Here are some essential things about Mathematics for Machine Learning and Linear Algebra...

### **Vectors: Operations and Properties**

- Introduction to vectors as directed line segments. - Vector addition, subtraction, and scalar multiplication.

### **Vectors: Modulus, Inner Product, and Projection**

- Modulus (magnitude) of a vector. Inner product (dot product) of vectors. Deriving the cosine rule from the dot product.
- Visualizing vector projection. Calculation of vector projection.

### **Vectors: Changing Basis and Applications**

- Introduction to changing coordinate systems. Representing vectors in different bases.
- Application of changing basis in transformation.

#### **Matrices: Introduction and Transformation**

- Introduction to matrices and their representation. Visualization of matrix transformations in 2D.
- Classification of matrix transformations: scaling, rotation, etc. Composing multiple matrix transformations.

#### Matrices: Gaussian Elimination, Inverse, and Determinants

- Introduction to Gaussian elimination for solving linear systems. Understanding the concept of an inverse matrix.
- Determinants and their role in matrix inverses.

### Matrices in Linear Algebra II: Summation, Orthonormal Matrices, and Basis Changes

- Introduction to summation notation and symmetry of dot product.
- Revisiting changing coordinate systems and their applications.
- Performing transformations in a changed coordinate system.
- Definition and properties of orthonormal matrices.
- Constructing an orthonormal basis from arbitrary vectors.
- Application of orthonormal matrices to reflect in a plane.

### **Eigenproblems: Introduction to Eigenvalues and Eigenvectors**

- Introduction to eigenvalues and eigenvectors. Special cases of eigenvalues and eigenvectors.
- Methods for calculating eigenvectors. Determining an eigenbasis. Example of finding an eigenbasis.
- Application of eigenvalues and eigenvectors to Google's PageRank algorithm.

# These notes cover the key concepts and topics discussed

3Blue1Brown's Linear Algebra series offers intuitive visual explanations for fundamental concepts in linear algebra. The series uses animations and geometric insights to help learners grasp complex mathematical ideas.

**ZAGAZIG Student Branch** 

ent chapter

# **Vectors and Vector Spaces:**

- Visualizing vectors as arrows in space.
- Vector addition, subtraction, and scalar multiplication.
- Linear combinations and spans.
- Linear independence and basis vectors.

# **Linear Transformations:**

- Understanding transformations through animations.
- Matrices as transformation operators.
- Image and kernel (nullspace) of a transformation.
- Composition of transformations.

### **Matrix Multiplication:**

- Visualization of matrix multiplication.
- Associative and distributive properties.
- Matrix-vector products.
- Inverse matrices and determinants.

## **Eigenvalues and Eigenvectors:**

- Geometric interpretation of eigenvalues and eigenvectors.
- Diagonalization of matrices.
- Applications in understanding dynamic systems.

### Singular Value Decomposition (SVD):

- Decomposing matrices into three fundamental transformations.
- Application in data compression and image compression.

## **Change of Basis:**

- Coordinate transformations using different bases.
- Understanding change of basis matrices.
- Similarity transformations.

# Dot Products and Duality: & AUTOMATION SO

- Orthogonal vectors and orthogonal projections. U C e n t C n a p t e r
  Dual spaces and linear functionals.

### **Cross Products and Determinants:**

- Geometric interpretation of cross products.
- Determinants as volume scaling factors.
- Cofactor expansion and properties.

### **Differential Equations and Fundamental Subspaces:**

- Connection between solutions of differential equations and fundamental subspaces.



