

9.00

ELJOKER

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ELECTRONICS

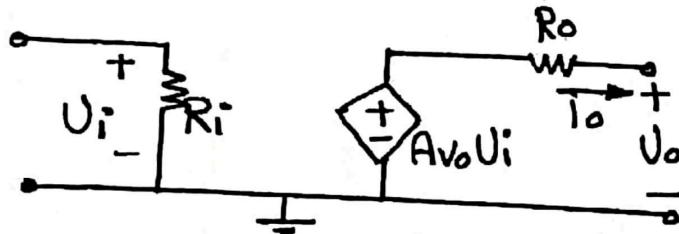
SHEET 6

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Summary for Sheet 6

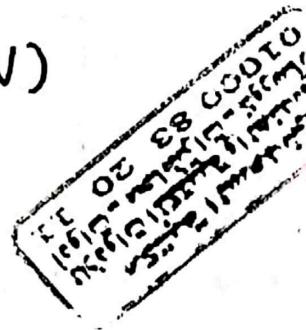
Some important Notes
Amplifier types

① Voltage amplifier



- Open Circuit Voltage Gain

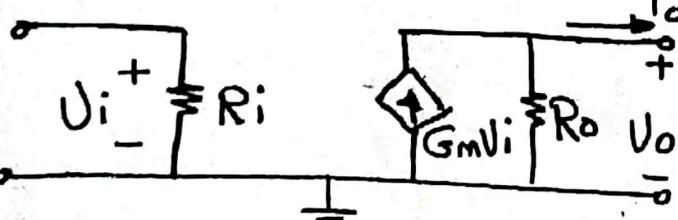
$$A_{v0} = \frac{U_o}{U_i} \Big|_{i_o=0} \quad (\text{V/V})$$



- $R_i = \infty$

- $R_o = 0$

③ transconductance amplifier



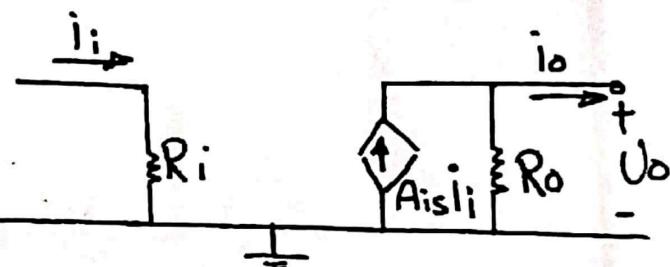
Short-Circuit transconductance

$$G_m = \frac{i_o}{U_i} \Big|_{U_o=0} \quad (\text{A/V})$$

- $R_i = \infty$

- $R_o = \infty$

② Current amplifier



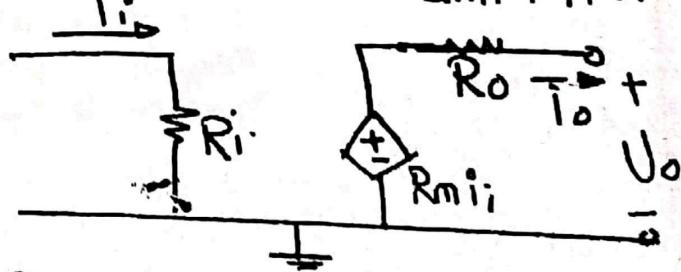
- Short-Circuit Current Gain

$$A_{is0} = \frac{i_o}{i_i} \Big|_{U_o=0} \quad (\text{A/A})$$

- $R_i = 0$

- $R_o = \infty$

④ transresistance amplifier



- Open circuit transresistance

$$R_{m0} = \frac{U_o}{i_i} \Big|_{U_o=0} \quad (\text{V/A})$$

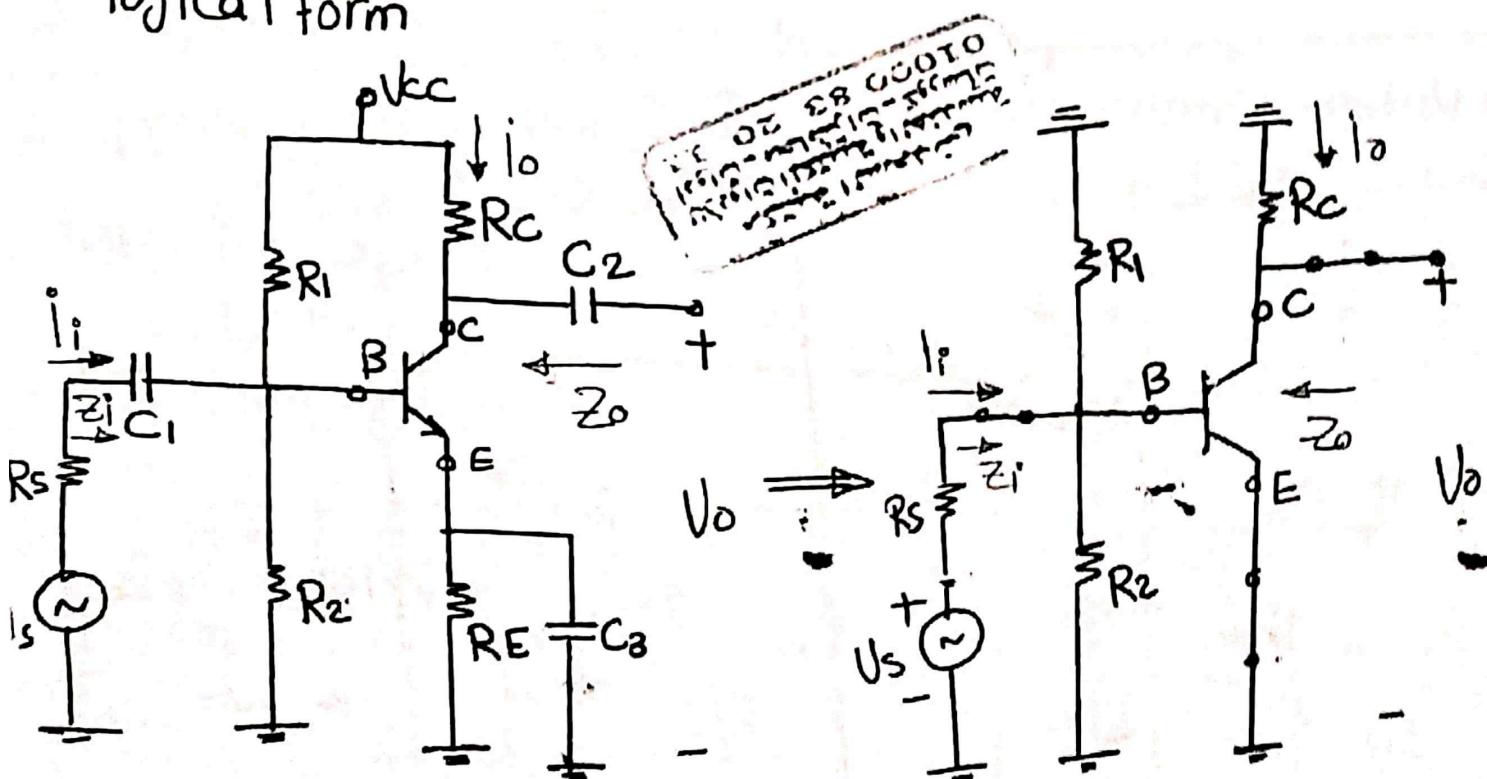
- $R_i = 0$

- $R_o = 0$

Analysis of BJT

the ac equivalent of a transistor Network is obtained by

- ① Setting all dc Sources to zero and Replacing them by a short-circuit equivalent
- ② Replacing all Capacitors by a short circuit equivalent
- ③ Removing all elements bypassed by the short-circuit equivalents introduced by step ① and ②
- ④ Redrawing the Network in more convenient and logical form

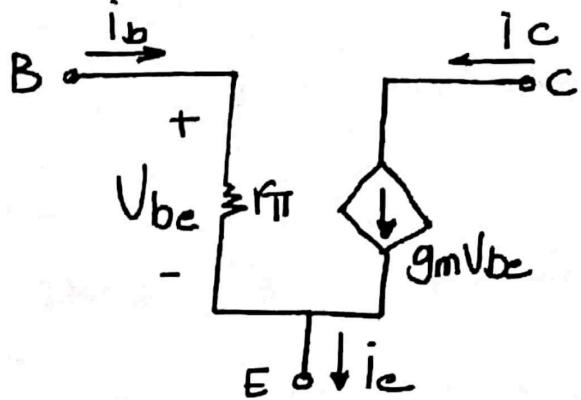


- ⑤ Replacing the BJT with appropriate model

→ τ model
or → Hybrid model (hybrid π model)

* Hybrid π model 8-

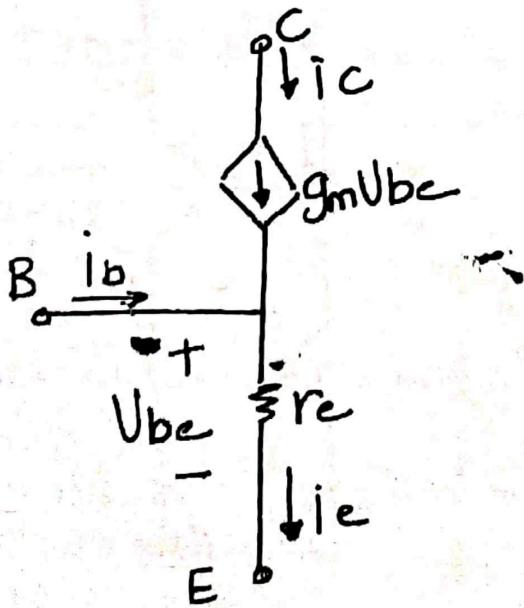
① Voltage Controlled Current Source "VccS"



$$\cdot g_m = \frac{I_C}{V_T}$$

$$\cdot r_\pi = \frac{V_T}{I_B}$$

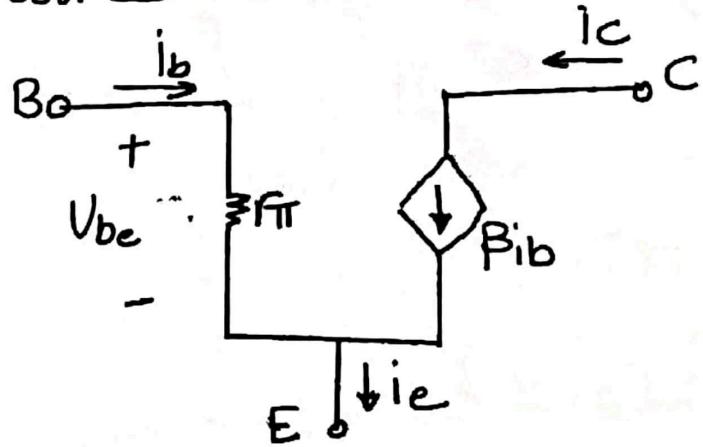
③ Voltage Controlled Current Source "VccS"



$$g_m = \frac{I_C}{V_T}$$

$$r_e = \frac{V_T}{I_E}$$

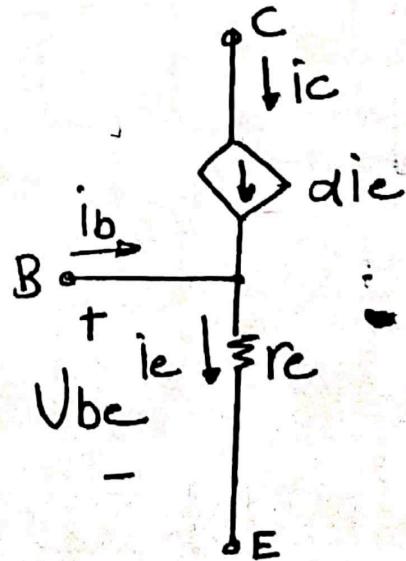
② Current Controlled Current Source "CCCS"



$$\cdot r_\pi = \frac{B}{g_m}$$

↳ $B = \alpha$

④ Current Controlled Current Source "CCCS"



$$r_e = \frac{\alpha}{g_m}$$

$$g_m = \frac{I_C}{V_T}$$

Steps for solving AC analysis of BJT

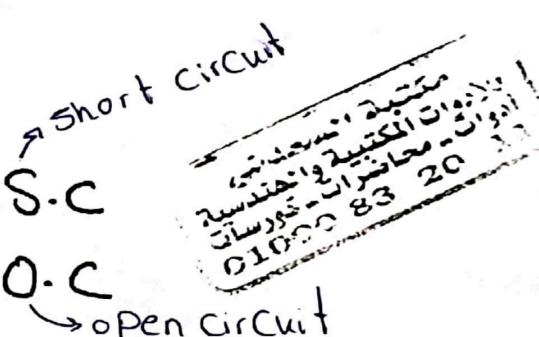
First DC analysis

Using the DC analysis to calculate the Parameters of Small Signal model g_m , r_{π} and r_e

Second AC analysis

① Replace all Capacitors by S.C

Replace all inductors by O.C



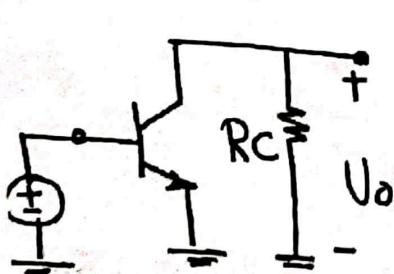
② Replace the DC Voltage Source by S.C

Replace the DC Current Source by O.C

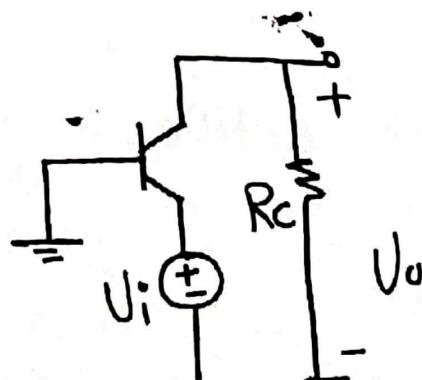
③ Replace the BJT by the Small Signal model

④ Analyze the Circuit to determine the amplifier gain

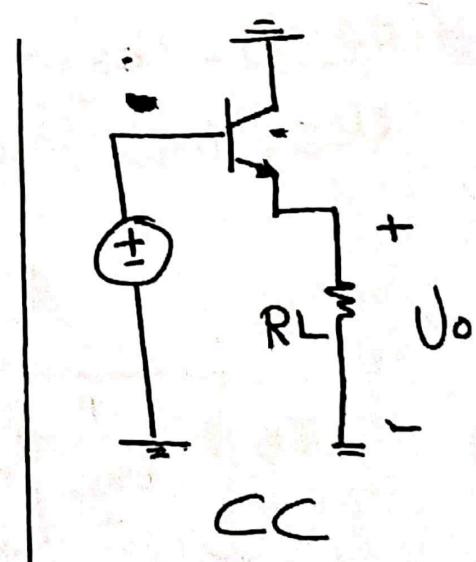
BJT Configuration



CE



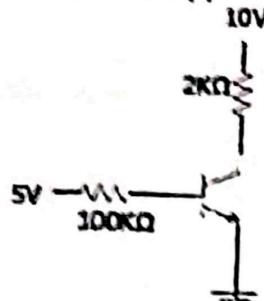
CB



CC

Sheet 6

1. For the circuits shown, draw the equivalent AC circuit model. Denote on your schematic the values of r_π and r_o . ($\beta = 100$, $V_A = 100 \text{ V}$)



Sol:-

→ DC analysis

i/P loop

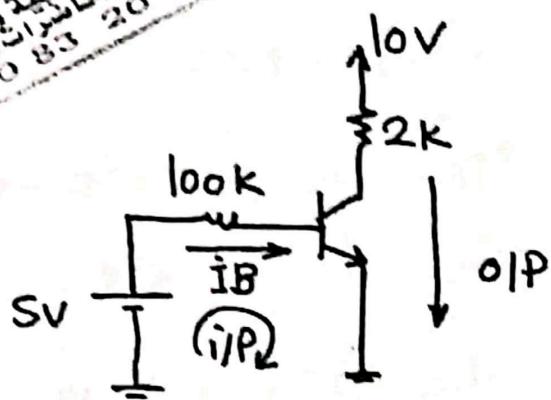
$$5 - I_B(100) - V_{BE} = 0$$

$$5 - I_B(100) - 0.7 = 0$$

$$I_B = 0.043 \text{ mA}$$

$$I_C = \beta I_B = 4.3 \text{ mA}$$

$$I_E = (1 + \beta) I_B = 4.343 \text{ mA}$$



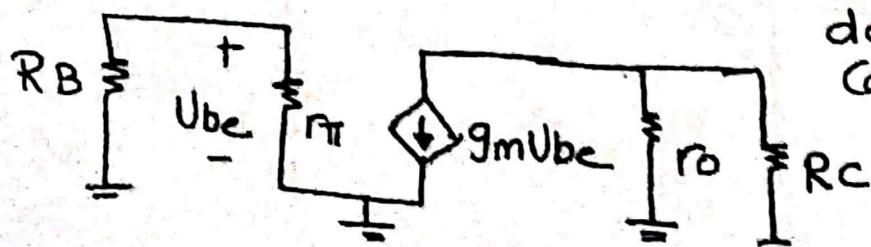
o/P loop

$$V_{CC} - I_C R_C - U_{CE} = 0$$

$$10 - (4.3)(2) - U_{CE} = 0$$

$$U_{CE} = 1.4 > U_{BE} \quad \text{active}$$

→ AC



dc Volt Source S.C
dc Current Source O.C
Capacitors S.C

$$g_m = \frac{I_C}{V_T} = \frac{4.3 \times 10^{-3}}{0.025} = 0.172 \text{ A/V}$$

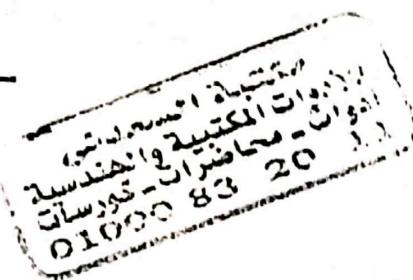
$$= 172 \text{ mA/V}$$

$$\rightarrow r_{\pi} = \frac{V_T}{I_B}$$

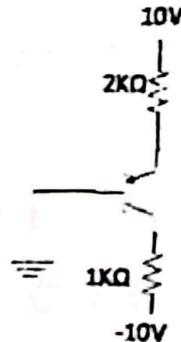
$$= \frac{0.025}{0.043} = 581.39 \Omega$$

$$\rightarrow r_o = \frac{U_A}{I_C}$$

$$= \frac{100}{4.3 \times 10^{-3}} = 23.25 \text{ k}\Omega$$



- 2- For the circuits shown, draw the equivalent AC circuit model. Denote on your schematic the values of π and r_o . ($\beta = 100$, $V_A = 100 \text{ V}$)



Sol:-

→ DC analysis

input loop

$$I_O - I_E(2) - V_{EB} = 0$$

$$I_O - I_E(2) - 0.7 = 0$$

$$I_E = 4.65 \text{ mA}$$

$$I_B = 0.046 \text{ mA}$$

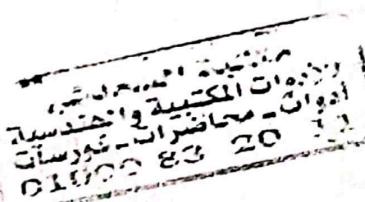
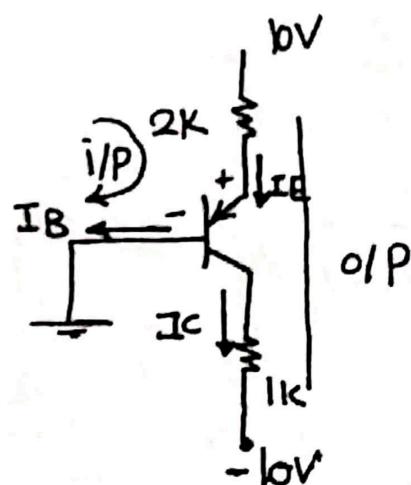
$$I_C = 4.603 \text{ mA}$$

output loop

$$I_O - I_E(2) - V_{EC} - I_C(1) + I_O = 0$$

$$I_O - (4.65)(2) - V_{EC} - (4.603)(1) + I_O = 0$$

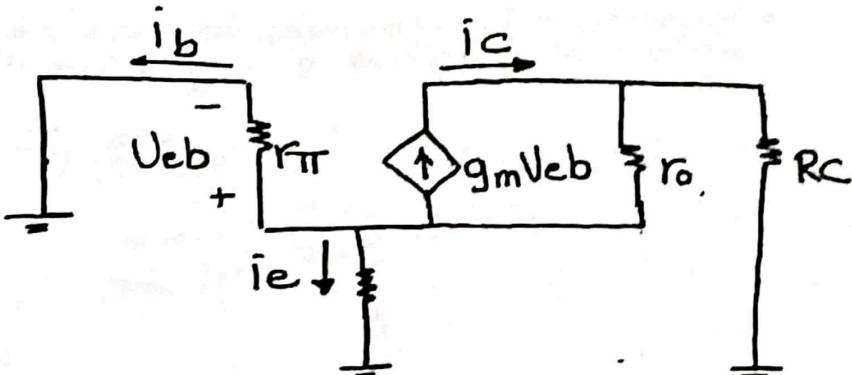
$$V_{EC} = 6.097 > V_{EB} \text{ active}$$



Equivalent Circuit

(4)

- Dc Volt Source s.c
- Dc Current Source o.c
- Capacitors s.c

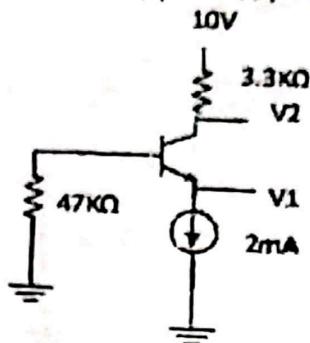


$$\rightarrow g_m = \frac{I_C}{U_T} = \frac{4.603 \times 10^{-3}}{0.025} = 184.12 \text{ mA/V}$$

$$\rightarrow r_{\pi} = \frac{U_T}{I_B} = \frac{0.025}{0.046 \times 10^{-3}} = 543.47 \Omega$$

$$\rightarrow r_o = \frac{U_A}{I_C} = \frac{100}{4.603 \times 10^{-3}} = 21.72 \text{ k}\Omega$$

3. For the circuits shown, draw the equivalent AC circuit model. Denote on your schematic the values of r_{π} and r_o . ($\beta = 100$, $V_A = 100 \text{ V}$)

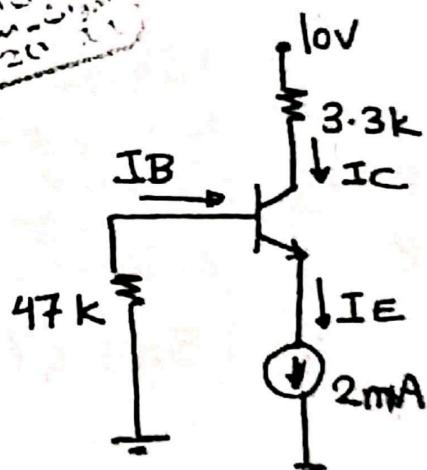


Sol:-

→ DC analysis

$$\therefore I_E = 2 \text{ mA}$$

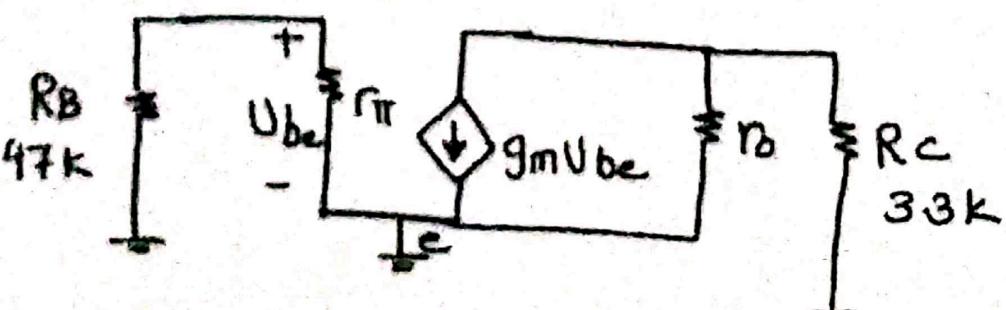
$$\therefore I_B = \frac{I_E}{1+\beta} = \frac{2 \text{ mA}}{101} = 0.0198 \text{ mA}$$



$$I_C = I_B \beta = 1.98 \text{ mA}$$

→ AC equivalent circuit

- DC Voltage Source S.C.
- DC Current Source O.C.
- Capacitors S.C.



$$g_m = \frac{I_C}{U_T}$$

$$= \frac{1.98}{0.025} = 79.2 \text{ mA/V}$$

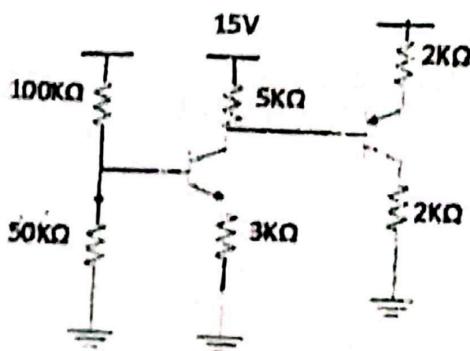
$$\rightarrow r_{\pi} = \frac{U_T}{I_B}$$

$$= \frac{0.025}{0.0198 \times 10^3} = 1262.6 \Omega$$

$$\rightarrow r_o = \frac{U_A}{I_C}$$

$$= \frac{100}{1.98 \times 10^3} = 50.5 \text{ k}\Omega$$

4. For the circuits shown, draw the equivalent AC circuit model. Denote on your schematic the values of μ and r_o . ($\beta = 100$, $V_A = 100 V$)



Sol -

$$U_{th} = \frac{IS \times S_0}{S_0 + 100}$$

$$= 5V$$

$$R_{th} = \frac{100 \times S_0}{100 + S_0}$$

$$= 33.3 k\Omega$$

i/P loop 1

$$U_{th} - I_{B1}(R_{th}) - V_{BE1} - I_{E1}(R_E) = 0$$

$$5 - I_{B1}(33.3) - 0.7 - (1+\beta) I_{B1}(3) = 0$$

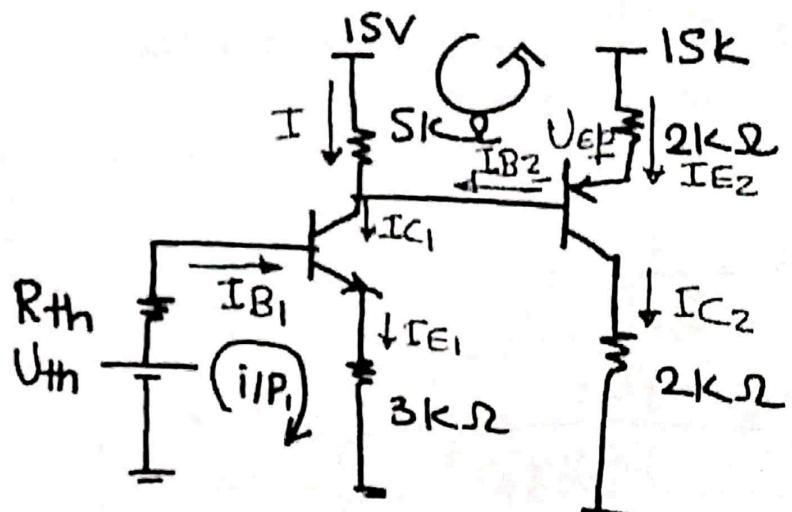
$$\therefore I_{B1} = 0.01278 mA$$

$$I_{C1} = \beta I_{B1} = 1.278 mA$$

$$I_{E1} = (1+\beta) I_{B1} = 1.291 mA$$

$$I + I_{B2} = I_{C1}$$

$$I = I_{C1} - I_{B2}$$



$$+S - I(5) + U_E b + I E_2(2) - 1S = 0$$

$$-\left[(I_{C1} - I_{B2})(S) \right] + 0.7 + (1+\beta)I_{B2}$$

$$-(5)IC_1 + (5)IB_2 + 0.7 + (101)(2)IB_2 = 0$$

$$- (S)(1.278) + (S)IB_2 + 0.7 + (101)(2)IB_2 = 0$$

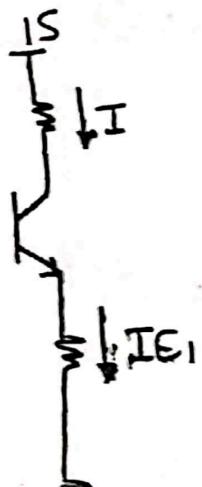
$$I_{B2} = 0.0275 \text{ mA}$$

$$IC_2 = 2.75 \text{ mA}$$

$$I_{E2} = 277 \text{ mA}$$

$$I = I_{C1} - I_{B2} = 1.25 \text{ mA}$$

o IP loop



$$IS - I(S) - \cup_{CE_1} - IE_1(3) = 0$$

$$1S - 1 \cdot 25(5) - V_{CE_1} - (1 \cdot 291)(3) = 0$$

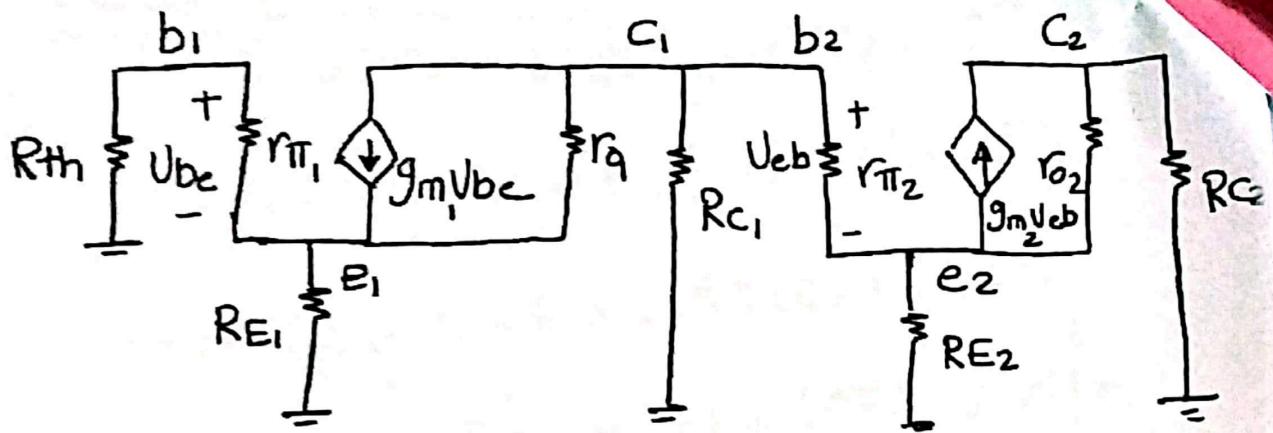
$$U_{CE1} = 4.877 > U_{BE}$$

oPloop₂

$$IS - I_{E2}(2) - V_{EC2} - I_{C2}(2) = 0$$

$$V_{EC2} = 3.96 > U_{EB}$$

→ HC equivalent circuit



$$g_{m1} = \frac{I_{C1}}{V_T} = \frac{1.278}{0.025} = 51.12 \text{ mA/V}$$

$$r_{\pi 1} = \frac{V_T}{I_{B1}} = \frac{0.025}{0.01278 \times 10^3} = 1956.18 \Omega$$

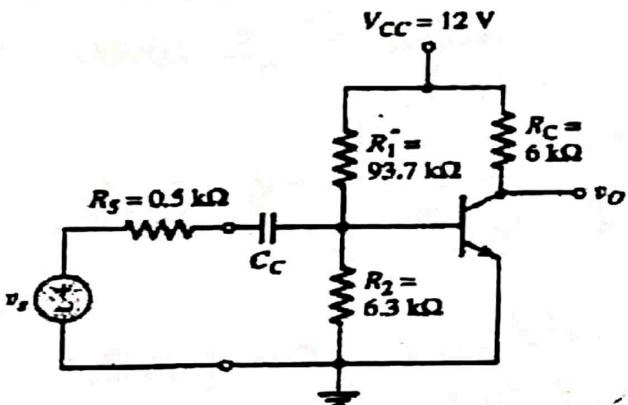
$$r_o = \frac{V_A}{I_{C1}} = \frac{100}{1.278} = 78.24 \text{ k}\Omega$$

$$g_{m2} = \frac{I_{C2}}{V_T} = \frac{2.75}{0.025} = 110 \text{ mA/V}$$

$$r_{\pi 2} = \frac{V_T}{I_{B2}} = \frac{0.025}{0.0275 \times 10^3} = 909.09 \Omega$$

$$r_o = \frac{V_A}{I_{C2}} = \frac{100}{2.75} = 36.36 \text{ k}\Omega$$

5. Determine the small-signal voltage gain, input resistance, and output resistance of the circuit shown. Assume the transistor parameters are: $\beta=100$, $V_{BE(on)} = 0.7V$, and $V_A = 100V$



Sol 8 -

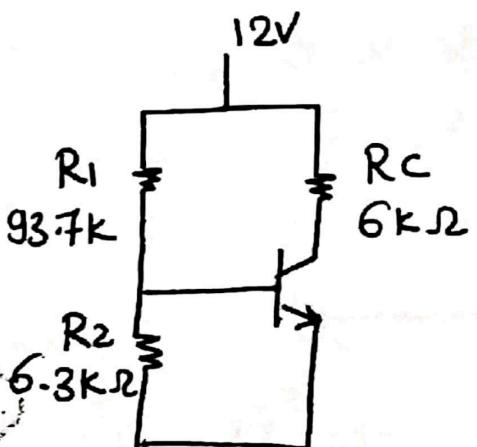
→ Dc analysis

$$U_{th} = \frac{12 * R_2}{R_1 + R_2}$$

$$= 0.756V$$

$$R_{th} = \frac{R_1 R_2}{R_1 + R_2}$$

$$= 5.9 k\Omega$$



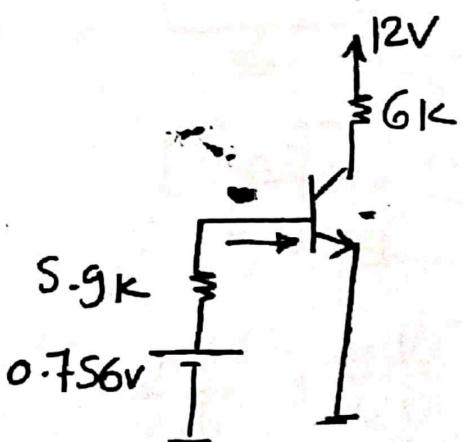
i/P loop

$$0.756 - I_B(5.9) - V_{BE} = 0$$

$$I_B = 9.49 \mu A$$

$$I_C = 0.949 mA$$

$$I_E = 0.958 mA$$



o/P loop

$$12 - 6 I_C - V_{CE} = 0$$

$$V_{CE} = 6.3 > V_{BE}$$

► Ac analysis

$$g_m = \frac{I_C}{V_T} = \frac{0.949}{0.025} = 37.96 \text{ mA/V}$$

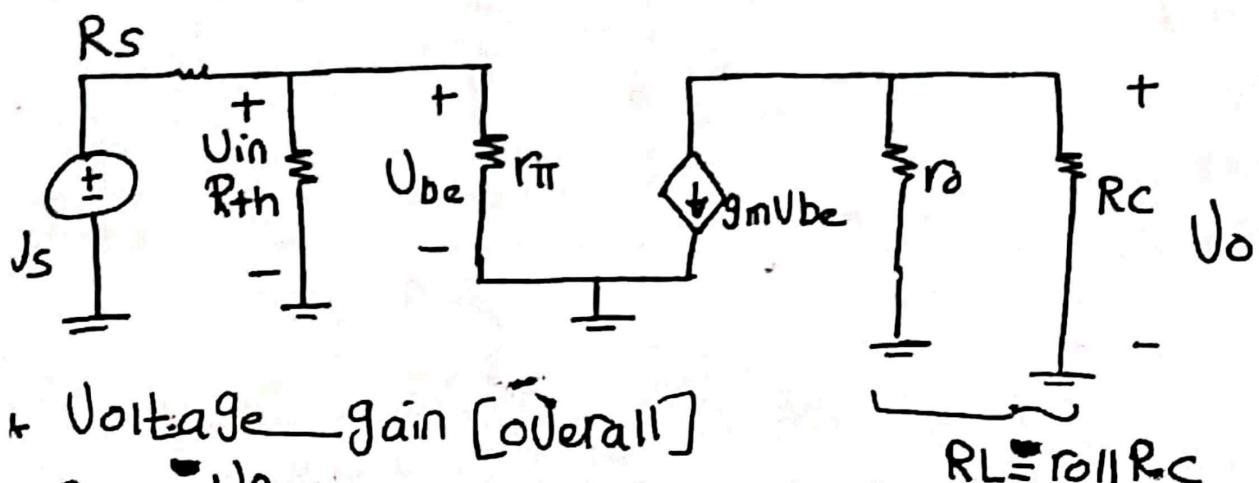
$$r_{\pi} = \frac{V_T}{I_B} = \frac{0.025}{9.49 \times 10^{-6}} = 2634.3 \Omega$$

$$r_o = \frac{U_A}{I_C} = \frac{100}{0.949} = 105.4 \text{ k}\Omega$$

► Ac equivalent circuit

Dc Voltage Source S.C

Capacitors S.C



► Voltage gain [overall]

$$G_V = \frac{U_o}{U_s}$$

$$= \frac{U_o}{U_{be}} * \frac{U_{be}}{U_{in}} * \frac{U_{in}}{U_s}$$

$$U_o = -g_m U_{be} R_L$$

$$\frac{U_o}{U_{be}} = -g_m R_L$$

at Resistance

$$\rightarrow R_{in} = R_{th} \parallel r_{pi}$$

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11

$$U_{be} = U_{in}$$

$$U_{in} = U_s \frac{R_{in}}{R_{in} + R_s}$$

$$\frac{U_{in}}{U_s} = \frac{R_{in}}{R_{in} + R_s}$$

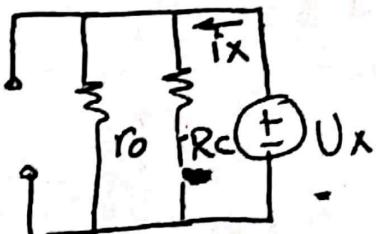
$$G_V = \frac{U_o}{U_{be}} * \frac{U_{be}}{U_{in}} * \frac{U_{in}}{U_s}$$

$$G_V = [-g_m R_L] \left[\frac{R_{in}}{R_{in} + R_s} \right]$$

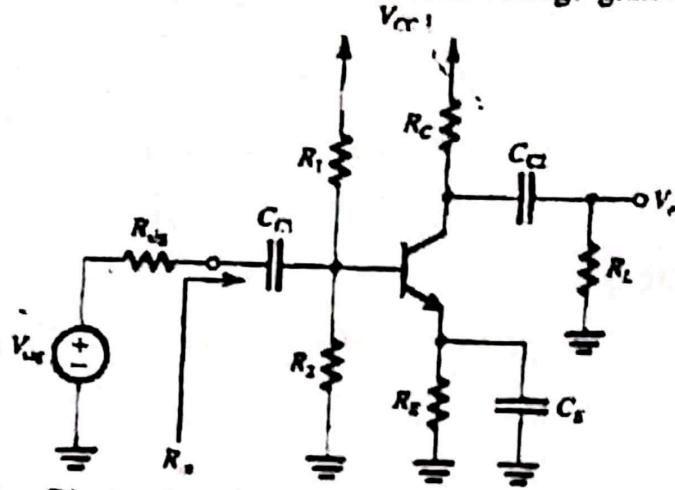
* output resistance

$$R_{out} = \frac{U_x}{I_x}$$

$$\therefore = R_C \parallel r_o$$



- 6- For the common-emitter amplifier shown, let $V_{CC} = 15 \text{ V}$, $R_1 = 27 \text{ k}\Omega$, $R_2 = 15 \text{ k}\Omega$, $R_E = 2.4 \text{ k}\Omega$, and $R_C = 3.9 \text{ k}\Omega$. The transistor has $\beta = 100$. Calculate the dc bias current I_C . If the amplifier operates between a source for which $R_{sig} = 2 \text{ k}\Omega$ and a load of $2 \text{ k}\Omega$, replace the transistor with its hybrid- π model, and find the values of R_{in} , R_{out} , A_{vo} , A_v , and the overall voltage gain G_v (v_o / v_{sig}).



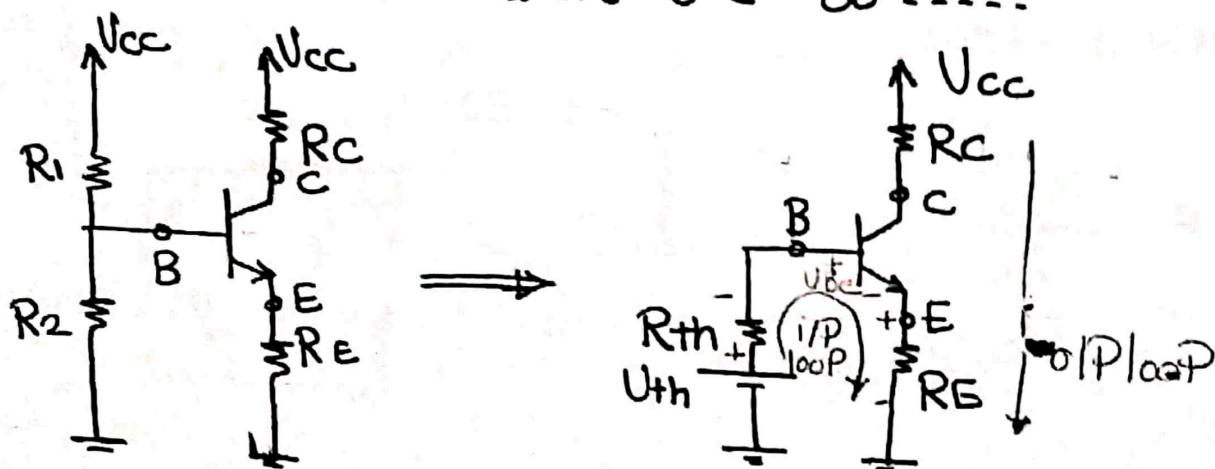
Sol 8-

$$V_{CC} = 15 \text{ V}, \beta = 100$$

$$R_1 = 27 \text{ k}\Omega, R_2 = 15 \text{ k}\Omega, R_C = 3.9 \text{ k}\Omega, R_E = 2.4 \text{ k}\Omega$$

① Calculate dc bias current I_C

From DC analysis all capacitors o.c So ----.



$$\bullet R_{th} = \frac{R_1 R_2}{R_1 + R_2} = \frac{27 \times 15}{27 + 15} = 9.64 \text{ k}\Omega$$

$$\bullet U_{th} = V_{CC} * \frac{R_2}{R_1 + R_2} = \frac{15 * 15}{15 + 27} = 5.36 \text{ V}$$

i/P loop

$$U_{th} - I_B R_{th} - U_{BE} - I_E R_E = 0$$

$$U_{th} - I_B R_{th} - U_{BE} - (1+\beta) I_B R_E = 0$$

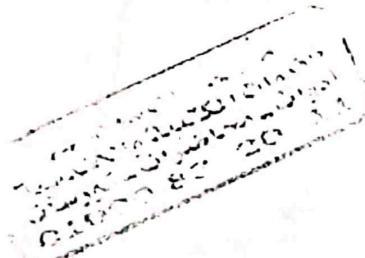
$$5.36 - (9.64 \text{ k}) I_B - 0.7 - (101)(2.4 \text{ k}\Omega) I_B = 0$$

$$I_B = 0.01848 \text{ mA}$$

$$I_E = (1+\beta) I_B = 1.867 \text{ mA}$$

$$I_C = \beta I_B = 1.848 \text{ mA} \quad \checkmark$$

From o/P loop

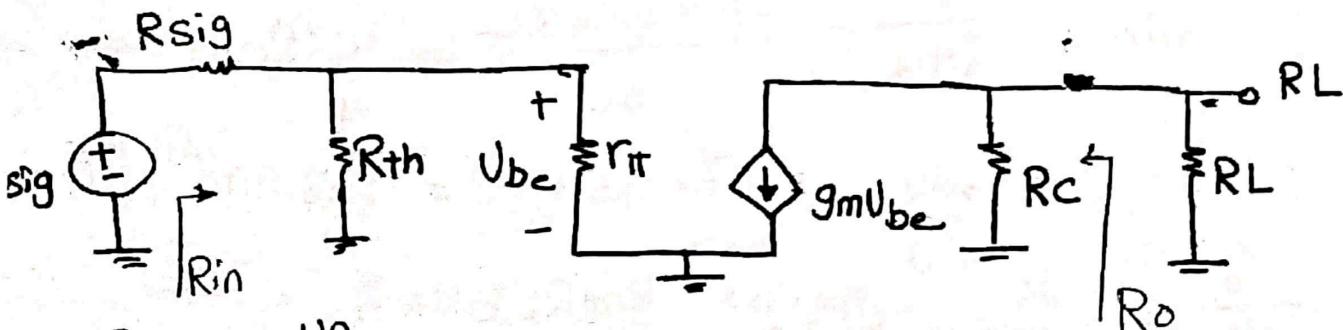


$$U_{cc} - I_C R_C - U_{CE} - I_E R_E = 0$$

$$15 - (1.84)(3.9) - U_{CE} - (1.867)(2.4) = 0$$

$$U_{CE} = 3.3432 > U_{BE} \text{ active}$$

② If $R_{sig} = 2 \text{ k}\Omega$, $R_L = 2 \text{ k}\Omega$ replace Tr by π hybrid model
then find R_{in} , R_{out} , A_{vo} , A_v and G_v (V_o/V_{sig})
all G.P SC, DC J.S S.C, DC CS o.c $\xrightarrow{\text{overall voltage gain}}$



$$\textcircled{1} \quad r_o = \frac{U_A}{I_C} \quad U_A \text{ not given} \\ \text{so neglect } r_o$$

$$\textcircled{2} \quad g_m = \frac{I_C}{U_T} = \frac{1.848}{0.025} = 73.9 \text{ mA/V} \quad \leftarrow \text{room temp}$$

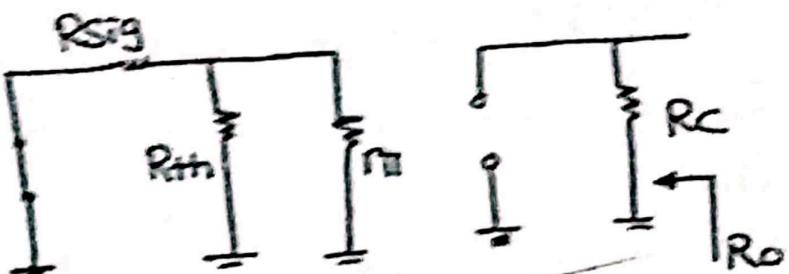
$$\textcircled{3} \quad r_{\pi} = \frac{\beta}{g_m} = \frac{U_T}{I_B} = 1.35 \text{ k}\Omega$$

→ input resistance

$$R_{in} = R_m \parallel r_\pi = \frac{9.64+1.35}{9.64+1.35} = 1.187 \text{ k}\Omega$$

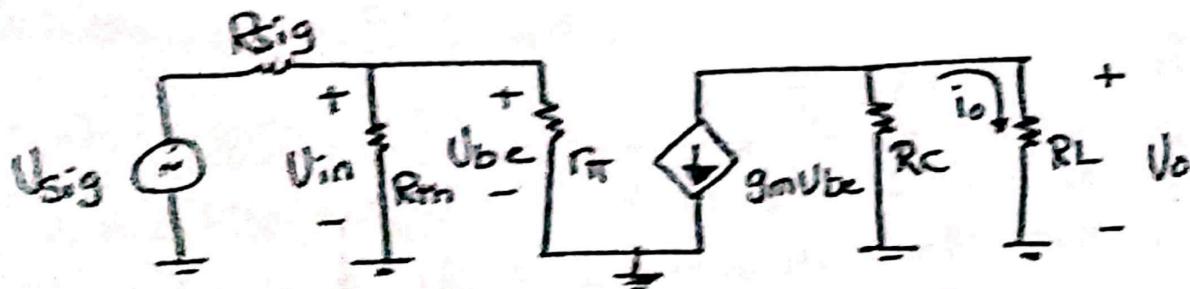
→ output resistance

$$R_{out} = R_C = 39 \text{ k}\Omega$$



$$\rightarrow A_{V0} = \frac{U_0}{U_{in}} = \frac{U_0}{U_{be}}$$

→ Called Voltage gain without \$RL\$



$$A_{V0} = \frac{U_0}{U_{in}} = \frac{U_0}{U_{be}} = \frac{g_m U_{be} \times R_C}{U_{be}} = g_m R_C$$

$$= -73.96 \times 3.9 = -288.444 \text{ V/V}$$

$$\rightarrow A_V = \frac{U_0}{U_{in}} = \frac{U_0}{U_{be}} = \frac{-g_m U_{be} (R_C \parallel R_L)}{U_{be}}$$

→ Voltage gain with \$RL\$

$$= -73.96 \times \left(\frac{2 \times 3.9}{2 + 3.9} \right) = -97.77$$

$$= \frac{U_o}{U_{sig}} = \frac{U_o}{U_{in}} * \frac{U_{in}}{U_{sig}}$$

(15)

↳ overall Voltage gain

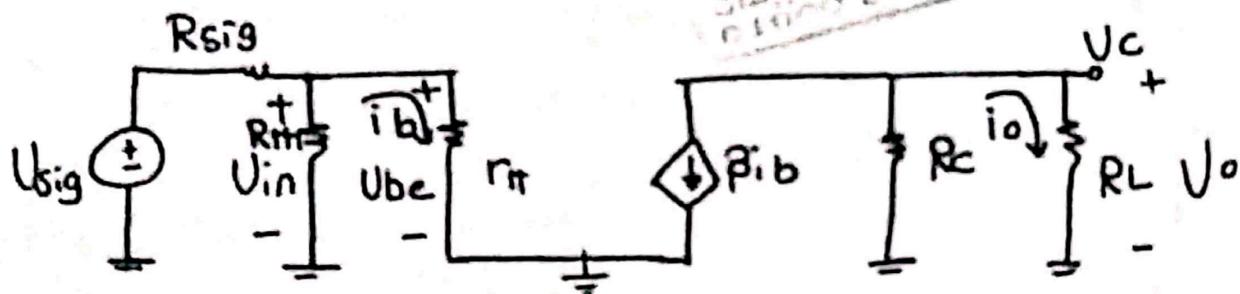
$$= \frac{U_o}{U_{sig}} * \frac{U_{be}}{U_{sig}}$$

$$U_{be} = U_{sig} * \frac{R_{in}}{R_{in} + R_{sig}}, \quad \frac{U_{be}}{U_{sig}} = \frac{R_{in}}{R_{in} + R_{sig}} = 0.374$$

$$\therefore G_V = [-g_m (R_C || R_L)] \left[\frac{R_{in}}{R_{in} + R_{sig}} \right]$$

$$= -97.77 * 0.374 = -36.414 \text{ V/V}$$

another Solution



$$\rightarrow R_{in} = R_{in} || r_{pi} = 1.187 \text{ k}\Omega$$

$$\rightarrow R_{out} = R_C = 3.9 \text{ k}\Omega$$

$$\rightarrow A_{V_o} = \frac{U_o}{U_{in}} = \frac{U_o}{i_b} * \frac{i_b}{U_{be}} * \frac{U_{be}}{U_{in}}$$

$$\frac{U_o}{i_b} = -\beta * R_C = -100 * 3.9 = -390$$

$$\frac{i_b}{U_{be}} = \frac{1}{r_{pi}} = \frac{1}{1.35} = 0.740$$

$$\frac{U_{be}}{U_{in}} = 1$$

$$A_{V_o} = -288.8 \text{ V/V}$$

$$\rightarrow A_V = \frac{U_o}{U_{in}} = \frac{U_o}{i_b} * \frac{i_b}{U_{be}} * \frac{U_{be}}{U_{in}}$$

$$\frac{U_o}{i_b} = -\beta(R_C \parallel R_L) = -100 \left(\frac{2+3.9}{2+3.9} \right) = -132.2$$

$$\frac{i_b}{U_{be}} = \frac{1}{r_\pi} = 0.740$$

$$\frac{U_{be}}{U_{in}} = 1$$

$$\therefore A_V = -97.8 \text{ V/V}$$

$$\rightarrow G_V = \frac{U_o}{U_{sig}} = \frac{U_o}{i_b} * \frac{i_b}{U_{be}} * \frac{U_{be}}{U_{in}} * \frac{U_{in}}{U_{sig}}$$

$$\frac{U_o}{i_b} = -\beta (R_C \parallel R_L) = -132.2$$

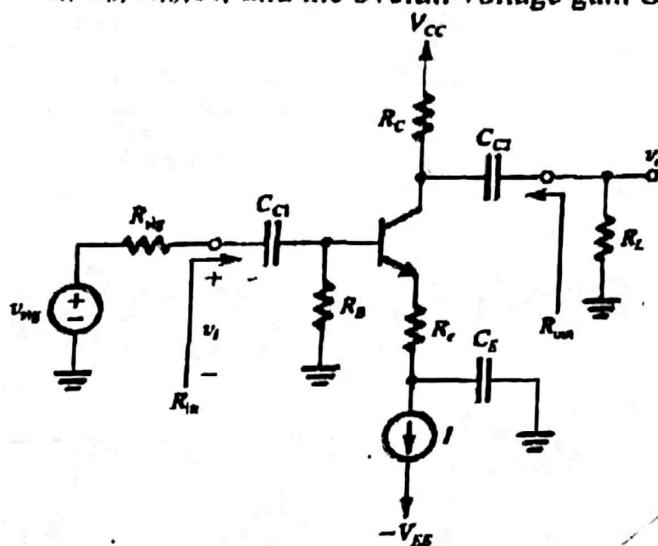
$$\frac{i_b}{U_{be}} = \frac{1}{r_\pi} = 0.74$$

$$\frac{U_{be}}{U_{in}} = 1$$

$$\frac{U_{in}}{U_{sig}} = \frac{R_{in}}{R_{in} + R_{sig}} = 0.372$$

$$G_V = -36.392 \text{ V/V}$$

- 7- For the common-emitter amplifier with an Emitter resistance shown. Find the equations of R_{in} , R_o , A_{vo} , A_v and the overall voltage gain G_v (v_o/v_{sig}).

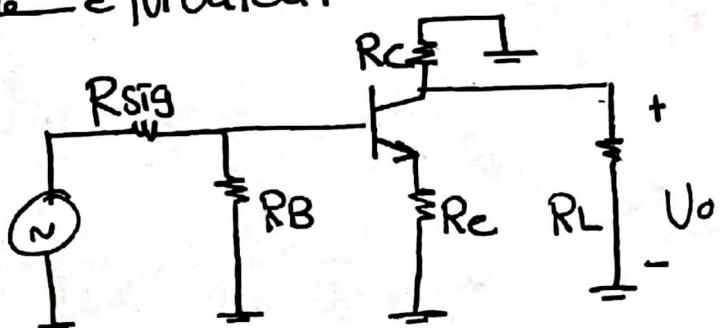


Sol:-

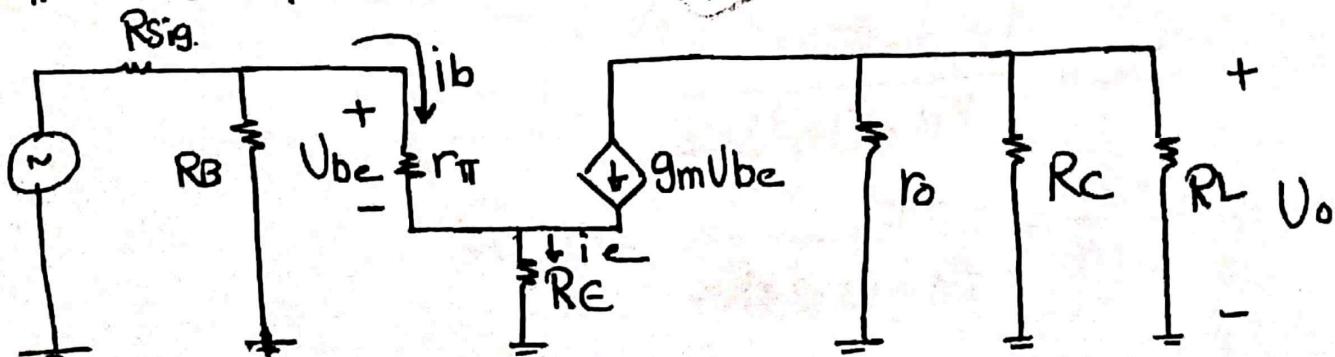
for ac analysis

- ① all Capacitors S.C
- ② Dc Voltage Source S.C
- ③ Dc Current Source O.C

the equivalent circuit



Using π model

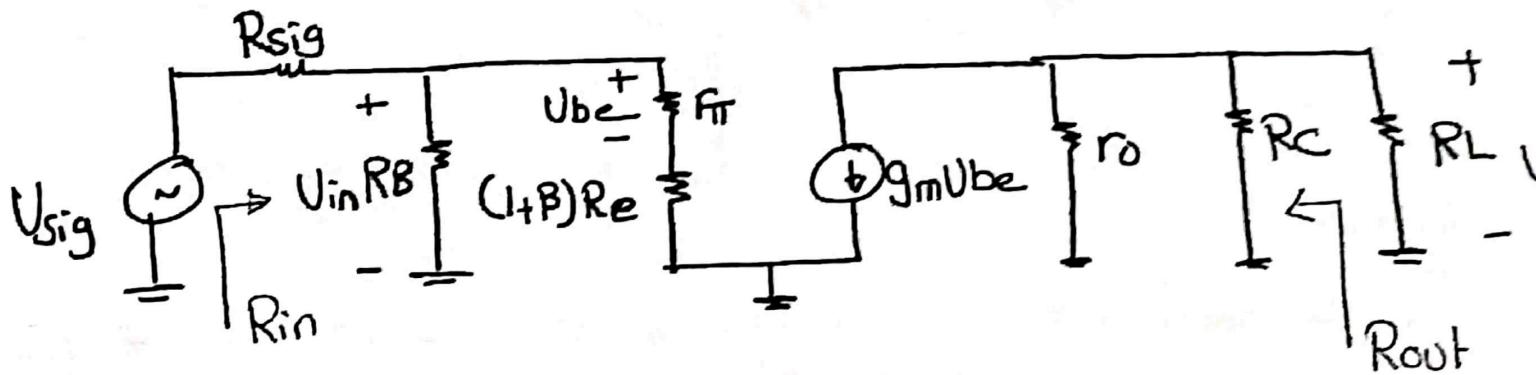


$$r_o = \frac{U_A}{I_C} , r_{\pi} = \frac{U_T}{I_B} , g_m = \frac{I_C}{U_T}$$

Note that

$$\therefore i_e = (1 + \beta) i_b$$

the equivalent circuit can be simplified



$$\rightarrow R_{in} = R_B \parallel (r_{\pi} + (1 + \beta) R_E)$$

$$\rightarrow R_{out} = r_o \parallel R_C$$

$$\rightarrow A_{V_o} = \frac{U_o}{U_{in}} = \frac{U_o}{U_{be}} \times \frac{U_{be}}{U_{in}}$$

Without RL

$$U_o = -g_m U_{be} + (r_o \parallel R_C)$$

$$\frac{U_o}{U_{be}} = -g_m (r_o \parallel R_C) \rightarrow ①$$

$$U_{be} = \frac{U_{in} * r_{\pi}}{r_{\pi} + (1 + \beta) R_E}$$

$$\frac{U_{be}}{U_{in}} = \frac{r_{\pi}}{r_{\pi} + (1 + \beta) R_E} \rightarrow ②$$

$$V_o = [-g_m (r_{\pi} || R_c)] \left[\frac{r_{\pi}}{r_{\pi} + (1+\beta)R_e} \right]$$

$$\rightarrow A_V = \frac{V_o}{V_{in}} = \frac{V_o}{U_{be}} * \frac{U_{be}}{V_{in}}$$

with RL

$$V_o = -g_m U_{be} (r_{\pi} || R_c || RL)$$

$$\frac{V_o}{U_{be}} = -g_m (r_{\pi} || R_c || RL)$$

$$\frac{U_{be}}{V_{in}} = \frac{r_{\pi}}{r_{\pi} + (1+\beta)R_e}$$

$$A_V = [-g_m (r_{\pi} || R_c || RL)] \left[\frac{r_{\pi}}{r_{\pi} + (1+\beta)R_e} \right]$$

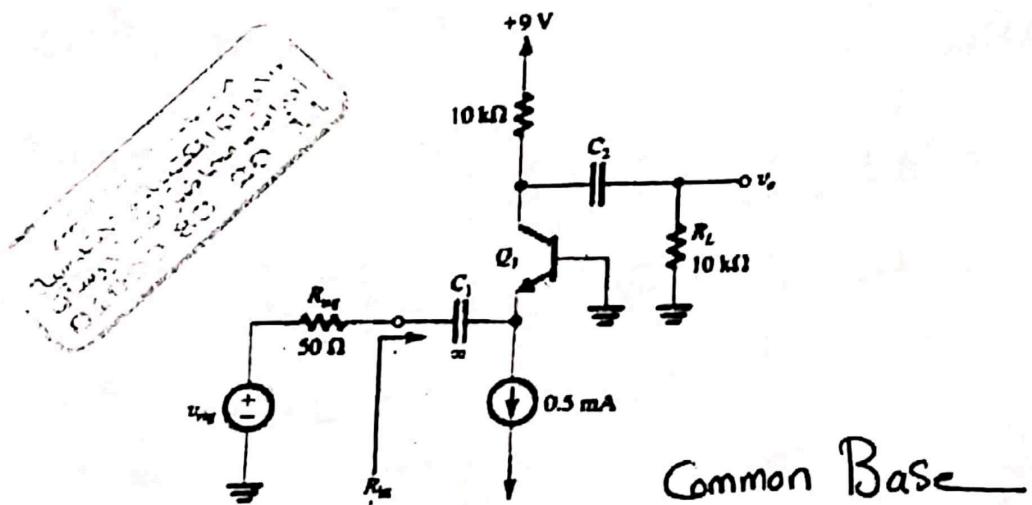
$$\rightarrow G_V = \frac{V_o}{V_{sig}} = \frac{V_o}{U_{be}} * \frac{U_{be}}{V_{in}} * \frac{V_{in}}{V_{sig}}$$

$$V_{in} = V_{sig} \frac{R_{in}}{R_{in} + R_{sig}}$$

$$\frac{V_{in}}{V_{sig}} = \frac{R_{in}}{R_{in} + R_{sig}}$$

$$G_V = [-g_m (r_{\pi} || R_c || RL)] \left[\frac{r_{\pi}}{r_{\pi} + (1+\beta)R_e} \right] \left[\frac{R_{in}}{R_{in} + R_{sig}} \right]$$

- 8- For the circuit shown, draw a complete small-signal equivalent circuit (use $\alpha = 0.99$). Your circuit should show the values of all components, including the model parameters. What is the input resistance R_{in} ? Calculate the voltage gain (v_o/v_{sig}).

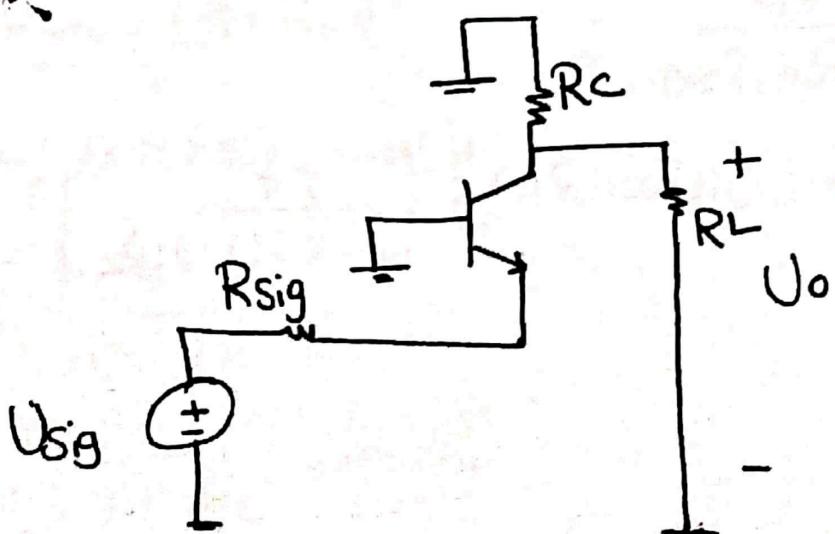


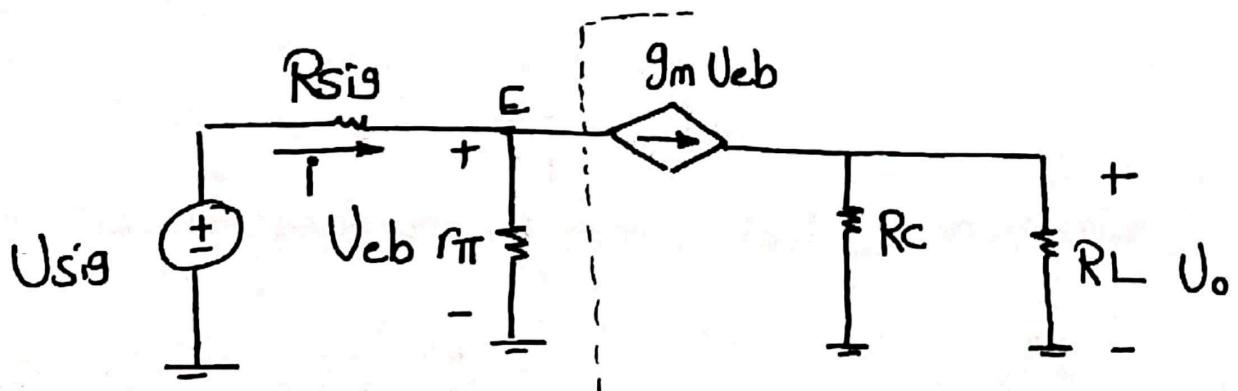
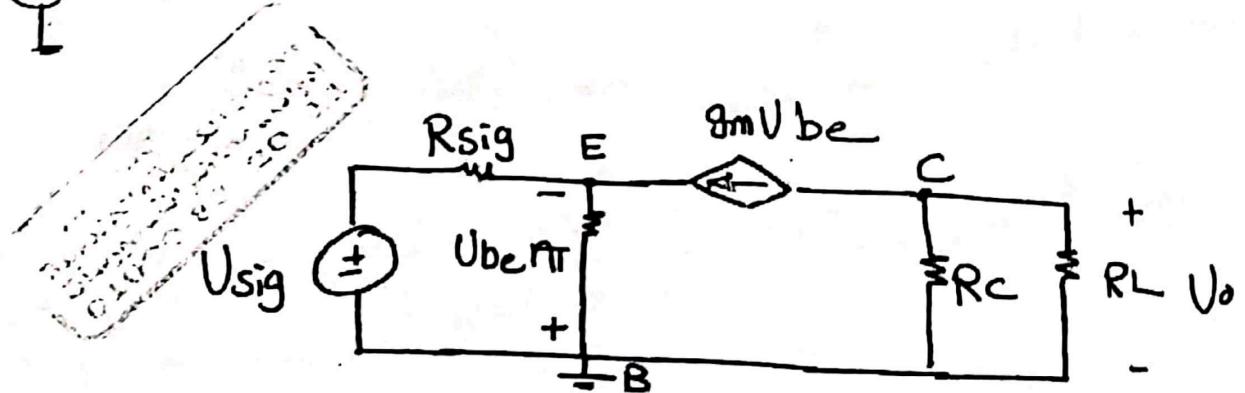
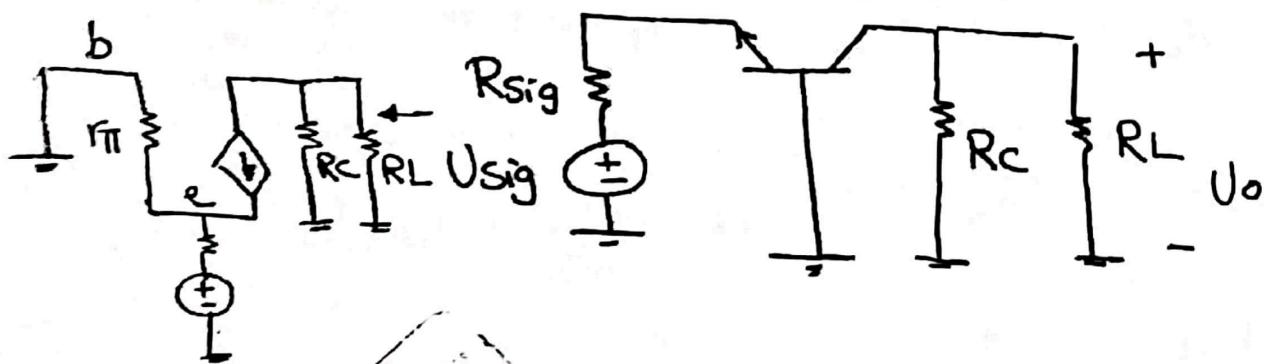
Sol₈-

in ac analysis

- ① all Capacitors S.C
- ② Dc Voltage Source S.C
- ③ Dc Current Source O.C

the equivalent circuit





$$i = \frac{U_{eb}}{r_\pi} + g_m U_{eb}$$

$$i = U_{eb} \left[\frac{1}{r_\pi} + g_m \right]$$

$$R = \frac{U_{eb}}{g_m U_{eb}} = \frac{1}{g_m}$$

$$R_{in} = r_\pi // R$$

$$\begin{aligned} R_{in} &= \frac{U_{eb}}{i} = \frac{1}{\frac{1}{r_\pi} + g_m} = \frac{1}{\frac{1}{r_\pi} + \frac{1}{g_m r_\pi}} = \frac{r_\pi}{1 + g_m r_\pi} \\ &= r_\pi // \frac{1}{g_m} \approx \frac{1}{g_m} \end{aligned}$$

L

$$G_V = \frac{V_o}{V_{sig}} = \frac{V_o}{V_{eb}} * \frac{V_{eb}}{V_{sig}}$$

$$\Rightarrow V_o = g_m V_{eb} (R_c // R_L) \rightarrow \boxed{\frac{V_o}{V_{eb}} = g_m (R_c // R_L)}$$

$$\Rightarrow i = V_{eb} \left[\frac{1}{r_\pi} + g_m \right]$$

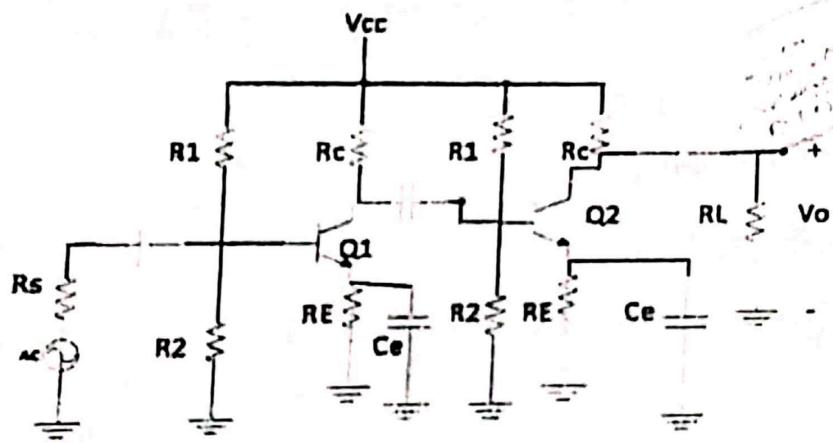
$$\Rightarrow V_{sig} = i R_{sig} + V_{eb}$$

$$\Rightarrow V_{sig} = V_{eb} \left[\frac{1}{r_\pi} + g_m \right] R_{sig} + V_{eb}$$

$$\boxed{\frac{V_{eb}}{V_{sig}} = \left(\frac{1}{r_\pi} + g_m \right) R_{sig} + 1}$$

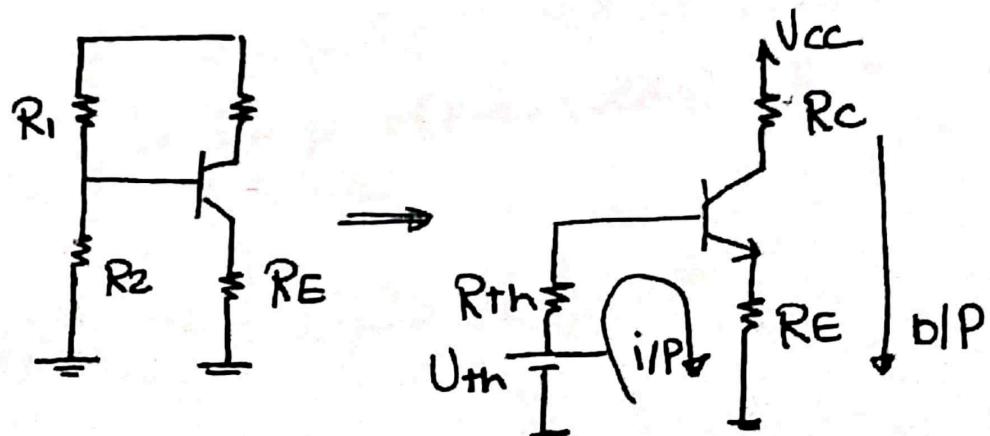
$$\Rightarrow G_V = \frac{V_o}{V_{eb}} * \frac{V_{eb}}{V_{sig}} = \left[\left(\frac{1}{r_\pi} + g_m \right) R_{sig} + 1 \right] \boxed{g_m (R_c // R_L)}$$

- 9- The amplifier consists of two identical common-emitter amplifiers connected in cascade. Observe that the input resistance of the second stage, R_{in2} , constitutes the load resistance of the first stage.
- (a) For $V_{cc} = 9\text{ V}$, $R_1 = 100\text{ k}\Omega$, $R_2 = 47\text{ k}\Omega$, $R_E = 3.9\text{ k}\Omega$, $R_C = 6.8\text{ k}\Omega$, and $\beta = 100$, determine the dc collector current and dc collector voltage of each transistor.
- (b) Draw the small-signal equivalent circuit of the entire amplifier and give the values of all its components.



Sol_o

i] Dc analysis for each one [same identical transistor]



$$U_{th} = \frac{9 \times 47}{47 + 100} = 2.87\text{ V}$$

$$R_{th} = \frac{R \times R_2}{R_1 + R_2} = 32\text{ k}\Omega$$

for i/P loop

$$U_{th} - I_B R_{th} - U_{BE} - I_E R_E = 0$$

$$U_{th} I_B R_{th} - U_{BE} - (1 + \beta) I_B R_E = 0$$

$$9 - I_B (32) - 0.7 - (101)(3.9) I_B = 0$$

$$I_B = 6.66 \text{ mA}$$

$$I_E = 0.672 \text{ mA}$$

$$I_C = 0.666 \text{ mA}$$

for o/I P Loop

$$U_{cc} - I_C R_C - U_{CE} - I_E R_E = 0$$

$$U_{CE} = 1.8 > U_{BE} \quad \text{active}$$

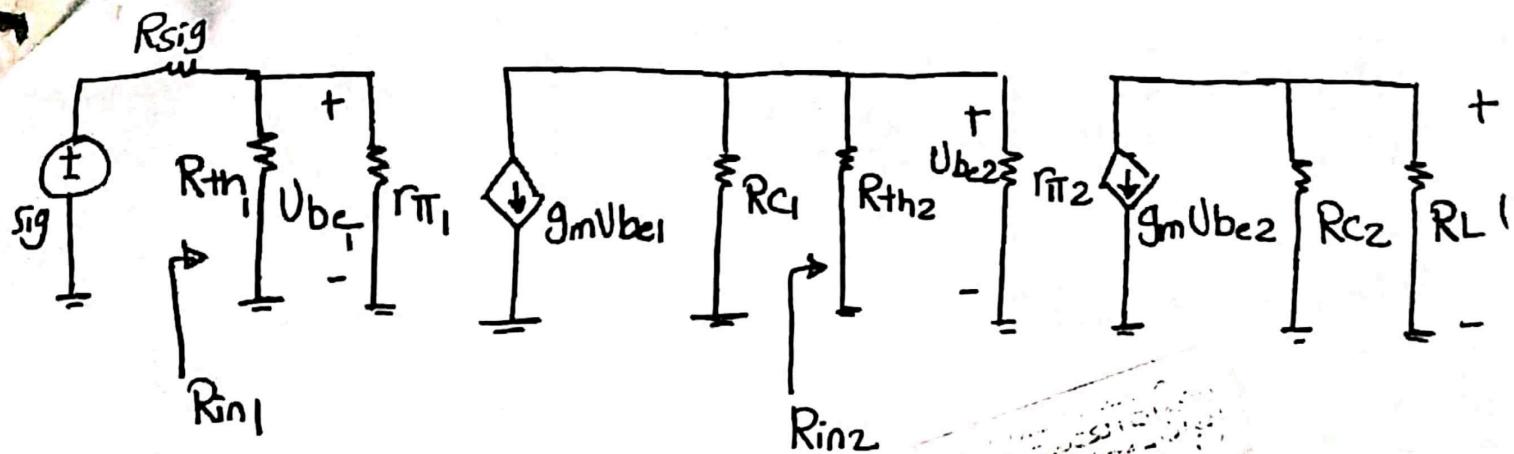
$$U_C = U_{cc} - I_C R_C$$

$$= 9 - (0.666)(6.8) = 4.47 \text{ V}$$

والآن زيد بالطبع

Small Signal analysis

25



$$R_{th1} = R_{th2} = 32 \text{ k}\Omega$$

$$g_{m1} = g_{m2} = \frac{I_C}{V_T} = \frac{0.666}{0.025} = 26.64 \text{ mA/V}$$

$$r_{\pi1} = r_{\pi2} = \frac{\beta}{g_m} = \frac{V_T}{I_B} \approx 3.75 \text{ k}\Omega$$

$$R_{C1} = R_{C2} = 6.8 \text{ k}\Omega$$

$$R_O1 = R_O2 = \infty$$

الخطوات التالية آتى



$$R_{in1} = R_{th1} \parallel r_{\pi1} = 2.4 \text{ k}\Omega$$

$$R_{in2} = R_{th2} \parallel r_{\pi2} = 2.4 \text{ k}\Omega$$

$$\frac{U_o}{U_s} = \frac{U_o}{U_{be2}} * \frac{U_{be2}}{U_{be1}} * \frac{U_{be1}}{U_s}$$

$$\therefore U_o = -g_{m2} U_{be2} (R_{C2} \parallel R_L)$$

$$\frac{U_o}{U_{be2}} = -g_{m2} (R_{C2} \parallel R_L)$$

$$\cdot U_{be2}^2 = -g_m \cdot U_{be1} \cdot (R_{C1} \parallel R_{in2})$$

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$$\frac{U_{be2}}{U_{be1}} = -g_m \cdot (R_{C1} \parallel R_{in2})$$

$$U_{be1} = U_s \cdot \frac{R_{in1}}{R_s + R_{in1}}$$

$$\frac{U_{be1}}{U_s} = \frac{R_{in1}}{R_s + R_{in1}}$$

$$\frac{U_o}{U_s} = \left[\frac{R_{in1}}{R_{in1} + R_s} \right] \left[-g_m \cdot (R_{C1} \parallel R_{in2}) \right] \left[-g_m \cdot (R_{C2} \parallel R_L) \right]$$

الحل