

# Electronic Devices

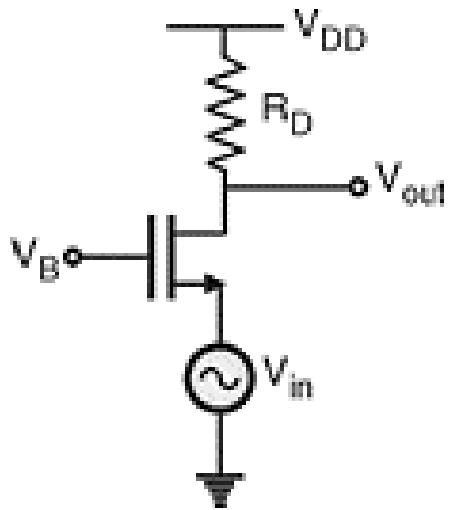
## Lecture 19

### Field Effect Transistor

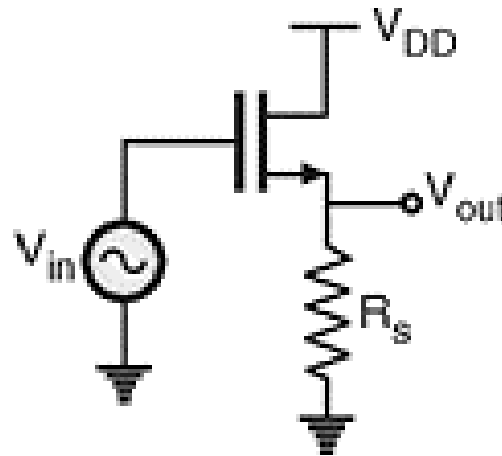
### “MOSFET”

**Dr. Roaa Mubarak**

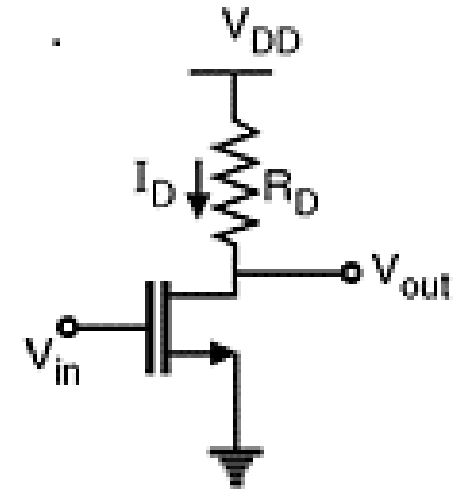
# MOSFET as an amplifier



Common gate amplifier



Common drain amplifier



Common source amplifier

# Common Source Amplifier

$$v_{GS} = V_{GS} + v_{gs}$$

$$i_D = \frac{1}{2} k'_n \frac{W}{L} (V_{GS} + v_{gs} - V_t)^2$$

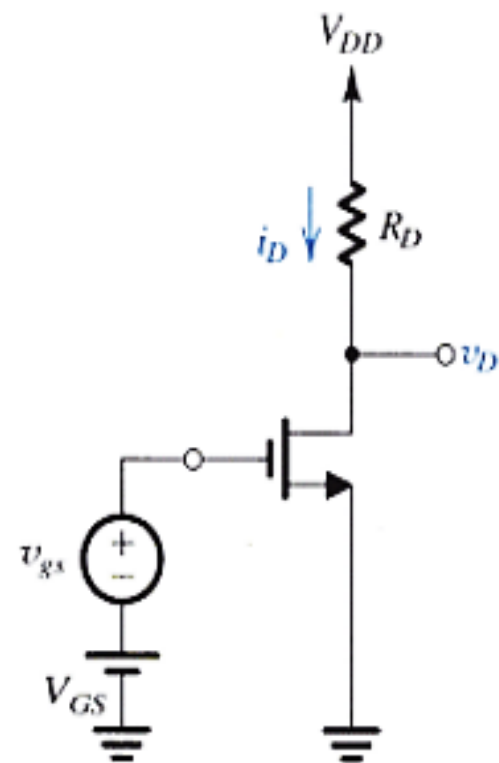
$$= \frac{1}{2} k'_n \frac{W}{L} (V_{GS} - V_t)^2 + k'_n \frac{W}{L} (V_{GS} - V_t) v_{gs} + \frac{1}{2} k'_n \frac{W}{L} v_{gs}^2$$

For small input signal that  $\frac{1}{2} k'_n \frac{W}{L} v_{gs}^2 \ll k'_n \frac{W}{L} (V_{GS} - V_t) v_{gs}$

which results in  $v_{gs} \ll 2(V_{GS} - V_t)$   $V_{gs} < 0.2(V_{GS} - V_t)$  is commonly required.

we obtain,

$$i_D = \underbrace{\frac{1}{2} k'_n \frac{W}{L} (V_{GS} - V_t)^2}_{I_D} + \underbrace{k'_n \frac{W}{L} (V_{GS} - V_t) v_{gs}}_{i_d}$$

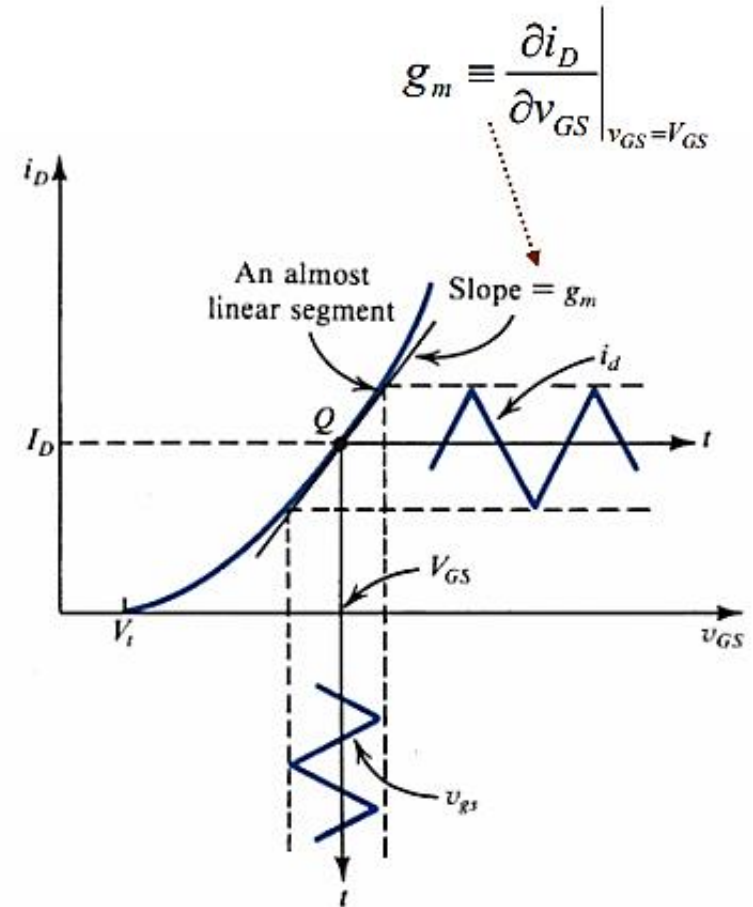


# Transconductance $g_m$

$$i_D = \underbrace{\frac{1}{2}k'_n \frac{W}{L}(V_{GS} - V_t)^2}_{I_D} + \underbrace{k'_n \frac{W}{L}(V_{GS} - V_t)v_{gs}}_{i_d}$$

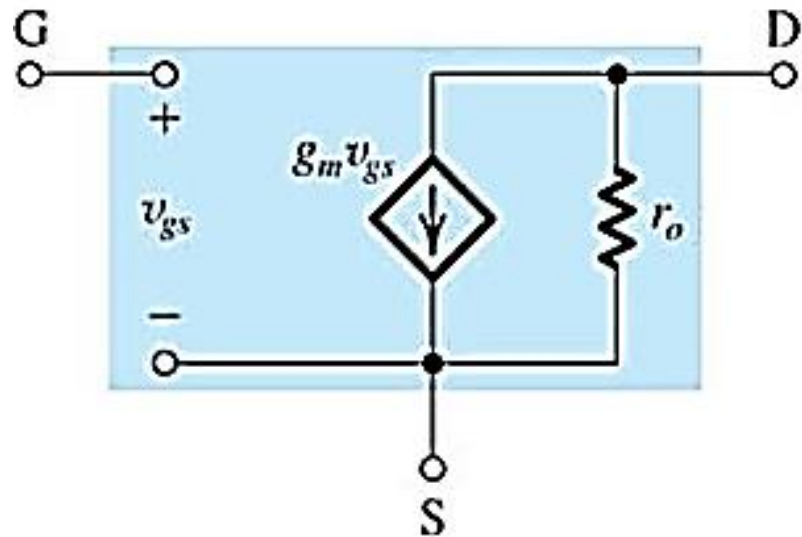
$$\rightarrow g_m = \frac{i_d}{v_{gs}} = k'_n \frac{W}{L}(V_{GS} - V_t)$$

Graphic interpretation:

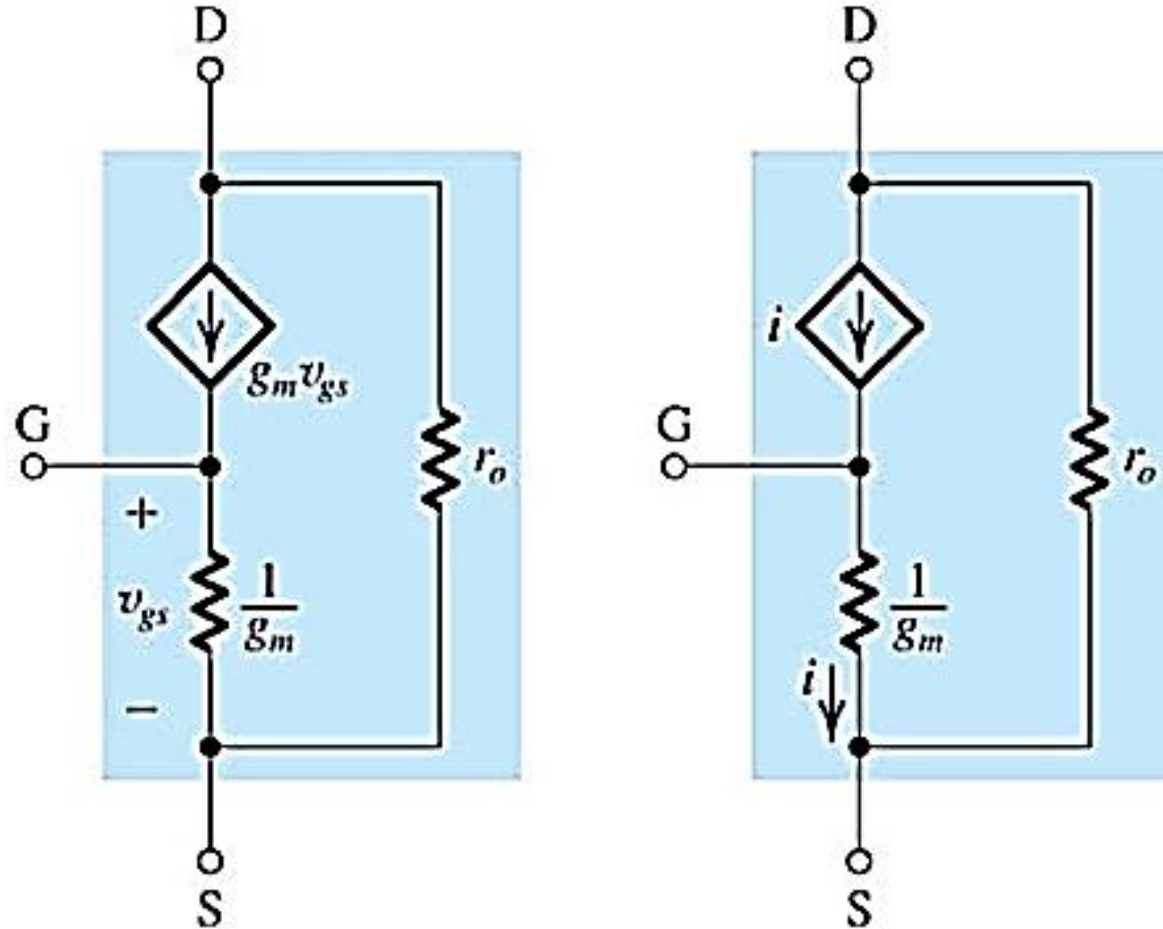


# MOSFET small signal model (Hybrid Model)

$\pi$  Model



T- Model



# NMOS Hybrid $\pi$ Model

- Small signal parameters:

Transconductance “ $g_m$ ”

MOSFET works in saturation mode to act as an amplifier:

$$g_m = \left[ \frac{\partial i_D}{\partial v_{GS}} \right]_{Q \text{ point}}$$

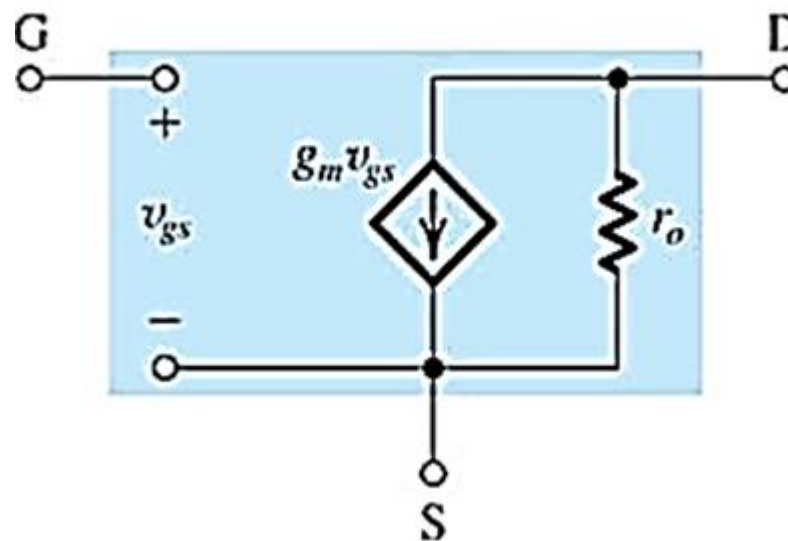
$$i_D = \frac{1}{2} K_n (V_{GS} - V_{th})^2$$

$$g_m = K_n (V_{GS} - V_{th}) = \frac{2I_D}{(V_{GS} - V_{th})}$$

$$K_n = \mu_n C_{ox} \left( \frac{W}{L} \right)$$

$$r_o = \frac{V_A}{I_D}$$

(replacing  $\mu_n$  by  $\mu_p$  for PMOS)



$$g_m \equiv \left. \frac{\partial i_D}{\partial v_{GS}} \right|_{v_{GS}=V_{GS}} = \frac{i_d}{v_{gs}} = k'_n \frac{W}{L} (V_{GS} - V_t)$$

$$r_o \equiv \left[ \left. \frac{\partial i_D}{\partial v_{DS}} \right|_{v_{GS}=V_{GS}} \right]^{-1} = \frac{1 + \lambda V_{DS}}{\lambda I_D} \cong \frac{1}{\lambda I_D}$$

$r_o$  is output resistance due to channel length modulation effect.

# Common source Amplifier

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$\text{i.e. } I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2$$

But by KVL,

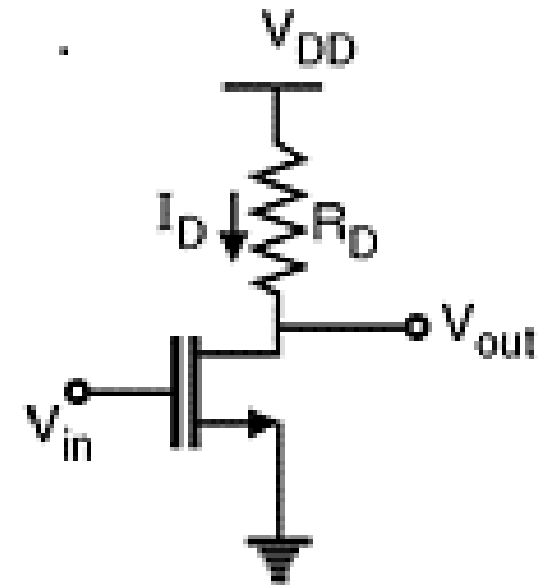
$$V_{DD} - I_D R_D = V_{out}$$

$$\therefore V_{out} = V_{DD} - \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2 R_D$$

Differentiating this equation with respect to  $V_{in}$

$$\frac{dV_{out}}{dV_{in}} = -\mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH}) R_D$$

$$\text{Hence, The voltage gain } A_v = -g_m R_D \quad \left[ \because g_m = \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH}) \right]$$



# Common source Amplifier

By applying KVL

We get

$$V_{in} - V_{GS} = 0$$

$$\text{i.e. } V_{in} = V_{GS}$$

By applying KCL at node A

We get,

$$g_m V_{GS} + \frac{V_{out} - 0}{r_o} + \frac{V_{out} - 0}{R_D} = 0$$

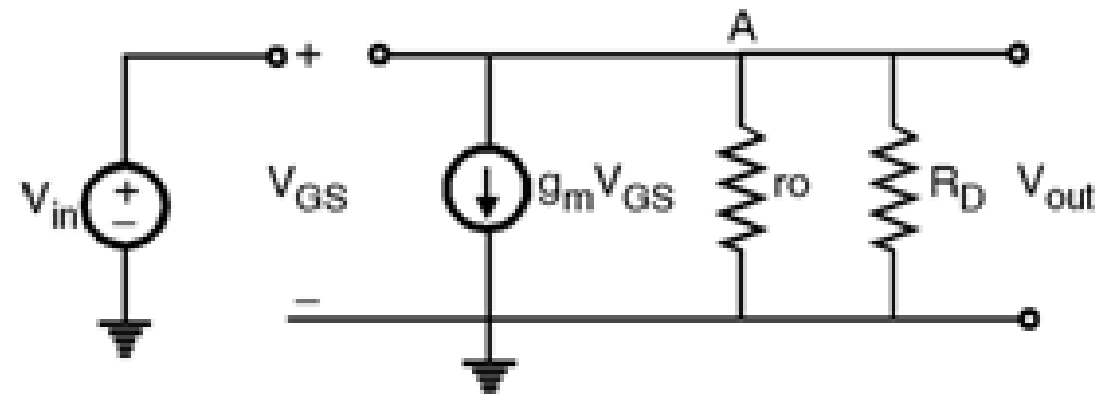
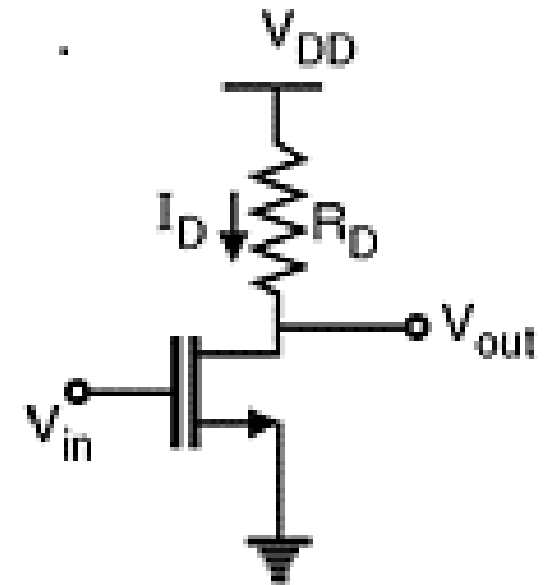
$$\therefore g_m V_{in} = - \left[ \frac{V_{out}}{r_o} + \frac{V_{out}}{R_D} \right]$$

$$\therefore g_m V_{in} = -V_{out} \left( \frac{1}{r_o} + \frac{1}{R_D} \right)$$

$$\therefore \frac{V_{out}}{V_{in}} = A_v = \frac{-g_m}{\left( \frac{1}{r_o} + \frac{1}{R_D} \right)}$$

$$\therefore A_v = -g_m(r_o \parallel R_D)$$

$\therefore$  The voltage gain of CS amplifier is  $-g_m(r_o \parallel R_D)$





# Common source Amplifier

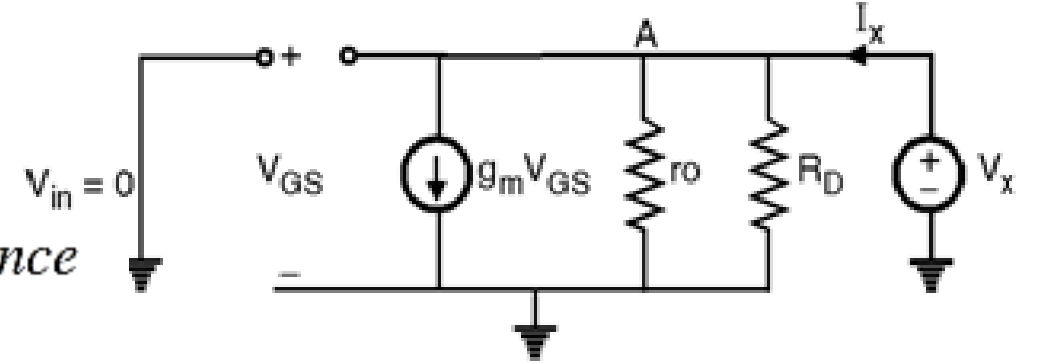
Determine the output resistance and input resistance

$$[V_{GS} = V_{in} = 0]$$

*Also, because of zero gate current the input impedance of CS amplifier is also infinite.*

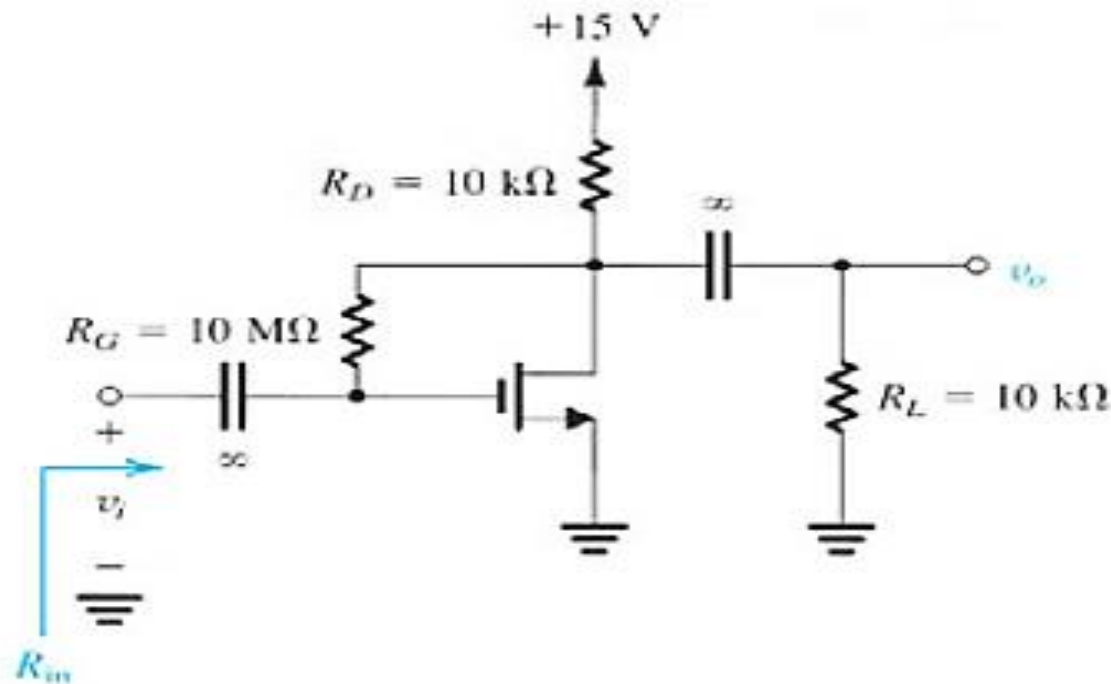
$$\therefore R_{in} = \infty$$

$$R_{out} = (r_o \parallel R_D)$$



## Example

A discrete common source MOSFET amplifier utilizing the drain to gate feedback biasing arrangement. The input signal is coupled to the gate via a large capacitor, and the output signal at the drain is coupled to the load resistance via another large capacitor. Analyze the amplifier to determine its small signal voltage gain. The transistor has  $V_{th} = 1.5$  V,  $K_n = 0.25$  mA/V<sup>2</sup> and  $V_A = 50$  V.



# Solution

First find  $I_D$  and  $V_D$  and then find  $g_m$ ,  $r_o$  and  $A_v$  from the following equations.

$$I_D = \frac{1}{2} K'_n \left( \frac{W}{L} \right) (V_{GS} - V_t)^2 \quad (\text{No gate current so } V_{GS} = V_D)$$

$$I_D = \frac{1}{2} * 0.25 * (V_D - 1.5)^2$$

$$V_D = V_{DD} - R_D I_D$$

$$g_m = K'_n \left( \frac{W}{L} \right) (V_{GS} - V_t)$$

$$r_o = \frac{|V_A|}{I_D}$$

$$A_v = \frac{v_o}{v_i} = -g_m (R_D \parallel R_L \parallel r_o)$$

