

# COMS 30115

## Global Illumination

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# Introduction

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- Clipping
  - Same story as rendering
  - first lines, then triangles
  - homogenous coordinates

# Clip Space<sup>1</sup>

1. Map from world space to clip space

$$[x, y, z, 1]^T \rightarrow [x, y, z, \frac{z}{f}]^T$$

2. Clip x and y plane of view frustum

$$-w \cdot x_{\max} \leq x \leq w \cdot x_{\max}$$

$$-w \cdot y_{\max} \leq y \leq w \cdot y_{\max}$$

3. Map homogenous coordinate to screen space by homogenising coordinate

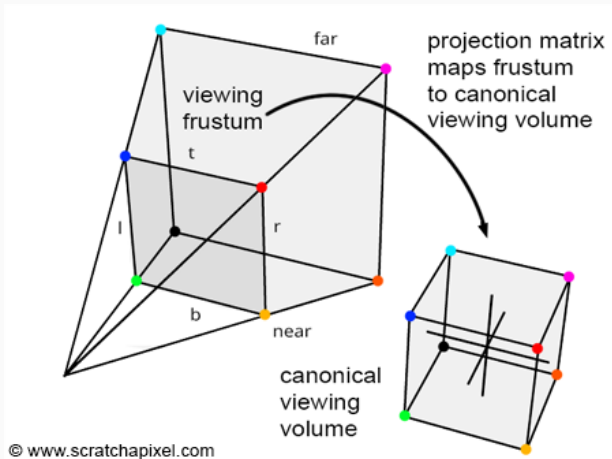
$$[x_{clipped}, y_{clipped}, z, \frac{z}{f}]^T \rightarrow [x_{clipped} \frac{f}{z}, y_{clipped} \frac{f}{z}, z \frac{f}{z}, \frac{z}{f} \frac{f}{z}]^T = [u_{clipped}, v_{clipped}, f, 1]^T$$

A little bit strange to get ones head around but its easier than one thinks

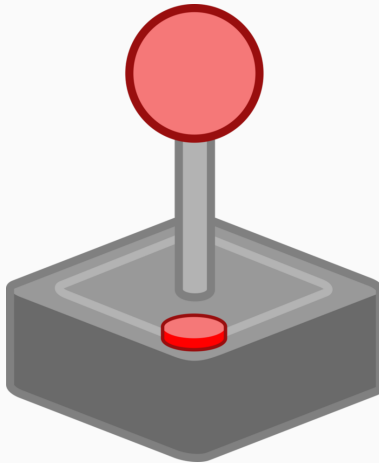
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<sup>1</sup><http://www.lighthouse3d.com/tutorials/view-frustum-culling/clip-space-approach-extracting-the-planes/>

# Clip Space



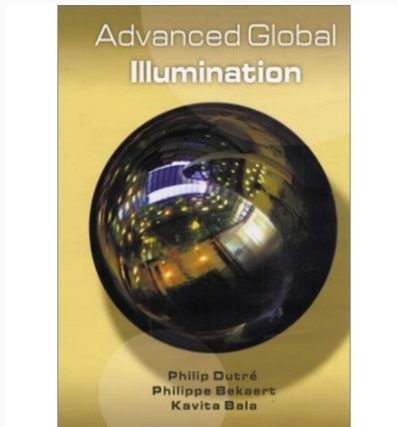
# Homework



- Introduce Global Illumination
- Introduce the terms
- Some mathematical tools we need

# The Book

- Scratchapixel on Global Illumination
- Equation compendium that later turned into “the book”
- Monte-Carlo Methods in Global Illumination free textbook





# Global Illumination

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- Quantification of Light
  - what are the quantities that are involved in Global Illumination

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- Quantification of Light
  - what are the quantities that are involved in Global Illumination
- We want to have a simple way of summing incoming light to a specific location
  - hemisphere
- We want to be able to describe outgoing light as a function of incoming light
  - BRDF
- Formulate appearance as light transport
  - How to solve for equilibrium state

# Quantification of Light

**Radiant Power/Flux** - the total amount of energy that flows per unit time

- $\Phi$  - [Watt = Joule/sec]

**Irradiance** the **incident** radiant power on a surface per unit surface area

- $E(x)$  - [Watt/m<sup>2</sup>]

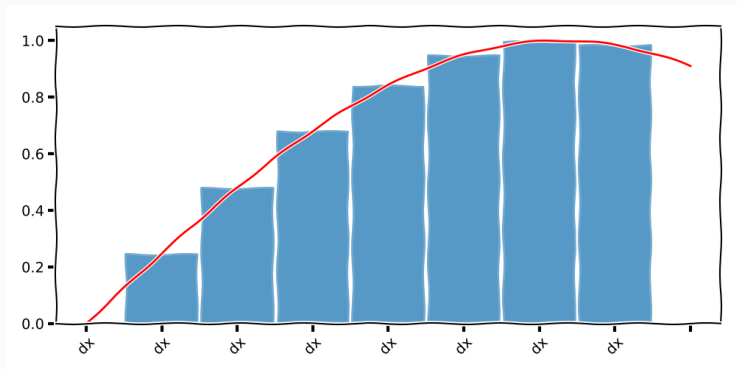
**Radiosity** the **exitant** radiant power on a surface per unit surface area

- $B(x)$  - [Watt/m<sup>2</sup>]

**Radiance** the radiant power per unit projected area per unit solid angle

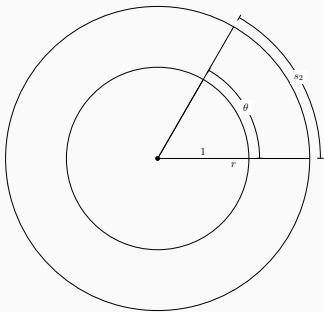
- $L(x)$  - [Watt/steradian · m<sup>2</sup>]

# Riemannian Sums



$$A = \int f(x)dx$$

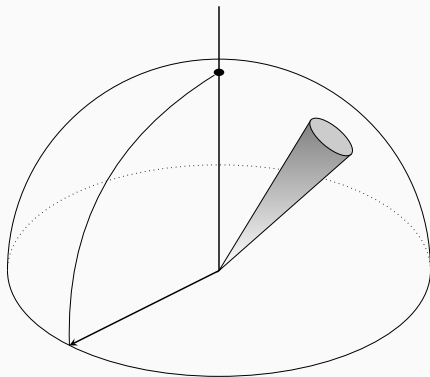
# Solid Angles



$$\frac{\theta}{2\pi \cdot 1} = \frac{s}{2\pi \cdot r} \Rightarrow \theta = \frac{s}{r}$$

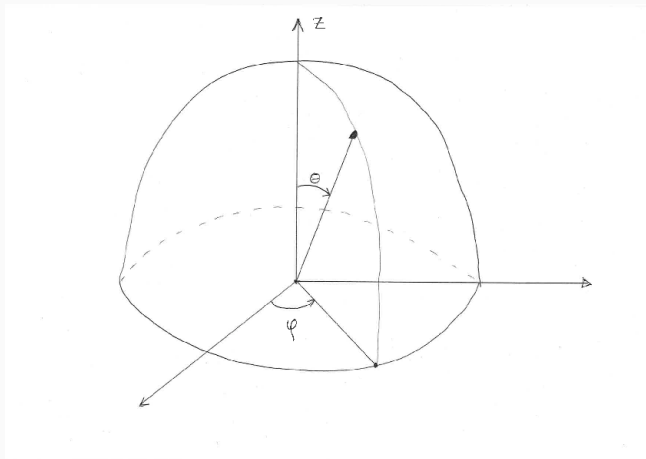


# Solid Angles

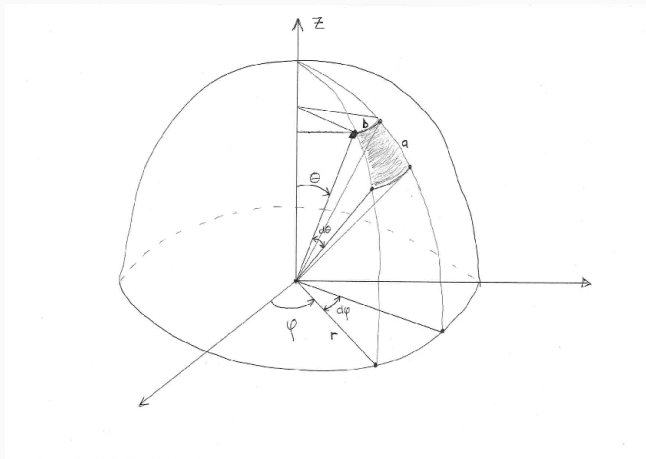


$$\frac{\omega}{4\pi \cdot 1^2} = \frac{A}{4\pi \cdot r^2} \quad \omega = \frac{A}{r^2}$$

# Solid Angles

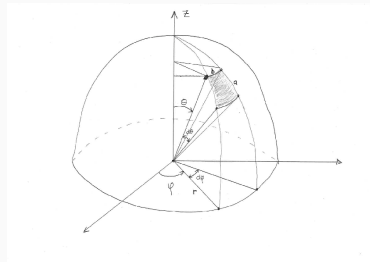


# Solid Angles



# Solid Angles

$$\begin{aligned}dA = d\omega_{\Theta} &= \lim_{d\phi \rightarrow 0, d\theta \rightarrow 0} a \cdot b \\b &= \sin(\theta) r d\phi \\a &= r d\theta \\\Rightarrow d\omega_{\Theta} &= r^2 \sin(\theta) d\phi d\theta\end{aligned}$$



We can parametrise a differential surface which can be used as an interface for computing light transport through the geometry

## Example: Surface of sphere

$$A_{sphere} = \int dA = \int d\omega$$

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$$\begin{aligned} A_{\text{sphere}} &= \int dA = \int d\omega = \int_{\theta=0}^{\pi} \int_{\phi=0}^{2\pi} \sin(\theta) d\theta d\phi \\ &= \underbrace{\int_0^{2\pi} d\phi}_{2\pi} \int_0^{\pi} \sin(\theta) d\theta \end{aligned}$$

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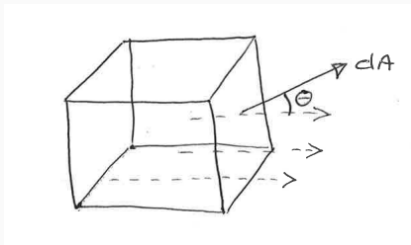


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- Remember that  $dA = r \cdot d\omega$

# Quantification of Light



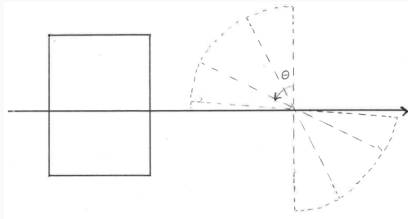
## Radiance

the radiant power per unit projected area per unit solid angle

- $L(x)$  - [Watt/steradian  $\cdot m^2$ ]

$$L = \frac{d^2\Phi}{d\omega dA^\perp} = \frac{d^2\Phi}{d\omega \cos(\theta) dA}$$

# Quantification of Light



- Number of particles/photons that passes through surface  $dA$  in time  $dt$

$$N = p(x, \omega, \lambda) \underbrace{cdtdA\cos(\theta)}_{dV} d\omega d\lambda$$

- Flux is energy per unit time.

$$\Phi = E \cdot p(x, \omega, \lambda) cdA\cos(\theta) d\omega d\lambda,$$

$$E = \frac{c}{\lambda} h$$

- This is the Planck-Einstein relation
- $h$  is Planck's constant

$$h \approx 6.626070040 \cdot 10^{-34} (\text{Joules}/s)$$

# Quantification of Light

- We can write the radiance,

$$L(x, \omega, \lambda) = \frac{d^2\Phi}{d\omega dA \cos(\theta)} = p(x, \omega, \lambda) h \frac{c}{\lambda} d\lambda$$

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- Flux, Irradiance & Radiosity

$$\Phi(x) = \int \int L(x \leftarrow \Theta) \cos(\theta) d\omega_{\Theta} dA_x$$

$$E(x) = \frac{d\Phi}{dA_x} = \int L(x \leftarrow \Theta) \cos(\theta) d\omega_{\Theta}$$

$$B(x) = \frac{d\Phi}{dA_x} = \int L(x \rightarrow \Theta) \cos(\theta) d\omega_{\Theta}$$

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- Now we have everything in radiance

$$B(x) = \int_{\Omega} L(x \rightarrow \Theta) \cos(\theta) d\omega_{\Theta}$$

- The total radiant power leaving area  $dA_x$  and arriving at area  $dA_y$  is,

$$(d^2\Phi)_{xy} = L(x \rightarrow y) \cos(\theta_x) d\omega_{xy} dA_x$$

- $d\omega_{xy}$  solid angle under which  $dA_y$  is seen from  $x$
- The total radiant power arriving at area  $dA_y$  and from area  $dA_x$  is,

$$(d^2\Phi)_{yx} = L(y \leftarrow x) \cos(\theta_y) d\omega_{yx} dA_y$$



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i.e. the medium is vacuum then,

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$$\left\{ \begin{array}{l} d\omega_{xy} = \frac{dA}{r} = \frac{\cos(\theta_y) dA_y}{r_{xy}} \\ d\omega_{yx} = \frac{dA}{r} = \frac{\cos(\theta_x) dA_x}{r_{xy}} \end{array} \right\}$$

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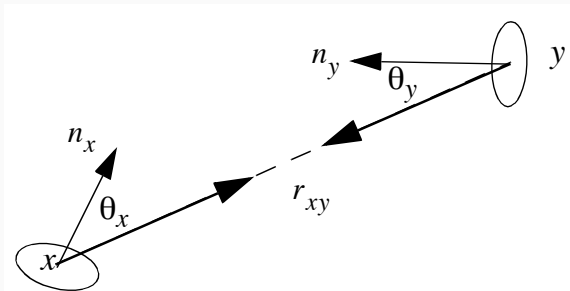
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$$L(x \rightarrow y) \cos(\theta_x) d \frac{\cos(\theta_y) dA_y}{r_{xy}} dA_x = L(y \leftarrow x) \cos(\theta_y) d \frac{\cos(\theta_x) dA_x}{r_{xy}} dA_y$$

$$\Rightarrow L(x \rightarrow y) = L(y \leftarrow x)$$

# The Physics of Light Transport



## Radiance

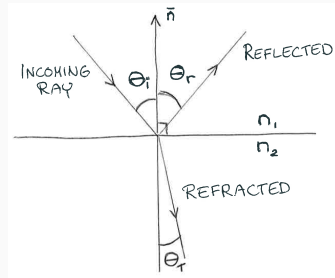
$$L(x \rightarrow y) = L(y \rightarrow x)$$

The radiance leaving point  $x$  directed towards point  $y$  is the same as the radiance arriving at point  $y$  leaving point  $x$ . Assuming that the light is travelling through vacuum.

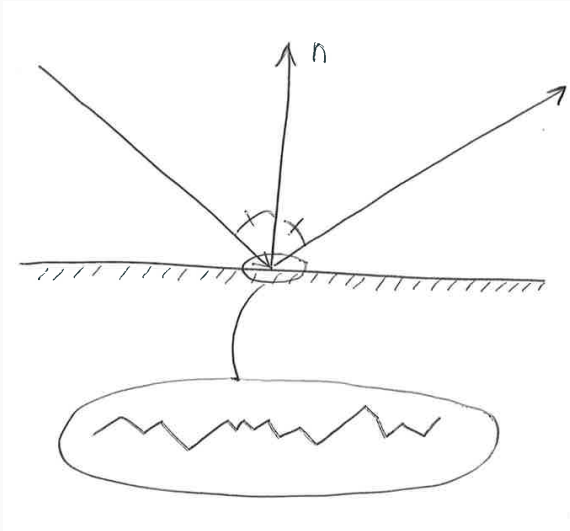
# BRDFs

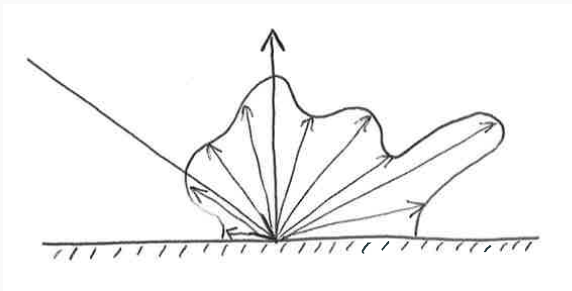
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- Light still behaves the same
- Incoming light
- Outgoing
  - Reflected
  - Refracted
- **BRDF** parametrises behaviour

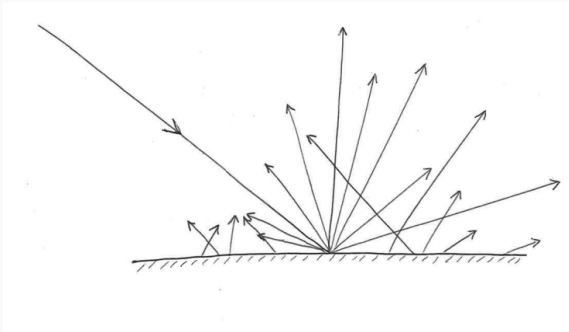








# Bidirectional Scattering Surface Reflectance Distribution Function

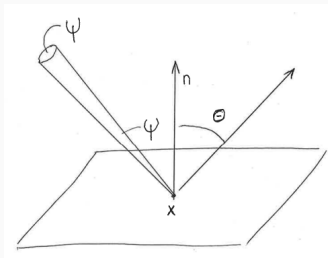


# Bidirectional Reflectance Distribution Function

## Definition

*ratio of the differential radiance reflected in an exitant direction  $\Theta$  and the differential irradiance incident through a differential solid angle  $\Psi$*

$$\begin{aligned} f_r(x, \Psi \rightarrow \Theta) &= \frac{dL(x \rightarrow \Theta)}{dE(x \leftarrow \Psi)} \\ &= \left\{ E(x) = \int L(x \leftarrow \Theta) \cos(\theta) d\omega_{\Theta} \right\} \\ &= \frac{dL(x \rightarrow \Theta)}{L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_{\Psi}} \end{aligned}$$



$$f_r(x, \psi \rightarrow \theta) = \frac{dL(x \rightarrow \theta)}{dE(x \leftarrow \psi)} = \frac{dL(x \rightarrow \theta)}{L(x \leftarrow \psi) \cos(\mathbf{n}_x, \psi) d\omega_\psi}$$

- *Defined over whole sphere to represent transparency*
- *Dimension: Four dimensional, input direction (2) and output direction (2)*
- *Reciprocity: Reversing the direction of light does not alter the BRDF*

$$f_r(x, \Psi \rightarrow \Theta) = f_r(x, \Theta \rightarrow \Psi)$$

- Incident & reflected Radiance: *the BRDF is independent of irradiance from other incident angles. This means it is linear (i.e. additive) with respect to all incident directions*
- This means we can easily compute the **total** reflected radiance,

$$f_r(x, \Psi \rightarrow \Theta) = \frac{dL(x \rightarrow \Theta)}{L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi}$$

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$$dL(x \rightarrow \Theta) = f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

- *Relating incoming to outgoing light!*



# Properties of BRDF

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$$L(x \rightarrow \Theta) = \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

- *Relating incoming to outgoing light!*

- Energy Conservation: *the amount of power reflected over all directions of a point must be the same or smaller than the total amount of energy incident to on the surface*

$$E(x) = \int_{\Omega_x} L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

$$M(x) = \int_{\Omega_x} L(x \rightarrow \Theta) \cos(\mathbf{n}_x, \Theta) d\omega_\Theta$$

- Energy is conserved if  $\frac{M(x)}{E(x)} \leq 1$

- Definition of BRDF allows us to write

$$L(x \rightarrow \Theta) = \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

# BRDF Energy Conservation

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$$L(x \rightarrow \Theta) = \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

- We can re-write the reflected power  $M(x)$

$$\int_{\Omega_x} \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) \cos(\mathbf{n}_x, \theta) d\omega_\Psi d\omega_\theta$$

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- The relationship

$$\frac{M(x)}{E(x)} = \frac{\int_{\Omega_x} \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) \cos(\mathbf{n}_x, \theta) d\omega_\Psi d\omega_\theta}{\int_{\Omega_x} L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi}$$

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- The above has to be true for **any** incident radiance function  $L(x \leftarrow \Psi)$

- Rewrite incident radiance

$$L(x \leftarrow \Psi) = L_{in}\delta(\Psi - \theta)$$

- Rewrite incident radiance

$$L(x \leftarrow \Psi) = L_{in}\delta(\Psi - \theta)$$

- Delta functions are really easy to integrate

$$\begin{aligned} & \int f(x)\delta(x)dx = f(0) \\ & \int_{\Omega_x} L(x \leftarrow \Psi)\cos(\mathbf{n}_x, \Psi)d\omega_\Psi \\ &= \int_{\Omega_x} L_{in}\delta(\Psi - \theta)\cos(\mathbf{n}_x, \Psi)d\omega_\Psi = L_{in}\cos(\mathbf{n}_x, \theta) \end{aligned}$$



$$\begin{aligned}\frac{M(x)}{E(x)} &= \frac{\int_{\Omega_x} \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) \cos(\mathbf{n}_x, \theta) d\omega_\Psi d\omega_\theta}{\int_{\Omega_x} L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi} \\&= \frac{\int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L_{in} \cos^2(\mathbf{n}_x, \theta) d\omega_\theta}{L_{in} \cos(\mathbf{n}_x, \theta)} \\&= \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) \cos(\mathbf{n}_x, \theta) d\omega_\theta \leq 1\end{aligned}$$

## Rendering Equation

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# Rendering Equation<sup>2</sup>

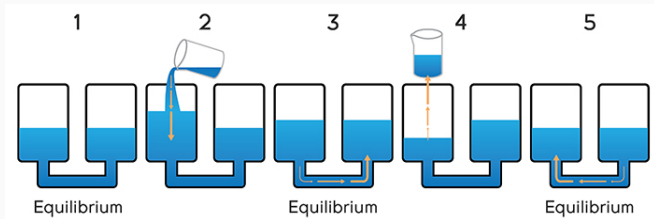
- Now we have all the building blocks
  - Solid angles allows us to define computational interfaces
  - BRDFs allows us to parametrise interactions
  - Properties of BRDFs guarantees physical correctness



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<sup>2</sup><http://blenderartists.org/forum/showthread.php?146041-Cornell-Box-with-BI>

# Rendering Equation



Light is very very fast, so we can assume that the equilibrium happens instantly (at least for world size scenes)

# Rendering Equation

Radiance going out from a point  $x$  in a direction  $\Theta$

- Emitted radiance (light source):

$$L_e(x \rightarrow \Theta)$$

- Reflected radiance

$$L_r(x \rightarrow \Theta)$$

- Total outgoing radiance:

$$L(x \rightarrow \Theta) = L_e(x \rightarrow \Theta) + L_r(x \rightarrow \Theta)$$

# Rendering Equation

- The BRDF tells us how to represent reflected radiance in terms of incoming radiance

$$L_r(x \rightarrow \Theta) = \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

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- Putting these together gives the rendering equation,

$$\begin{aligned} L(x \rightarrow \Theta) &= L_e(x \rightarrow \Theta) \\ &+ \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi \end{aligned}$$

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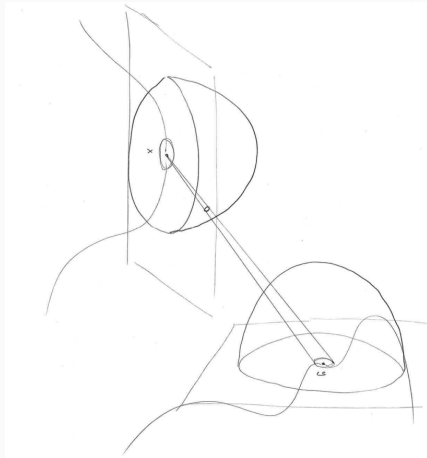
- Putting these together gives the rendering equation,

$$\begin{aligned} L(x \rightarrow \Theta) &= L_e(x \rightarrow \Theta) \\ &+ \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi \end{aligned}$$

- We want to solve for the radiance  $L(\forall x \rightarrow \forall \theta)$  for the whole scene, why is this complicated?



# Rendering Equation



$$L(x \rightarrow \Theta) = L_e(x \rightarrow \Theta) + \int_{\Omega_x} f_r(x, \Psi \rightarrow \Theta) L(x \leftarrow \Psi) \cos(\mathbf{n}_x, \Psi) d\omega_\Psi$$

## Summary

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- We want to include indirect light in our rendering
- Hemispherical coordinates provides interface to do computations on
- Derivation of Rendering equation through BRDF
- Rendering as a transport problem

## **Lecture** Global Illumination

- First rendering technique for GI

## **Lab** Finish up the 50% mark

- Think about extensions

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