

Number System

Lecture 2

What is Data

Data is simply

any **numbers**, **letters** or **symbols** that can be entered into a computer system.

Data values **don't have any meaning** unless we put them into **context**

Information = Data + Context

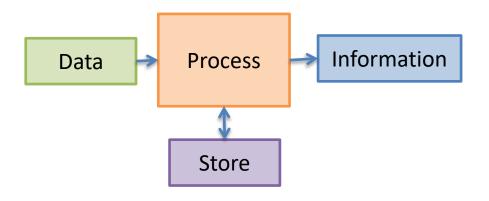
What is a System



- 1. Something feeds into the system (the input)
- 2. The system does something with the input (the **process**)
- 3. The process gives a result (the output)

What is a Computer?

 A computer is a device that stores and processes information according to a set of instructions.

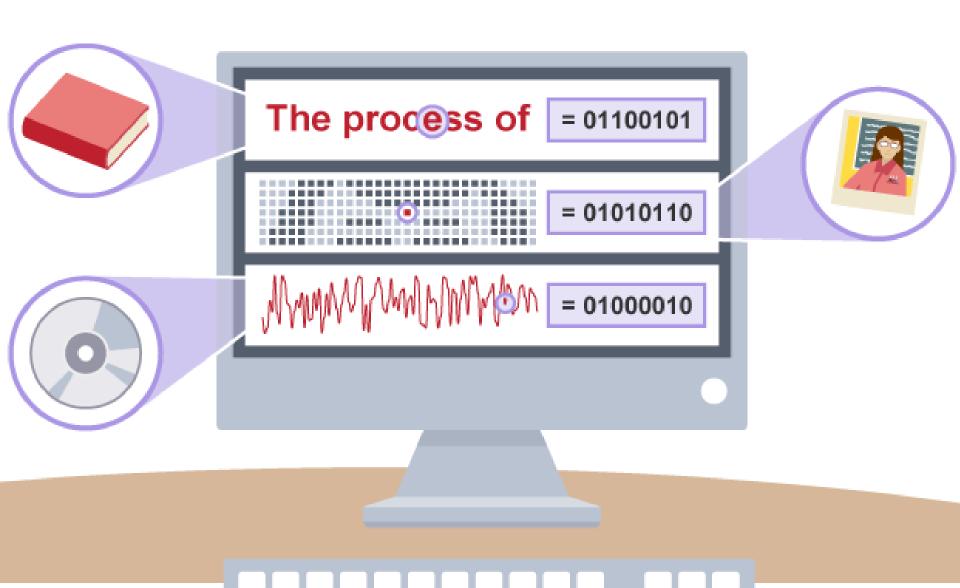




Activity

•	Data Name	Data Type	Example Data
•	Name	Text	"Bob Gripper"
•	Height	Real	1.85
•	Date of Birth	Date	19 May 1980
•	Phone No.	Alphanumeric	92-42-11128128
•	Pay Rate	Currency	£35.75
•	Tax Rate	Percentage	15%

Computers Process Data



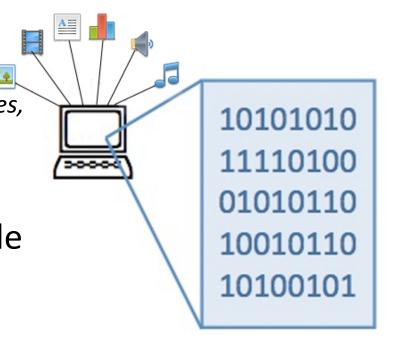
Computers Process Data

- Computers are used to process all types of information in a broad spectrum fields.
 - Numeric data consisting of Integers and real numbers are used in programs calculating payroll. We typically perform arithmetic operations on numeric data.
 - Strings of alphabets and numbers (Alphanumeric Data) are processed in customer record keeping systems.
 - Multimedia content including images, sound and text are frequently used in a large collection of application areas.
 - Signals representing various types of information like temperature, pressure, presence or absence of objects etc. are processed by computers in Robotics, IoT, monitoring and control applications.

How is Data Actually Stored in Computer

Everything that is stored and processed inside a computer (all data, information, instructions, files, images, etc.) is stored as Numbers

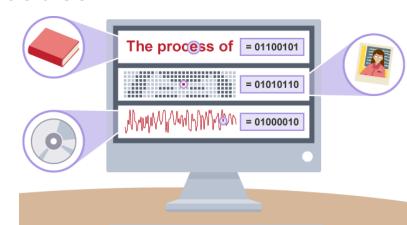
Digital computers have been made such that all data and instructions(program) for processing must be stored in computers memory before processing.



How to store text and pictures as numbers?

- The solution is to use **numeric codes**:
 - Different letters in a text document are given different numeric codes
 - Different pixels (colored dots) in an image are given different numeric codes
 - Different sounds in a music file are given different numeric codes

Everything is numbers!



What can be represented using a Bit

- Computers use binary the digits 0 and 1 to store data.
- A binary digit, or bit, is the smallest unit of data in computing.
- Single Bit can be used to represent two different quantities
 - ON means TRUE and OFF means FALSE
 - ON means number 79 and OFF means number -23
 - ON means 23.5 and OFF means 39.25
 - ON means RED COLOR and OFF means BLUE COLOR
- Most commonly ON means 1 and OFF means 0 and therefore
 Bit is also known as Binary Digit (Bit)

Memory Measuring Units

(As viewed by computer scientists)

 Bits can be grouped together to make them easier to work with. A group of 8 bits is called

a byte.

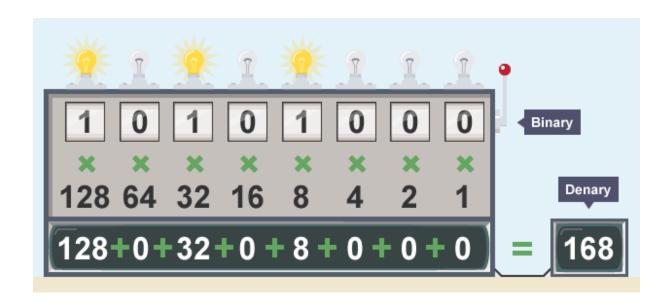
	ABBBEWATION	ATABAAE
UNIT	ABBREVIATION	STORAGE
Bit	В	Binary Digit, Single 1 or 0
Nibble	-	4 bits
Byte/Octet	В	8 bits
Kilobyte	KB	1024 bytes
Megabyte	MB	1024 KB
Gigabyte	GB	1024 MB
Terabyte	TB	1024 GB
Petabyte	PB	1024 TB
Exabyte	EB	1024 PB
Zettabyte	ZB	1024 EB
Yottab∨te	YB	1024 ZB

Storage units (www.byte-notes.com

Most computers can process millions of bits every second. A hard drive's storage capacity is measured in gigabytes or terabytes. RAM is often measured in megabytes or gigabytes.

Bytes as Numbers

 We can view each byte as a binary number. For Example the following Binary number (10101000) represents the quantity ONE Hundred and SIXTY EIGHT



Can you see the similarity between Binary and Decimal numbers?

Exercise # 1

 What Quantities are Represented by the following 8-bit binary numbers.

Bit#	7	6	5	4	3	2	1	0	Ans
	2 ⁷	2 ⁶	2 ⁵	24	2 ³	2 ²	21	2 ⁰	
Place Value	128	64	32	16	8	4	2	1	
a.	0	1	1	1	0	1	0	1	117
b.	1	0	1	1	1	0	1	1	187
c.	0	1	0	0	0	1	0	0	68
d.	1	0	1	0	0	0	0	0	160
e.	0	0	0	0	1	1	1	1	15

Exercise # 2

If a Byte is assumed to represent a number, as described earlier, then what is the range (minimum and maximum values) of numbers that can be stored in a 8-bit Byte?

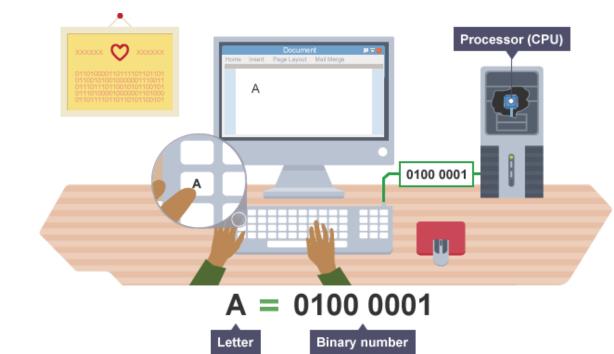
• Min: 0

Max: 128+64+32+16+8+4+2+1 = 255

How can we represent a character?

• IDEA.

- Assign numeric codes to characters and represent each character in a Byte using it's numeric code.
- Can we assign numeric codes of our choice to each character?.
 What might be a problem with this approach?



How can we represent a character?

IDEA

- Create a Standard coding scheme so that information can be easily shared between devices from different vendors.
- Standard Codes
 - ASCII (American Standard Code for Information Interchange)
 - Unicode
 - Unicode Transformation Format(UTF) UTF-8, UTF-16
 - ANSI Character Set

ASCII Character Encoding

	Letter Number Punctuation Symbol Other undefined															
	ASCII (1977/1986)															
	_0	_1	_2	_3	_4	_5	_6	_7	_8	_9	_A	_B	_c	_D	_E	_F
	NUL	SOH	STX	ETX	EOT	ENQ	ACK	BEL	BS	HT	LF	VT	FF	CR	so	SI
0_	0000	0001	0002	0003	0004	0005	0006	0007	0008	0009	000A	000B	000C	000D	000E	000F
	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
	DLE	DC1	DC2	DC3	DC4	NAK	SYN	ETB	CAN	EM	SUB	ESC	FS	GS	RS	US
1_	0010	0011	0012	0013	0014	0015	0016	0017	0018	0019	001A	001B	001C	001D	001E	001F
	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
2	SP	!	"	#	\$	용	<u>&</u>	'	()	*	+	,	_	-	/
2_	0020 32	0021 33	0022 34	0023 35	0024 36	0025 37	0026 38	0027 39	0028 40	0029 41	002A 42	002B 43	002C	002D 45	002E 46	002F
																47
3	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
	0030 48	0031 49	0032 50	0033 51	0034 52	0035 53	0036 54	0037 55	0038 56	0039 57	003A 58	003B 59	003C	003D 61	003E 62	003F 63
	@	A	В	С	D	E	F	G	Н	I	J	K	L	М	N	0
4_	0040	0041	0042	0043	0044	0045	0046	0047	0048	0049	004A	004B	004C	004D	004E	004F
	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79
	P	Q	R	S	Т	υ	V	W	Х	Y	Z	[1]	^	
5_	0050	0051	0052	0053	0054	0055	0056	0057	0058	0059	005A	005B	005C	005D	005E	005F
	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95
	×	a	b	С	d	е	f	g	h	i	j	k	1	m	n	0
6_	0060	0061	0062	0063	0064	0065	0066	0067	0068	0069	006A	006B	006C	006D	006E	006F
	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111
	p	q	r	s	t	u	v	W	x	У	Z	{	1	}	~	DEL
7_	0070	0071	0072	0073	0074	0075	0076	0077	0078	0079	007A	007B	007C	007D	007E	007F
	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127

Exercise # 4

- The following 24 values represents a message consisting of 24 characters stored in RAM.
- If the message has been written using 8-Bit Extended ASCII codes then decipher the message

87 104 97 84 32 105 83 32 89 111 117 82 32 70 105 82 83 84 32 78 65 77 69 63

WhaT iS YouR FiRST NAME?

Exercise # 5

 Use ASCII encoding to give answer to the question in the previous Exercise?



ASCII to Binary 0s and 1s

Converting the text "hope" into binary

Characters:	h	0	p	e
ASCII Values:	104	111	112	101
Binary Values:	01101000	01101111	01110000	01100101
Bits:	8	8	8	8

Representing Non-Negative(Unsigned) Integer Values

- Idea No 1.
 - Each integer is a sequence of characters and hence we can use character encoding to represent each quantity as a sequence of characters.
 - -371 = 515549 (ASCII)

Exercise # 5

 Represent the following integer quantities as sequence of bytes encoded using ASCII characters.

Integer	ASCII REPRESENTATION
20456	50 48 52 53 54
196	49 57 54
1024	49 48 50 52
32	51 50
100015	49 48 48 49 53

Representing Non-Negative(Unsigned) Integer Values

- Idea No 2.
 - Integer quantities can be represented using the idea of place value using binary number system. That is each bit has a place value and total value stored is sum of all the place values included in the number.

Representing Non-Negative(Unsigned) Integer Values

Problem

 A byte has only eight bits and hence we can not represent quantities bigger than 255 in a byte. For processing integer quantities this is an unacceptably low value.

Solution

Use 2 or more bytes to store an integer quantity

	Byte 1							Byte 0							
15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0

Exercise # 6

Use 2-Bytes to represent each of the following quantity

Integer	2 Byte Representation
20456	01001111 11101000
196	00000000 11000100
1024	00000100 00000000
32	0000000 0100000
100015	?

What is the Maximum unsigned integer value that can be represented using 2 Bytes? $(2^{16}-1) = 65535$

Exercise # 7

Use 4-Bytes to represent each of the following quantity

Integer	4 Byte Representation
20456	0000000 00000000 01001111 11101000
196	0000000 00000000 00000000 11000100
1024	0000000 00000000 00000100 00000000
32	0000000 00000000 00000000 0100000
100015	0000000 00000001 10000110 10101111

• What is the Maximum unsigned integer value that can be represented using 4 Bytes? $(2^{32}-1) = 4294967295$

Representing Signed Integer Values

Problem

— How can we represent Signed (Both negative and positive) numbers?

Solution

 FIX ONE OF THE BIT FOR REPRESENTING SIGN (Sign-Magnitude method)

```
• (01101101)_2 = +(109)_{10}

• (11101101)_2 = -(109)_{10}

• (00101011)_2 = +(43)_{10}

• (10101011)_2 = -(43)_{10}
```

Exercise

• Represent each of the following quantity in 1-bytes using sign-magnitude method.

Integer	1 Byte Representation
65536	??
-64	11000000
64	01000000
-110	10010010

• What is the Maximum signed integer value that can be represented using 1 Byte? $(2^{8-1}-1) = 127$ For 2 Bytes $(2^{16-1}-1) = 32767$

Representing Signed Integer Values

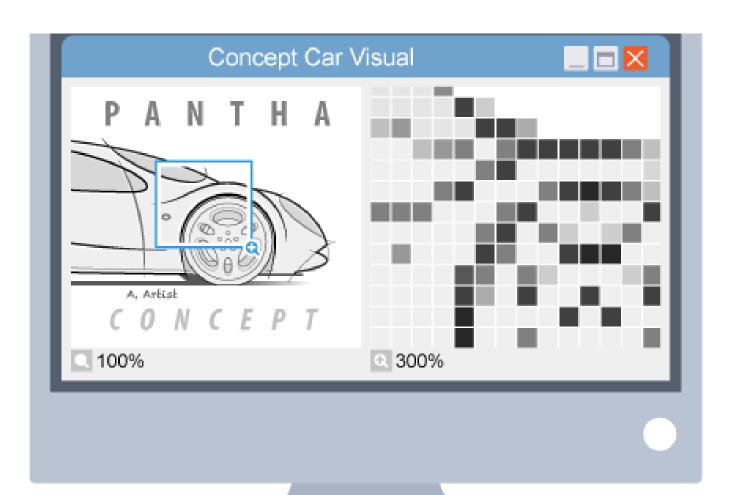
- Problem
 - How can we represent Signed (Both negative and positive) numbers?
- Use 2's Complement Representation
 - 1's complement of a binary number is another binary number obtained by toggling all bits in it, i.e., transforming the 0 bit to 1 and the 1 bit to 0
 - 1's complement of "0111" is "1000"
 - 1's complement of "1100" is "0011"
 - 2's complement of a binary number is 1 added to the 1's complement of the binary number.
 - 2's complement of "0111" is "1001"
 2's complement of "1100" is "0100"

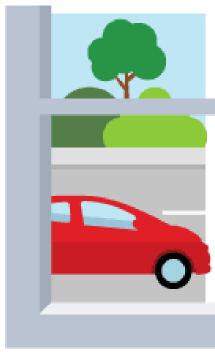
Exercise

 Represent each of the following quantity in 2's Complement method.

Integer	1 Byte Representation
12	00001100
-12	11110100
-53	11001011
30	00011110
-110	10010010

Image Representation



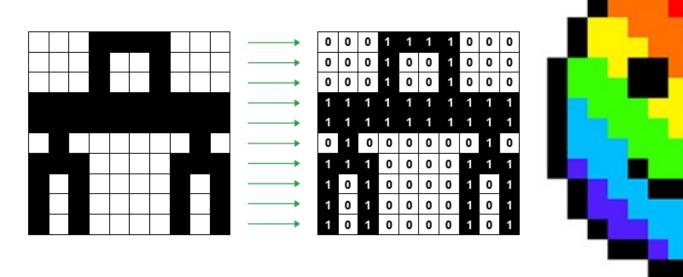


Representing Images in Binary

 Graphics on a screen are made up of tiny blocks called pixels.

Each color of an image is stored as

a binary number.

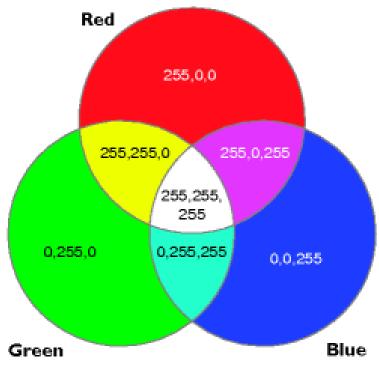


RGB

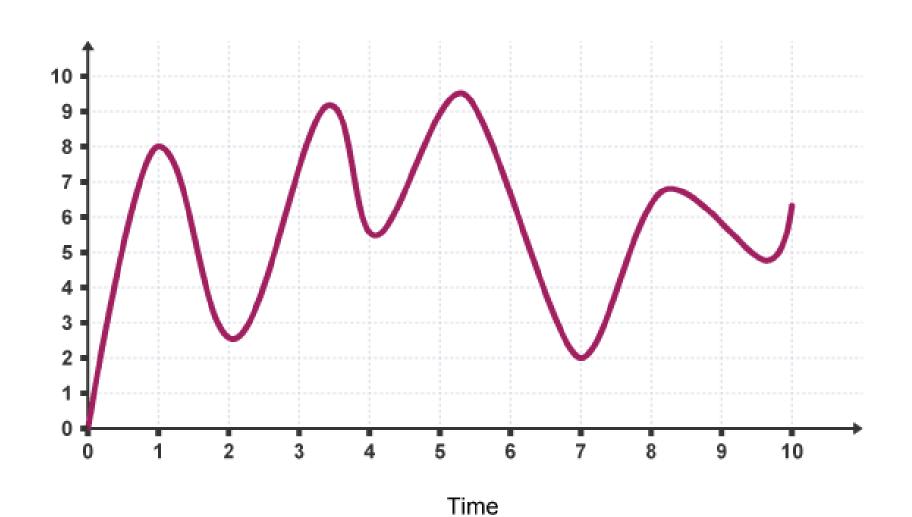
- 1 bit per pixel (0 or 1): two possible colors
- 2 bits per pixel (00 to 11): four possible colors
- 3 bits per pixel (000 to 111): eight possible colors
- 4 bits per pixel (0000 1111): 16 possible colors



16 Million Distinct Colors

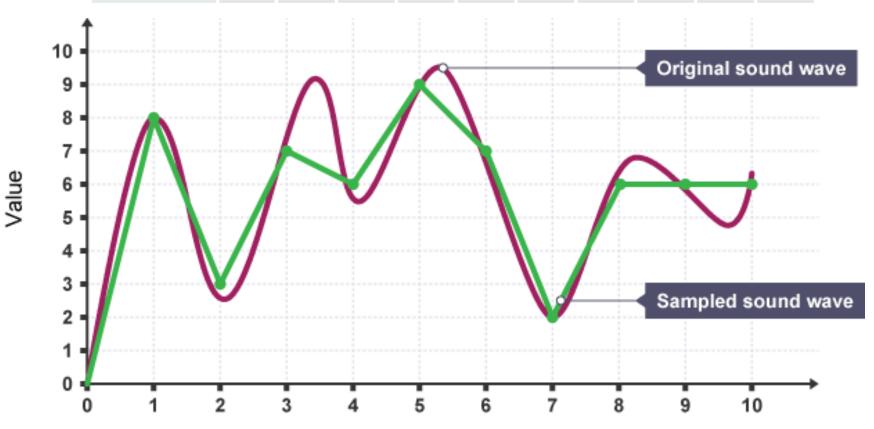


Sound Representation



Sound Representation

Time sample	1	2	3	4	5	6	7	8	9	10
Denary	8	3	7	6	9	7	2	6	6	6
Binary	1000	0011	0111	0110	1001	0111	0010	0100	0110	0110



Time

Number Systems

Decimal, Binary, Hexa-Decimal

Common Number Systems

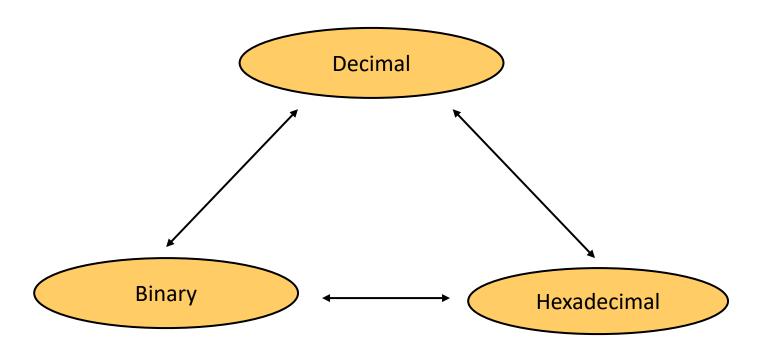
System	Base	Symbols	Used by humans?	Used in computers?
Decimal	10	0, 1, 9	Yes	No
Binary	2	0, 1	No	Yes
Hexa- decimal	16	0, 1, 9, A, B, F	No	No

Conversion Chart

Decimal	Binary	Hex
00	0000	0
01	0001	1
02	0010	2
03	0011	3
04	0100	4
05	0101	5
06	0110	6
07	0111	7
08	1000	8
09	1001	9
10	1010	Α
11	1011	В
12	1100	С
13	1101	D
14	1110	E
15	1111	F

Conversion Among Bases

• The possibilities:



Quick Example

$$25_{10} = 11001_2 = 19_{16}$$

Base

- Decimal to Binary
- Decimal to Hexadecimal

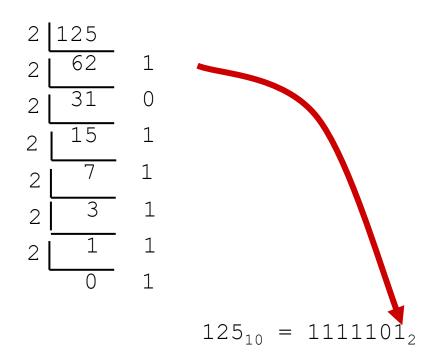
- Binary to Decimal
- Binary to Hexadecimal

- Hexadecimal to Decimal
- Hexadecimal to Binary

Decimal to Binary

- Technique
 - Divide by two, keep track of the remainder

$$125_{10} = ?_2$$



- Decimal to Binary
- Decimal to Hexadecimal

- Binary to Decimal
- Binary to Hexadecimal

- Hexadecimal to Decimal
- Hexadecimal to Binary

Decimal to Hexadecimal

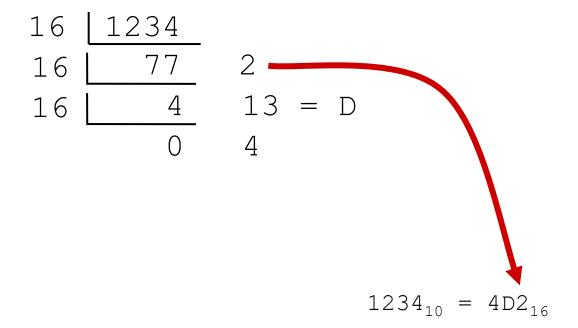
- Numbers having base 16
- Possible digits are

Decimal	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Hexa Decimal	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	E	F

- Technique
 - Divide by 16
 - Keep track of the remainder

Example: Decimal to Hexadecimal

$$1234_{10} = ?_{16}$$



- Decimal to Binary
- Decimal to Hexadecimal

- Binary to Decimal
- Binary to Hexadecimal

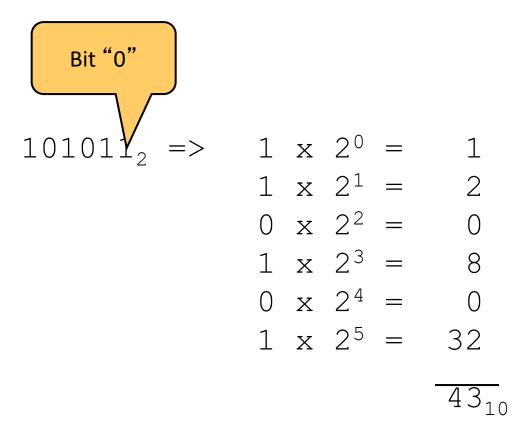
- Hexadecimal to Decimal
- Hexadecimal to Binary

Binary to Decimal

Technique

- Multiply each bit by 2^n , where n is the "weight" of the bit
- The weight is the position of the bit, starting from
 0 on the right
- Add the results

Example: Binary to Decimal



2 ⁵	2 ⁴	2 ³	2 ²	2 ¹	2 ⁰	
32	16	8	4	2	1	
1	0	1	0	1	1	32+8+2+1 = 43

- Decimal to Binary
- Decimal to Hexadecimal

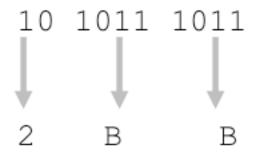
- Binary to Decimal
- Binary to Hexadecimal

- Hexadecimal to Decimal
- Hexadecimal to Binary

Binary to Hexadecimal

- Technique
 - Group bits in fours, starting on right
 - Convert to hexadecimal digits

$$1010111011_2 = ?_{16}$$



- Decimal to Binary
- Decimal to Hexadecimal

- Binary to Decimal
- Binary to Hexadecimal

- Hexadecimal to Decimal
- Hexadecimal to Binary

Hexadecimal to Decimal

- Technique
 - Multiply each bit by 16ⁿ, where n is the "weight"
 of the bit
 - The weight is the position of the bit, starting from
 0 on the right
 - Add the results

Example

$$ABC_{16} = ?_{10}$$

$$ABC_{16} \Rightarrow C \times 16^{0} = 12 \times 1 = 12$$

$$B \times 16^{1} = 11 \times 16 = 176$$

$$A \times 16^{2} = 10 \times 256 = 2560$$

$$2748_{10}$$

16 ²	16 ¹	16 ⁰	
256	16	1	
А	В	С	
256X10	16X11	12X1	2560+176+12=2748

- Decimal to Binary
- Decimal to Hexadecimal

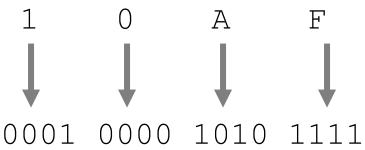
- Binary to Decimal
- Binary to Hexadecimal

- Hexadecimal to Decimal
- Hexadecimal to Binary

Hexadecimal to Binary

- Technique
 - Convert each hexadecimal digit to a 4-bit equivalent binary representation

$$10AF_{16} = ?_2$$



$$10AF_{16} = 0001000010101111_2$$

Exercise

Decimal	Binary	Hexa- decimal
33		
	1110101	
		1AF

Answer

Decimal	Binary	Hexa- decimal
33	100001	21
117	1110101	75
431	110101111	1AF

Activity

	Information in File 1	Coded Information in File 2
1	Your NUCES ID	Coded using ASCII Codes
		(one eight bit code for each ASCII character)
2	Your Full Name	Name Coded using ASCII Codes
		(Do remember to code the blank space as well)
3	Father's Name	Coded using ASCII Codes
4	Marks in F.Sc.	Coded using 16 bit unsigned code
5	Your favorite Color from the	e Coded as 24 bit RGB color space using 8-bit for each
	following list	of the R, G and B components
	i) Pure Red, ii) Pure Green iii)
	Pure Blue	

Activity

Some information has been coded in the ten bytes given above. Decode the information in each of the following cases

- Case 1: if these bytes contain characters coded using extended-ASCII or ANSI coding standard
- Case 2: if the bytes contain 5 integer values each stored using two byte unsigned integer representation.
- Case 3: if the bytes contain 5 integer values each stored using two byte signed integers represented using sign-magnitude method.

10010011 01001101 01000101 01010011 01010011 01000001 01000111 01000101 10010100 00101110

Homework

- How to represent Real Numbers?
 - Fixed point representation.
 - Floating Point Representation.

Lets Play a Game

 https://games.penjee.com/binary-numbersgame/

Recommended

 https://www.youtube.com/watch?v=1GSjbWt 0c9M

- https://www.khanacademy.org/computing/computer-science/how-computers-work2/v/khan-academy-and-codeorg-introducing-how-computers-work
- https://www.youtube.com/watch?v=ptzGI9Va ZmQ



Thank You