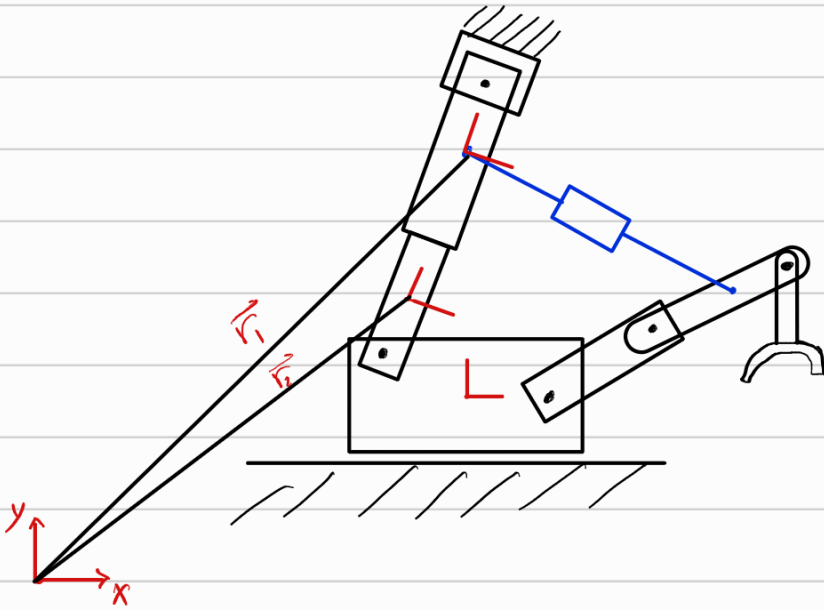
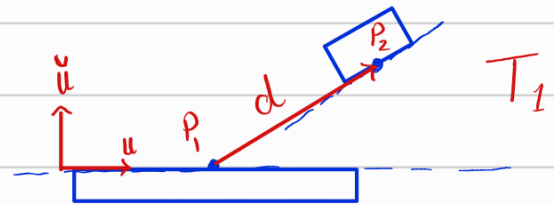


Ref. frame: 5
 vectors: 10
 constraints: 5



for the translational joint



- r_1 $R_1: S_1^{R_1}, S_2^{R_1}$
- r_2 $R_2: S_2^{R_2}, S_3^{R_2}$
- r_3 $R_3: S_3^{R_3}, S_4^{R_3}$
- r_4 $R_4: S_1^{R_4}, S_5^{R_4}$
- r_5 $R_5: S_6^{R_5}, S_6^{R_5}$
- r_6

$R_2:$

$$\underline{r}_2 + \underline{S}_2^{R_2} - \underline{r}_3 - \underline{S}_3^{R_2} = 0$$

$T_2:$

$$\underline{u}_c^T \underline{d} = 0$$

$$\phi_5 - \phi_6 - \phi_c = 0 \leftarrow \text{constant angle between bodies 5 \& 6.}$$

$$DOF = 3 \times \overset{\substack{\text{num. of links} \\ \uparrow \\ \text{to exclude} \\ \text{ground}}}{(n-1)} - 2 \times \overset{\substack{\text{num. of joints} \\ \uparrow}}{L} - h$$

or number of coordinates - num. of constraints

q3) a) 14

b) $\text{Dof} = 4$

c) Drive constraints = D.O.F. = 4

q4) a) $\underline{\underline{M}}_1 = \begin{bmatrix} m_1 & 0 & 0 \\ 0 & m_1 & 0 \\ 0 & 0 & J_1 \end{bmatrix} \dots \dots \underline{\underline{M}}_6$

b) $\underline{\underline{M}} = \begin{bmatrix} \underline{\underline{M}}_1 & & \\ & \ddots & \\ & & \underline{\underline{M}}_6 \end{bmatrix}$

c) $\underline{h}_1 = \begin{bmatrix} 0 \\ -m_1 g \\ 0 \end{bmatrix}$, h_2, h_4, h_5 all the same with diff. mass.

$\underline{h}_3 = \begin{bmatrix} {}^a f_x \\ {}^a f_y - m_3 g \\ 0 \end{bmatrix}$, $\underline{h}_6 = \begin{bmatrix} -{}^a f_x \\ -{}^a f_y - m_6 g \\ 0 \end{bmatrix}$



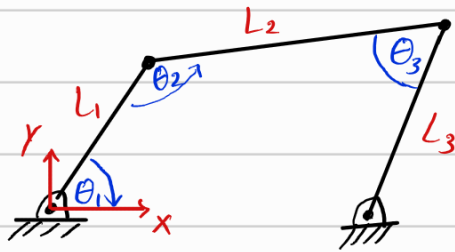
d) $\underline{h} = \begin{bmatrix} \underline{h}_1 \\ \vdots \\ \underline{h}_6 \end{bmatrix}$

e) $\underline{\ddot{C}}_1 = \begin{bmatrix} \ddot{x}_1 \\ \ddot{y}_1 \\ \ddot{\theta}_1 \end{bmatrix}$, $\underline{\ddot{C}} = \begin{bmatrix} \underline{\ddot{C}}_1 \\ \vdots \\ \underline{\ddot{C}}_6 \end{bmatrix}$

f)

	1	2	3	4	5	6
R_1	XX	XX				
R_2		XX	XX			
R_3			XX	XX		
R_4	XX				XX	
R_5						XX
T_1	XX					
T_2					XX	XX

9.5:



not in the question

	1	2	3
R_1	XX		
R_2	XX	XX	
R_3		XX	XX
R_4			XX

num. of constraints

8 x 9

num. of coordinates (3 bodies * 3 conditions)

this answer is good.

b) 2 Constraints $\begin{cases} L_1 \cdot \cos \phi_1 + L_2 \cdot \cos \phi_2 + L_3 \cdot \cos \phi_3 - a \leq 0 \\ L_1 \cdot \sin \phi_1 + L_2 \cdot \sin \phi_2 + L_3 \cdot \sin \phi_3 - b \leq 0 \end{cases}$

3 coord.: ϕ_1, ϕ_2, ϕ_3

$$DoF = 3 - 2 = 1$$

There will be a question about Rotation matrix!

(inverse matrix = transpose matrix)

q6) A) \rightarrow Yes, it's a rotation matrix.

columns & rows are perpendicular to each other.

B) is a rotation matrix as well.

because if you multiply 2 rotation matrices, you will get a rotation matrix

q7) a) $2\dot{x}_1 + 7\dot{x}_2 - 2x_3\dot{x}_3 = 0$

$$2\cos x_1 \dot{x}_1 + 7\cos x_2 \dot{x}_2 - \dot{x}_4 = 0$$

$$2\dot{x}_1 x_2 + 2x_1 \dot{x}_2 + 7\dot{x}_2 x_3 x_4 + 7x_2 \dot{x}_3 x_4 + 7x_2 x_3 \dot{x}_4 = 0$$

b) $\underline{D} =$

$$\begin{bmatrix} \dot{x}_1 & \dot{x}_2 & \dot{x}_3 & \dot{x}_4 \\ 2 & 7 & -2x_3 & 0 \\ 2\cos x_1 & 7\cos x_2 & 0 & -1 \\ 2x_2 & 7x_3 x_4 + 2x_1 & 7x_2 x_4 & 7x_2 x_3 \end{bmatrix}$$