

The basic flow of simulated annealing algorithm is as follows:

- (1) Initialization: initial temperature  $T$ , initial solution state  $s$ , number of iterations  $L$ ;
- (2) for each temperature state, repeat  $L$  cycles to generate and probabilistic accept new solutions:
- (3) generate a new solution  $s'$  from the current solution  $s$  through the transformation operation;
- (4) calculate the energy difference  $\Delta E$ , that is, the difference between the objective function of the new solution and the objective function of the original solution;
- (5) if  $\Delta E < 0$ , accept  $s'$  as the new current solution, otherwise accept  $s'$  as the new current solution with probability  $\exp(-\Delta E / T)$ ;
- (6) after completing  $L$  cycles in each temperature state, reduce the temperature  $T$  until the termination temperature is reached.

## **Multivariable function optimization problem**

The classical function optimization problem and

combinatorial optimization problem are selected as test cases.

Problem 1: schwefel test function is a complex multimodal function with a large number of local extremum regions.

$$F(X) = 418.9829 \times n - \sum_{i=1, n} \left[ |x_i| \cdot \sin\left(\sqrt{|x_i|}\right) \right]$$

In this paper, we take  $d = 10$ ,  $x = [-500, 500]$ , and the function is the global minimum  $f(x) = 0.0$  at  $x = (420.9687, \dots, 420.9687)$ .

The basic scheme of using simulated annealing algorithm: control the temperature to decay exponentially according to  $t(k) = a * t(k-1)$ , and the attenuation coefficient is  $a$ ; As shown in equation (1), accept the new solution according to metropolis criteria. For problem 1 (schwefel function), a new solution is generated by applying a random disturbance of normal distribution to an independent variable of the current solution.