



جامعة الأزهر  
AL-AZHAR UNIVERSITY  
LOGO.ADHAM90.COM



# AI PROJECT

**Under supervision: ENG. MOHAMMED ELREFAEI**

# OUR TEAM



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# The problem

8-puzzle problem is a puzzle invented and popularized by Noyes Palmer Chapman in the 1870s. It is played on a 3-by-3 grid with 8 square blocks labeled 1 through 8 and a blank square. It is required to rearrange the blocks in the order required using the empty space. you can slide four adjacent (left, right, above and below) blocks into the empty space.

1	3				1		3			1	2	3			1	2	3			1	2	3
4	2	5	=>		4	2	5	=>		4		5	=>		4	5		=>		4	5	6
7	8	6			7	8	6			7	8	6			7	8	6			7	8	
initial										goal												

Search strategies to be applied:

- Depth-First
- Breadth-First
- Best-First

Note: **In Best-First**; the success of this approach depends on the choice of priority function for a state.  
consider two priority functions:

- **Hamming priority function**. The number of tiles in the wrong position. A state with a small number of blocks in the wrong position is close to the goal state, so it will be preferred.
- **Manhattan priority function**. The sum of the distances (sum of the vertical and horizontal distance) from the blocks to their goal positions, so it will be preferred.

For example:

<div> <div>8 1 3</div> <div>4 2</div> <div>7 6 5</div> </div> <div>initial</div>	<div> <div>1 2 3</div> <div>4 5 6</div> <div>7 8</div> </div> <div>goal</div>	<div> <div>1 2 3 4 5 6 7 8</div> <div>-----</div> <div>1 1 0 0 1 1 0 1</div> </div> <div>Hamming = 5</div>	<div> <div>1 2 3 4 5 6 7 8</div> <div>-----</div> <div>1 2 0 0 2 2 0 3</div> </div> <div>Manhattan = 10</div>
--	---	--	---

**The objective:** build a problem solver for 8-puzzle game.

1) Implement the solution for the problem based on the above search techniques **using the python.**

Given the **initial state:**

1	8	2
4	3	
7	6	5

and the **goal state:**

1	2	3
4	5	6
7	8	

Make the program able to display:

- The solution.
- Number of states enqueued.
- Number of moves.:

2) **Test the implementation for the instance** (other initial state):

8	1	2
4	3	
7	6	5

and the goal state:

1	2	3
4	5	6
7	8	

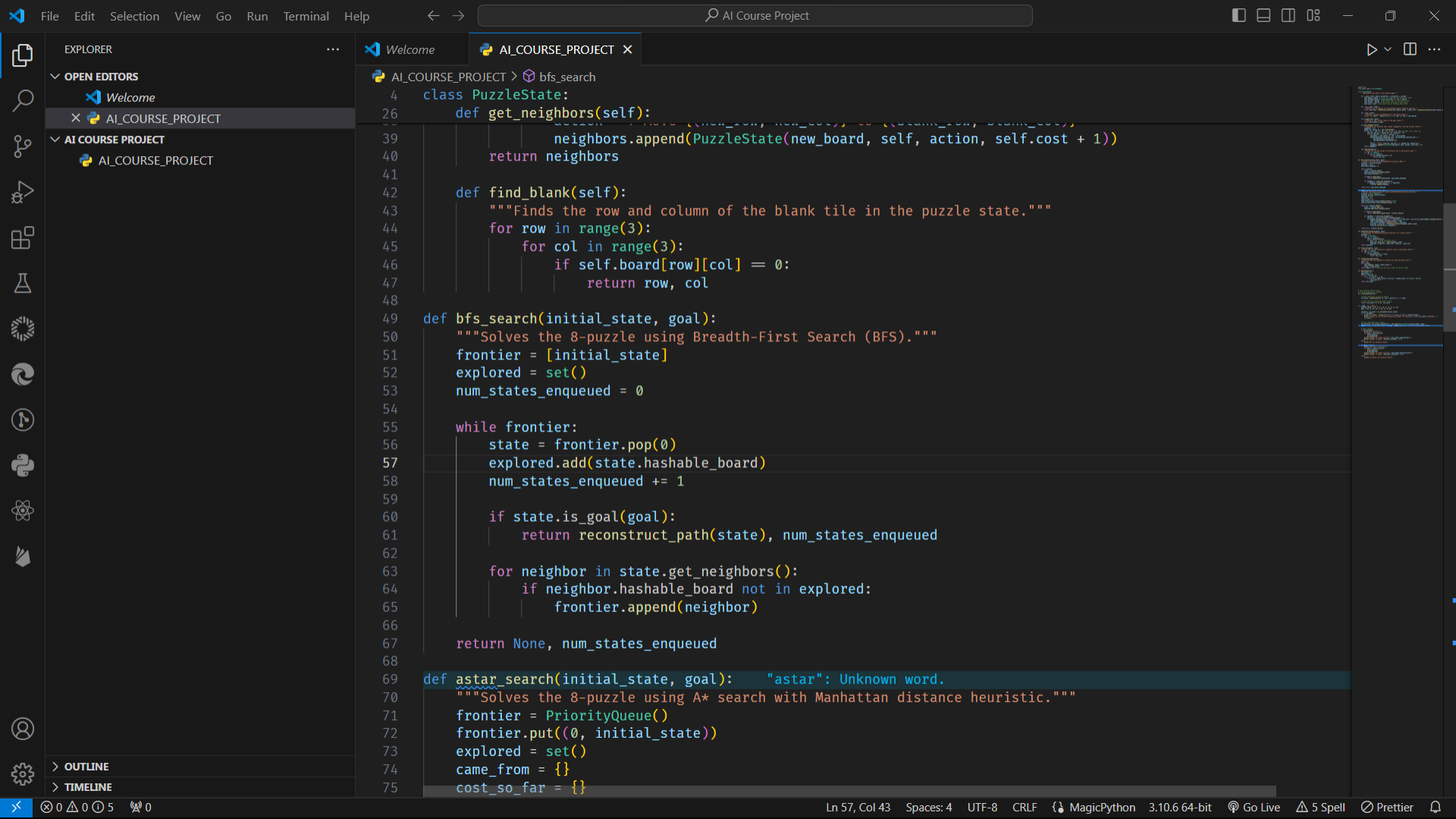
Is that instance of 8-puzzle is solvable? Explain.



# CODE







```

68
69 def astar_search(initial_s
70     """Solves the 8-puzzle
71     frontier = PriorityQue
72     frontier.put((0, initi
73     explored = set()
74     came_from = {}
75     cost_so_far = {}
76     came_from[initial_stat
77     cost_so_far[initial_st
78
79     while not frontier.empty
80         state = frontier.g
81         explored.add(state
82
83         if state.is_goal(g
84             return reconst
85
86         for neighbor in st
87             new_cost = cos
88             if neighbor.ha
89                 came_from[
90                     cost_so_fa
91                     priority =
92                     frontier.p
93
94     return None, frontier.
95
96 def manhattan_distance(boa
97     """Calculates the Manh
98     distance = 0
99     for row in range(3):
100         for col in range(3
101             tile = board[r
102             if tile != 0:
103                 goal_row,
104                 distance +
105     return distance
106
107 def find_tile(board, tile

```

```

68 def astar_search(initial_state, goal):    "astar": Unknown word.
69     """Solves the 8-puzzle using A* search with Manhattan distance heuristic."""
70     frontier = PriorityQueue()
71     frontier.put((0, initial_state))
72     explored = set()
73     came_from = {}
74     cost_so_far = {}
75     came_from[initial_state.hashable_board] = None
76     cost_so_far[initial_state.hashable_board] = 0
77
78     while not frontier.empty():
79         state = frontier.get()[1]
80         explored.add(state.hashable_board)
81
82         if state.is_goal(goal):
83             return reconstruct_path(state), frontier.qsize()
84
85         for neighbor in state.get_neighbors():
86             new_cost = cost_so_far[state.hashable_board] + 1
87             if neighbor.hashable_board not in explored and new_cost < cost_so_far.get(neighbor.hashable_board, float('inf')):
88                 came_from[neighbor.hashable_board] = state
89                 cost_so_far[neighbor.hashable_board] = new_cost
90                 priority = new_cost + manhattan_distance(neighbor.board, goal)
91                 frontier.put((priority, neighbor))
92
93     return None, frontier.qsize()
94
95 def manhattan_distance(board, goal):
96     """Calculates the Manhattan distance heuristic for a given state."""
97     distance = 0
98     for row in range(3):
99         for col in range(3):
100             tile = board[row][col]
101             if tile != 0: # Skip the blank tile
102                 goal_row, goal_col = find_tile(goal, tile)
103                 distance += abs(row - goal_row) + abs(col - goal_col)
104     return distance
105
106 def find_tile(goal, tile):
107     for row in range(3):
108         for col in range(3):
109             if goal[row][col] == tile:
110                 return row, col
111     return None, None

```

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AI Course Project

EXPLORER

...

OPEN EDITORS

Welcome

AI\_COURSE\_PROJECT

AI COURSE PROJECT

AI\_COURSE\_PROJECT

OUTLINE

TIMELINE

AI\_COURSE\_PROJECT > ...

107

<

def find\_tile(board, tile):

"""Finds the row and column of a specific tile in the puzzle state."""

108

for row in range(3):

109

for col in range(3):

110

if board[row][col] == tile:

111

return row, col

112

113

114

<

def reconstruct\_path(state):

"""Reconstructs the sequence of actions to reach the goal state."""

115

path = []

116

while state:

117

path.append(( state, state.action ))

118

state = state.parent

119

return path[::-1] # Reverse the path to get the correct order

120

121

122

<

def getInvCount(arr):

123

inv\_count = 0

124

empty\_value = 0

125

for i in range(0, 9):

126

for j in range(i + 1, 9):

127

if arr[j] != empty\_value and arr[i] != empty\_value and arr[i] > arr[j]:

128

inv\_count += 1

129

return inv\_count

130

131

132

133

134

135

# This function returns true

136

# if given 8 puzzle is solvable.

137

<

def is\_solvable(puzzle) :

138

139

# Count inversions in given 8 puzzle

140

inv\_count = getInvCount([j for sub in puzzle for j in sub])

141

142

# return true if inversion count is even.

143

return (inv\_count % 2 == 0), inv\_count

144

145

<

if \_\_name\_\_ == "\_\_main\_\_":

Ln 144, Col 1

Spaces: 4

UTF-8

CRLF

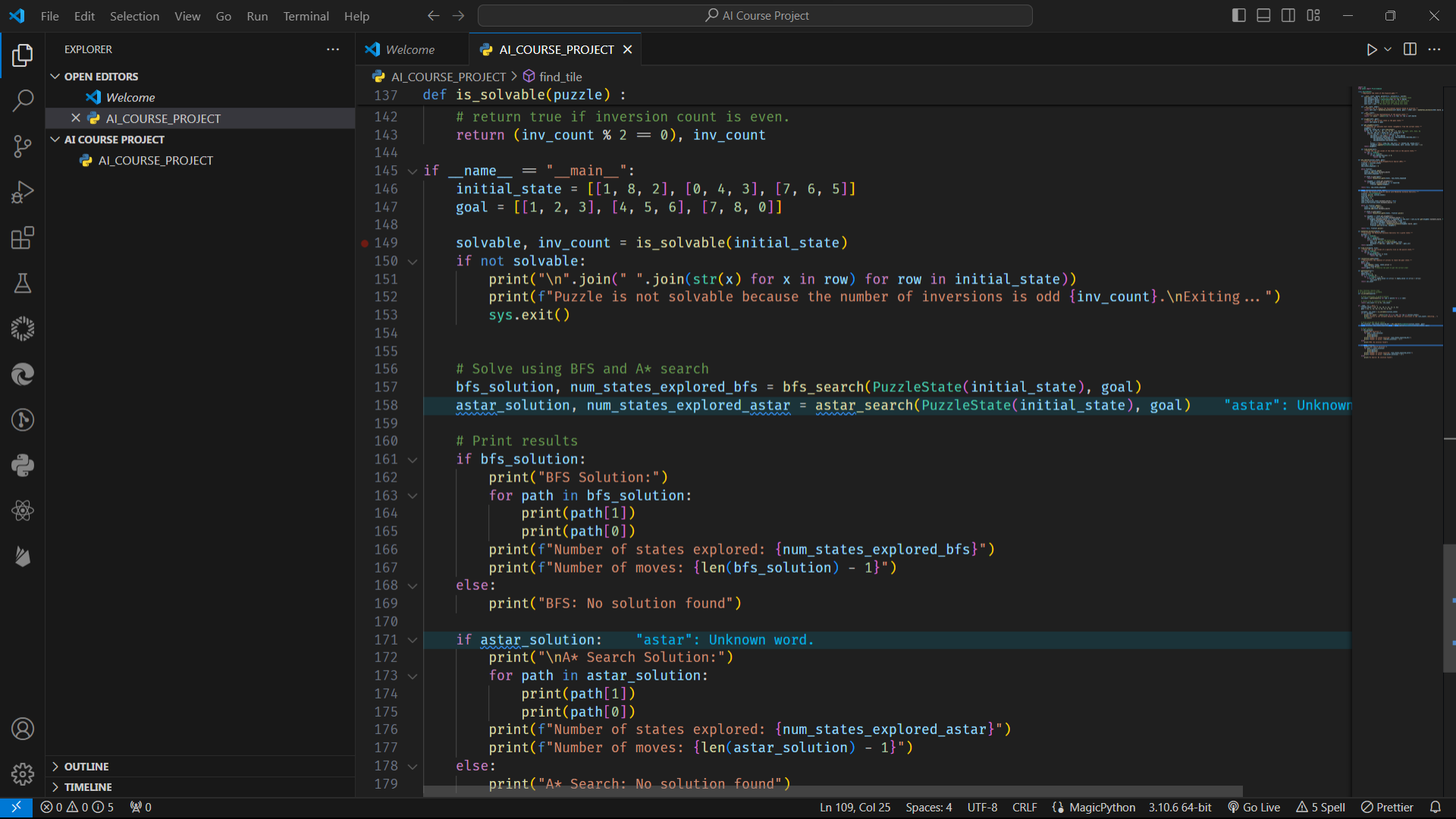
MagicPython

3.10.6 64-bit

Go Live

5 Spell

Prettier



```
File Edit Selection View Go Run Terminal Help
AL_COURSE_PROJECT
def is_solvable(puzzle):
    # return true if inversion count is even.
    return (inv_count % 2 == 0), inv_count

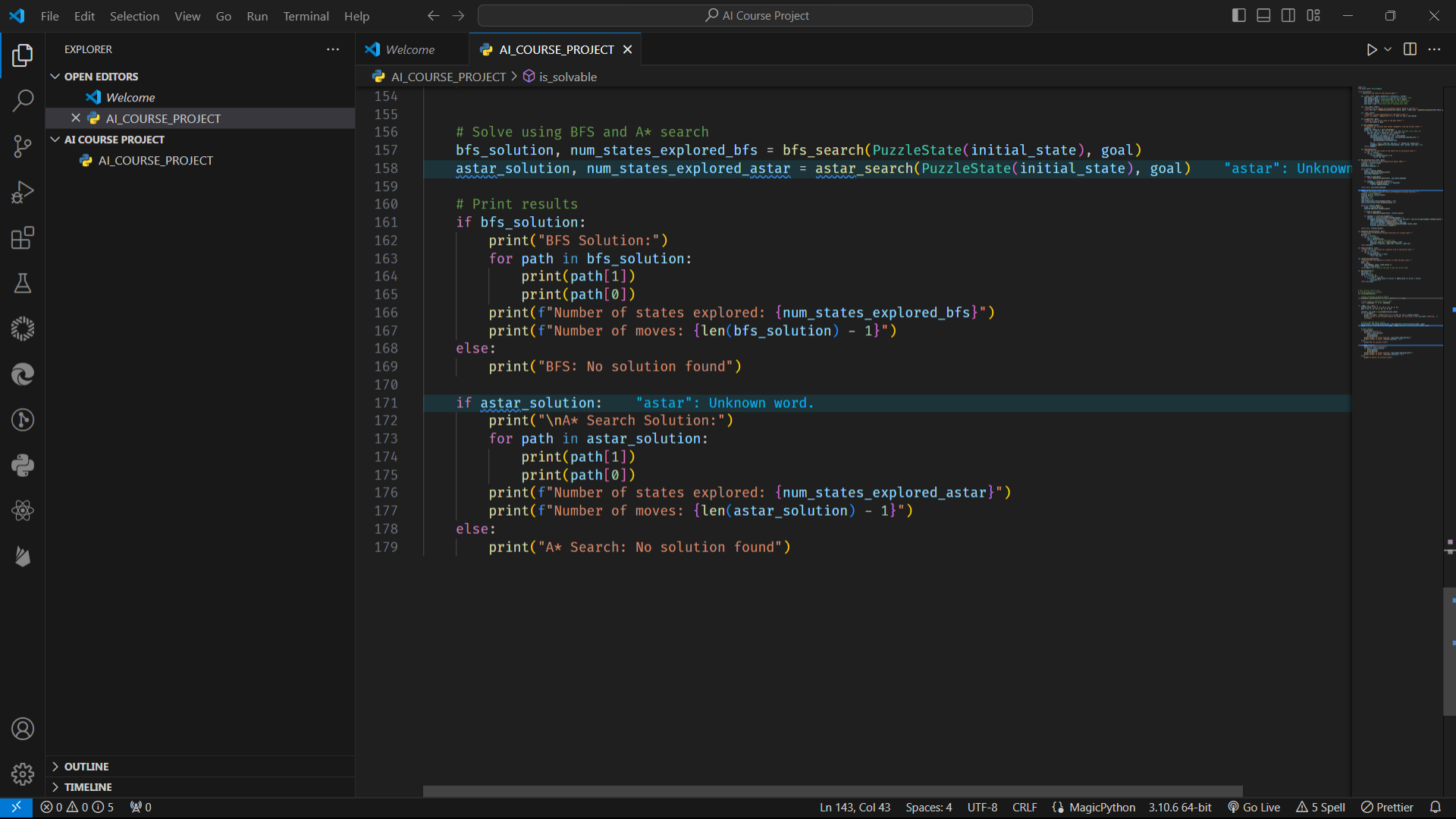
if __name__ == "__main__":
    initial_state = [[1, 8, 2], [0, 4, 3], [7, 6, 5]]
    goal = [[1, 2, 3], [4, 5, 6], [7, 8, 0]]

    solvable, inv_count = is_solvable(initial_state)
    if not solvable:
        print("\n".join(" ".join(str(x) for x in row) for row in initial_state))
        print(f"Puzzle is not solvable because the number of inversions is odd {inv_count}.\nExiting...")
        sys.exit()

    # Solve using BFS and A* search
    bfs_solution, num_states_explored_bfs = bfs_search(PuzzleState(initial_state), goal)
    astar_solution, num_states_explored_astar = astar_search(PuzzleState(initial_state), goal) "astar": Unknown

    # Print results
    if bfs_solution:
        print("BFS Solution:")
        for path in bfs_solution:
            print(path[1])
            print(path[0])
        print(f"Number of states explored: {num_states_explored_bfs}")
        print(f"Number of moves: {len(bfs_solution) - 1}")
    else:
        print("BFS: No solution found")

    if astar_solution: "astar": Unknown word.
        print("\nA* Search Solution:")
        for path in astar_solution:
            print(path[1])
            print(path[0])
        print(f"Number of states explored: {num_states_explored_astar}")
        print(f"Number of moves: {len(astar_solution) - 1}")
    else:
        print("A* Search: No solution found")
```



```
File Edit Selection View Go Run Terminal Help
AI_COURSE_PROJECT
Welcome
AI_COURSE_PROJECT > is_solvable
154
155
156 # Solve using BFS and A* search
157 bfs_solution, num_states_explored_bfs = bfs_search(PuzzleState(initial_state), goal)
158 astar_solution, num_states_explored_astar = astar_search(PuzzleState(initial_state), goal) "astar": Unknown
159
160 # Print results
161 if bfs_solution:
162     print("BFS Solution:")
163     for path in bfs_solution:
164         print(path[1])
165         print(path[0])
166     print(f"Number of states explored: {num_states_explored_bfs}")
167     print(f"Number of moves: {len(bfs_solution) - 1}")
168 else:
169     print("BFS: No solution found")
170
171 if astar_solution: "astar": Unknown word.
172     print("\nA* Search Solution:")
173     for path in astar_solution:
174         print(path[1])
175         print(path[0])
176     print(f"Number of states explored: {num_states_explored_astar}")
177     print(f"Number of moves: {len(astar_solution) - 1}")
178 else:
179     print("A* Search: No solution found")
```



# RUN

 AI\_COURSE\_PROJECT

> Python

Navigation icons: back, search, home, info, and signal strength.

```
None
1 8 2
0 4 3
7 6 5
Move (1, 1) to (1, 0)
1 8 2
4 0 3
7 6 5
Move (0, 1) to (1, 1)
1 0 2
4 8 3
7 6 5
Move (0, 2) to (0, 1)
1 2 0
4 8 3
7 6 5
Move (1, 2) to (0, 2)
1 2 3
4 8 0
7 6 5
Move (2, 2) to (1, 2)
1 2 3
4 8 5
7 6 0
Move (2, 1) to (2, 2)
1 2 3
4 8 5
7 0 6
Move (1, 1) to (2, 1)
1 2 3
4 0 5
7 8 6
Move (1, 2) to (1, 1)
1 2 3
4 5 0
7 8 6
Move (2, 2) to (1, 2)
1 2 3
4 5 6
7 8 0
Number of states explored: 11
Number of moves: 9
PS D:\AI Course Project>
```