

Relational Algebra

Chapter 4, Part A

Relational Query Languages

- * Query languages: Allow manipulation and retrieval of data from a database.
- * Relational model supports simple, powerful QLs:
- Strong formal foundation based on logic.
- Allows for much optimization.
- Query Languages != programming languages!
- QLs not expected to be "Turing complete".
- QLs not intended to be used for complex calculations.
- QLs support easy, efficient access to large data sets.

Formal Relational Query Languages

basis for "real" languages (e.g. SQL), and for Two mathematical Query Languages form the implementation:

- Relational Algebra: More operational, very useful for representing execution plans.
- Relational Calculus: Lets users describe what they want, rather than how to compute it. (Non-operational, declarative.)
- Tunderstanding Algebra & Calculus is key to
- understanding SQL, query processing!

Preliminaries

- * A query is applied to relation instances, and the result of a query is also a relation instance.
- Schemas of input relations for a query are fixed (but query will run regardless of instance!)
- fixed! Determined by definition of query language The schema for the result of a given query is also constructs.

Positional vs. named-field notation:

- Positional notation easier for formal definitions, named-field notation more readable.
- Both used in SQL

Example Instances

R1	sid	<u>bid</u>	day
	22	101	10/10/96
	28	103	11/12/96

- "Sailors" and "Reserves" relations for our examples.
- We'll use positional or named field notation, assume that names of fields in query results are inherited' from names of fields in query input relations.

sid	sname	rating	age
22	dustin	7	45.0
31	lubber	∞	55.5
28	rusty	10	35.0

age	35.0	55.5	35.0	35.0
rating	6	∞	ν	10
sname	yuppy	lubber	guppy	rusty
$\underline{\text{sid}}$	28	31	44	58
S 2				

Relational Algebra

Basic operations:

- *Selection* (σ) Selects a subset of rows from relation.
- $\overline{Projection}$ (\mathcal{I}) Deletes unwanted columns from relation.
- <u>Cross-product</u> (X) Allows us to combine two relations.
 - Set-difference (—) Tuples in reln. 1, but not in reln. 2.
- <u>Union</u> (Y) Tuples in reln. 1 and in reln. 2.

Additional operations:

- Intersection, join, division, renaming: Not essential, but (very!) useful.
- Since each operation returns a relation, operations can be composed! (Algebra is "closed".)

Projection

- Deletes attributes that are not in projection list.
- Schema of result contains exactly the fields in the projection list, with the same names that they had in the (only) input relation.

sname, rating

- Projection operator has to eliminate duplicates! (Why??)
- Note: real systems typically don't do duplicate elimination unless the user explicitly asks for it. (Why not?)

sname	rating
yuppy	6
lubber	∞
guppy	rV
rusty	10

,e	0.0	ι.
age	32	55

$$\pi_{age}(S2)$$

Selection

- Selects rows that satisfy selection condition.
- No duplicates in result!(Why?)
- Schema of resultidentical to schema of(only) input relation.
- * Result relation can be the *input* for another relational algebra operation! (Operator composition.)

sid	sname	rating	age
28	yuppy	6	35.0
58	rusty	10	35.0

$$\sigma_{rating>8}(S2)$$

sname	rating
yuppy	6
rusty	10

 $\pi_{sname, rating}(\sigma_{rating>8}(S2))$

Union, Intersection, Set-Difference

All of these operations take two input relations, which must be <u>union-compatible</u>:

45.0

dustin

lubber

age

sname rating

sid

55.5

35.0

35.0

- Same number of fields.
- Corresponding' fields have the same type.

 $S1 \cup S2$

yuppy 9

guppy

44

rusty

58

What is the schema of result?

	· · ·
age	45.0
rating	7
sname	dustin
sid	22

sid	sname	rating	age
31	lubber	∞	55.5
58	rusty	10	35.0

$S1 \cap S2$

S1 - S2

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Cross-Product

- * Each row of S1 is paired with each row of R1.
- * Result schema has one field per field of S1 and R1, with field names 'inherited' if possible.
- Conflict: Both S1 and R1 have a field called sid.

(sid)	sname	rating	age	(sid) bid day	bid	day
22	dustin	7	45.0	22	101	10/10/96
22	dustin	_	45.0	28	103	11/12/96
31	lubber	∞	55.5	22	101	10/10/96
31	lubber	8	55.5	28	103	11/12/96
28	rusty	10	35.0	22	101	10/10/96
28	rusty	10	35.0	28	103	11/12/96

\sim Renaming operator: ρ ($C(1 \rightarrow sid1, 5 \rightarrow sid2)$, $S1 \times R1$)

Joins

* Condition Join:

$$R \times_{c} S = \sigma_{c} (R \times S)$$

(sid)	sname	rating	age	(sid)	bid	day
22	dustin		45.0	58	103	11/12/96
31	lubber	∞	55.5	58	103	11/12/96

$$S1 \times S1.sid < R1.sid$$

- * Result schema same as that of cross-product.
- Fewer tuples than cross-product, might be able to compute more efficiently
- * Sometimes called a *theta-join*.

Joins

* *Equi-Join*: A special case of condition join where the condition c contains only equalities.

sid	sname	rating	age	bid	day
22	dustin	7	45.0	101	10/10/96
58	rusty	10	35.0	103	11/12/96

$$S1 \times sid$$
 RI

- one copy of fields for which equality is specified. * Result schema similar to cross-product, but only
- * Natural Join: Equijoin on all common fields.

Division

 Not supported as a primitive operator, but useful for expressing queries like:

Find sailors who have reserved all boats.

- \diamond Let *A* have 2 fields, *x* and *y*; *B* have only field *y*:
 - $-A/B = \{\langle x \rangle | \exists \langle x, y \rangle \in A \ \forall \langle y \rangle \in B \}$
- i.e., A/B contains all x tuples (sailors) such that for every ytuple (boat) in B, there is an xy tuple in A.
- (sailor) in A contains all y values in B, the x value is in A/B. Or: If the set of y values (boats) associated with an x value
- \diamond In general, x and y can be any lists of fields; y is the list of fields in *B*, and $x \cup y$ is the list of fields of *A*.

Examples of Division A/B

pno p1 p2 p4 p4 B3 sno s1	A/B3
property by proper	A/B2
pno pno sno s1 s2 s3 s4	A/B1
sho pho sl pl sl p2 sl p2 sl p3 sl p4 sl p2 sl p4 sl p2	A

Database Management Systems, R. Ramakrishnan and J. Gehrke

Expressing A/B Using Basic Operators

- Division is not essential op; just a useful shorthand.
- (Also true of joins, but joins are so common that systems implement joins specially.)
- * *Idea*: For A/B, compute all x values that are not 'disqualified' by some y value in B.
- x value is disqualified if by attaching y value from B, we obtain an *xy* tuple that is not in *A*.

Disqualified x values:
$$\pi_{\chi}((\pi_{\chi}(A) \times B) - A)$$

/B:
$$\pi_{\chi}(A)$$
 – all disqualified tuples

Find names of sailors who've reserved boat #103

Solution 1:

 $\pi_{sname}((\sigma_{bid=103} \text{Reserves}) \times \text{Sailors})$

Solution 2:

 ρ (Templ, σ bid=103 Reserves)

 ρ (Temp2, Temp1 \times Sailors)

 π_{sname} (Temp2)

Solution 3:

Find names of sailors who've reserved a red boat

 Information about boat color only available in Boats; so need an extra join:

$$\pi_{sname}((\sigma_{color="red"}, Boats) \times Reserves \times Sailors)$$

* A more efficient solution:

$$\pi$$
 sname $(\pi_{sid}((\pi_{bid}\sigma_{color='red}, Boats) \times Res) \times Sailors)$

* A query optimizer can find this given the first solution!

Find sailors who've reserved a red or a green boat

 Can identify all red or green boats, then find sailors who've reserved one of these boats:

$$\rho$$
 (Tempboats, (σ color='red' \vee color='green', Boats))

$$\pi_{sname}(Tempboats \times Reserves \times Sailors)$$

- Can also define Tempboats using union! (How?)
- ❖ What happens if ∨ is replaced by ∧ in this query?

Find sailors who've reserved a red <u>and</u> a green boat

Previous approach won't work! Must identify intersection (note that sid is a key for Sailors): who've reserved green boats, then find the sailors who've reserved red boats, sailors

 ρ (Tempred, $\pi_{sid}((\sigma_{color='red}, Boats) \times Reserves))$

 ρ (Tempgreen, $\pi_{sid}((\sigma_{color}=green, Boats) \times Reserves))$

 $\pi_{sname}((Tempred \cap Tempgreen) \times Sailors)$

Find the names of sailors who've reserved all boats

 Uses division; schemas of the input relations to / must be carefully chosen:

$$\rho$$
 (Tempsids, (π sid, bid Reserves) / (π bid Boats))

$$\pi$$
 sname (Tempsids \times Sailors)

* To find sailors who've reserved all 'Interlake' boats:

...
$$/\pi$$
 bid $(\sigma bname = Interlake, Boats)$

Summary

- The relational model has rigorously defined query languages that are simple and powerful.
- Relational algebra is more operational; useful as internal representation for query evaluation plans.
- Several ways of expressing a given query; a query optimizer should choose the most efficient version.