None : False :
False : NonNegativeReals
      ('B', 'Tehran', 'Tabriz') :      0 :      500.0 : None : False :
False : NonNegativeReals
      G : Size=8, Index=Depots*Markets
          Key : Lower : Value : Upper : Fixed : Stale : Domain
          ('Isfahan', 'Ahvaz') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Kerman') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Mashhad') :      0 :   4.0 : None : False : False :
NonNegativeIntegers
          ('Isfahan', 'Tabriz') :      0 :  10.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Ahvaz') :      0 :  10.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Kerman') :      0 :   6.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Mashhad') :      0 :   3.0 : None : False : False :
NonNegativeIntegers
          ('Tehran', 'Tabriz') :      0 :   5.0 : None : False : False :
NonNegativeIntegers
      l : Size=8, Index=Depots*Markets
          Key : Lower : Value : Upper : Fixed : Stale : Domain
          ('Isfahan', 'Ahvaz') :      0 :   1.0 :      1 : False : False : Binary
          ('Isfahan', 'Kerman') :      0 :   1.0 :      1 : False : False : Binary
          ('Isfahan', 'Mashhad') :      0 :   1.0 :      1 : False : False : Binary
          ('Isfahan', 'Tabriz') :      0 :   1.0 :      1 : False : False : Binary
          ('Tehran', 'Ahvaz') :      0 :   1.0 :      1 : False : False : Binary

```

```

      ('Tehran', 'Kerman') :      0 :   1.0 :      1 : False : False : Binary
      ('Tehran', 'Mashhad') :      0 :   1.0 :      1 : False : False : Binary
      ('Tehran', 'Tabriz') :      0 :   1.0 :      1 : False : False : Binary
d : Size=2, Index={1, 2}
  Key : Lower : Value : Upper : Fixed : Stale : Domain
    1 :      0 : None :      1 : False : True : Binary
    2 :      0 : None :      1 : False : True : Binary
R : Size=4, Index=Alloys*{1, 2}
  Key      : Lower : Value : Upper : Fixed : Stale : Domain
  ('A', 1) :      0 :      0 : None : False : True : NonNegativeReals
  ('A', 2) :      0 :      0 : None : False : True : NonNegativeReals
  ('B', 1) :      0 :      0 : None : False : True : NonNegativeReals
  ('B', 2) :      0 :      0 : None : False : True : NonNegativeReals

```

Objectives:

```

revenue : Size=1, Index=None, Active=True
  Key : Active : Value
  None : True : 1593740.3030303027

```

Constraints:

```

Max_extracted_ore_limit : Size=3
  Key : Lower : Body : Upper
    1 : None : 560.0 : 560
    2 : None : 1000.0 : 1000
    3 : None : 1440.0 : 1440
Alloy_sum_limit : Size=2
  Key : Lower : Body : Upper
    A : None : 2.9558577807620168e-12 : 0.0
    B : None : 6.821210263296962e-13 : 0.0
Metal_sum_limit_Z : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 0.0 : 0.0
    3 : None : -576.969696969697 : 0.0
Metal_sum_limit_F : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 0.0 : 0.0
    3 : None : 0.0 : 0.0
Metal_sum_limit_C : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 2.984279490192421e-13 : 0.0
    3 : None : -72.0 : 0.0
Metal_sum_limit_A : Size=3
  Key : Lower : Body : Upper
    1 : None : 0.0 : 0.0
    2 : None : 0.0 : 0.0

```

```

3 : None : 0.0 : 0.0
Metal_in_alloy_limit_A_Z_f : Size=1
Key : Lower : Body : Upper
None : None : -515.69696969697 : 0.0
Metal_in_alloy_limit_A_Z_t : Size=1
Key : Lower : Body : Upper
None : None : -729.393939393942 : 0.0
Metal_in_alloy_limit_A_C_f : Size=1
Key : Lower : Body : Upper
None : None : -184.666666666667 : 0.0
Metal_in_alloy_limit_A_C_t : Size=1
Key : Lower : Body : Upper
None : None : -1371.696969696973 : 0.0
Metal_in_alloy_limit_A_A_f : Size=1
Key : Lower : Body : Upper
None : None : 2.0463630789890885e-12 : 0.0
Metal_in_alloy_limit_A_A_t : Size=1
Key : Lower : Body : Upper
None : None : -700.3636363636399 : 0.0
Metal_in_alloy_limit_A_F_f : Size=1
Key : Lower : Body : Upper
None : None : 0.0 : 0.0
Metal_in_alloy_limit_A_F_t : Size=1
Key : Lower : Body : Upper
None : None : -389.09090909091 : 0.0
Metal_in_alloy_limit_B_Z_f : Size=1
Key : Lower : Body : Upper
None : None : -133.333333333333 : 0.0
Metal_in_alloy_limit_B_Z_t : Size=1
Key : Lower : Body : Upper
None : None : -533.333333333339 : 0.0
Metal_in_alloy_limit_B_C_f : Size=1
Key : Lower : Body : Upper
None : None : 1.1368683772161603e-13 : 0.0
Metal_in_alloy_limit_B_C_t : Size=1
Key : Lower : Body : Upper
None : None : -433.333333333336 : 0.0
Metal_in_alloy_limit_B_A_f : Size=1
Key : Lower : Body : Upper
None : None : 0.0 : 0.0
Metal_in_alloy_limit_B_A_t : Size=1
Key : Lower : Body : Upper
None : None : -466.6666666666686 : 0.0
Metal_in_alloy_limit_B_F_f : Size=1
Key : Lower : Body : Upper
None : None : 1.7053025658242404e-13 : 0.0
Metal_in_alloy_limit_B_F_t : Size=1
Key : Lower : Body : Upper

```



```

None : None : -166.66666666666686 : 0.0
Export_from_main_fac_limit : Size=2
  Key : Lower : Body : Upper
    A : None : 0.0 : 0.0
    B : None : 5.684341886080802e-14 : 0.0
buy_from_fac_limit_f : Size=2
  Key : Lower : Body : Upper
    1 : None : -576.969696969697 : 0.0
    2 : None : 0.0 : 0.0
buy_from_fac_limit_t : Size=2
  Key : Lower : Body : Upper
    1 : None : -2423.030303030303 : 0.0
    2 : None : 0.0 : 0.0
container_limit : Size=6
  Key : Lower : Body : Upper
    (1, 'Isfahan') : None : -523.030303030303 : 0.0
    (1, 'Tehran') : None : 0.0 : 0.0
    (2, 'Isfahan') : None : 0.0 : 0.0
    (2, 'Tehran') : None : 0.0 : 0.0
    ('Main', 'Isfahan') : None : -76.96969696969308 : 0.0
    ('Main', 'Tehran') : None : 0.0 : 0.0
transportation_limit_t : Size=6
  Key : Lower : Body : Upper
    (1, 'Isfahan') : None : -18.0 : 0.0
    (1, 'Tehran') : None : -11.0 : 0.0
    (2, 'Isfahan') : None : 0.0 : 0.0
    (2, 'Tehran') : None : 0.0 : 0.0
    ('Main', 'Isfahan') : None : -2.0 : 0.0
    ('Main', 'Tehran') : None : -15.0 : 0.0
transportation_limit_f : Size=6
  Key : Lower : Body : Upper
    (1, 'Isfahan') : None : -2.0 : 0.0
    (1, 'Tehran') : None : -9.0 : 0.0
    (2, 'Isfahan') : None : 0.0 : 0.0
    (2, 'Tehran') : None : 0.0 : 0.0
    ('Main', 'Isfahan') : None : -13.0 : 0.0
    ('Main', 'Tehran') : None : 0.0 : 0.0
transportation_limit2 : Size=2
  Key : Lower : Body : Upper
    Isfahan : 30.0 : 30.0 : 70.0
    Tehran : 20.0 : 24.0 : 65.0
transp_from_dep_to_market_limit : Size=4
  Key : Lower : Body : Upper
    ('A', 'Isfahan') : None : -3.865352482534945e-12 : 0.0
    ('A', 'Tehran') : None : 0.0 : 0.0
    ('B', 'Isfahan') : None : -2.2737367544323206e-13 : 0.0
    ('B', 'Tehran') : None : 0.0 : 0.0
container_limit2 : Size=8

```

```

Key                : Lower : Body                : Upper
('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
('Isfahan', 'Kerman') : None : 0.0 : 0.0
('Isfahan', 'Mashhad') : None : -3.268496584496461e-13 : 0.0
('Isfahan', 'Tabriz') : None : 0.0 : 0.0
('Tehran', 'Ahvaz') : None : 0.0 : 0.0
('Tehran', 'Kerman') : None : 0.0 : 0.0
('Tehran', 'Mashhad') : None : 0.0 : 0.0
('Tehran', 'Tabriz') : None : 0.0 : 0.0
market_sell_limit_f : Size=8
Key                : Lower : Body : Upper
('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
('Isfahan', 'Kerman') : None : 0.0 : 0.0
('Isfahan', 'Mashhad') : None : 0.0 : 0.0
('Isfahan', 'Tabriz') : None : 0.0 : 0.0
('Tehran', 'Ahvaz') : None : 0.0 : 0.0
('Tehran', 'Kerman') : None : 0.0 : 0.0
('Tehran', 'Mashhad') : None : 0.0 : 0.0
('Tehran', 'Tabriz') : None : 0.0 : 0.0
market_sell_limit_t : Size=8
Key                : Lower : Body : Upper
('Isfahan', 'Ahvaz') : None : 0.0 : 0.0
('Isfahan', 'Kerman') : None : 0.0 : 0.0
('Isfahan', 'Mashhad') : None : 0.0 : 0.0
('Isfahan', 'Tabriz') : None : 0.0 : 0.0
('Tehran', 'Ahvaz') : None : 0.0 : 0.0
('Tehran', 'Kerman') : None : 0.0 : 0.0
('Tehran', 'Mashhad') : None : 0.0 : 0.0
('Tehran', 'Tabriz') : None : 0.0 : 0.0
max_market_demand_limit : Size=8
Key                : Lower : Body                : Upper
('Ahvaz', 'A') : None : 0.0 : 1500.0
('Ahvaz', 'B') : None : 1500.0 : 1500.0
('Kerman', 'A') : None : 800.0 : 800.0
('Kerman', 'B') : None : 300.0 : 1200.0
('Mashhad', 'A') : None : 356.3636363636363 : 600.0
('Mashhad', 'B') : None : 343.6363636363637 : 400.0
('Tabriz', 'A') : None : 400.0 : 1400.0
('Tabriz', 'B') : None : 1100.0 : 1100.0

```

results saved in results.yaml

you can see result file using code below:

```
[1]: !cat results.yaml
```

```

# =====
# = Solver Results                                =
# =====
# -----

```

```

# Problem Information
# -----
Problem:
- Name: x1
  Lower bound: 1439591.6161616163
  Upper bound: 1439600.1414141413
  Number of objectives: 1
  Number of constraints: 97
  Number of variables: 82
  Number of binary variables: 11
  Number of integer variables: 25
  Number of continuous variables: 57
  Number of nonzeros: 304
  Sense: maximize
# -----
# Solver Information
# -----
Solver:
- Status: ok
  Return code: 0
  Message: Model was solved to optimality (subject to tolerances), and an
optimal solution is available.
  Termination condition: optimal
  Termination message: Model was solved to optimality (subject to tolerances),
and an optimal solution is available.
  Wall time: 0.008729934692382812
  Error rc: 0
  Time: 0.11020445823669434
# -----
# Solution Information
# -----
Solution:
- number of solutions: 0
  number of solutions displayed: 0

```

1.5 Sensitivity Analysis

here we produce sensitivity analysis, be aware that, here we should eliminate binaries and integers to make sensitivity analysis, because glpk does not work with MIP(Mixed Integer Problem) problems, we will use this file later on.

```
[2]: !glpsol -m model.lp --lp --ranges sensit.sen
```

```

GLPSOL--GLPK LP/MIP Solver 5.0
Parameter(s) specified in the command line:
  -m model.lp --lp --ranges sensit.sen
Reading problem data from 'model.lp'...
107 rows, 88 columns, 342 non-zeros

```

```

808 lines were read
GLPK Simplex Optimizer 5.0
107 rows, 88 columns, 342 non-zeros
Preprocessing...
99 rows, 88 columns, 324 non-zeros
Scaling...
  A: min|aij| = 5.000e-02  max|aij| = 1.000e+09  ratio = 2.000e+10
GM: min|aij| = 1.160e-01  max|aij| = 8.621e+00  ratio = 7.433e+01
EQ: min|aij| = 1.350e-02  max|aij| = 1.000e+00  ratio = 7.408e+01
Constructing initial basis...
Size of triangular part is 99
   0: obj = -0.000000000e+00  inf = 1.586e+03 (2)
  10: obj = -2.613400000e+05  inf = 0.000e+00 (0)
* 108: obj = 1.660813370e+06  inf = 6.698e-11 (0)
OPTIMAL LP SOLUTION FOUND
Time used: 0.0 secs
Memory used: 0.2 Mb (197469 bytes)
Write sensitivity analysis report to 'sensit.sen'...

```

1.5.1 Sensit file

to see sensit.sen, we run code below:

```
[9]: !cat sensit.sen
```

```

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Page 1

```

```

Problem:
Objective: revenue = 1660813.37 (MAXimum)

```

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value at	Limiting				
range	break point	variable		Marginal	Upper bound	range

1	c_u_Max_extracted_ore_limit(1)_					
		NU	560.00000	.	-Inf	471.42857
-209.57253	1.64225e+06	c_u_max_market_demand_limit(Mashhad_B)_		209.57253	560.00000	628.57143
+Inf	1.67518e+06	g(B_Isfahan_Mashhad)				
2	c_u_Max_extracted_ore_limit(2)_					
		NU	1000.00000	.	-Inf	896.66667
-325.65010	1.62716e+06	c_u_max_market_demand_limit(Mashhad_B)_		325.65010	1000.00000	1077.74879
+Inf	1.68613e+06	c_u_discount_limit_4(1)_				

3	c_u_Max_extracted_ore_limit(3)_	NU	1440.00000	.	-Inf	1316.00000
-127.51434	1.645e+06	c_u_max_market_demand_limit(Mashhad_B)_	127.51434	1440.00000		1536.00000
+Inf	1.67305e+06	g(B_Isfahan_Mashhad)				
4	c_u_Alloy_sum_limit(A)_	NU	.	.	-Inf	-576.96970
.	1.66081e+06	c_u_Metal_sum_limit_Z(3)_	.	.		225.69697
+Inf	1.66081e+06	Z(3_A)				
5	c_u_Alloy_sum_limit(B)_	NU	.	.	-Inf	-533.33333
.	1.66081e+06	c_u_Metal_in_alloy_limit_B_Z_t_	.	.		133.33333
+Inf	1.66081e+06	c_u_Metal_in_alloy_limit_B_Z_f_				
6	c_u_Metal_sum_limit_Z(1)_	NU	.	.	-Inf	-140.00000
.	1.66081e+06	Z(1_A)	.	.		225.69697
+Inf	1.66081e+06	Z(3_A)				
7	c_u_Metal_sum_limit_Z(2)_	NU	.	.	-Inf	-150.00000
.	1.66081e+06	Z(2_A)	.	.		225.69697
+Inf	1.66081e+06	Z(3_A)				
8	c_u_Metal_sum_limit_Z(3)_	BS	-576.96970	576.96970	-Inf	-648.96970
.	1.66081e+06	C(3_A)	.	.		-436.96970
.	1.66081e+06	c_u_Metal_sum_limit_Z(1)_				
9	c_u_Metal_sum_limit_F(1)_	NU	.	.	-Inf	-28.00000
-1097.37778	1.63009e+06	F(1_B)	1097.37778	.		21.42857
+Inf	1.68433e+06	C(2_A)				
10	c_u_Metal_sum_limit_F(2)_	NU	.	.	-Inf	-139.63636
-1097.37778	1.50758e+06	t(B_Main_Isfahan)	1097.37778	.		21.42857
+Inf	1.68433e+06	C(2_A)				

GLPK 5.0 - SENSITIVITY ANALYSIS REPORT

Page 2

Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at Limiting		Marginal	Upper bound	range
range	break point	variable				

11	c_u_Metal_sum_limit_F(3)_	NU	.	.	-Inf	-72.00000
-1097.37778	1.5818e+06	F(3_B)		1097.37778	.	21.42857
+Inf	1.68433e+06	C(2_A)				
12	c_u_Metal_sum_limit_C(1)_	NU	.	.	-Inf	-168.00000
.	1.66081e+06	C(1_A)		.	.	225.69697
+Inf	1.66081e+06	Z(3_A)				
13	c_u_Metal_sum_limit_C(2)_	NU	.	.	-Inf	-16.66667
.	1.66081e+06	C(2_A)		.	.	225.69697
+Inf	1.66081e+06	Z(3_A)				
14	c_u_Metal_sum_limit_C(3)_	BS	-72.00000	72.00000	-Inf	-72.00000
-Inf	+Inf			.	.	153.69697
.	1.66081e+06	C(3_A)				
15	c_u_Metal_sum_limit_A(1)_	NU	.	.	-Inf	-31.00000
-570.58182	1.64313e+06	c_u_max_market_demand_limit(Mashhad_B)_		570.58182	.	24.00000
+Inf	1.67451e+06	g(B_Isfahan_Mashhad)				
16	c_u_Metal_sum_limit_A(2)_	NU	.	.	-Inf	-31.00000
-570.58182	1.64313e+06	c_u_max_market_demand_limit(Mashhad_B)_		570.58182	.	24.00000
+Inf	1.67451e+06	g(B_Isfahan_Mashhad)				

```

17 c_u_Metal_sum_limit_A(3)_
    NU      .      .      -Inf      -31.00000
-570.58182  1.64313e+06 c_u_max_market_demand_limit(Mashhad_B)_
    570.58182      .      24.00000
+Inf  1.67451e+06 g(B_Isfahan_Mashhad)

```

```

18 c_u_Metal_in_alloy_limit_A_Z_f_
    BS    -515.69697    515.69697    -Inf    -683.69697
.    1.66081e+06 c_u_Metal_sum_limit_C(1)_
    .      .      -443.69697
.    1.66081e+06 C(3_A)

```

```

19 c_u_Metal_in_alloy_limit_A_Z_t_
    BS    -729.39394    729.39394    -Inf    -801.39394
.    1.66081e+06 C(3_A)
.      .      -561.39394
.    1.66081e+06 c_u_Metal_sum_limit_C(1)_

```

```

20 c_u_Metal_in_alloy_limit_A_C_f_
    BS    -184.66667    184.66667    -Inf    -256.66667
.    1.66081e+06 C(3_A)
.      .      -16.66667
.    1.66081e+06 c_u_Metal_sum_limit_C(1)_

```

GLPK 5.0 - SENSITIVITY ANALYSIS REPORT

Page 3

Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

```

-----
-----

```

```

21 c_u_Metal_in_alloy_limit_A_C_t_
    BS    -1371.69697    1371.69697    -Inf    -1539.69697
.    1.66081e+06 c_u_Metal_sum_limit_C(1)_
    .      .      -1299.69697
.    1.66081e+06 C(3_A)

```

```

22 c_u_Metal_in_alloy_limit_A_A_f_
    NU      .      .      -Inf    -31.00000
-570.58182  1.64313e+06 c_u_max_market_demand_limit(Mashhad_B)_
    570.58182      .      24.00000
+Inf  1.67451e+06 g(B_Isfahan_Mashhad)

```

23	c_u_Metal_in_alloy_limit_A_A_t_	BS	-700.36364	700.36364	-Inf	-700.36364
-Inf		+Inf				
				.	.	-644.00000
313.82000	1.44103e+06	c_u_Metal_in_alloy_limit_A_A_f_				
24	c_u_Metal_in_alloy_limit_A_F_f_	BS	.	.	-Inf	-28.00000
-1097.37778	1.66081e+06	F(1_A)				
			.	.		.
+Inf	1.66081e+06					
25	c_u_Metal_in_alloy_limit_A_F_t_	BS	-389.09091	389.09091	-Inf	-389.09091
-Inf		+Inf				
			.	.		-361.09091
1097.37778	1.23383e+06	F(1_A)				
26	c_u_Metal_in_alloy_limit_B_Z_f_	BS	-133.33333	133.33333	-Inf	-666.66667
.	1.66081e+06	c_u_Alloy_sum_limit(B)_		.	.	-116.66667
.	1.66081e+06	c_u_Metal_in_alloy_limit_B_C_f_				
27	c_u_Metal_in_alloy_limit_B_Z_t_	BS	-533.33333	533.33333	-Inf	-550.00000
.	1.66081e+06	c_u_Metal_in_alloy_limit_B_C_f_		.	.	43.63636
.	1.66081e+06	c_u_Alloy_sum_limit(B)_				
28	c_u_Metal_in_alloy_limit_B_C_f_	NU	.	.	-Inf	-16.66667
.	1.66081e+06	C(2_A)		.	.	225.69697
+Inf	1.66081e+06	Z(3_A)				
29	c_u_Metal_in_alloy_limit_B_C_t_	BS	-433.33333	433.33333	-Inf	-433.33333
-Inf		+Inf		.	.	-416.66667
.	1.66081e+06	c_u_Metal_in_alloy_limit_B_C_f_				
30	c_u_Metal_in_alloy_limit_B_A_f_	BS	.	.	-Inf	-31.00000
-570.58182	1.66081e+06	A(1_B)		.	.	.
+Inf	1.66081e+06					

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

31	c_u_Metal_in_alloy_limit_B_A_t_					
		BS	-466.66667	466.66667	-Inf	-466.66667
-Inf	+Inf					
570.58182	1.39454e+06	A(1_B)		.	.	-435.66667
32	c_u_Metal_in_alloy_limit_B_F_f_					
		NU	.	.	-Inf	-92.30769
-1097.37778	1.55952e+06	c_u_Metal_in_alloy_limit_B_Z_f_		1097.37778	.	21.42857
+Inf	1.68433e+06	C(2_A)				
33	c_u_Metal_in_alloy_limit_B_F_t_					
		BS	-166.66667	166.66667	-Inf	-166.66667
-Inf	+Inf					
705.45714	1.54324e+06	c_u_Metal_in_alloy_limit_B_F_f_		.	.	-23.07692
34	c_u_Export_from_main_fac_limit(A)_					
		NU	.	.	-Inf	-56.36364
-313.82000	1.64313e+06	c_u_max_market_demand_limit(Mashhad_B)_		313.82000	.	43.63636
+Inf	1.67451e+06	g(B_Isfahan_Mashhad)				
35	c_u_Export_from_main_fac_limit(B)_					
		NU	.	.	-Inf	-310.30303
-493.82000	1.50758e+06	t(B_Main_Isfahan)		493.82000	.	76.96345
+Inf	1.69882e+06	c_u_discount_limit_4(1)_				
36	c_u_buy_from_fac_limit_f(1)_					
		BS	-1517.97980	1517.97980	-Inf	-1517.97980
-.42000	1.66145e+06	c_u_container_limit(2_Isfahan)_		.	.	-1414.54545
.06000	1.66072e+06	c_u_transportation_limit_t(1_Tehran)_				

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37 c_u_buy_from_fac_limit_f(2)_
    BS      .      .      -Inf      .
-.26400    1.66081e+06 t(B_2_Tehran)
.03600    1.66081e+06 c_u_transportation_limit_t(2_Isfahan)_

38 c_u_buy_from_fac_limit_t(1)_
    BS      -70.50505    70.50505    -Inf    -329.09091
-.02400    1.66082e+06 c_u_transportation_limit_t(1_Tehran)_
.16800    1.6608e+06 c_u_container_limit(2_Isfahan)_
-70.50505

39 c_u_buy_from_fac_limit_t(2)_
    BS      .      .      -Inf      .
-.01500    1.66081e+06 c_u_transportation_limit_t(2_Isfahan)_
.11000    1.66081e+06 t(B_2_Tehran)

40 c_u_container_limit(1_Tehran)_
    NU      .      .      -Inf    -310.30303
-1.82000    1.66025e+06 t(B_Main_Isfahan)
1.82000    .      84.60606
+Inf    1.66097e+06 c_u_buy_from_fac_limit_t(1)_

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Problem:
Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
41	c_u_container_limit(1_Isfahan)_	BS	-600.00000	600.00000	-Inf	-1223.03030
-2.12000	1.66209e+06	r_l_transportation_limit2(Isfahan)_				-600.00000
.14000	1.66073e+06	c_u_container_limit(2_Isfahan)_				
42	c_u_container_limit(2_Tehran)_	NU	.	.	-Inf	.
-2.40000	1.66081e+06	c_u_transportation_limit_t(2_Tehran)_		2.40000	.	.
+Inf	1.66081e+06	B(2_Tehran)				

43	c_u_container_limit(2_Isfahan)_	NU	.	.	-Inf	.
-.14000	1.66081e+06 c_u_buy_from_fac_limit_f(2)_			.14000	.	.
+Inf	1.66081e+06 c_u_buy_from_fac_limit_t(2)_					
44	c_u_container_limit(Main_Tehran)_	NU	.	.	-Inf	-1188.48485
-2.00000	1.65844e+06 c_u_transportation_limit_t(Main_Tehran)_			2.00000	.	311.51515
+Inf	1.66144e+06 c_u_transportation_limit_f(Main_Tehran)_					
45	c_u_container_limit(Main_Isfahan)_	NU	.	.	-Inf	-84.60606
-.18000	1.6608e+06 c_u_buy_from_fac_limit_t(1)_			.18000	.	623.03030
+Inf	1.66093e+06 c_u_transportation_limit_f(Main_Tehran)_					
46	c_u_transportation_limit_t(1_Tehran)_	NU	.	.	-Inf	-3.10303
-2.00000	1.66081e+06 t(B_Main_Isfahan)			2.00000	.	.84606
+Inf	1.66082e+06 c_u_buy_from_fac_limit_t(1)_					
47	c_u_transportation_limit_t(1_Isfahan)_	NU	.	.	-Inf	-6.23030
-2.00000	1.6608e+06 c_u_transportation_limit_f(Main_Tehran)_			2.00000	.	.84606
+Inf	1.66082e+06 c_u_buy_from_fac_limit_t(1)_					
48	c_u_transportation_limit_t(2_Tehran)_	BS	.	.	-Inf	.
-3.60000	1.66081e+06 c_u_transportation_limit_t(2_Isfahan)_			.	.	.
16.50000	1.66081e+06 t(B_2_Tehran)					
49	c_u_transportation_limit_t(2_Isfahan)_	NU	.	.	-Inf	.
-6.00000	1.66081e+06 c_u_transportation_limit_f(2_Isfahan)_			6.00000	.	.
+Inf	1.66081e+06 c_u_buy_from_fac_limit_t(2)_					
50	c_u_transportation_limit_t(Main_Tehran)_	BS	-11.88485	11.88485	-Inf	-15.00000
-4.00000	1.66086e+06 c_u_transportation_limit_t(1_Isfahan)_			.	.	-6.00000
.	1.66081e+06 h(Main)					

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at Limiting		Marginal	Upper bound	range
range	break point	variable				

51	c_u_transportation_limit_t(Main_Isfahan)_					
		BS	-5.88485	5.88485	-Inf	-7.43636
-4.00000	1.66084e+06	c_u_transportation_limit_t(1_Tehran)_		.	.	6.00000
.	1.66081e+06	h(Main)				
52	c_u_transportation_limit_f(1_Tehran)_					
		BS	-10.58990	10.58990	-Inf	-12.66667
-6.00000	1.66088e+06	c_u_transportation_limit_t(1_Isfahan)_		.	.	-8.52121
3.00000	1.66078e+06	c_u_transportation_limit_t(1_Tehran)_				
53	c_u_transportation_limit_f(1_Isfahan)_					
		BS	-10.58990	10.58990	-Inf	-11.62424
-6.00000	1.66088e+06	c_u_transportation_limit_t(1_Tehran)_		.	.	-6.43636
3.00000	1.66078e+06	c_u_transportation_limit_t(1_Isfahan)_				
54	c_u_transportation_limit_f(2_Tehran)_					
		BS	.	.	-Inf	.
-33.00000	1.66081e+06	t(B_2_Tehran)		.	.	.
18.00000	1.66081e+06	c_u_transportation_limit_t(2_Isfahan)_				
55	c_u_transportation_limit_f(2_Isfahan)_					
		BS	.	.	-Inf	.
-21.00000	1.66081e+06	c_u_container_limit(2_Isfahan)_		.	.	.
18.00000	1.66081e+06	c_u_transportation_limit_t(2_Isfahan)_				
56	c_u_transportation_limit_f(Main_Tehran)_					
		BS	-3.11515	3.11515	-Inf	-4.58636
.	1.66081e+06	h(Main)		.	.	2.00000
4.00000	1.6608e+06	c_u_transportation_limit_t(1_Isfahan)_				

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57 c_u_transportation_limit_f(Main_Isfahan)_
      BS      -9.11515      9.11515      -Inf      -10.58636
.      1.66081e+06 h(Main)
.
.
-7.56364
4.00000      1.66078e+06 c_u_transportation_limit_t(1_Tehran)_

58 r_l_transportation_limit2(Tehran)_
      BS      24.00000      -4.00000      20.00000      23.56364
-18318.00000      1.22118e+06 l(Tehran_Tabriz)
.
+Inf      27.10303
182.00000      1.66518e+06 c_u_container_limit(1_Tehran)_

59 r_u_transportation_limit2(Tehran)_
      BS      24.00000      41.00000      -Inf      23.56364
-18318.00000      1.22118e+06 l(Tehran_Tabriz)
.
65.00000      27.10303
182.00000      1.66518e+06 c_u_container_limit(1_Tehran)_

60 r_l_transportation_limit2(Isfahan)_
      NL      30.00000      .      30.00000      29.15394
-Inf      1.66099e+06 c_u_buy_from_fac_limit_t(1)_
      -212.00000      +Inf      36.23030
212.00000      1.65949e+06 c_u_transportation_limit_f(Main_Tehran)_

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
61	r_u_transportation_limit2(Isfahan)_	BS	30.00000	40.00000	-Inf	30.00000
-Inf	-Inf				70.00000	36.23030
212.00000	1.66717e+06	r_l_transportation_limit2(Isfahan)_				
62	c_u_transp_from_dep_to_market_limit(A_Tehran)_	NU	.	.	-Inf	-56.36364
-315.82000	1.64301e+06	c_u_max_market_demand_limit(Mashhad_B)_		315.82000	.	43.63636
+Inf	1.67459e+06	g(B_Isfahan_Mashhad)				

63	c_u_transp_from_dep_to_market_limit(A_Isfahan)_				
	NU	.	.	-Inf	-56.36364
-314.00000	1.64312e+06	c_u_max_market_demand_limit(Mashhad_B)_			
		314.00000	.		43.63636
+Inf	1.67452e+06	g(B_Isfahan_Mashhad)			
64	c_u_transp_from_dep_to_market_limit(B_Tehran)_				
	NU	.	.	-Inf	-310.30303
-495.82000	1.50696e+06	t(B_Main_Isfahan)			
		495.82000	.		76.96345
+Inf	1.69897e+06	c_u_discount_limit_4(1)_			
65	c_u_transp_from_dep_to_market_limit(B_Isfahan)_				
	NU	.	.	-Inf	-70.50505
-494.00000	1.62598e+06	c_u_buy_from_fac_limit_t(1)_			
		494.00000	.		76.96345
+Inf	1.69883e+06	c_u_discount_limit_4(1)_			
66	c_u_container_limit2(Tehran_Mashhad)_				
	NU	.	.	-Inf	-76.96345
-204.18000	1.6451e+06	c_u_discount_limit_4(1)_			
		204.18000	.		56.36364
+Inf	1.67232e+06	c_u_max_market_demand_limit(Mashhad_B)_			
67	c_u_container_limit2(Tehran_Kerman)_				
	NU	.	.	-Inf	-76.96345
-194.18000	1.64587e+06	c_u_discount_limit_4(1)_			
		194.18000	.		310.30303
+Inf	1.72107e+06	t(B_Main_Isfahan)			
68	c_u_container_limit2(Tehran_Ahvaz)_				
	NU	.	.	-Inf	-76.96345
-234.18000	1.64279e+06	c_u_discount_limit_4(1)_			
		234.18000	.		.
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_			
69	c_u_container_limit2(Tehran_Tabriz)_				
	NU	.	.	-Inf	-43.63636
-184.18000	1.65278e+06	g(B_Isfahan_Mashhad)			
		184.18000	.		56.36364
+Inf	1.67119e+06	c_u_max_market_demand_limit(Mashhad_B)_			
70	c_u_container_limit2(Isfahan_Mashhad)_				
	NU	.	.	-Inf	-43.63636
-206.00000	1.65182e+06	g(B_Isfahan_Mashhad)			
		206.00000	.		56.36364
+Inf	1.67242e+06	c_u_max_market_demand_limit(Mashhad_B)_			

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

71	c_u_container_limit2(Isfahan_Kerman)_	NU	.	.	-Inf	-76.96345
-196.00000	1.64573e+06	c_u_discount_limit_4(1)_		196.00000	.	70.50505
+Inf	1.67463e+06	c_u_buy_from_fac_limit_t(1)_				
72	c_u_container_limit2(Isfahan_Ahvaz)_	NU	.	.	-Inf	-76.96345
-236.00000	1.64265e+06	c_u_discount_limit_4(1)_		236.00000	.	.
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_				
73	c_u_container_limit2(Isfahan_Tabriz)_	NU	.	.	-Inf	-43.63636
-186.00000	1.6527e+06	g(B_Isfahan_Mashhad)		186.00000	.	56.36364
+Inf	1.6713e+06	c_u_max_market_demand_limit(Mashhad_B)_				
74	c_u_market_sell_limit_f(Tehran_Mashhad)_	BS	.	.	-Inf	.
-Inf	1.66081e+06					.76963
20308.00000	1.66081e+06	c_u_market_sell_limit_t(Tehran_Mashhad)_				
75	c_u_market_sell_limit_f(Tehran_Kerman)_	BS	.	.	-Inf	.
-Inf	1.66081e+06					.76963
19333.00000	1.66081e+06	c_u_market_sell_limit_t(Tehran_Kerman)_				
76	c_u_market_sell_limit_f(Tehran_Ahvaz)_	BS	.	.	-Inf	.
-Inf	1.66081e+06					.76963
23298.00000	1.66081e+06	c_u_market_sell_limit_t(Tehran_Ahvaz)_				

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77 c_u_market_sell_limit_f(Tehran_Tabriz)_
      BS      .      .      -Inf      .
-Inf  1.66081e+06      .      .      .43636
18318.00000  1.66081e+06 c_u_market_sell_limit_t(Tehran_Tabriz)_

78 c_u_market_sell_limit_f(Isfahan_Mashhad)_
      BS      .      .      -Inf      .
-Inf  1.66081e+06      .      .      .43636
20500.00000  1.66081e+06 c_u_market_sell_limit_t(Isfahan_Mashhad)_

79 c_u_market_sell_limit_f(Isfahan_Kerman)_
      BS      .      .      -Inf      .
-Inf  1.66081e+06      .      .      .76963
19500.00000  1.66081e+06 c_u_market_sell_limit_t(Isfahan_Kerman)_

80 c_u_market_sell_limit_f(Isfahan_Ahvaz)_
      BS      .      .      -Inf      .
-Inf  1.66081e+06      .      .      .76963
23490.00000  1.66081e+06 c_u_market_sell_limit_t(Isfahan_Ahvaz)_

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
81	c_u_market_sell_limit_f(Isfahan_Tabriz)_	BS	.	.	-Inf	.
-Inf	1.66081e+06					.43636
18510.00000	1.66081e+06	c_u_market_sell_limit_t(Isfahan_Tabriz)_				
82	c_u_market_sell_limit_t(Tehran_Mashhad)_	NU	.	.	-Inf	.
-20308.00000	1.66081e+06	c_u_market_sell_limit_f(Tehran_Mashhad)_				.56364
	20308.00000					
+Inf	1.67226e+06	c_u_max_market_demand_limit(Mashhad_B)_				

83	c_u_market_sell_limit_t(Tehran_Kerman)_				
	NU	.	.	-Inf	.
-19333.00000	1.66081e+06	c_u_market_sell_limit_f(Tehran_Kerman)_			
		19333.00000	.		3.10303
+Inf	1.7208e+06	t(B_Main_Isfahan)			
84	c_u_market_sell_limit_t(Tehran_Ahvaz)_				
	NU	.	.	-Inf	.
-23298.00000	1.66081e+06	c_u_market_sell_limit_f(Tehran_Ahvaz)_			
		23298.00000	.		.
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_			
85	c_u_market_sell_limit_t(Tehran_Tabriz)_				
	NU	.	.	-Inf	.
-18318.00000	1.66081e+06	c_u_market_sell_limit_f(Tehran_Tabriz)_			
		18318.00000	.		.56364
+Inf	1.67114e+06	c_u_max_market_demand_limit(Mashhad_B)_			
86	c_u_market_sell_limit_t(Isfahan_Mashhad)_				
	NU	.	.	-Inf	.
-20500.00000	1.66081e+06	c_u_market_sell_limit_f(Isfahan_Mashhad)_			
		20500.00000	.		.56364
+Inf	1.67237e+06	c_u_max_market_demand_limit(Mashhad_B)_			
87	c_u_market_sell_limit_t(Isfahan_Kerman)_				
	NU	.	.	-Inf	.
-19500.00000	1.66081e+06	c_u_market_sell_limit_f(Isfahan_Kerman)_			
		19500.00000	.		.70505
+Inf	1.67456e+06	c_u_buy_from_fac_limit_t(1)_			
88	c_u_market_sell_limit_t(Isfahan_Ahvaz)_				
	NU	.	.	-Inf	.
-23490.00000	1.66081e+06	c_u_market_sell_limit_f(Isfahan_Ahvaz)_			
		23490.00000	.		.
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_			
89	c_u_market_sell_limit_t(Isfahan_Tabriz)_				
	NU	.	.	-Inf	.
-18510.00000	1.66081e+06	c_u_market_sell_limit_f(Isfahan_Tabriz)_			
		18510.00000	.		.56364
+Inf	1.67125e+06	c_u_max_market_demand_limit(Mashhad_B)_			
90	c_u_max_market_demand_limit(Mashhad_A)_				
	BS	356.36364	243.63636	-Inf	300.00000
-30.00000	1.65012e+06	c_u_max_market_demand_limit(Tabriz_B)_			
		.	600.00000		400.00000
30.00000	1.6715e+06	c_u_max_market_demand_limit(Kerman_A)_			

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at Limiting		Marginal	Upper bound	range
range	break point	variable				

91	c_u_max_market_demand_limit(Mashhad_B)_					
		BS	343.63636	56.36364	-Inf	300.00000
-30.00000	1.6505e+06	c_u_max_market_demand_limit(Kerman_A)_			400.00000	700.00000
30.00000	1.67112e+06	c_u_max_market_demand_limit(Tabriz_B)_				
92	c_u_max_market_demand_limit(Kerman_A)_					
		NU	800.00000	.	-Inf	756.36364
-30.00000	1.6595e+06	g(B_Isfahan_Mashhad)				
			30.00000	800.00000		856.36364
+Inf	1.6625e+06	c_u_max_market_demand_limit(Mashhad_B)_				
93	c_u_max_market_demand_limit(Kerman_B)_					
		BS	300.00000	900.00000	-Inf	223.03655
-193.33000	1.60281e+06	l(Tehran_Kerman)			1200.00000	343.63636
30.00000	1.66981e+06	c_u_max_market_demand_limit(Kerman_A)_				
94	c_u_max_market_demand_limit(Ahvaz_A)_					
		BS	.	1500.00000	-Inf	.
-Inf	1.66081e+06					
			.	1500.00000		56.36364
60.00000	1.66081e+06	g(A_Isfahan_Ahvaz)				
95	c_u_max_market_demand_limit(Ahvaz_B)_					
		BS	1500.00000	.	-Inf	1443.63636
-60.00000	1.57081e+06	g(A_Isfahan_Ahvaz)				
			.	1500.00000		1500.00000
+Inf	+Inf					
96	c_u_max_market_demand_limit(Tabriz_A)_					
		BS	400.00000	1000.00000	-Inf	356.36364
-183.18000	1.58754e+06	l(Tehran_Tabriz)			1400.00000	456.36364
30.00000	1.67281e+06	c_u_max_market_demand_limit(Tabriz_B)_				

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97 c_u_max_market_demand_limit(Tabriz_B)_
      NU      1100.00000      .      -Inf      1043.63636
-30.00000      1.65912e+06 c_u_max_market_demand_limit(Mashhad_B)_
                                30.00000      1100.00000      1143.63636
+Inf      1.66212e+06 g(B_Isfahan_Mashhad)

98 c_u_discount_limit_1(1)_
      NU      2500.00000      .      -Inf      76.96970
.      1.66081e+06 d(1)
.      .      2500.00000      2576.96325
+Inf      1.66081e+06 c_u_discount_limit_4(1)_

99 c_u_discount_limit_1(2)_
      BS      .      3000.00000      -Inf      .
-Inf      1.66081e+06
.      .      3000.00000      .
19.14006      1.66081e+06 c_u_discount_limit_2(2)_

100 c_u_discount_limit_2(1)_
      BS      -2500.00000      2500.00000      -Inf      -2500.00000
-Inf      +Inf
.      .      .      -76.96970
.      1.66081e+06 c_u_discount_limit_1(1)_

```

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Page 11

Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Row name	St	Activity	Slack	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

101	c_u_discount_limit_2(2)_					
		NU	.	.	-Inf	.
-19.14006	1.66081e+06	c_u_buy_from_fac_limit_f(2)_		19.14006	.	.
+Inf	1.66081e+06	c_u_buy_from_fac_limit_t(2)_				
102	c_u_discount_limit_3(1_A)_					
		NU	.	.	-Inf	.
-18.75000	1.66081e+06	R(A_1)		18.75000	.	3.07853e+07
+Inf	5.78885e+08	c_u_discount_limit_4(1)_				

```

103 c_u_discount_limit_3(1_B)_
      NU      .      .      -Inf      -2576.96970
-26.00000    1.59381e+06 R(B_1)
                        26.00000      .      3.07853e+07
+Inf    8.02079e+08 c_u_discount_limit_4(1)_

104 c_u_discount_limit_3(2_A)_
      NU      .      .      -Inf      .
-19.49994    1.66081e+06 R(A_2)
                        19.49994      .      .
+Inf    1.66081e+06 c_u_buy_from_fac_limit_f(2)_

105 c_u_discount_limit_3(2_B)_
      NU      .      .      -Inf      .
-26.99994    1.66081e+06 R(B_2)
                        26.99994      .      .
+Inf    1.66081e+06 c_u_buy_from_fac_limit_f(2)_

106 c_u_discount_limit_4(1)_
      BS -3.07853e+07  3.07853e+07      -Inf      -9.99997e+08
.      1.66081e+06 c_u_discount_limit_1(1)_
                        .      .      -3.07853e+07
.00005    1.65934e+06 c_u_discount_limit_4(2)_

107 c_u_discount_limit_4(2)_
      NU      .      .      -Inf      .
-.00006    1.66081e+06 c_u_buy_from_fac_limit_f(2)_
                        .00006      .      .
+Inf    1.66081e+06 c_u_buy_from_fac_limit_t(2)_

```

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Page 12

Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
1	g(A_Tehran_Mashhad)					
		NL		520.00000		-43.63636
-Inf	1.66081e+06	g(B_Isfahan_Mashhad)				
					+Inf	300.00000
520.00000	1.66081e+06	g(B_Tehran_Mashhad)				

2 g(A_Tehran_Kerman)					
	BS	300.00000	540.00000	.	256.36364
510.00000	1.65181e+06	c_u_max_market_demand_limit(Kerman_A)_			
			.	+Inf	600.00000
540.00000	1.66081e+06	g(B_Isfahan_Kerman)			
3 g(A_Tehran_Ahvaz)					
	NL	.	490.00000	.	.
-Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_			
			-60.00000	+Inf	56.36364
550.00000	1.65743e+06	c_u_max_market_demand_limit(Mashhad_B)_			
4 g(A_Tehran_Tabriz)					
	NL	.	500.00000	.	-155.15152
-Inf	1.66081e+06	t(B_Main_Isfahan)			
			.	+Inf	400.00000
500.00000	1.66081e+06	g(A_Isfahan_Tabriz)			
5 g(A_Isfahan_Mashhad)					
	BS	356.36364	520.00000	.	56.36364
520.00000	1.66081e+06	g(A_Tehran_Mashhad)			
			.	+Inf	400.00000
550.00000	1.6715e+06	c_u_max_market_demand_limit(Kerman_A)_			
6 g(A_Isfahan_Kerman)					
	BS	500.00000	540.00000	.	200.00000
540.00000	1.66081e+06	g(B_Isfahan_Kerman)			
			.	+Inf	500.00000
+Inf	+Inf				
7 g(A_Isfahan_Ahvaz)					
	NL	.	490.00000	.	.
-Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_			
			-60.00000	+Inf	56.36364
550.00000	1.65743e+06	c_u_max_market_demand_limit(Mashhad_B)_			
8 g(A_Isfahan_Tabriz)					
	BS	400.00000	500.00000	.	-100.00000
500.00000	1.66081e+06	g(A_Tehran_Tabriz)			
			.	+Inf	456.36364
530.00000	1.67281e+06	c_u_max_market_demand_limit(Tabriz_B)_			
9 g(B_Tehran_Mashhad)					
	BS	300.00000	700.00000	.	-56.36364
700.00000	1.66081e+06	g(A_Tehran_Mashhad)			
			.	+Inf	300.00000
+Inf	+Inf				

```

10 g(B_Tehran_Kerman)
      BS      300.00000      690.00000      .      -200.00000
690.00000      1.66081e+06 g(B_Isfahan_Kerman)
      .      +Inf      343.63636
720.00000      1.66981e+06 c_u_max_market_demand_limit(Kerman_A)_

```

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Page 13

Problem:
Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting	Marginal	Upper bound	range
range	break point	variable				

11 g(B_Tehran_Ahvaz)						
		BS	1000.00000	730.00000	.	943.63636
670.00000	1.60081e+06	g(A_Tehran_Ahvaz)		.	+Inf	1000.00000
+Inf	+Inf					
12 g(B_Tehran_Tabriz)						
		BS	500.00000	710.00000	.	100.00000
710.00000	1.66081e+06	g(A_Tehran_Tabriz)		.	+Inf	500.00000
+Inf	+Inf					
13 g(B_Isfahan_Mashhad)						
		BS	43.63636	700.00000	.	-111.51515
670.00000	1.6595e+06	c_u_max_market_demand_limit(Kerman_A)_		.	+Inf	343.63636
700.00000	1.66081e+06	g(A_Tehran_Mashhad)				
14 g(B_Isfahan_Kerman)						
		NL	.	690.00000	.	-155.15152
-Inf	1.66081e+06	t(B_Main_Isfahan)		.	+Inf	300.00000
690.00000	1.66081e+06	g(B_Tehran_Kerman)				
15 g(B_Isfahan_Ahvaz)						
		BS	500.00000	730.00000	.	443.63636
670.00000	1.63081e+06	g(A_Isfahan_Ahvaz)		.	+Inf	500.00000
+Inf	+Inf					

```

16 g(B_Isfahan_Tabriz)
      BS      600.00000      710.00000      .      543.63636
680.00000      1.64281e+06 c_u_max_market_demand_limit(Tabriz_B)_
      .      +Inf      1000.00000
710.00000      1.66081e+06 g(A_Tehran_Tabriz)

```

```

17 Extracted_ore(1)
      BS      560.00000      -45.00000      .      471.42857
-254.57253      1.54345e+06 c_u_Max_extracted_ore_limit(1)_
      .      +Inf      560.00000
+Inf      +Inf

```

```

18 Extracted_ore(2)
      BS      1000.00000      -65.00000      .      896.66667
-390.65010      1.33516e+06 c_u_Max_extracted_ore_limit(2)_
      .      +Inf      1000.00000
+Inf      +Inf

```

```

19 Extracted_ore(3)
      BS      1440.00000      -70.00000      .      1316.00000
-197.51434      1.47719e+06 c_u_Max_extracted_ore_limit(3)_
      .      +Inf      1440.00000
+Inf      +Inf

```

```

20 t(A_1_Tehran)
      NL      .      -375.00000      .      .
-Inf      1.66081e+06 R(A_1)
      -42.25000      +Inf      43.63636
-332.75000      1.65897e+06 g(B_Isfahan_Mashhad)

```

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Problem:
Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

```

-----
21 t(A_1_Isfahan)
      NL      .      -375.00000      .      .
-Inf      1.66081e+06 R(A_1)
      -42.25000      +Inf      43.63636
-332.75000      1.65897e+06 g(B_Isfahan_Mashhad)

```

22	t(A_2_Tehran)	NL	.	-390.00000	.	.
-Inf	1.66081e+06 R(A_2)			-37.94000	+Inf	.
-352.06000	1.66081e+06 c_u_buy_from_fac_limit_t(2)_					
23	t(A_2_Isfahan)	NL	.	-390.00000	.	.
-Inf	1.66081e+06 R(A_2)			-37.50000	+Inf	.
-352.50000	1.66081e+06 t(B_2_Isfahan)					
24	t(B_1_Tehran)	BS	1588.48485	-520.00000	.	1433.33333
-520.04000	1.66075e+06 c_u_transportation_limit_t(1_Tehran)_			.	+Inf	1900.00000
-519.96000	1.66088e+06 c_u_transportation_limit_t(1_Isfahan)_					
25	t(B_1_Isfahan)	BS	988.48485	-520.00000	.	676.96970
-520.04000	1.66077e+06 c_u_transportation_limit_t(1_Isfahan)_			.	+Inf	1143.63636
-519.96000	1.66085e+06 c_u_transportation_limit_t(1_Tehran)_					
26	t(B_2_Tehran)	NL	.	-540.00000	.	.
-Inf	1.66081e+06 B(2_Tehran)			-.44000	+Inf	.
-539.56000	1.66081e+06 c_u_buy_from_fac_limit_t(2)_					
27	t(B_2_Isfahan)	BS	.	-540.00000	.	.
-540.44000	1.66081e+06 t(B_2_Tehran)			.	+Inf	.
-520.86000	1.66081e+06 c_u_discount_limit_4(2)_					
28	h(1)	BS	.52949	-120.00000	.	.52949
-960.00000	1.66037e+06 c_u_container_limit(2_Isfahan)_			.	1.00000	.58121
.	1.66088e+06 c_u_transportation_limit_t(1_Tehran)_					
29	h(2)	BS	.	-90.00000	.	.
-750.00000	1.66081e+06 t(B_2_Tehran)			.	1.00000	.
.	1.66081e+06 c_u_transportation_limit_t(2_Isfahan)_					
30	B(1_Tehran)	BS	15.88485	-180.00000	.	14.33333

-184.00000	1.66075e+06	c_u_transportation_limit_t(1_Tehran)_	.	+Inf	19.00000
-176.00000	1.66088e+06	c_u_transportation_limit_t(1_Isfahan)_	.		

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range

31	B(1_Isfahan)	BS	15.88485	-210.00000	.	12.76970
-214.00000	1.66075e+06	c_u_transportation_limit_t(1_Isfahan)_	.		+Inf	17.43636
-206.00000	1.66088e+06	c_u_transportation_limit_t(1_Tehran)_	.			
32	B(2_Tehran)	BS	.	-240.00000	.	.
-Inf	1.66081e+06		.		+Inf	.
-196.00000	1.66081e+06	t(B_2_Tehran)				
33	B(2_Isfahan)	BS	.	-220.00000	.	.
-264.00000	1.66081e+06	t(B_2_Tehran)	.		+Inf	.
-206.00000	1.66081e+06	c_u_container_limit(2_Isfahan)_				
34	B(Main_Tehran)	BS	8.11515	-200.00000	.	5.00000
-204.00000	1.66078e+06	c_u_transportation_limit_t(1_Isfahan)_	.		+Inf	9.66667
-196.00000	1.66085e+06	c_u_transportation_limit_t(1_Tehran)_				
35	B(Main_Isfahan)	BS	14.11515	-230.00000	.	12.56364
-234.00000	1.66076e+06	c_u_transportation_limit_t(1_Tehran)_	.		+Inf	17.23030
-226.00000	1.66087e+06	c_u_transportation_limit_t(1_Isfahan)_				
36	G(Tehran_Mashhad)	BS	3.00000	-110.00000	.	2.23037
-20418.00000	1.59989e+06	l(Tehran_Mashhad)	.		+Inf	3.00000
+Inf	+Inf					

```

37 G(Tehran_Kerman)
      BS      6.00000      -85.00000      .      5.23037
-19418.00000      1.54482e+06      1(Tehran_Kerman)
      .
+Inf      +Inf      +Inf      6.00000

```

```

38 G(Tehran_Ahvaz)
      BS      10.00000      -120.00000      .      9.23037
-23418.00000      1.42783e+06      1(Tehran_Ahvaz)
      .
+Inf      +Inf      +Inf      10.00000

```

```

39 G(Tehran_Tabriz)
      BS      5.00000      -100.00000      .      4.56364
-18418.00000      1.56922e+06      1(Tehran_Tabriz)
      .
+Inf      +Inf      +Inf      5.00000

```

```

40 G(Isfahan_Mashhad)
      BS      4.00000      -100.00000      .      3.56364
-20600.00000      1.57881e+06      1(Isfahan_Mashhad)
      .
+Inf      +Inf      +Inf      4.00000

```

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Problem:
Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
-----	-----	--	-----	-----	-----	-----
-----	-----	-----	-----	-----	-----	-----

```

41 G(Isfahan_Kerman)
      BS      5.00000      -100.00000      .      4.23037
-19600.00000      1.56331e+06      1(Isfahan_Kerman)
      .
+Inf      +Inf      +Inf      5.00000

```

```

42 G(Isfahan_Ahvaz)
      BS      5.00000      -110.00000      .      4.23037
-23600.00000      1.54336e+06      1(Isfahan_Ahvaz)
      .
+Inf      +Inf      +Inf      5.00000

```

43	G(Isfahan_Tabriz)	BS	10.00000	-90.00000	.	9.56364
-18600.00000	1.47571e+06	l(Isfahan_Tabriz)		.	+Inf	10.00000
+Inf	+Inf					
44	R(A_1)	BS	.	18.75000	.	-Inf
.	1.66081e+06	c_u_discount_limit_3(1_A)_		.	+Inf	43.63636
61.00000	1.66081e+06	t(A_1_Tehran)				
45	R(A_2)	BS	.	19.50000	.	.
.00006	1.66081e+06	c_u_discount_limit_3(2_A)_		.	+Inf	.
57.00000	1.66081e+06	t(A_2_Isfahan)				
46	R(B_1)	BS	2576.96970	26.00000	.	2576.96970
6.86000	1.61149e+06	c_u_discount_limit_4(2)_		.	+Inf	2647.11111
251.42714	2.24173e+06	c_u_Max_extracted_ore_limit(3)_				
47	R(B_2)	BS	.	27.00000	.	.
.00014	1.66081e+06	c_u_discount_limit_3(2_B)_		.	+Inf	.
46.14000	1.66081e+06	c_u_discount_limit_4(2)_				
48	U(A)	BS	1556.36364	.	.	1500.00000
-280.53156	1.2242e+06	c_u_Max_extracted_ore_limit(3)_		.	+Inf	1556.36364
+Inf	+Inf					
49	Z(1_A)	BS	140.00000	.	.	-436.96970
.	1.66081e+06	c_u_Metal_sum_limit_Z(1)_		.	+Inf	140.00000
+Inf	+Inf					
50	Z(2_A)	BS	150.00000	.	.	16.66667
.	1.66081e+06	Z(2_B)		.	+Inf	150.00000
+Inf	+Inf					

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
-----	-----	--	-----	-----	-----	-----
51	Z(3_A)	BS	225.69697	.	.	153.69697
.	1.66081e+06	C(3_A)		.	+Inf	365.69697
.	1.66081e+06	c_u_Metal_sum_limit_Z(1)_		.		
52	C(1_A)	BS	168.00000	.	.	-65.33333
.	1.66081e+06	C(1_B)		.	+Inf	168.00000
+Inf	+Inf					
53	C(2_A)	BS	16.66667	.	.	-168.00000
.	1.66081e+06	c_u_Metal_sum_limit_C(2)_		.	+Inf	184.66667
.	1.66081e+06	C(1_B)		.		
54	C(3_A)	NL	.	.	.	-184.66667
-Inf	1.66081e+06	c_u_Metal_in_alloy_limit_A_C_f_		.	+Inf	72.00000
.	1.66081e+06	c_u_Metal_sum_limit_C(3)_		.		
55	A(1_A)	BS	196.00000	.	.	165.00000
-570.58182	1.54898e+06	A(1_B)		.	+Inf	196.00000
+Inf	+Inf					
56	A(2_A)	BS	300.00000	.	.	269.00000
-570.58182	1.48964e+06	A(2_B)		.	+Inf	300.00000
+Inf	+Inf					
57	A(3_A)	BS	360.00000	.	.	329.00000
-510.05737	1.47719e+06	c_u_Max_extracted_ore_limit(3)_		.	+Inf	360.00000
+Inf	+Inf					
58	F(1_A)	NL
-Inf	1.66081e+06	c_u_Metal_in_alloy_limit_A_F_f_		.	+Inf	28.00000
1097.37778	1.63009e+06	F(1_B)		.		
59	F(2_A)	NL
-Inf	1.66081e+06	c_u_Metal_in_alloy_limit_A_F_f_		.		

```

1097.37778      1.5215e+06 Z(3_A)
-1097.37778      +Inf      126.95455

60 F(3_A)      NL      .      .      .      .
-Inf      1.66081e+06 c_u_Metal_in_alloy_limit_A_F_f_
-1097.37778      +Inf      72.00000

1097.37778      1.5818e+06 F(3_B)

```

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Problem:
Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at Limiting				
range	break point	variable		Marginal	Upper bound	range

61	U(B)	BS	666.66667	.	.	604.44444
-493.82000	1.3316e+06	F(1_A)		.		
				.	+Inf	666.66667
+Inf	+Inf					
62	Z(1_B)	NL	.	.	.	-225.69697
-Inf	1.66081e+06	Z(3_A)		.		
				.	+Inf	133.33333
.	1.66081e+06	Z(3_B)				
63	Z(2_B)	NL	.	.	.	-225.69697
-Inf	1.66081e+06	Z(3_A)		.		
				.	+Inf	133.33333
.	1.66081e+06	Z(3_B)				
64	Z(3_B)	BS	133.33333	.	.	-6.66667
.	1.66081e+06	Z(1_B)		.		
				.	+Inf	666.66667
.	1.66081e+06	c_u_Alloy_sum_limit(B)_				
65	C(1_B)	NL	.	.	.	-16.66667
-Inf	1.66081e+06	C(2_A)		.		
				.	+Inf	168.00000
.	1.66081e+06	C(1_A)				
66	C(2_B)	BS	233.33333	.	.	65.33333
.	1.66081e+06	C(1_B)		.		
				.	+Inf	250.00000

```

.          1.66081e+06 c_u_Metal_in_alloy_limit_B_C_f_

67 C(3_B)      NL      .      .      .      -16.66667
-Inf  1.66081e+06 C(2_A)      .      +Inf      72.00000
.          1.66081e+06 c_u_Metal_sum_limit_C(3)_

68 A(1_B)      NL      .      .      .      .
-Inf  1.66081e+06 c_u_Metal_in_alloy_limit_B_A_f_
      -570.58182      +Inf      31.00000
570.58182  1.64313e+06 c_u_max_market_demand_limit(Mashhad_B)_

69 A(2_B)      NL      .      .      .      .
-Inf  1.66081e+06 c_u_Metal_in_alloy_limit_B_A_f_
      -570.58182      +Inf      31.00000
570.58182  1.64313e+06 c_u_max_market_demand_limit(Mashhad_B)_

70 A(3_B)      NL      .      .      .      .
-Inf  1.66081e+06 c_u_Metal_in_alloy_limit_B_A_f_
      -570.58182      +Inf      31.00000
570.58182  1.64313e+06 c_u_max_market_demand_limit(Mashhad_B)_

```

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
-----	-----	--	-----	-----	-----	-----
71 F(1_B)	BS	28.00000	.	.	-98.95455	
-1097.37778	1.63009e+06	F(1_A)	.	+Inf	28.00000	
+Inf	+Inf					
72 F(2_B)	BS	200.00000	.	.	73.04545	
-1097.37778	1.44134e+06	F(2_A)	.	+Inf	200.00000	
+Inf	+Inf					
73 F(3_B)	BS	72.00000	.	.	-54.95455	
-1097.37778	1.5818e+06	F(3_A)	.	+Inf	72.00000	
+Inf	+Inf					

```

74 t(A_Main_Tehran)
      BS      300.00000      .      .      256.36364
-30.00000      1.65181e+06 c_u_max_market_demand_limit(Kerman_A)_
      .      +Inf      600.00000
.      1.66081e+06 g(A_Tehran_Mashhad)

75 t(A_Main_Isfahan)
      BS      1256.36364      .      .      956.36364
.      1.66081e+06 g(A_Tehran_Mashhad)
      .      +Inf      1300.00000
30.00000      1.6985e+06 c_u_max_market_demand_limit(Kerman_A)_

76 t(B_Main_Tehran)
      BS      511.51515      .      .      211.51515
.      1.66081e+06 g(A_Tehran_Mashhad)
      .      +Inf      666.66667
.04000      1.66083e+06 c_u_transportation_limit_t(1_Tehran)_

77 t(B_Main_Isfahan)
      BS      155.15152      .      .      -639.09091
-.04000      1.66081e+06 c_u_transportation_limit_t(1_Tehran)_
      .      +Inf      455.15152
.      1.66081e+06 g(A_Tehran_Mashhad)

78 h(Main)      NU      1.00000      .      .      .70576
.      1.66081e+06 c_u_transportation_limit_t(Main_Isfahan)_
      .      1.00000      1.62303
+Inf      1.66081e+06 c_u_transportation_limit_f(Main_Tehran)_

79 l(Tehran_Mashhad)
      NU      1.00000      .      .      .74346
-60924.00000      1.64518e+06 c_u_discount_limit_4(1)_
      60924.00000      1.00000      1.18788
+Inf      1.67226e+06 c_u_max_market_demand_limit(Mashhad_B)_

80 l(Tehran_Kerman)
      NU      1.00000      .      .      .87173
-115998.00000      1.64593e+06 c_u_discount_limit_4(1)_
      115998.00000      1.00000      1.51717
+Inf      1.7208e+06 t(B_Main_Isfahan)

```

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Problem:

Objective: revenue = 1660813.37 (MAXimum)

No.	Column name	St	Activity	Obj coef	Lower bound	Activity
Obj coef	Obj value	at	Limiting			
range	break point	variable		Marginal	Upper bound	range
-----	-----	--	-----	-----	-----	-----
-----	-----	-----	-----	-----	-----	-----
81	l(Tehran_Ahvaz)					
		NU	1.00000	.	.	.92304
-232980.00000	1.64288e+06	c_u_discount_limit_4(1)_				
			232980.00000		1.00000	1.00000
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_				
82	l(Tehran_Tabriz)					
		NU	1.00000	.	.	.91273
-91590.00000	1.65282e+06	g(B_Isfahan_Mashhad)				
			91590.00000		1.00000	1.11273
+Inf	1.67114e+06	c_u_max_market_demand_limit(Mashhad_B)_				
83	l(Isfahan_Mashhad)					
		NU	1.00000	.	.	.89091
-82000.00000	1.65187e+06	g(B_Isfahan_Mashhad)				
			82000.00000		1.00000	1.14091
+Inf	1.67237e+06	c_u_max_market_demand_limit(Mashhad_B)_				
84	l(Isfahan_Kerman)					
		NU	1.00000	.	.	.84607
-97500.00000	1.64581e+06	c_u_discount_limit_4(1)_				
			97500.00000		1.00000	1.14101
+Inf	1.67456e+06	c_u_buy_from_fac_limit_t(1)_				
85	l(Isfahan_Ahvaz)					
		NU	1.00000	.	.	.84607
-117450.00000	1.64273e+06	c_u_discount_limit_4(1)_				
			117450.00000		1.00000	1.00000
+Inf	1.66081e+06	c_u_max_market_demand_limit(Ahvaz_B)_				
86	l(Isfahan_Tabriz)					
		NU	1.00000	.	.	.95636
-185100.00000	1.65274e+06	g(B_Isfahan_Mashhad)				
			185100.00000		1.00000	1.05636
+Inf	1.67125e+06	c_u_max_market_demand_limit(Mashhad_B)_				
87	d(1)	BS	.03079	.	.	.03079
-47849.99991	1.65934e+06	c_u_discount_limit_4(2)_				
			.		1.00000	1.03079
.	1.66081e+06	c_u_discount_limit_1(1)_				
88	d(2)	BS


```
-1.94999e+10    1.66081e+06 c_u_discount_limit_3(2_A)_
.
1.00000
57419.99989    1.66081e+06 c_u_discount_limit_4(2)_
```

End of report

1.5.2 Analysis G

From among the coefficients of the objective function, select one coefficient arbitrarily and, likewise, from among the values of the right-hand side constraints, consider one value arbitrarily. Then examine the effect of each of these changes on the value of the objective function by plotting a graph.

For right-hand side, we chose Max_ore of Factory 2 and for constraint coefficient we chose price_of_alloy_fac for Alloy B in Factory 2, the result are as shown:

```
[ ]: !python model_runner.py -g
```

the result will be a html output in your browser, because the code takes long to generate output page, some images of output are shown below.

