

**Theory Of Automata****(CS-3005)**

Date: Feb 29 2024

Course Instructor(s)

Mr. Fraz Yousaf

**Sessional-I Exam**

Total Time: 1 Hours

Total Marks: 25

Total Questions: 03

Semester: SP-2024

Campus: Lahore

Dept: Computer Science

Student Name

Roll No

Section

Student Signature

Vetted by

Vetter Signature

**CLO #:1 Identify formal language classes and prove language membership properties****Question1: [3+2+2marks]****PART A**

Give regular expression for the following language

 $L = \{x \mid x \in \{a,b\}^* \text{ where every } b \text{ is immediately followed by at least 3 } a\text{'s}\}$ 

Ans: \_\_\_\_\_

 $(a+baaa)^*$ **PART B**How many strings of length less than 4 contains the language described by the regular expression  $(x+y)^*y(a+ab)^*$ ?

a) 7

b) 10

☒ c) 12

d) 11

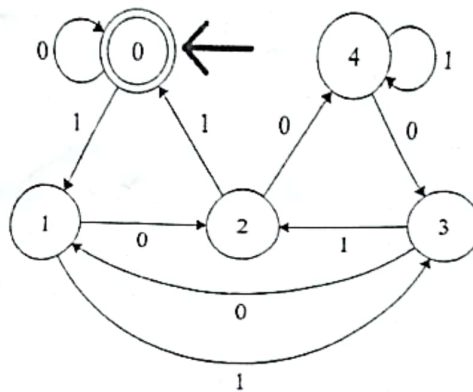
**PART C**Is it possible that for any language (denoted by  $L$ )  $L^*=L$ ? If so what is  $L$ ? (Yes/NO) \_\_\_\_\_ $L = \{\epsilon\}$

CLO #2 Differentiate and manipulate formal descriptions of languages, automata and grammars...

**Question 2:** Your task is to modify a given finite state machine that currently accepts binary strings divisible by 5 in 5 states. You need to modify the machine to accept strings whose reverse is divisible by 5 from the range 0 to 30. Once you've identified these strings, you should modify the machine so that it accepts all strings within the range from 0 to 30 where the reverse of the string is divisible by 5.

**Hint:** Specifically, In the range from 0 to 30, there is only one unique string that you need to identify within the range from 0 to 30 (both inclusive) whose reverse is not divisible by 5 but the string itself is divisible by 5.  $\Sigma = \{0,1\}^*$

**Note:** Marks will not be awarded for exceeding five states. [2+8marks]



Multiple of 5      Reverse

0000  
0101  
1010  
1111  
10100  
11001  
11110

Unique String

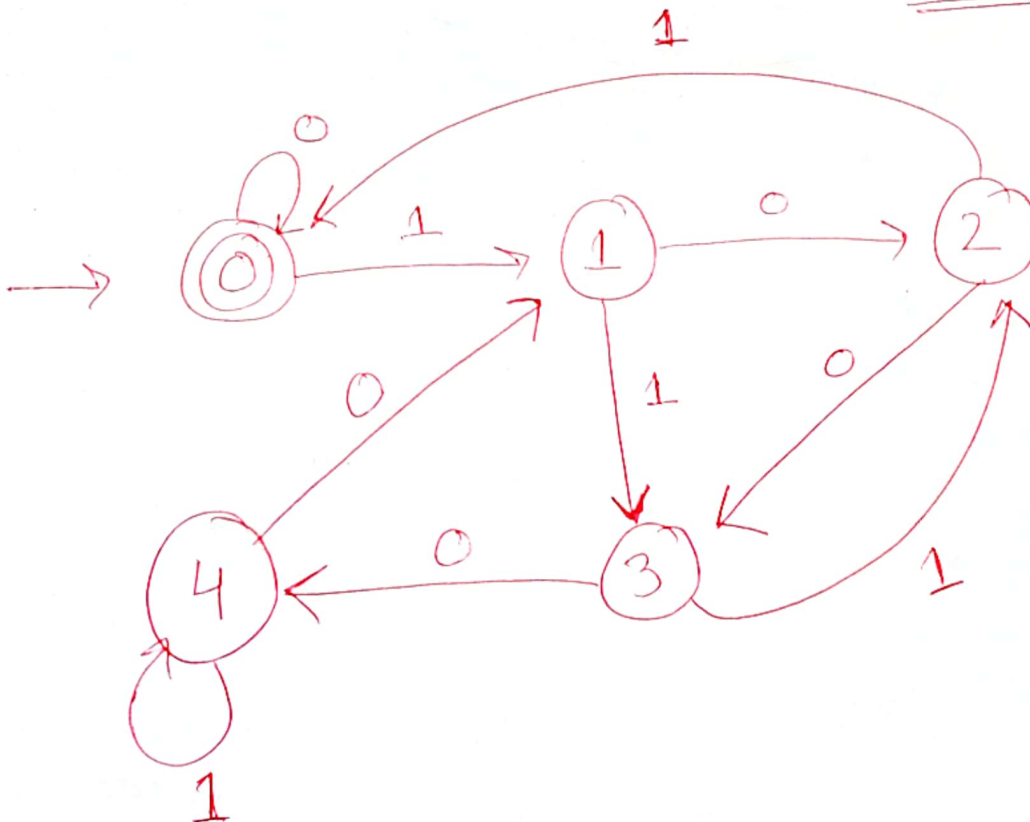
Final DFA:

0000  
1010  
0101  
1111  
00101  
10011  
01111

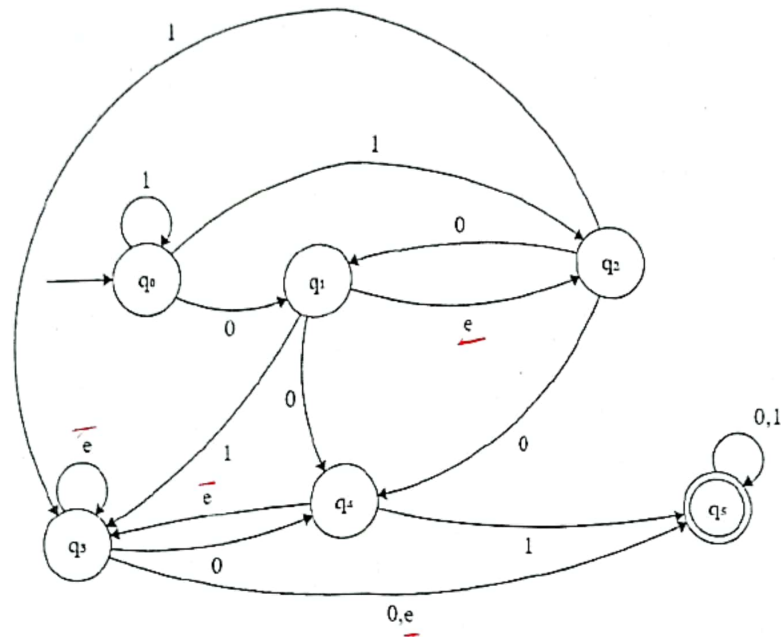
NEED  
TO  
← DESIGN  
MACHINE  
FOR  
THIS

UNIQUE =

10011



Question 3: Transform the provided NFA-epsilon language into an NFA.  $\Sigma = \{0,1\}^*$   
Show Complete Working [8 marks]



	$\epsilon$ -closure
$q_0$	$\{q_0\}$
$q_1$	$\{q_1, q_2\}$
$q_2$	$\{q_2\}$
* $q_3$	$\{q_3, q_5\}$
* $q_4$	$\{q_4, q_3, q_5\}$
* $q_5$	$\{q_5\}$

Transition table For NFA

	0	1
$\rightarrow q_0$	$q_1, q_2$	$q_0 q_2$
$q_1$	$q_1, q_2, q_3, q_4, q_5$	$q_3 q_5$
$q_2$	$q_1 q_2 q_3 q_4 q_5$	$q_3 q_5$
$\star q_3$	$q_3, q_4, q_5$	$q_5$
$\star q_4$	$q_3 q_4 q_5$	$q_5$
$\star q_5$	$q_5$	$q_5$
	$q_3 q_5$ $q_3 q_5$	$q_4 q_5$ $q_5$
	$q_4$	$q_3 q_4 q_5$ <del><math>q_4 q_5</math></del> $q_5$

$$① q_0 \rightarrow q_1 \rightarrow q_1 q_2$$

$$q_0 q_2 \rightarrow q_0 q_2$$

$$② 0 \rightarrow q_1 q_2 \quad q_4 q_1$$

$$1 \rightarrow q_1 q_2 \quad q_3 \text{ ~~q_4~~ } \rightarrow$$

Good luck!

$$③ 0 \rightarrow q_2 \quad q_1 q_4 \quad q_1 q_2 q_3 q_4 q_5$$

$$1 \rightarrow q_2 \quad q_3 \quad q_3 q_5$$

