

# **Wave shaping oscillators**

## **Lecture (7)**

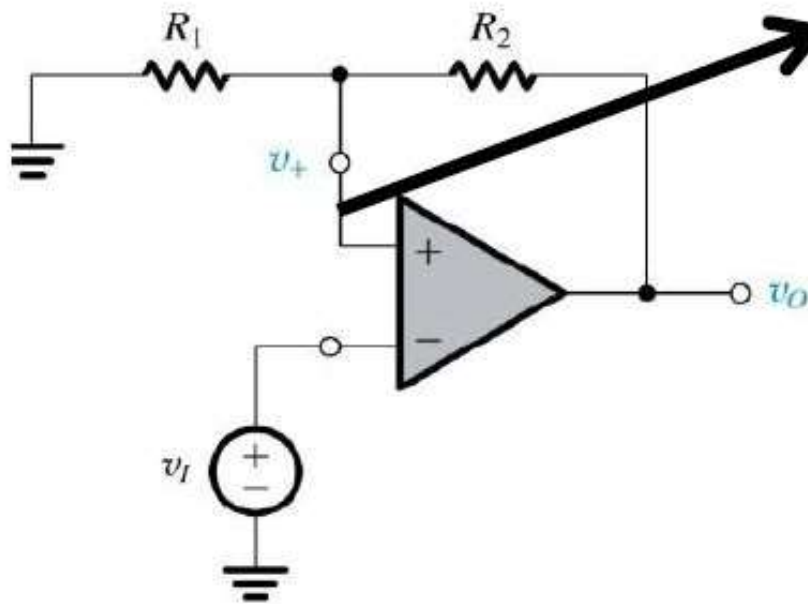
### **Biastable multivibrator**

# Op-Amp Astable (Bistable) Multivibrator

Positive-feedback loop Bistable Operation

**(Schmitt-trigger Circuit)**

Inverting Multivibrator



$$v^+ = V_T = \frac{R_1}{R_1 + R_2} V_o = \beta V_o$$

$$\beta = \frac{R_1}{R_1 + R_2}$$

$$V_{TH} = \beta L^+$$

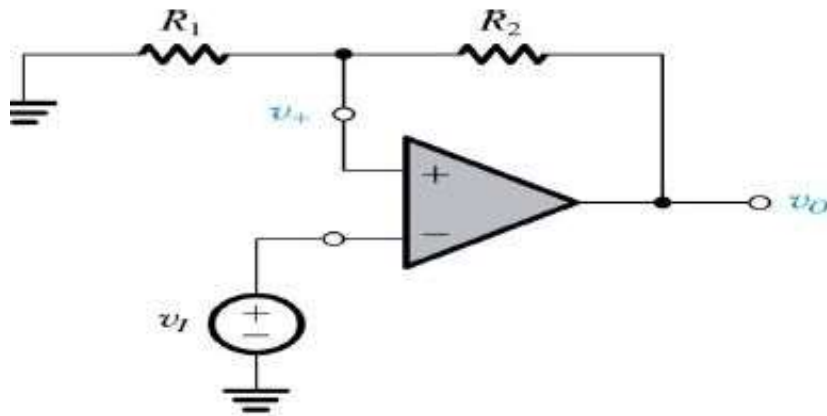
$$V_{TH} = \beta(+V_{CC})$$

$$V_{TL} = \beta L^-$$

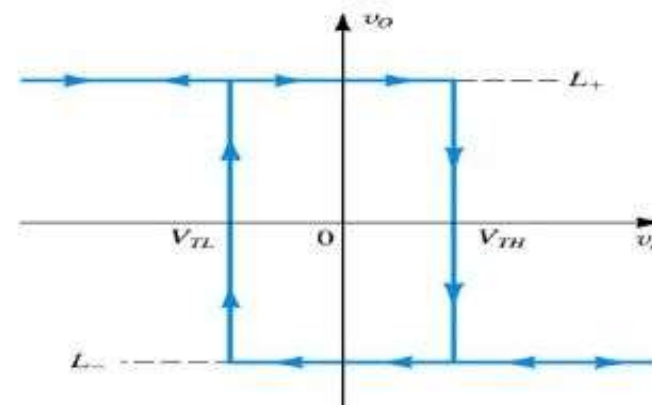
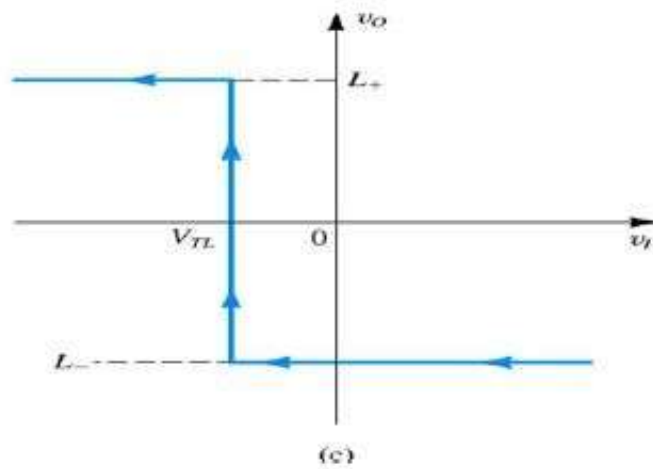
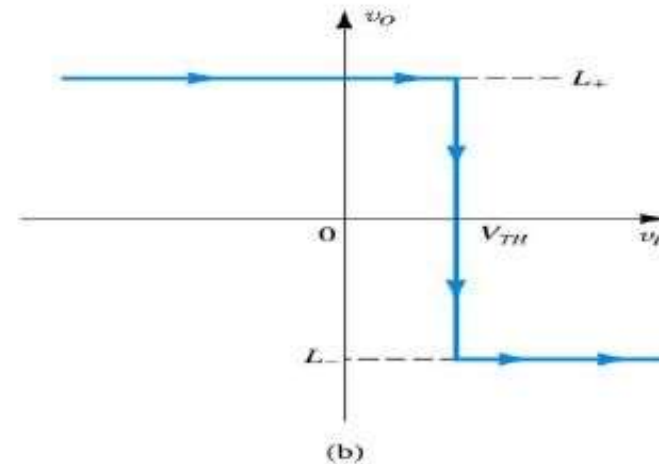
$$V_{TL} = \beta(-V_{CC})$$



# Positive-feedback loop Bistable Operation

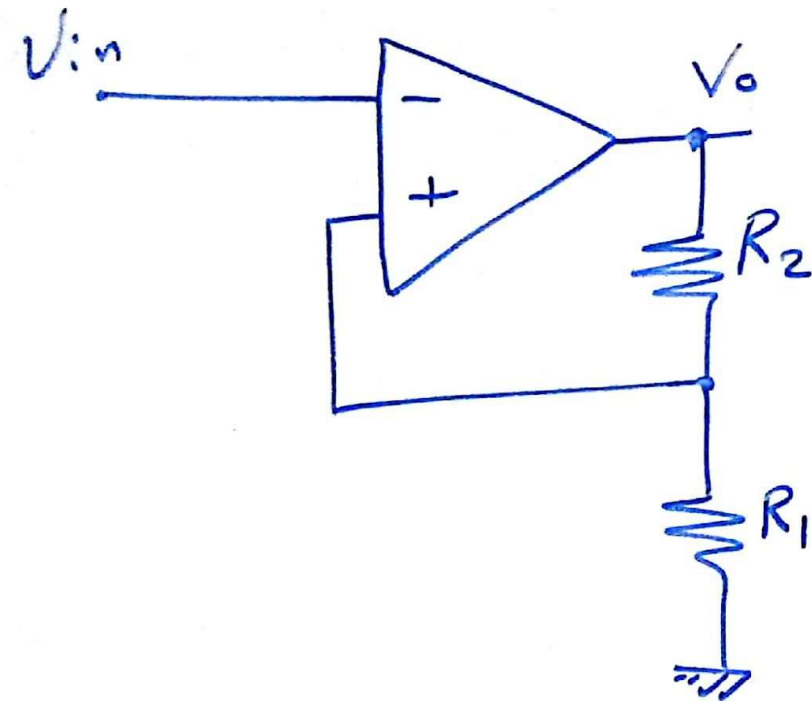
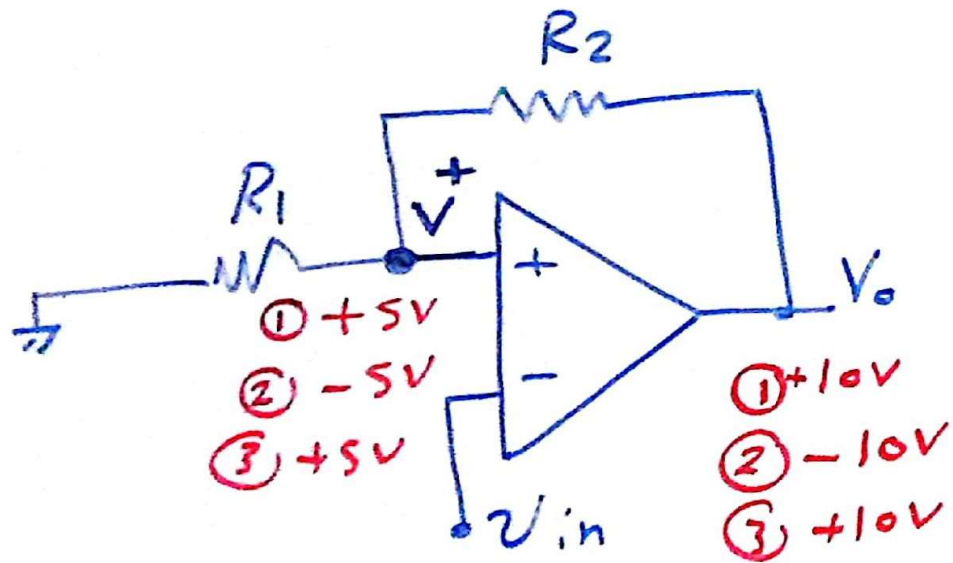


Inverting Multivibrator



Transfer characteristic

# Schmitt-Trigger Circuit (Summary)



Comparator

$$\begin{aligned} V^+ > V^- &\rightarrow V_o = +V_{cc} = L^+ \\ V^- > V^+ &\rightarrow V_o = -V_{cc} = L^- \end{aligned}$$

$$* V^+ = \frac{V_o \cdot R_1}{R_1 + R_2}$$

① For  $V_o = L^+$

$$V^+ = \left( \frac{R_1}{R_1 + R_2} \right) L^+$$

$$V^+ = \beta L^+$$

$V_o = L^+$  till  $V_{in} > \beta L^+$

② If  $V_{in} > \beta L^+$

$$\therefore V_o = L^-$$

$$V^+ = \frac{L^- \cdot R_1}{R_1 + R_2}$$

$$V^+ = \beta L^-$$

$V_o = L^-$  till  $V_{in} < \beta L^-$

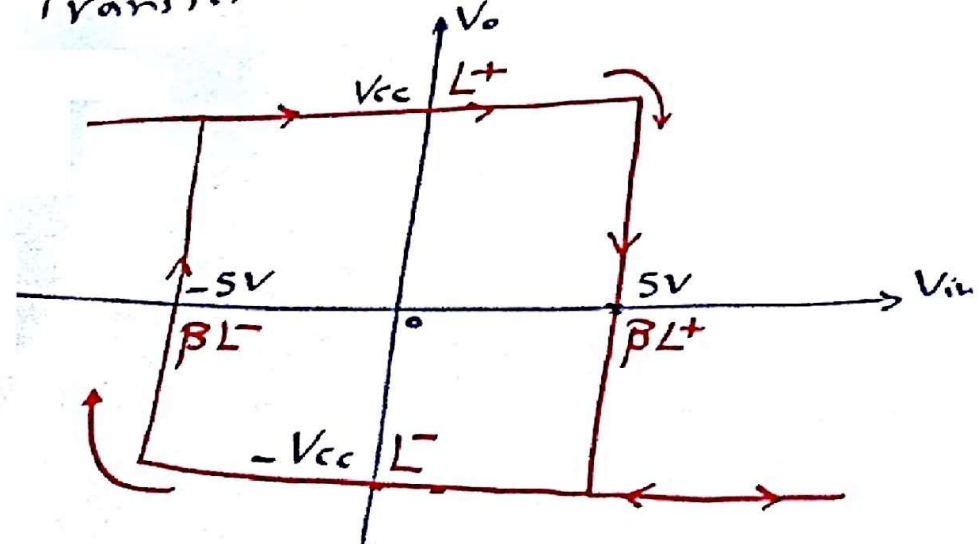
③ If  $V_{in} < \beta L^-$

Then  $V_o = L^+$

$$\therefore V^+ = \beta L^+$$

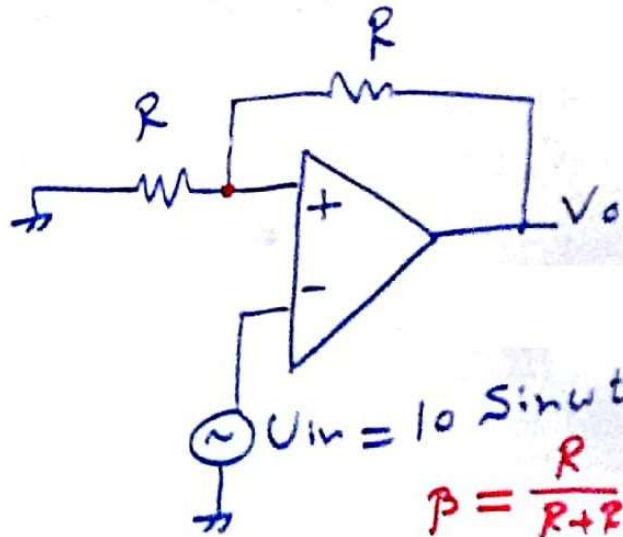
\* Hysteresis Curve

Transfer characteristics

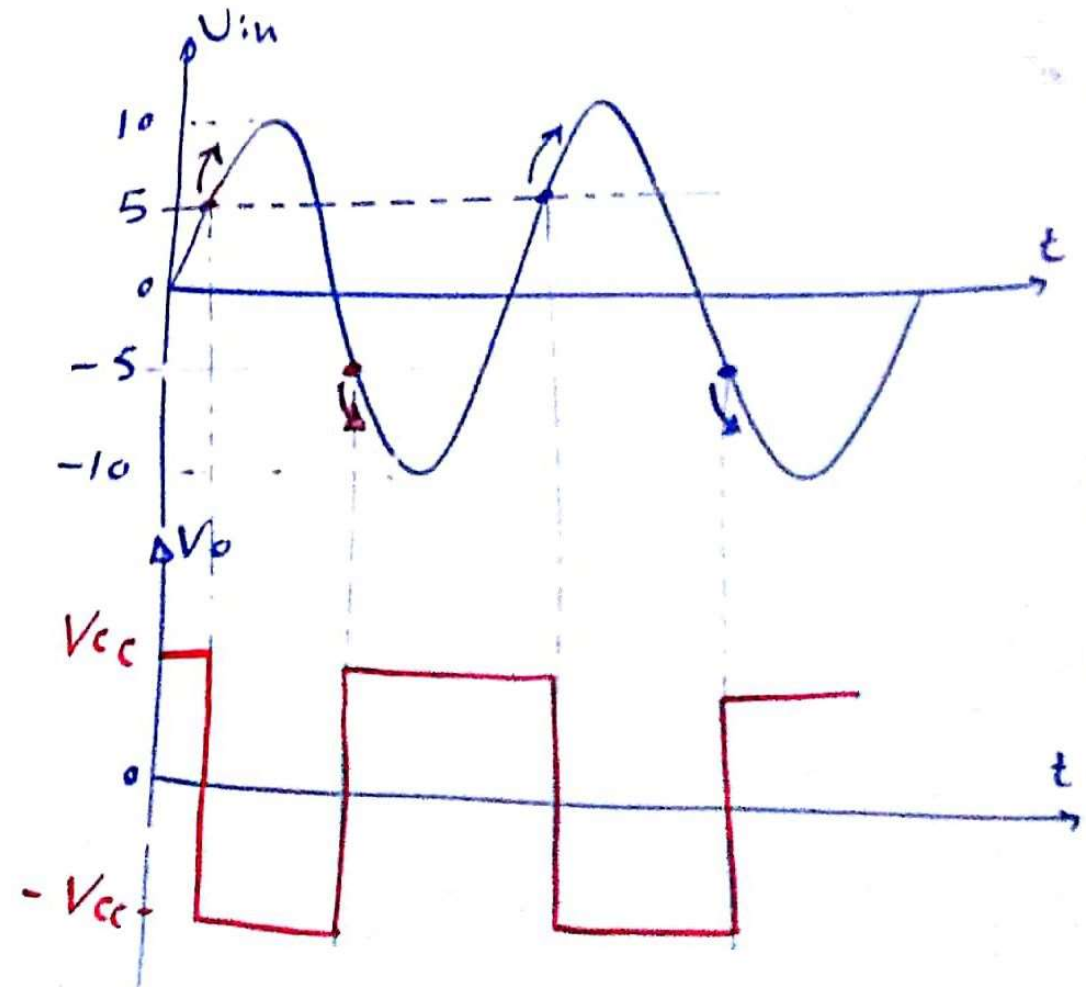


## Example

$$V_{CC} = 10V$$

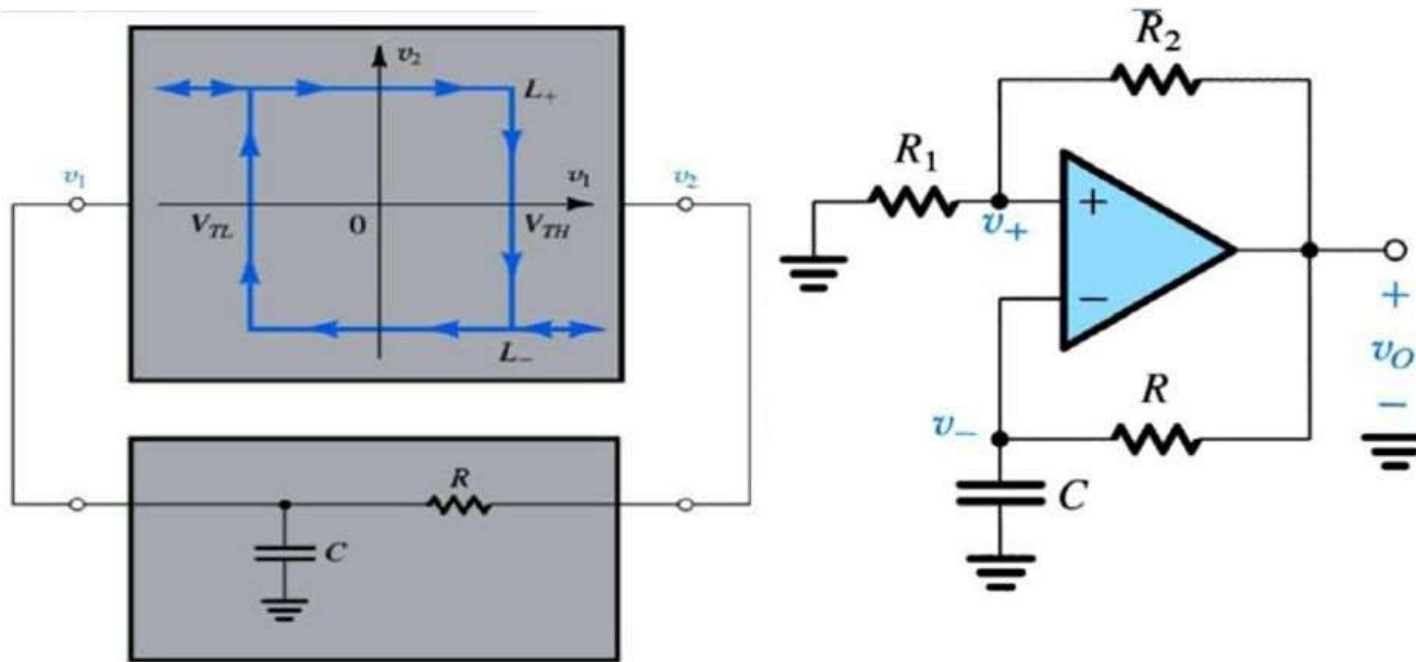


$$\beta = \frac{R}{R+R} = 0.5$$



# Applications:

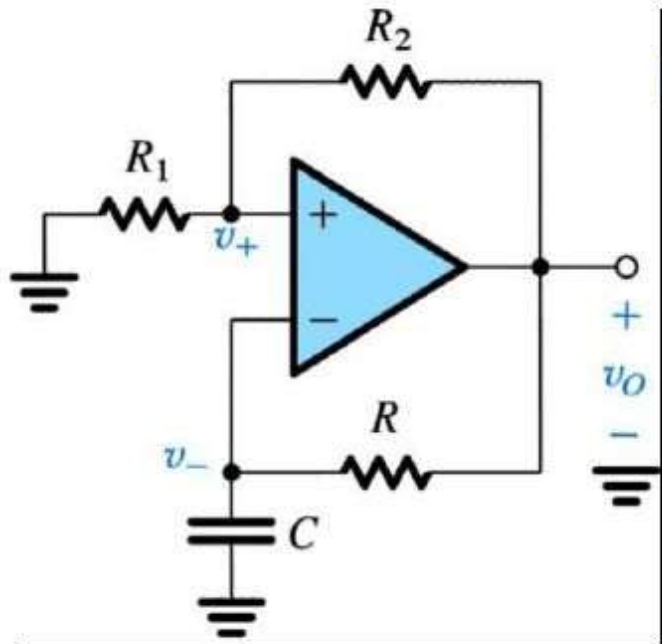
## 1. Astable Multivibrator (Square-Wave Generator)



Connecting a bistable multivibrator with inverting transfer characteristics in a feedback loop with an RC circuit results in a square-wave generator.



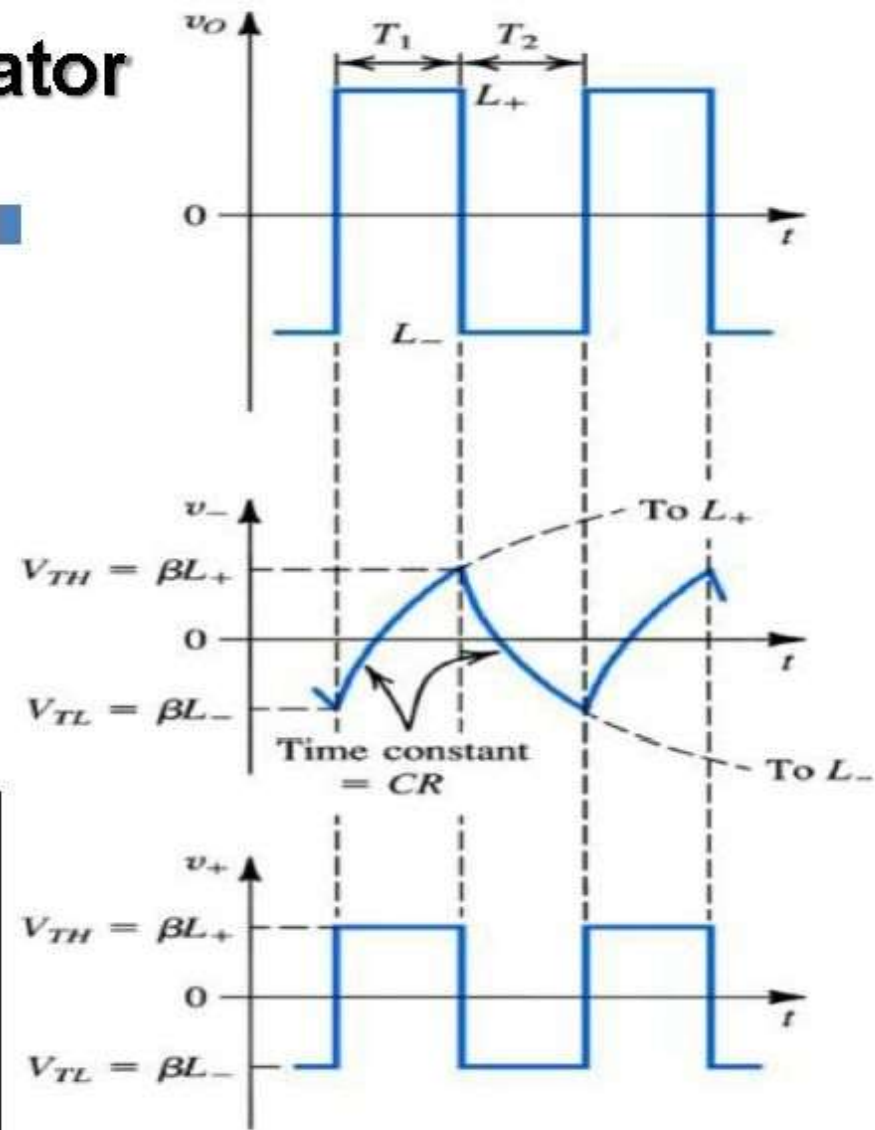
# Astable Multivibrator



$$V_T = \frac{R_1}{R_1 + R_2} V_O = \beta V_O$$

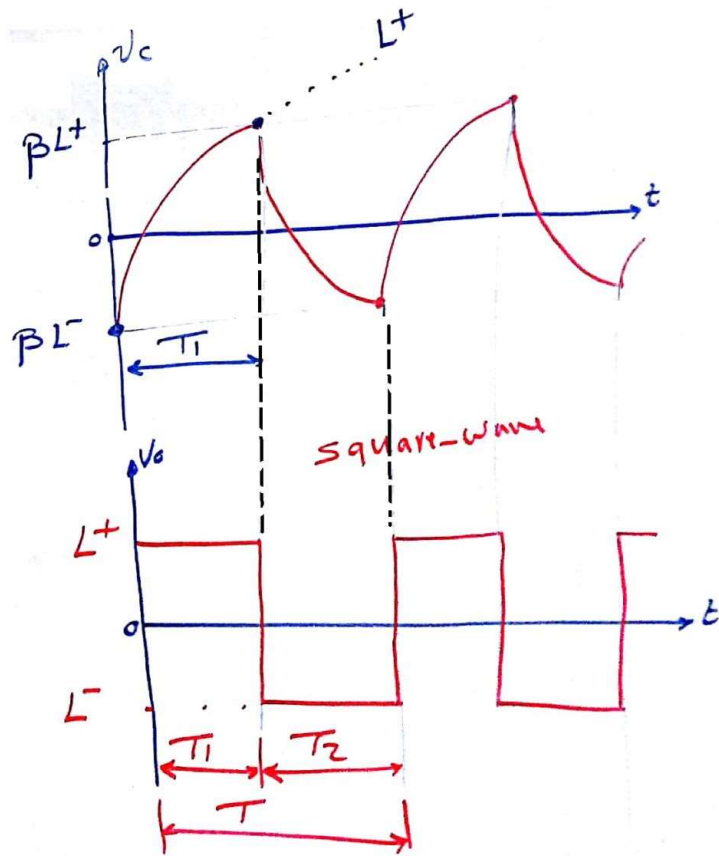
$$V_{TH} = \beta L^+ = \beta(+V_{CC})$$

$$V_{TL} = \beta L^- = \beta(-V_{CC})$$



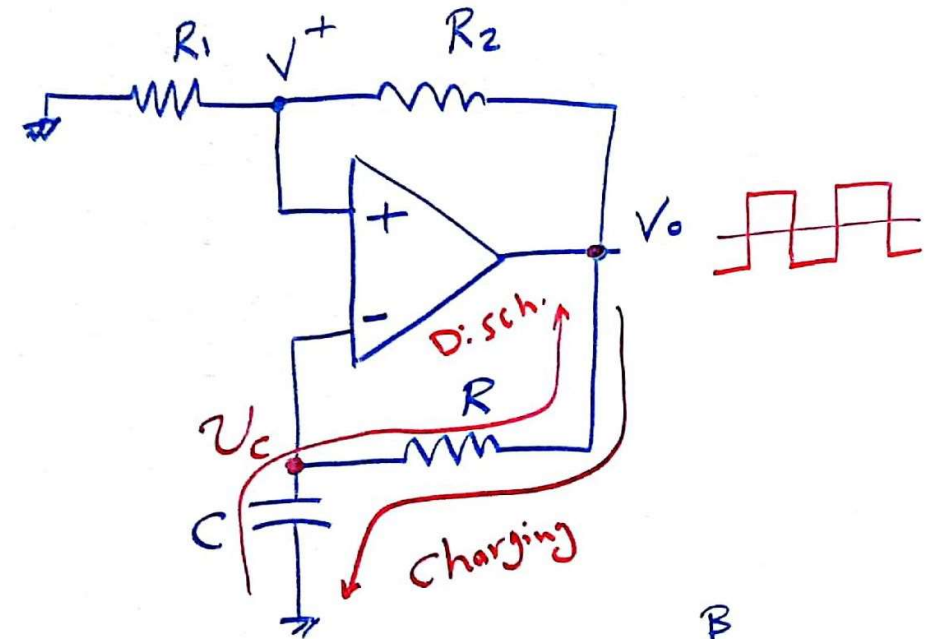


## Application: 1. Square-Wave Generator



$T = \text{Time-period} = T_1 + T_2$

Frequency  $f = \frac{1}{T}$



$$* V^+ = \frac{V_c}{R_1 + R_2} \cdot R_1 = \left( \frac{R_1}{R_1 + R_2} \right) V_o$$

For  $V_o = L^+ = V_{cc}$

$$\therefore V^+ = \beta L^+, \quad \beta = \frac{R_1}{R_1 + R_2}$$

Derive:-

In General,

$$V_c = V_F + (V_{ini} - V_F) e^{-t/\tau}$$

$V_F$  = Final-Value

$V_{ini}$  = initial Value

$\tau$  = time-constant

$$\tau = RC$$

① During  $T_1$

$$V_{ini} = \beta L^- , V_F = L^+$$

$$\therefore V_c = L^+ + (\beta L^- - L^+) e^{-t/\tau}$$

$$\text{at } t = T_1 , V_c = \beta L^+$$

$$\therefore \beta L^+ = L^+ + (\beta L^- - L^+) e^{-T_1/\tau}$$

$$\beta L^+ - L^+ = (\beta L^- - L^+) e^{-T_1/\tau}$$

$$e^{T_1/\tau} = \frac{\beta L^- - L^+}{\beta L^+ - L^+}$$

$$\frac{T_1}{\tau} = \ln \frac{\beta L^- - L^+}{\beta L^+ - L^+}$$

$$T_1 = \tau \ln \frac{\beta L^- - L^+}{\beta L^+ - L^+}$$

$$\text{at } L^- = -L^+$$

$$T_1 = RC \ln \left[ \frac{-\beta L^+ - L^+}{\beta L^+ - L^+} \right]$$

$$T_1 = RC \ln \frac{-\beta - 1}{\beta - 1}$$

$$T_1 = RC \ln \frac{-(1+\beta)}{-(1-\beta)}$$

$$T_1 = RC \ln \left( \frac{1+\beta}{1-\beta} \right)$$

For symmetrical square-wave

$$T_2 = T_1$$

$\therefore$  Time-period  $T = 2T_1$

$$T = 2RC \ln \left( \frac{1+\beta}{1-\beta} \right)$$

frequency  $f = \frac{1}{T}$

### Example

Design a square-wave generator of frequency 10 KHz with  $\beta = 0.6$ .

Solution

$$* T = \frac{1}{f} = \frac{1}{10 \times 10^3} = 10^{-4} \text{ Sec.}$$

$$T = 2RC \ln\left(\frac{1+\beta}{1-\beta}\right)$$

$$10^{-4} = 2RC \ln\left(\frac{1.6}{0.4}\right)$$

$$RC = 1.233152 \times 10^{-4}$$

Assuming  $C = 0.1 \mu\text{F}$

$$\therefore R = \frac{1.233152 \times 10^{-4}}{0.1 \times 10^{-6}}$$

$$R = 1233.2 \Omega$$

$$R = 1.233 \text{ k}\Omega$$

$$\beta = 0.6 = \frac{R_1}{R_1 + R_2}$$

$$\text{Let } R_1 = 10 \text{ k}\Omega$$

$$\therefore 0.6 = \frac{10}{10 + R_2}$$

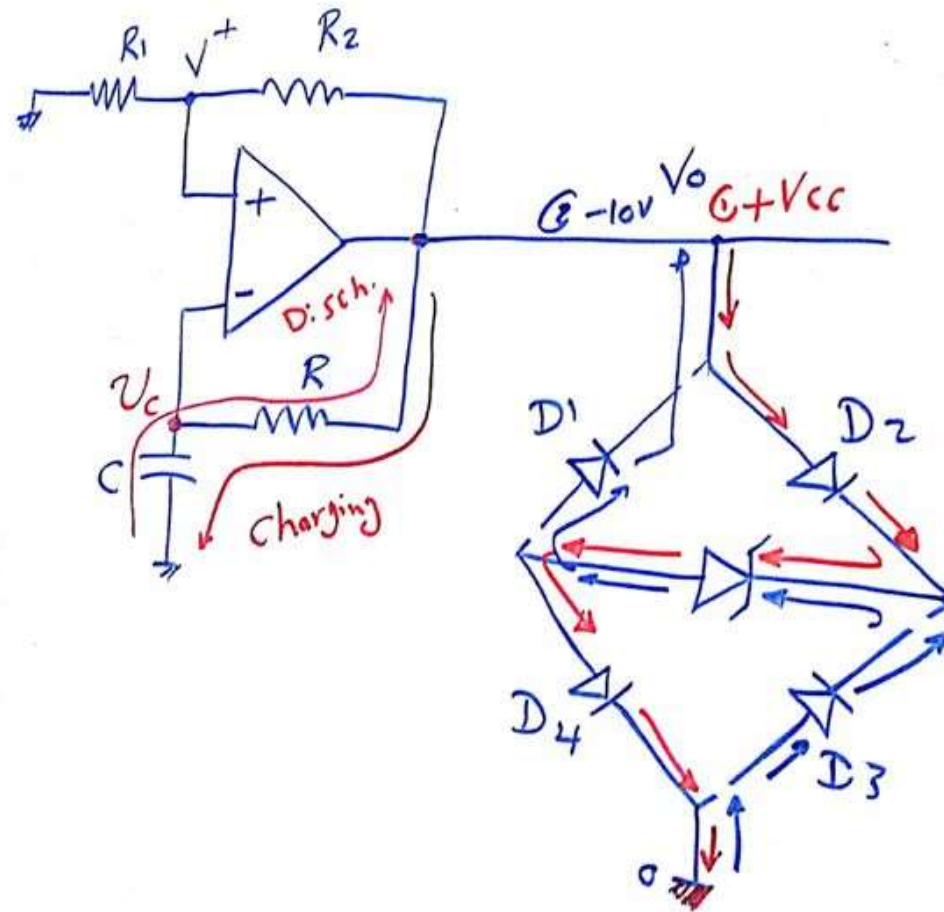
$$6 + 0.6R_2 = 10$$

$$0.6R_2 = 4$$

$$R_2 = 6.67 \text{ k}\Omega$$

# Square-Wave Generator with Amplitude Stabilization:

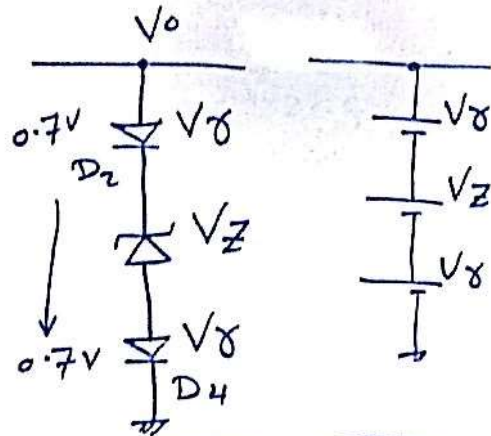
## Using Zener-Bridge Stabilizer:





# Operation:

a) For +ve half-cycle



$$V_o(\max) = V_{\gamma 2} + V_{\gamma 4} + V_Z$$

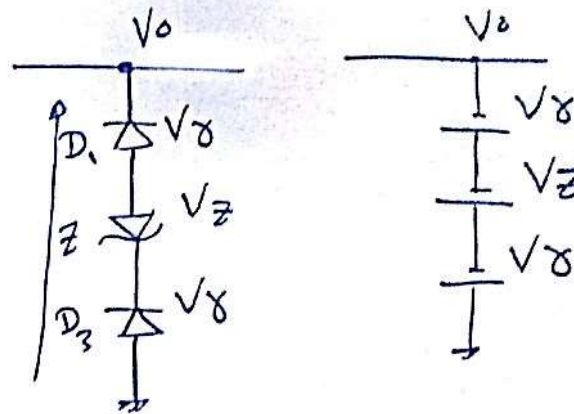
For  $V_{o\max} = 5V$

$$V_{\gamma} = 0.7V$$

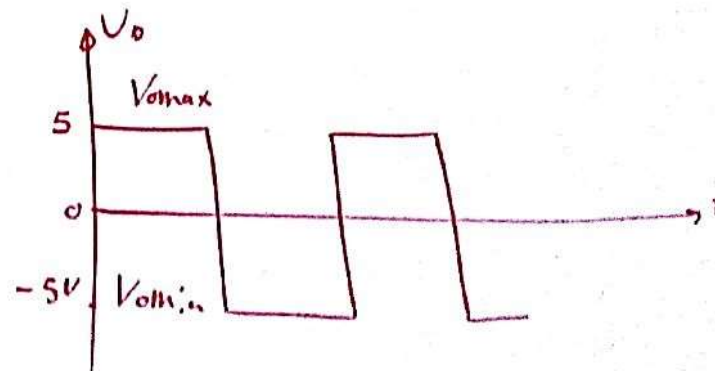
$$5 = 1.4 + V_Z$$

$$V_Z = 3.6V$$

b) For -ve half-cycle



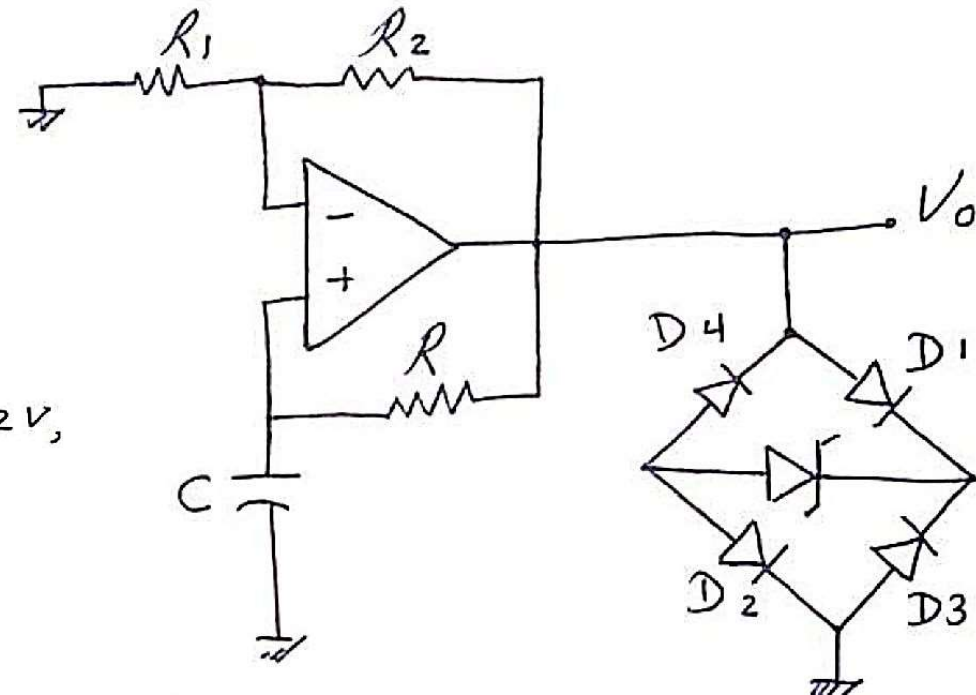
$$V_o(\min) = -(V_{\gamma 1} + V_{\gamma 3} + V_Z)$$



## Example

Design a square wave generator with amplitude stabilization using Zener-bridge circuit. The peak-to-peak output waveform should be 8V of frequency 5KHz. Assuming that  $\beta = 0.5$ , the Op Amp saturation voltages =  $\pm 12V$  and the current through  $R_1$  and  $R_2$  is 0.2mA.

1. Draw the circuit diagram.
2. Calculate  $V_Z$ .
3. Calculate  $R$ ,  $R_1$ ,  $R_2$  and  $C$ .



## Solution:

$$V_{op} = 4V$$
$$f = 5 \text{ KHz}, \beta = 0.5, V^+ = 12V, V^- = -12V,$$
$$I_{R_1, R_2} = 0.2 \text{ mA}$$



2. Calculate  $V_z$ .

$$* V_{OP} = 4V = V_Z + V_{D1} + V_{D2}, \quad V_D = 0.7V$$

$$\therefore 4 = V_Z + 0.7 + 0.7$$

$$\boxed{V_Z = 2.6V}$$

3. Calculate  $R$ ,  $R_1$ ,  $R_2$  and  $C$ .

$$* T = 2RC \ln\left(\frac{1+\beta}{1-\beta}\right)$$

$$\frac{1}{f} = 2RC \ln\left(\frac{1+\beta}{1-\beta}\right)$$

$$\frac{1}{5 \times 10^3} = 2RC \ln\left(\frac{1+0.5}{1-0.5}\right)$$

$$\boxed{RC = 9.1024 \times 10^{-5}}$$

$$\text{Let } \boxed{C = 10nF} \rightarrow$$

$$\therefore \boxed{R = 9102.4\Omega \approx 9.1k\Omega}$$

$$* I_{R1,2} = \frac{V_O}{R_1 + R_2} \rightarrow 0.2mA = \frac{4}{R_1 + R_2}$$

$$\boxed{R_1 + R_2 = 20k\Omega} \quad (1)$$

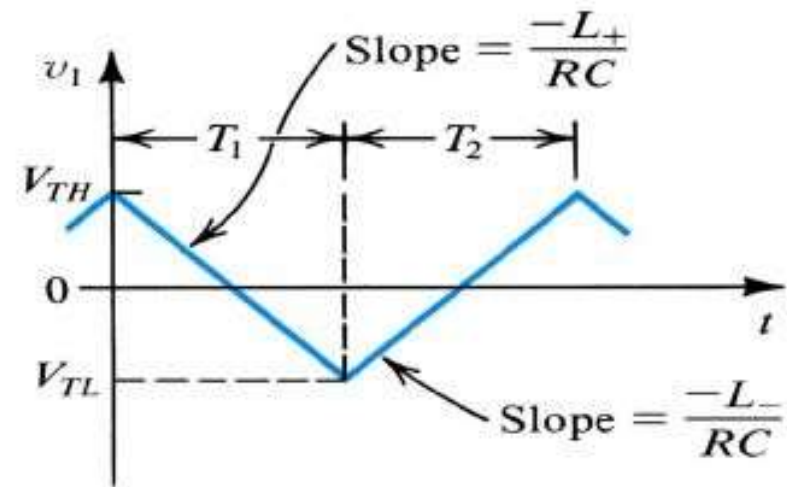
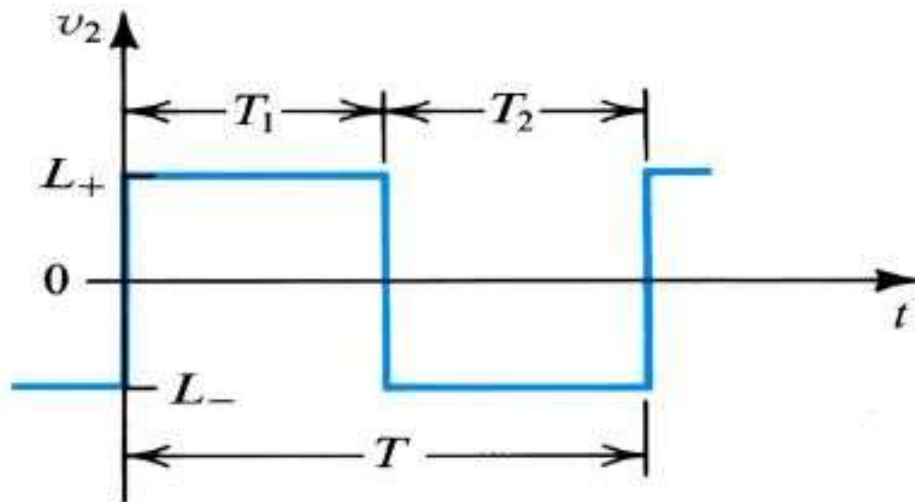
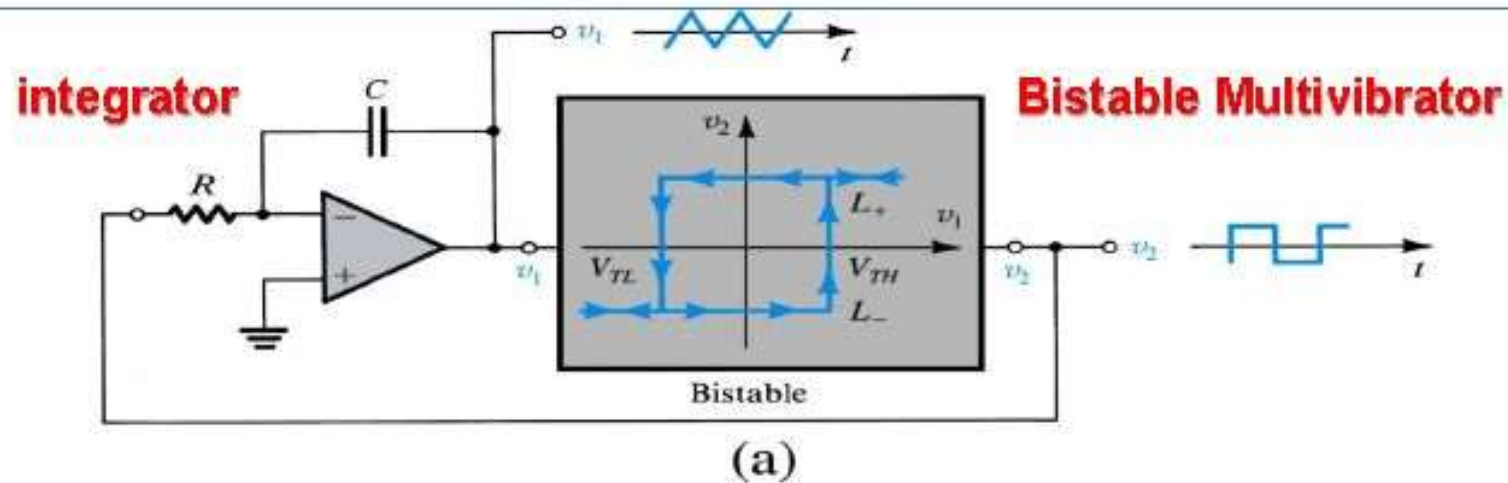
$$* \beta = 0.5 = \frac{R_1}{R_1 + R_2} \rightarrow 0.5 = \frac{R_1}{20}$$

$$\therefore \boxed{R_1 = 10k\Omega}$$

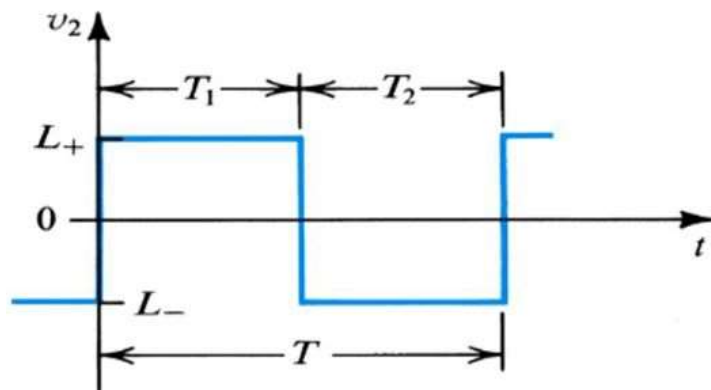
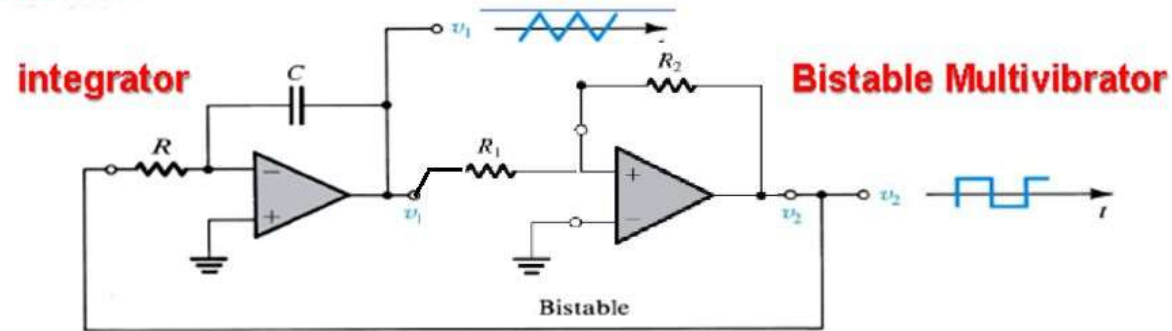
sub. in t. (1)

$$\therefore \boxed{R_2 = 10k\Omega}$$

## 2. Triangular and Square waveforms

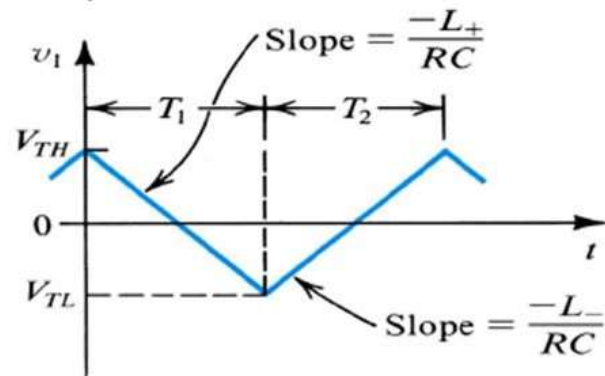


# Circuit



VTH----> Higher threshold level

VTL----> Lower threshold level



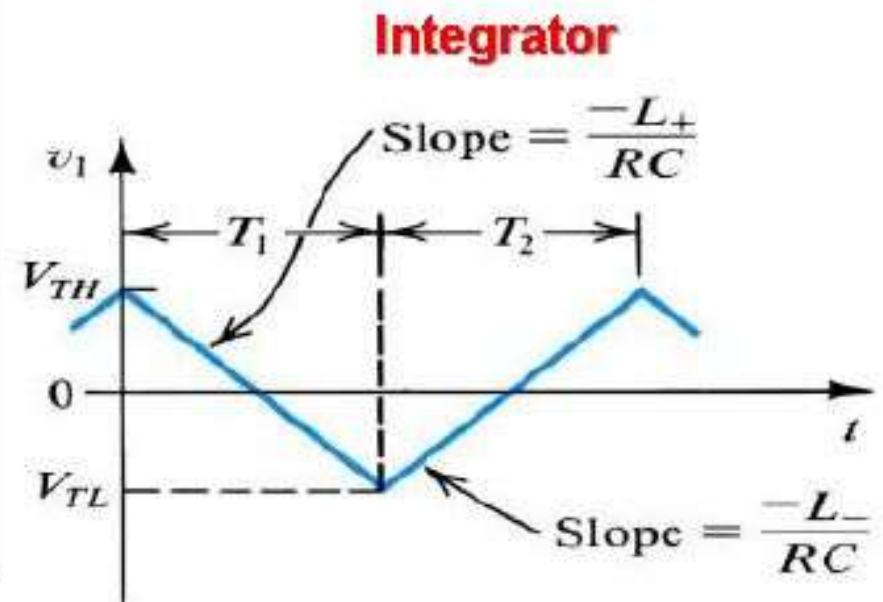
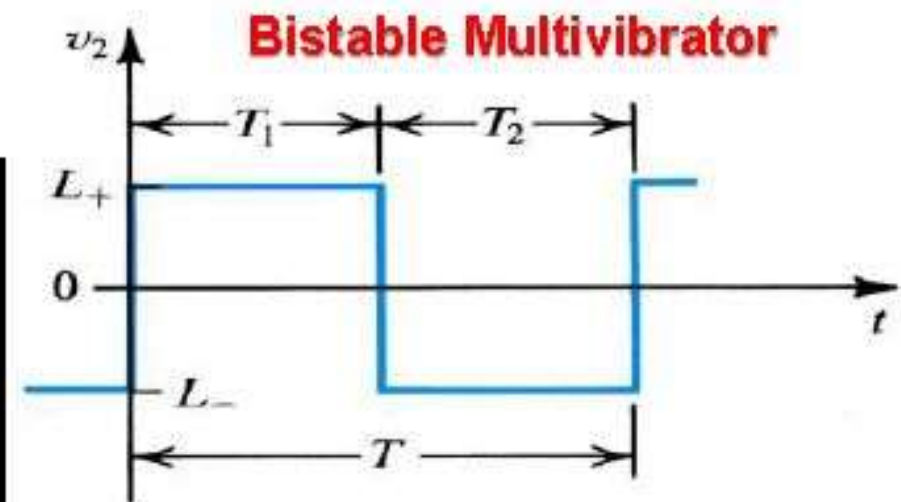
**For  $T_1$**

$$v_1(t) = \frac{-1}{RC} \int v_2(t) dt$$

$$v_1(t) = \frac{-1}{RC} \int V_{cc} dt = \frac{-V_{cc}}{RC} \int dt$$

$$v_1(t) = \frac{-V_{cc}}{RC} t$$

$$\text{slope} = \frac{-V_{cc}}{RC} = \frac{-L^+}{RC}$$



**For  $T_2$**

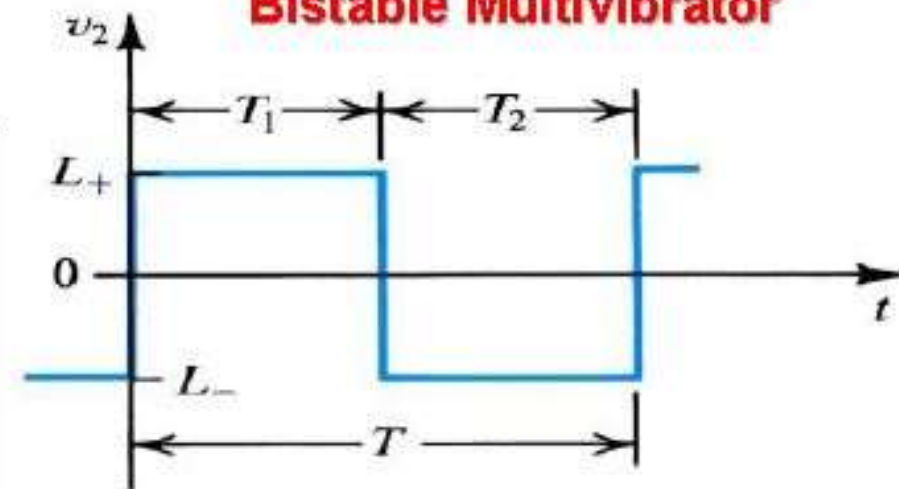
$$v_1(t) = \frac{-1}{RC} \int v_2(t) dt$$

$$v_1(t) = \frac{-1}{RC} \int -V_{cc} dt = -\frac{-V_{cc}}{RC} \int dt$$

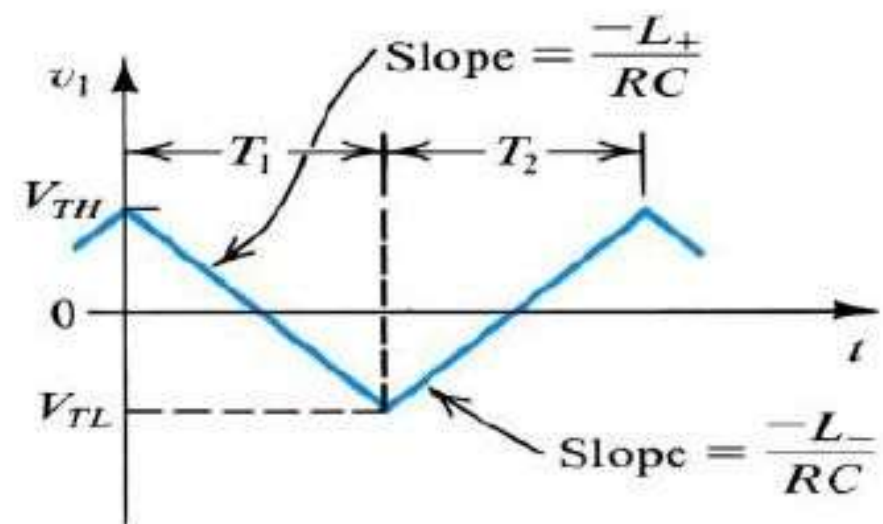
$$v_1(t) = -\frac{-V_{cc}}{RC} t$$

$$\text{slope} = -\frac{-V_{cc}}{RC} = \frac{-L^-}{RC}$$

### Bistable Multivibrator



### Integrator





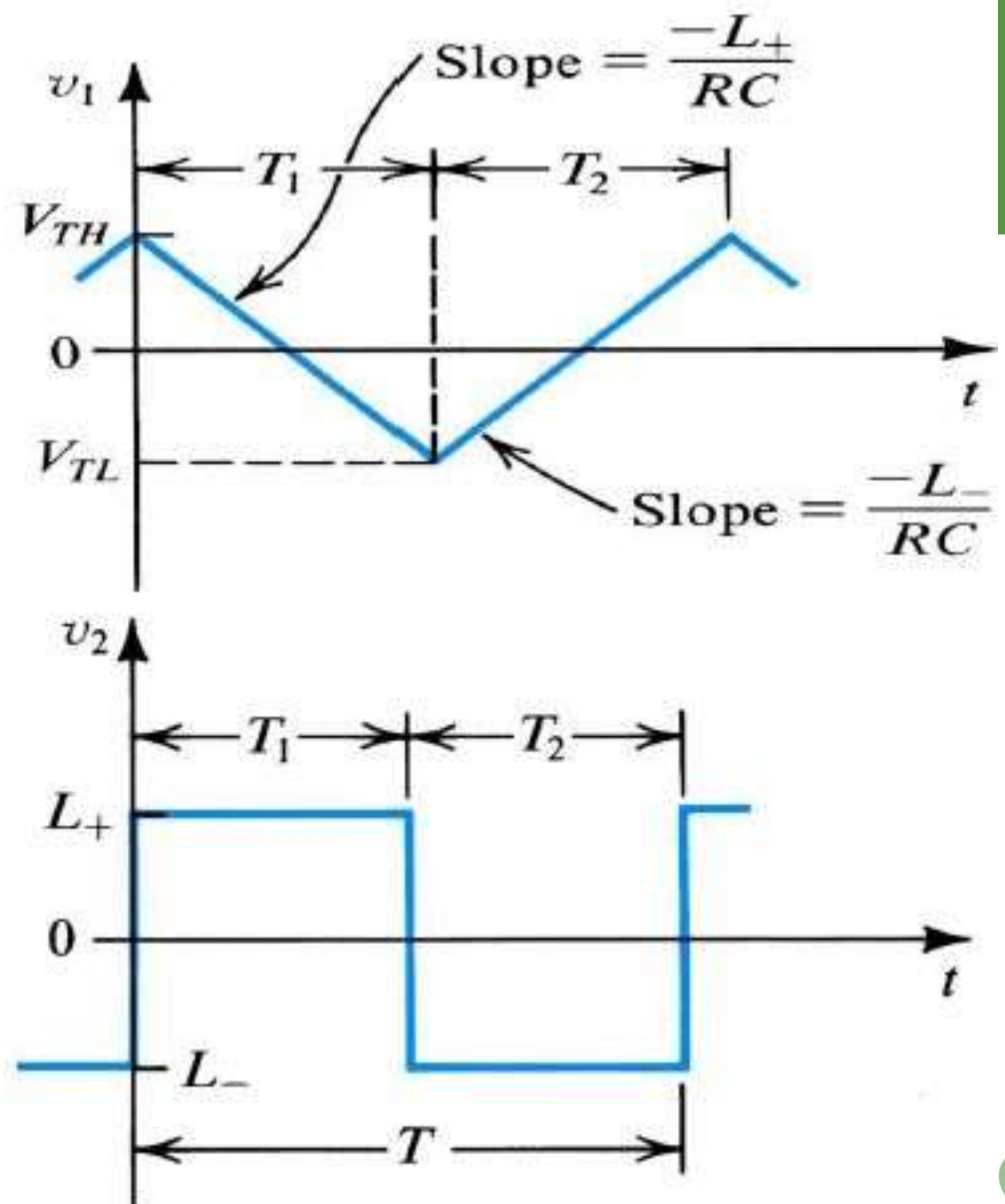
$$\text{slope} = \frac{L^+}{RC} = \frac{V_{TH} - V_{TL}}{T_H}$$

$$T_H = RC \frac{V_{TH} - V_{TL}}{L^+}$$

$$\text{slope} = \frac{-L^-}{RC} = \frac{V_{TH} - V_{TL}}{T_L}$$

$$T_L = RC \frac{V_{TH} - V_{TL}}{-L^-}$$

$$T_L = RC \frac{V_{TH} - V_{TL}}{L^+} = T_H$$



$$T_L = RC \frac{V_{TH} - V_{TL}}{L^+} = T_H$$

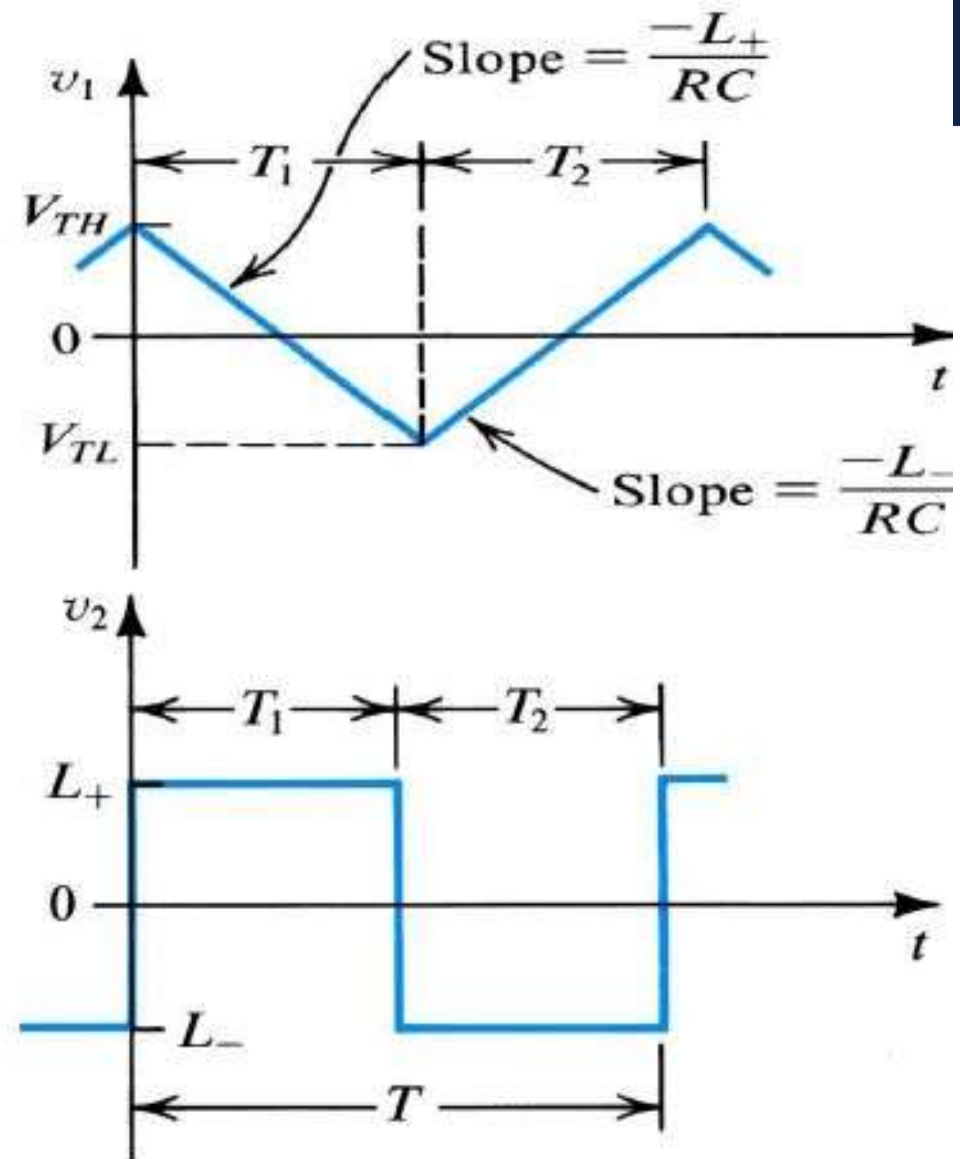
$$T = T_L + T_H = 2RC \frac{V_{TH} - V_{TL}}{L^+}$$

$$T = 2RC \frac{\beta L^+ - \beta L^-}{L^+}$$

$$T = 2RC \frac{\beta L^+ + \beta L^-}{L^+} = 4RC\beta$$

$$\beta = \frac{R_1}{R_2}$$

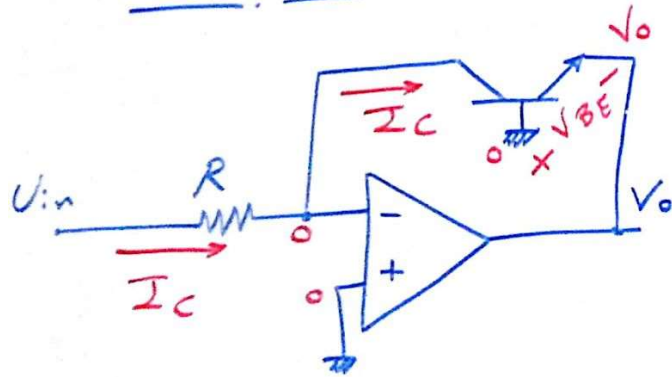
$$T = 4RC \frac{R_1}{R_2}, \quad f = \frac{1}{T}$$





# Non-linear Op-Amp applications

## □ Logarithmic Amplifier (Log - Amplifier)



$$I_C = I_S e^{\frac{V_{BE}}{V_T}}$$

$I_S$  = Reverse saturation current  
 $V_T$  = Thermal Voltage  
 $= 0.025 \text{ V}$  at room temp.

$$I_C = I_S e^{\frac{V_{BE}}{V_T}}$$

$$\downarrow$$

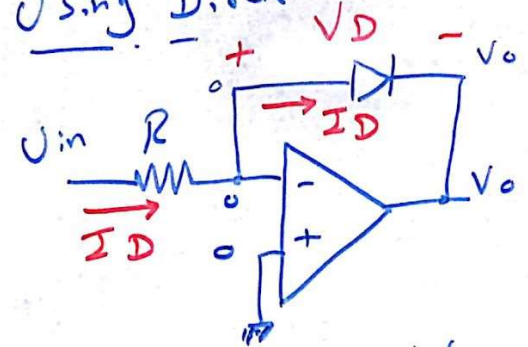
$$\frac{V_{in}}{R} = I_S e^{\frac{0 - V_o}{V_T}}$$

$$\frac{V_{in}}{I_S R} = e^{-\frac{V_o}{V_T}}$$

$$V_o = -V_T \ln\left(\frac{V_{in}}{I_S R}\right)$$

$$V_o \propto \ln V_{in}$$

Using Diode



$$I_D = I_S e^{\frac{V_D}{V_T}}$$

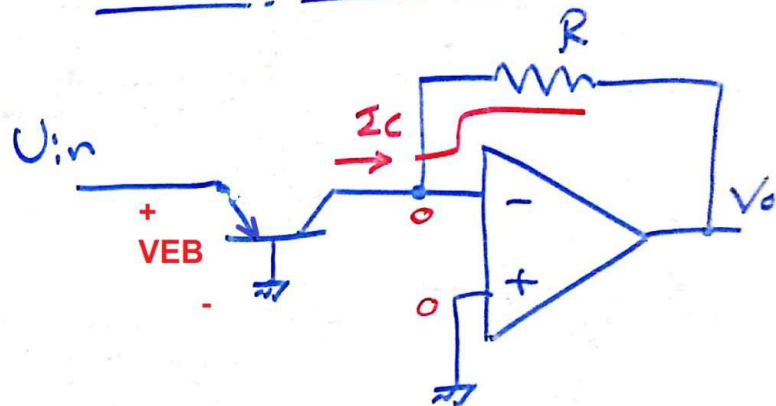
$$\downarrow$$

$$\frac{V_{in}}{R} = I_S e^{\frac{0 - V_o}{V_T}}$$

$$\frac{V_{in}}{I_S R} = e^{-\frac{V_o}{V_T}}$$

$$V_o = -V_T \ln\left(\frac{V_{in}}{I_S R}\right)$$

## 2] Anti-Logarithmic Amplifier (Anti-Log Amplifier)

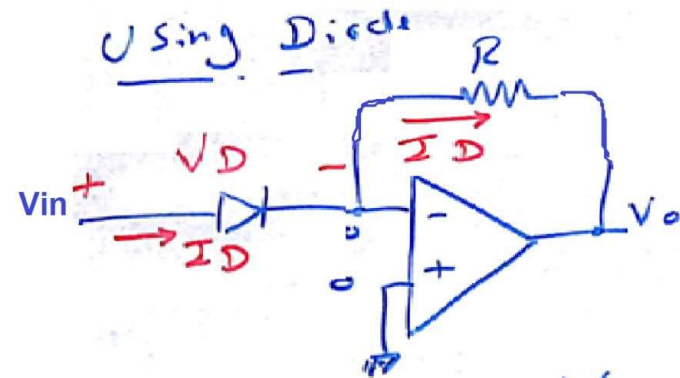


$$I_C = I_S e^{\frac{V_{EB}}{V_T}}$$

$$\downarrow$$

$$-\frac{V_o}{R} = I_S e^{\frac{V_{in}-0}{V_T}}$$

$$V_o = -I_S R e^{\frac{V_{in}}{V_T}}$$



$$I_D = I_S e^{\frac{V_D}{V_T}}$$

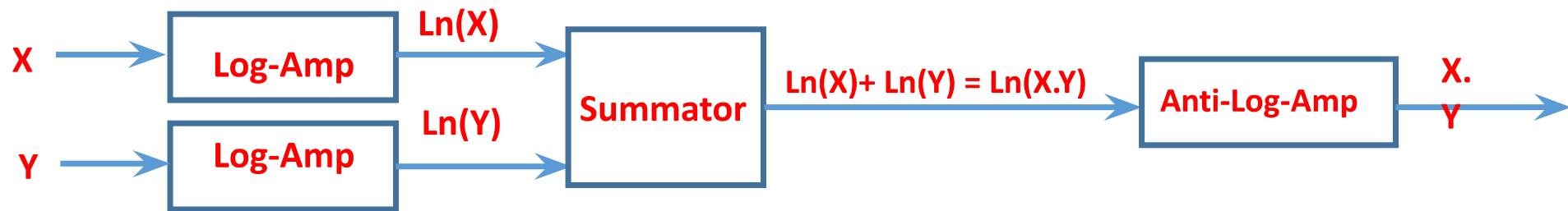
$$\downarrow$$

$$-\frac{V_o}{R} = I_S e^{\frac{V_{in}-0}{V_T}}$$

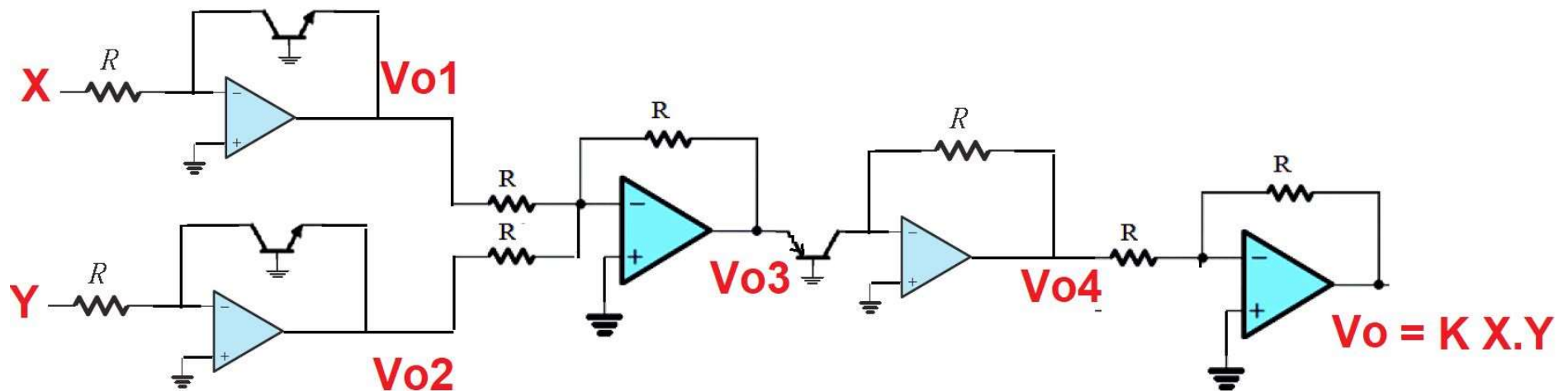
$$V_o = -I_S R e^{\frac{V_{in}}{V_T}}$$

# Analog Multiplier

## 1. Block-Diagram



## 2. Circuit-Diagram



$$\square V_{o1} = -V_T \ln\left(\frac{X}{I_s R}\right)$$

$$\square V_{o2} = -V_T \ln\left(\frac{Y}{I_s R}\right)$$

$$\square V_{o3} = -\frac{R}{R} (-V_T \ln\left(\frac{X}{I_s R}\right) - V_T \ln\left(\frac{Y}{I_s R}\right)) = V_T \ln\left(\frac{X}{I_s R}\right) + V_T \ln\left(\frac{Y}{I_s R}\right) = V_T \ln\left(\frac{X.Y}{(I_s R)^2}\right)$$

$$\square V_{o4} = -I_s R e^{V_T \ln\left(\frac{X.Y}{(I_s R)^2}\right)/V_T} = -I_s R \left(\frac{X.Y}{(I_s R)^2}\right) = \left(\frac{-1}{I_s R}\right) X.Y$$

$$\square V_{o4} = \left(\frac{-1}{I_s R}\right) X.Y$$

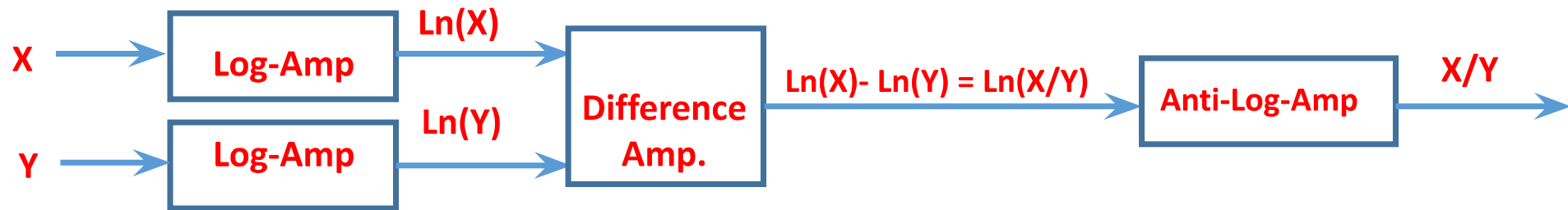
$$\square V_o = -\frac{R}{R} \left(\frac{-1}{I_s R}\right) X.Y = \frac{1}{I_s R} X.Y$$

$$\square \boxed{V_o = \frac{1}{I_s R} X.Y = K X.Y}$$

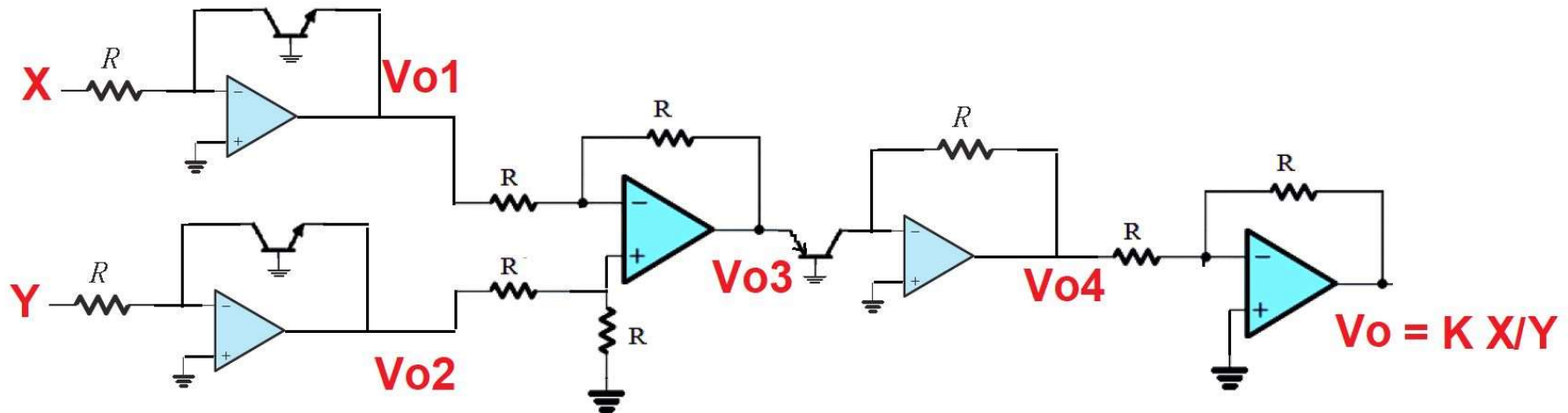
$$\text{Where } K = \frac{1}{I_s R}$$

# Analog Divider

## 1. Block-Diagram



## 2. Circuit-Diagram



$$\square V_{o1} = -V_T \ln\left(\frac{X}{I_s R}\right)$$

$$\square V_{o2} = -V_T \ln\left(\frac{Y}{I_s R}\right)$$

$$\square V_{o3} = \frac{R}{R} (-V_T \ln\left(\frac{Y}{I_s R}\right) - (-V_T \ln\left(\frac{X}{I_s R}\right))) = V_T \ln\left(\frac{X}{I_s R}\right) - V_T \ln\left(\frac{Y}{I_s R}\right) = V_T \ln\left(\frac{X}{Y}\right)$$

$$\square V_{o4} = -I_s R e^{V_T \ln\left(\frac{X}{Y}\right) / V_T} = -I_s R \left(\frac{X}{Y}\right)$$

$$\square V_{o4} = -I_s R \left(\frac{X}{Y}\right)$$

$$\square V_o = -\frac{R}{R} (-I_s R \left(\frac{X}{Y}\right)) = I_s R \left(\frac{X}{Y}\right)$$

$$\square V_o = I_s R \left(\frac{X}{Y}\right) = K \left(\frac{X}{Y}\right)$$

Where  $K = I_s R$



