

## lecture # 5

steps complement of a function  
① Take dual of the function then complement each literal

$$\textcircled{1} \quad F = \bar{x}y\bar{z} + x\bar{y}\bar{z} \rightarrow (x+\bar{y}+z)(\bar{x}+\bar{y}+z)$$

$$\textcircled{2} \quad G = (\bar{a}+bc)\bar{d}+e \rightarrow (a \cdot (\bar{b}+\bar{c})+\bar{d}) \cdot e$$

$\rightarrow F(x, y)$  then literals are  $x, \bar{x}, y, \bar{y}$

$\rightarrow \bar{A}\bar{B} + BC + CA \Rightarrow 5$  literals  $A, \bar{A}, B, \bar{B}, C$

## Boolean function

The representation of logic gate by interconnecting them is called boolean function.

① The output of one's logic gate is ~~only~~ input of other's logic gate. These logic gates ~~and~~ are called building blocks of combinational circuit.

## Combinational logic circuits C.L.C

Memoryless digital logic circuits whose output at any instant in time depends upon only on combination of its inputs.

→ No feedback

→ Immediate effect of input on output.

### Representation of C.L.C.

① Boolean Algebra

② Truth table

③ Logic Diagram.

### Expression Simplification.

$$\begin{aligned} & AB + \bar{A}CD + \bar{A}BD + \bar{A}\bar{C}\bar{D} + ABCD \\ = & AB + A\bar{B}CD + \bar{A}C(D+\bar{D}) + \bar{A}\bar{C}\bar{D} \rightarrow \text{Absorption Theorem} \\ = & AB + A\bar{B}CD + \bar{A}BD + \bar{A}\bar{C} \\ = & AB(1+CD) + \bar{A}BD + \bar{A}\bar{C} \\ = & AB[(1+C)(1+D)] + \bar{A}BD + \bar{A}\bar{C} \\ = & AB + \bar{A}BD + \bar{A}\bar{C} \\ = & B(A + \bar{A}D) + \bar{A}\bar{C} \\ = & B(\underbrace{A + \bar{A}}_1)(A+D) + \bar{A}\bar{C} \\ = & AB + BD + \bar{A}\bar{C} \quad \underline{\underline{5 \text{ Literals}}} \end{aligned}$$



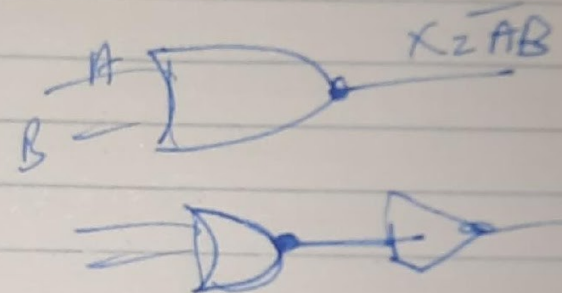
$$Z = \overline{(\bar{A} + C) \cdot (B + \bar{D})}$$

Dual

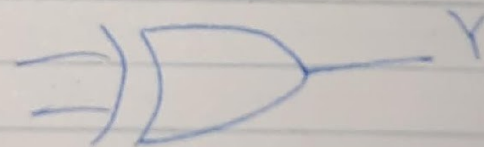
$$Z = (\bar{A} \cdot \bar{C}) + \overline{(B \cdot \bar{D})}$$

$$= A \cdot \bar{C} + \bar{B} \bar{\bar{D}} = A \cdot \bar{C} + \bar{B} D$$

NOR Gate



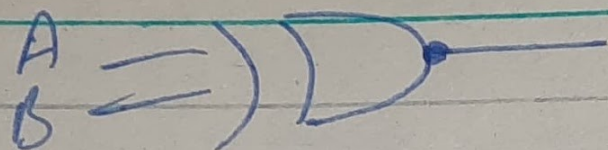
XOR



It's one if one ~~and~~ input is one.

X	Y	Y
0	0	0
1	1	0
0	1	1
1	0	1

XNOR



The inversion of XOR

Nand or Nor are universal gates