

# RELATIONAL ALGEBRA DEEP DIVE



# Relation

- Represents a kind of entity/object, with certain attributes.

`Car(make, model, year, color, transmission)`

- A **set** of tuples
  - Unordered
  - No duplicates

make	model	year	color	transmission
Toyota	Camry	2015	red	Auto
Honda	Civic	2012	blue	Manual
Ford	Focus	2015	grey	Auto

- A tuple = one entity/object
  - Specifies the attribute values

# Relation

- Values are atomic/scalar

`Car(make, model, year, color, transmission)`

- Primary key
  - Unique
  - Identifies a tuple

make	model	year	color	transmission
Toyota	Camry	2015	red	Auto
Honda	Civic	2012	blue	Manual
Ford	Focus	2015	grey	Auto

# Relation

- Values are atomic/scalar

`Car(id, make, model, year, color, transmission)`

- Primary key
  - Unique
  - Identifies a tuple

id	make	model	year	color	transmission
45	Toyota	Camry	2015	red	Auto
46	Honda	Civic	2012	blue	Manual
47	Ford	Focus	2015	grey	Auto

$\sigma$  Selection

$\rho$  Rename

$\pi$  Projection

$\cup$  Union

$\cap$  Intersection

$-$  Difference

$\times$  Product

$\bowtie$  Join





## Selection

- Output tuples that satisfy a condition
  - Combine conditions with  $\wedge$  (and),  $\vee$  (or)
- Syntax:  $\sigma_{condition(s)}(input)$

$Car(id, make, year)$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\sigma_{make='Toyota'}(Car)$

id	make	year
45	Toyota	2015
48	Toyota	2023

$\sigma_{make='Toyota' \wedge year < 2020}(Car)$

id	make	year
45	Toyota	2015



## Rename

- Output a relation with renamed attributes
- Syntax:  $\rho_{A1, A2, \dots, An}(input)$

$Car(\underline{id}, make, year)$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\rho_{id, brand, year}(Car)$

id	brand	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023



## Projection

- Output a relation that has only the specified attributes
- Can add, remove, and change attribute order
- Syntax:  $\pi_{A1, A2, \dots, An}(input)$

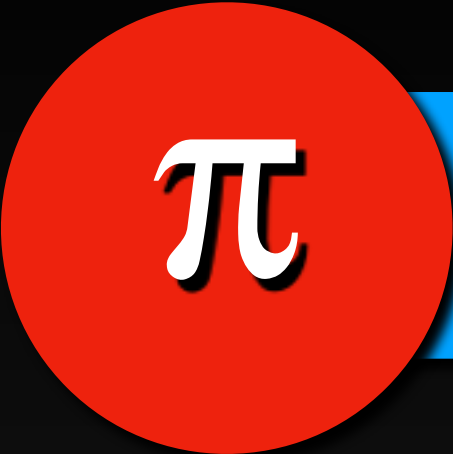
$Car(id, make, year)$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\pi_{year, make}(Car)$

year	make
2015	Toyota
2012	Honda
2015	Ford
2023	Toyota





# Projection

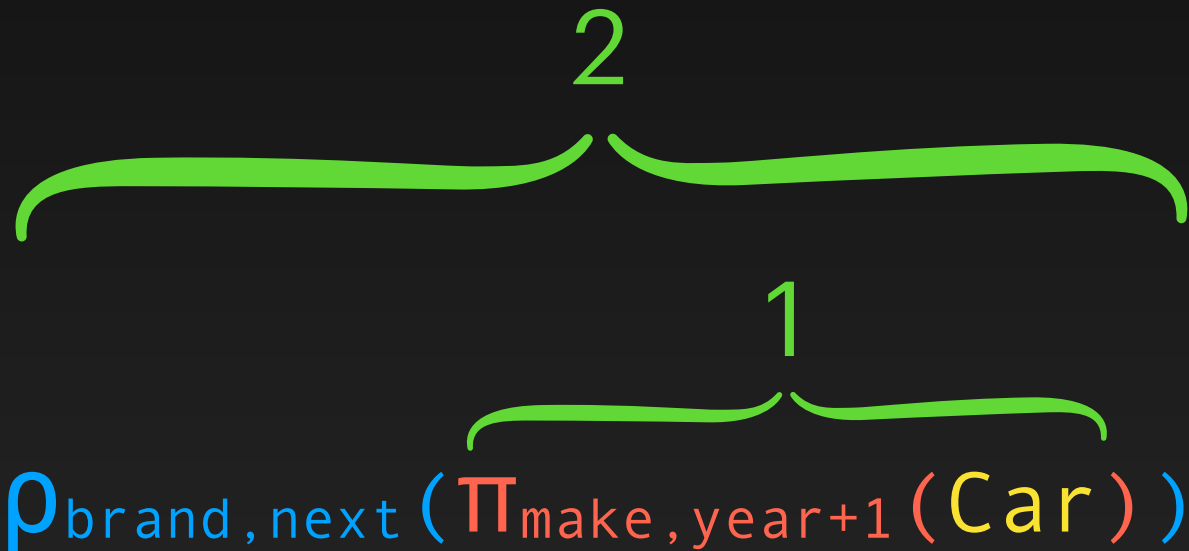
- Output a relation that has only the specified attributes
- Can add, remove, and change attribute order
- Syntax:  $\pi_{A1, A2, \dots, An}(input)$

$Car(id, make, year)$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\pi_{make, year+1}(Car)$

make	year+1
Toyota	2016
Honda	2013
Ford	2016
Toyota	2024



brand	next
Toyota	2016
Honda	2013
Ford	2016
Toyota	2024



## Projection

- Output a relation that has only the specified attributes
- Can add, remove, and change attribute order
- Syntax:  $\pi_{A_1, A_2, \dots, A_n}(\text{input})$

$\text{Car}(\text{id}, \text{make}, \text{year})$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\sigma_{\text{year}=2015}(\text{Car})$

id	make	year
45	Toyota	2015
47	Ford	2015

$\pi_{\text{make}}(\sigma_{\text{year}=2015}(\text{Car}))$

make
Toyota
Ford



## Projection

- Output a relation that has only the specified attributes
- Can add, remove, and change attribute order
- Syntax:  $\pi_{A_1, A_2, \dots, A_n}(\text{input})$

$\text{Car}(\underline{\text{id}}, \text{make}, \text{year})$

id	make	year
45	Toyota	2015
46	Honda	2012
47	Ford	2015
48	Toyota	2023

$\pi_{\text{make}}(\text{Car})$

make
Toyota
Honda
Ford

# U Union

- Output tuples that appear in one or both of the input relations
- Duplicates are removed
- Inputs must have same attributes
- Syntax: *input1* U *input2*

R(id, name)

id	name
1	Alice
2	Bob
3	Bob

S(id, name)

id	name
5	Tom
3	Jane
2	Bob

R U S

id	name
1	Alice
2	Bob
3	Bob
5	Tom
3	Jane

# U Union

- Output tuples that appear in one or both of the input relations
- Duplicates are removed
- Inputs must have same attributes
- Syntax: *input1* U *input2*

↓  
R(id, name)

id	name
1	Alice
2	Bob
3	Bob

↓  
S(id, label)

id	label
5	Tom
3	Jane
2	Bob

id, name      id, name  
↖              ↗  
R U ρ<sub>id, name</sub>(S)

id	name
1	Alice
2	Bob
3	Bob
5	Tom
3	Jane

# U Union

- Output tuples that appear in one or both of the input relations
- Duplicates are removed
- Inputs must have same attributes
- Syntax: *input1* U *input2*

R(id, name, country)

id	name	country
1	Alice	US
2	Bob	FR
3	Bob	UK

S(id, name, age)

id	name	age
5	Tom	25
3	Jane	22
2	Bob	36

name                  name  
↑                      ↑  
 $\pi_{\text{name}}(R)$  U  $\pi_{\text{name}}(S)$

name
Alice
Bob
Tom
Jane





## Intersection

- Output tuples that appear in both of the input relations
- Inputs must have same attributes
- Syntax: *input1*  $\cap$  *input2*

R(id, name)

id	name
1	Alice
2	Bob
3	Bob

S(id, name)

id	name
5	Tom
3	Jane
2	Bob

R  $\cap$  S

id	name
2	Bob

—

## Difference

- Output tuples that appear in the first but not in the second input relations
- Inputs must have same attributes
- Syntax: *input1* — *input2*

R(id, name)

id	name
1	Alice
2	Bob
3	Bob

S(id, name)

id	name
5	Tom
3	Jane
2	Bob

R — S

id	name
1	Alice
3	Bob



# Product

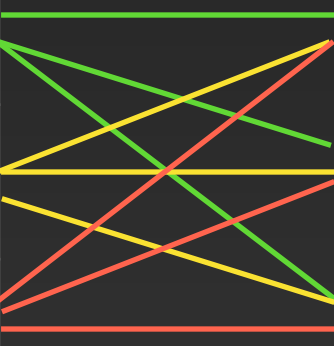
- AKA *Cartesian Product* or *Cross Product*
- Output all possible combinations of tuples from the input relations
- Syntax: *input1*  $\times$  *input2*

R(id, name)

id	name
1	Alice
2	Bob
3	Jane

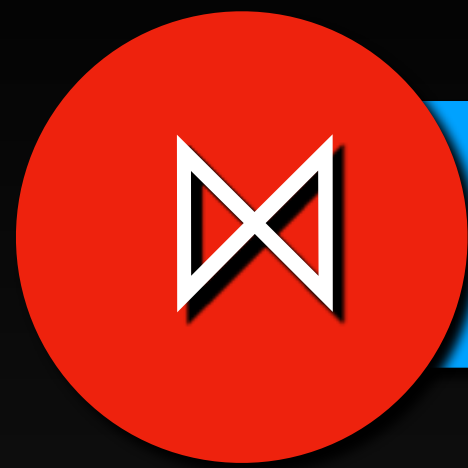
S(id, loc)

id	loc
5	UK
3	US
2	CA



R  $\times$  S

R.id	name	S.id	loc
1	Alice	5	UK
1	Alice	3	US
1	Alice	2	CA
2	Bob	5	UK
2	Bob	3	US
2	Bob	2	CA
3	Jane	5	UK
3	Jane	3	US
3	Jane	2	CA



## Join

- AKA *inner join*
- Syntax (1):  $input1 \bowtie_{attr(s)} input2$
- Output combinations of tuples from the input relations with matching attribute values
- **Join attributes** are output only once

R(id, name)

id	name
1	Alice
2	Bob
3	Jane

S(id, loc)

id	loc
5	UK
3	US
2	CA

$R \bowtie_{id} S$

id	name	loc
2	Bob	CA
3	Jane	US



## Join

- AKA *inner join*
- Syntax (2):  $\text{input1} \bowtie_{\text{condition(s)}} \text{input2}$
- More general form
- Output combinations of tuples from the input relations that satisfy the join conditions

R(id, name)

id	name
1	Alice
2	Bob
3	Jane

S(id, loc)

id	loc
5	UK
3	US
2	CA

$R \bowtie_{R.id=S.id} S$

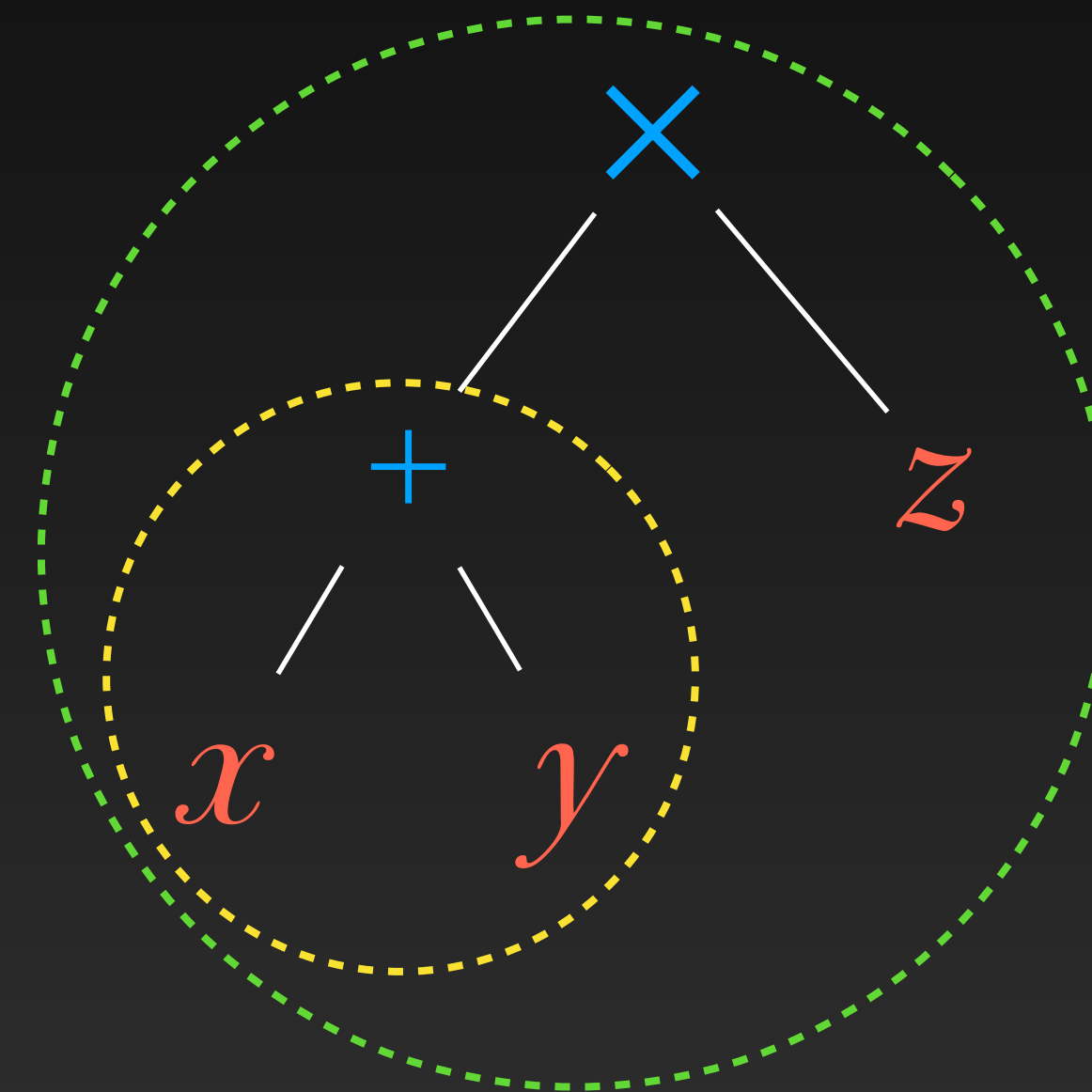
R.id	name	S.id	loc
2	Bob	2	CA
3	Jane	3	US

$\sigma_{R.id=S.id}(R \times S)$

# Tree Representation

$$\overbrace{(x + y) \times z}^2$$

1

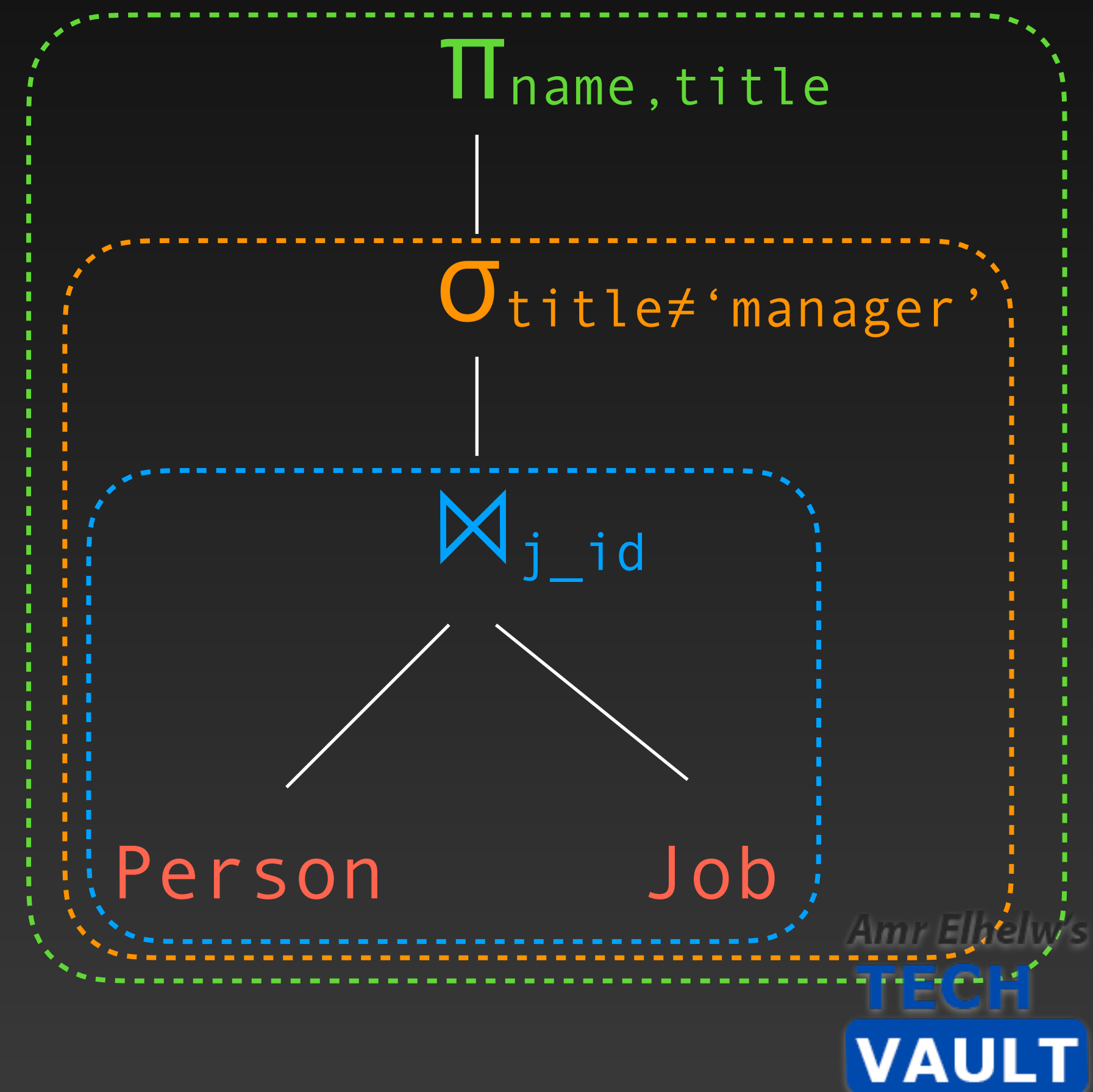




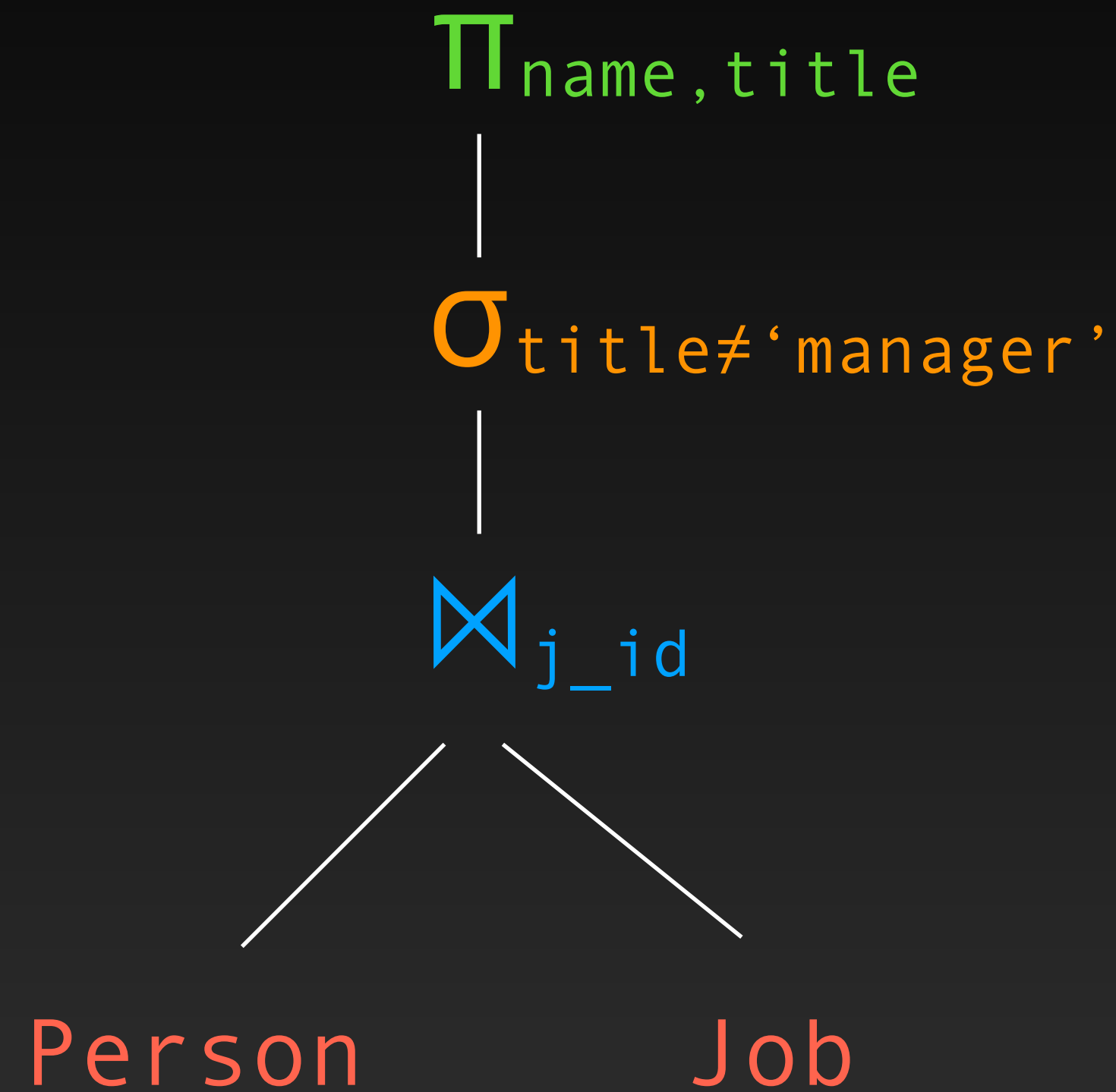
# Tree Representation

- Relations:
  - $Job(j\_id, title)$
  - $Person(p\_id, name, j\_id)$
- **Ask:** Return the name and job title for every person who is not a manager

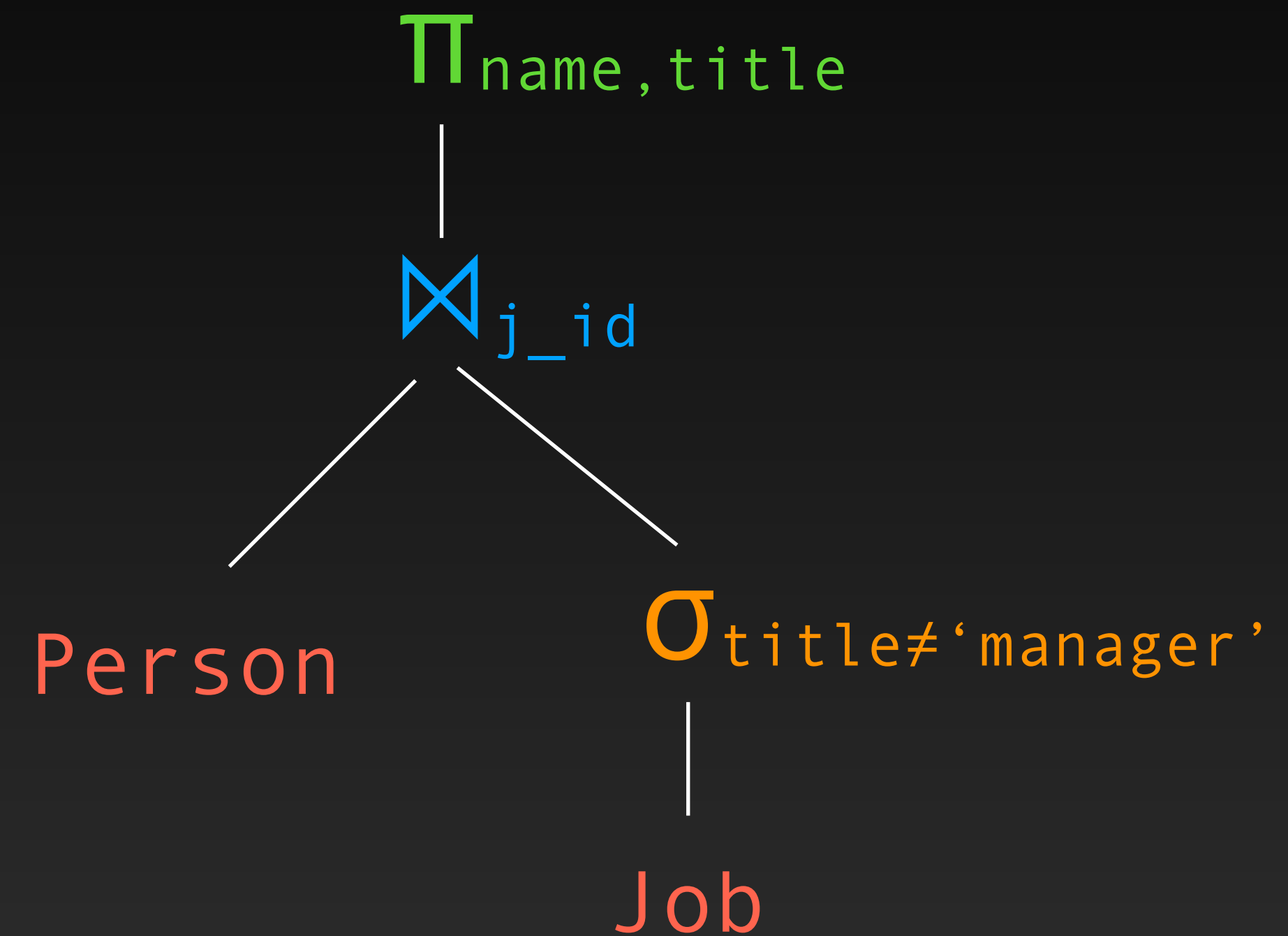
$\Pi_{name, title}(\sigma_{title \neq 'manager'}(Person \bowtie_{j\_id} Job))$



# Order of Operations



$\pi_{name, title}(\sigma_{title \neq 'manager'}(Person \Join_{j\_id} Job))$



$\pi_{name, title}(Person \Join_{j\_id} \sigma_{title \neq 'manager'}(Job))$