Artificial Neural Networks (ANN)

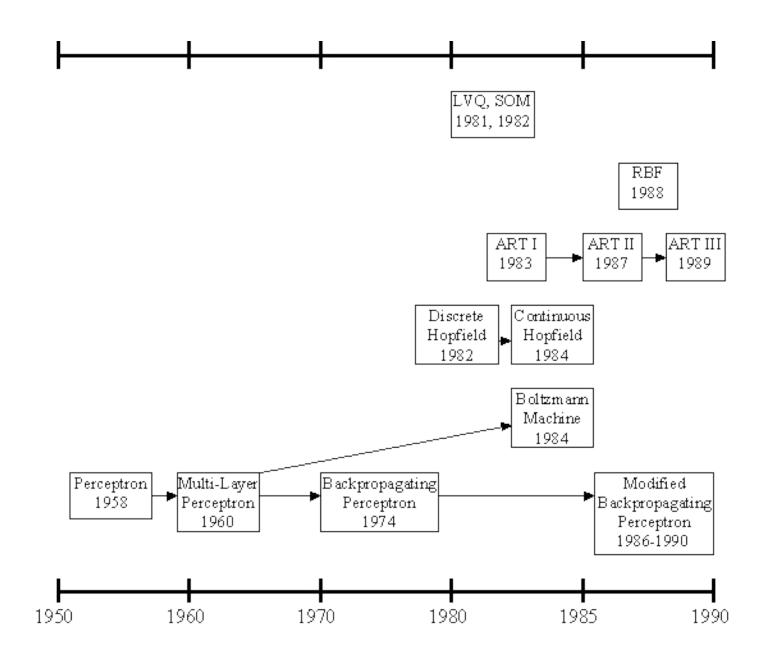
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History of the Artificial Neural Networks

- History of the ANNs stems from the 1940s, the decade of the first electronic computer.
- However, the first important step took place in 1957 when Rosenblatt introduced the first concrete neural model, the perceptron. Rosenblatt also took part in constructing the first successful neurocomputer, the Mark I Perceptron. After this, the development of ANNs has proceeded as described in *Figure*.



Artificial Neural Network

An artificial neural network consists of a pool of simple processing units which communicate by sending signals to each other over a large number of weighted connections.

Why Artificial Neural Networks?

There are two basic reasons why we are interested in building artificial neural networks (ANNs):

Technical viewpoint: Some problems such as character recognition or the prediction of future states of a system require massively parallel and adaptive processing.

Biological viewpoint: ANNs can be used to replicate and simulate components of the human (or animal) brain, thereby giving us insight into natural information processing.

How do our brains work?

The Brain is A massively parallel information processing system.

Our brains are a huge network of processing elements. A typical brain contains a network of 10 billion neurons.

How do our brains work?



Dendrites: Input

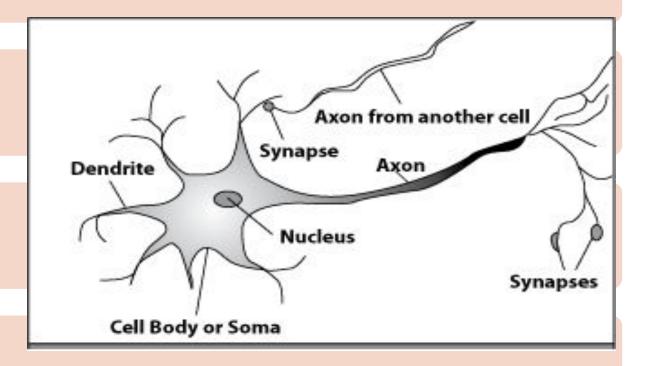
A processing element



Cell body: Processor



Synaptic: Link





Axon: Output

How do our brains work?

A neuron is connected to other neurons through about 10,000 synapses

A neuron receives input from other neurons. Inputs are combined.

Once input exceeds a critical level, the neuron discharges a spike - an electrical pulse that travels from the body, down the axon, to the next neuron(s)

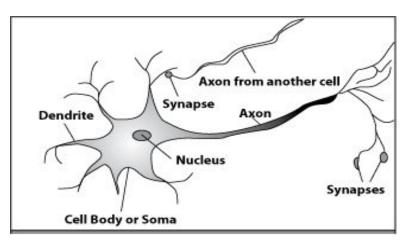
The axon endings almost touch the dendrites or cell body of the next neuron.

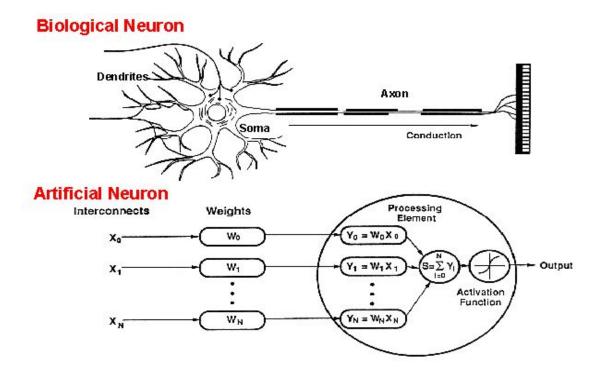
Transmission of an electrical signal from one neuron to the next is effected by neurotransmitters.

Neurotransmitters are chemicals which are released from the first neuron and which bind to the Second.

This link is called a synapse. The strength of the signal that reaches the next neuron depends on factors such as the amount of neurotransmitter available.

A processing element

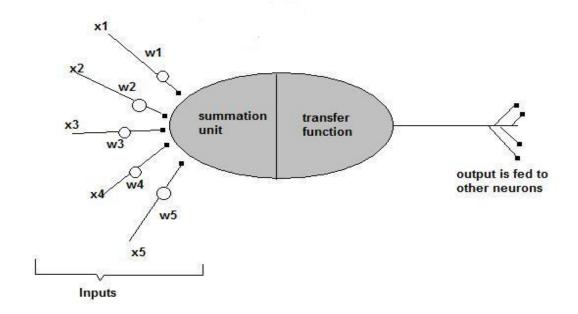


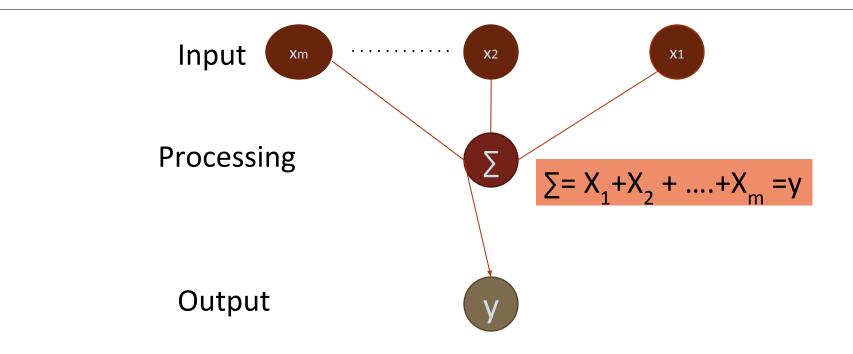


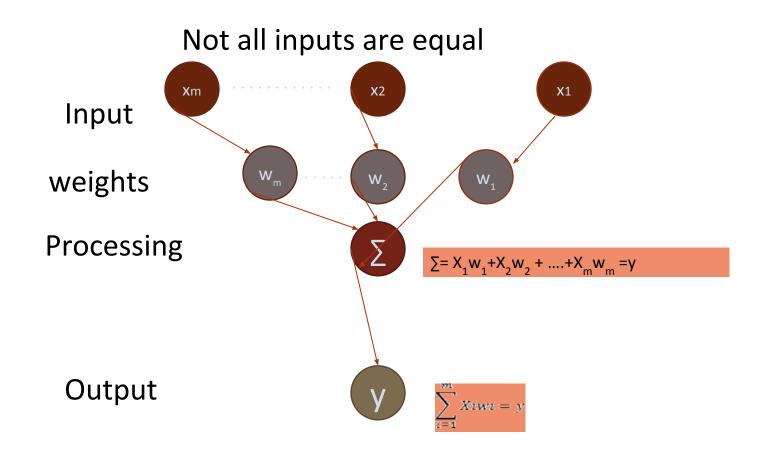
An artificial neuron is an imitation of a human neuron

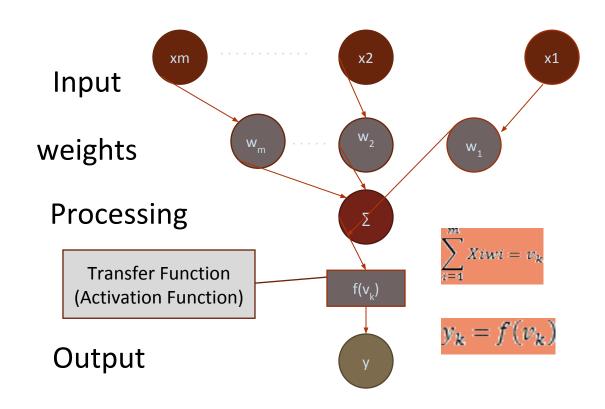
•Now, let us have a look at the model of an artificial neuron.

A Single Neuron

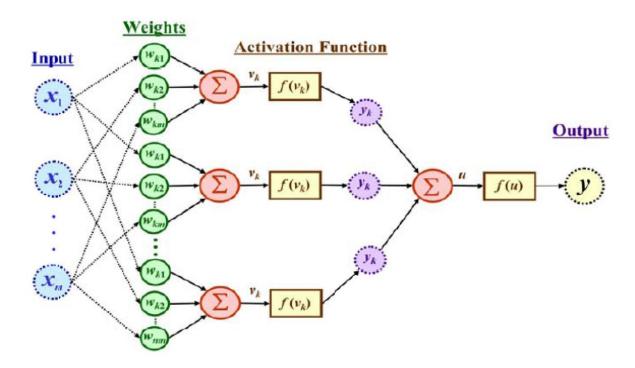








The output is a function of the input, that is affected by the weights, and the transfer functions



Network architectures

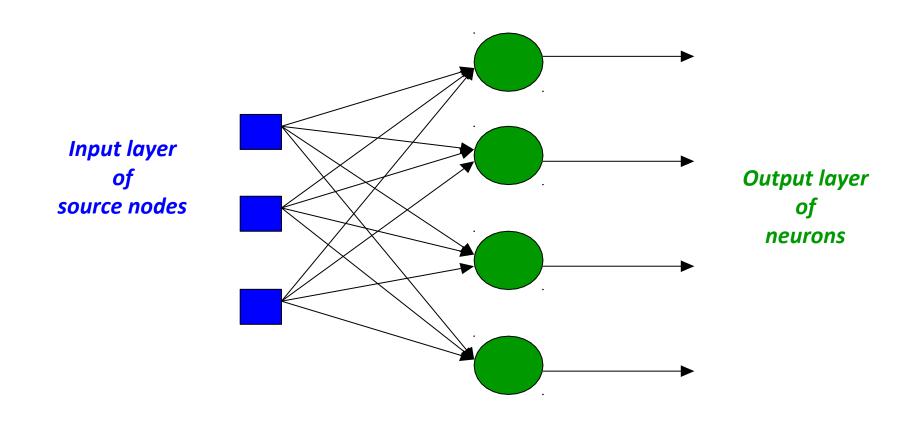
Three different classes of network architectures

- -single-layer feed-forward
- -multi-layerfeed-forward
- -recurrent

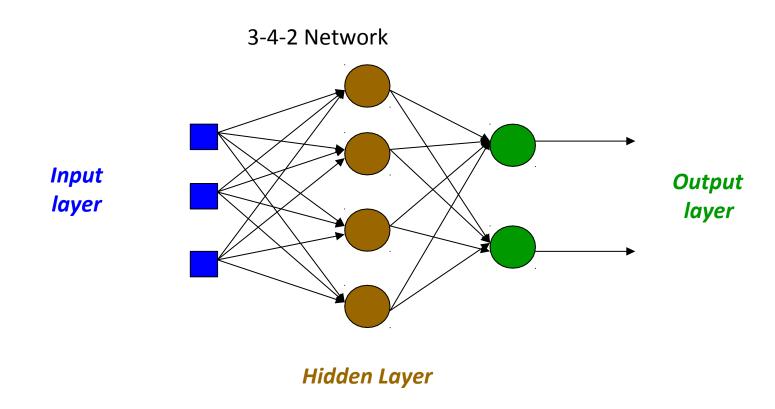
neurons are organized in acyclic layers

The architecture of a neural network is linked with the learning algorithm used to train

Single Layer Feed-forward

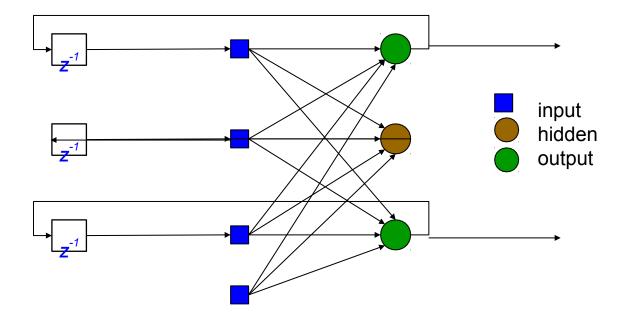


Multi layer feed-forward



Recurrent network

Recurrent Network with *hidden neuron(s)*: unit delay operator *z*⁻¹ implies dynamic system



Dimensions of a Neural Network

Various types of neurons

Various network architectures

Various learning algorithms

Various applications

Training Algorithm

Not guaranteed to converge to zero training error, may converge to local optima or oscillate indefinitely.

However, in practice, does converge to low error for many large networks on real data.

Many epochs (thousands) may be required, hours or days of training for large networks.

- To avoid local-minima problems, run several trials starting with different random weights (random restarts).
 - Take results of trial with lowest training set error.
 - Build a committee of results from multiple trials (possibly weighting votes by training set accuracy).

Backpropagation Training Algorithm

Create the 3-layer network with H hidden units with full connectivity between layers. Set weights to small random real values.

Until all training examples produce the correct value (within ε), or mean squared error ceases to decrease, or other termination criteria:

```
Begin epoch

For each training example, d, do:

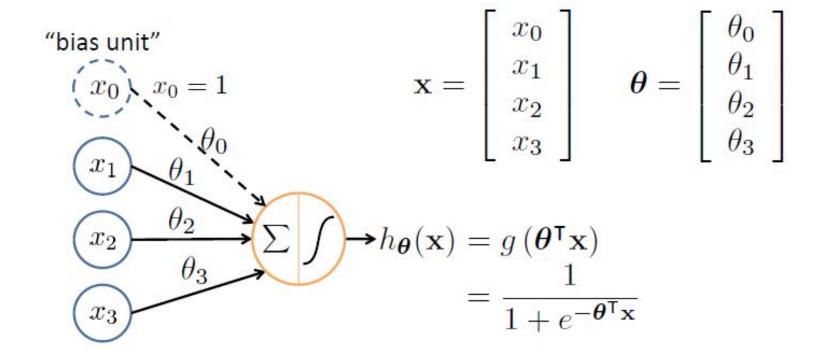
Calculate network output for d's input values

Compute error between current output and correct output for d

Update weights by backpropagating error and using learning rule

End epoch
```

Single Node



Sigmoid (logistic) activation function:
$$g(z) = \frac{1}{1 + e^{-z}}$$

Loss Function: A mathematical function that measures how well the neural network's predictions match the true labels. Common examples include:

Mean Squared Error (MSE) for regression tasks.

$$L(y, \hat{y}) = rac{1}{n} \sum_{i=1}^n (y_i - \hat{y}_i)^2$$

Cross-Entropy Loss for classification tasks.

$$L(y,\hat{y}) = -rac{1}{n}\sum_{i=1}^n y_i\log(\hat{y}_i)$$

The chain rule

Computing the derivative of a composite function:

$$f(x) = u(v(x))$$

$$\frac{df}{dx} = \frac{du}{dv} \cdot \frac{dv}{dx}$$

$$f(x) = u(v(w(x))) \qquad \frac{df}{dx} = \frac{du}{dv} \cdot \frac{dv}{dw} \cdot \frac{dw}{dx}$$

Example
$$L(a,b,c) = c(a+2b)$$

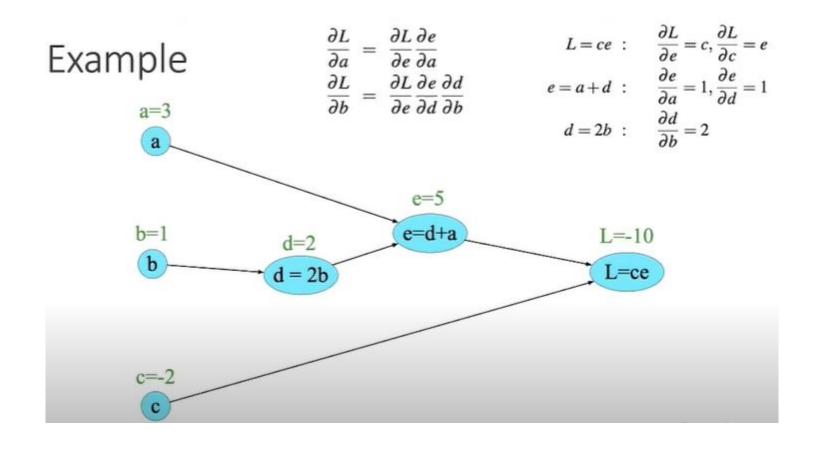
$$d = 2*b$$

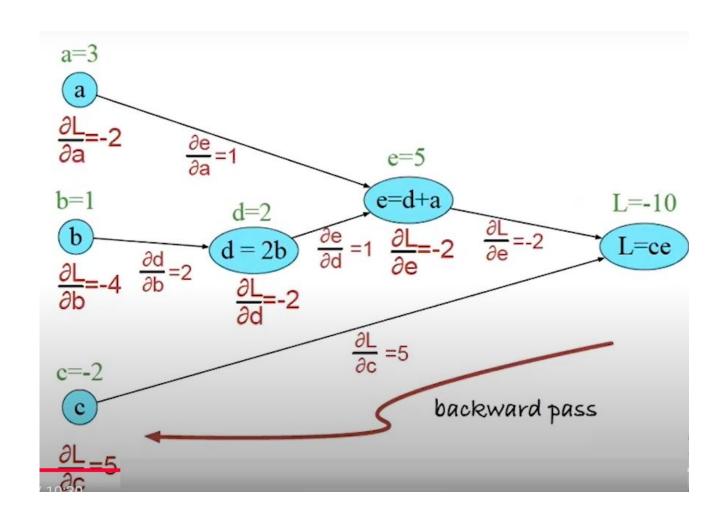
$$e = a+d$$

$$L = c*e$$

$$e = a+d : \frac{\partial L}{\partial e} = c, \frac{\partial L}{\partial e} = e$$

$$d = 2b : \frac{\partial L}{\partial e} = 1, \frac{\partial e}{\partial d} = 1$$





$$x_{1}$$

$$x_{2}$$

$$x_{2}$$

$$x_{3}$$

$$x_{4}$$

$$x_{5}$$

$$x_{2}$$

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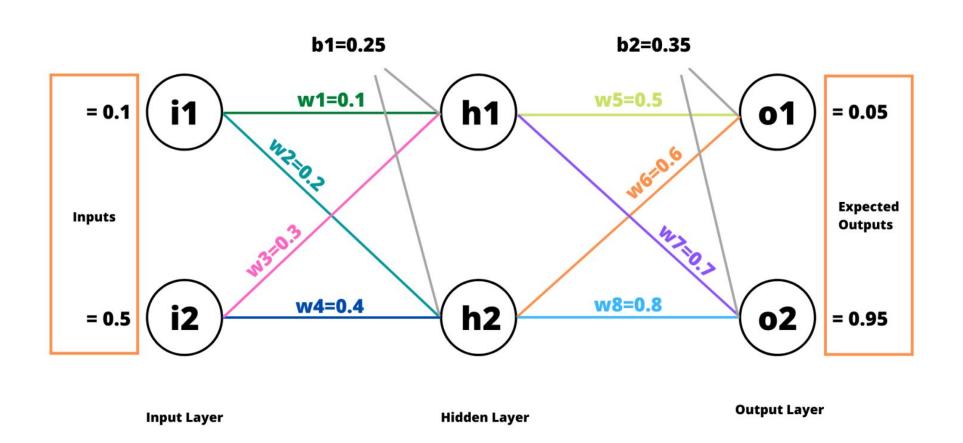
$$x_{2}$$

$$x_{4}$$

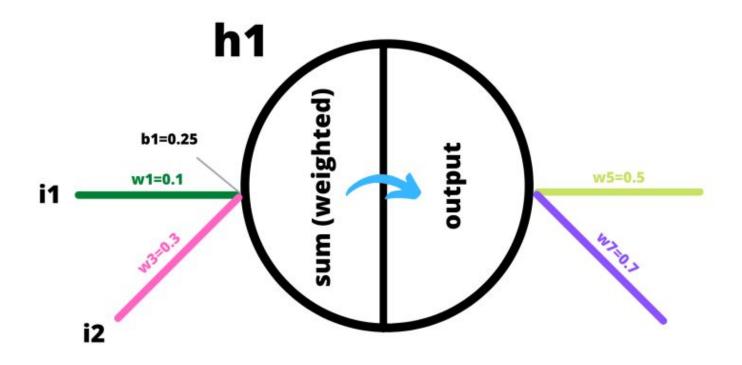
$$x_{5}$$

$$x_{5$$

Example Network



Single Neuron



Forward Pass

h,

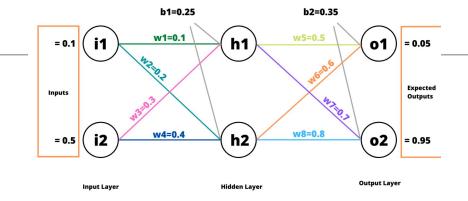
$$sum_{h1} = i_1 * w_1 + i_2 * w_3 + b_1$$
 $sum_{h1} = 0.1 * 0.1 + 0.5 * 0.3 + 0.25 = 0.41$

$$output_{h1} = rac{1}{1 + e^{-sum_{h1}}}$$
 $output_{h1} = rac{1}{1 + e^{-0.41}} = 0.60108$

 O_1

$$sum_{o1} = output_{h1} * w_5 + output_{h2} * w_6 + b_2 = 1.01977$$

$$output_{o1} = \frac{1}{1 + e^{-sum_{o1}}} = 0.73492$$



 $egin{aligned} \mathsf{h_2} \ &sum_{h2} = i_1 * w_2 + i_2 * w_4 + b_1 = 0.47 \ &output_{h2} = rac{1}{1 + e^{-sum_{h2}}} = 0.61538 \end{aligned}$

$$Sum_{o2} = output_{h1} * w_7 + output_{h2} * w_8 + b_2 = 1.26306$$
 $output_{o2} = \frac{1}{1 + e^{-sum_{o2}}} = 0.77955$

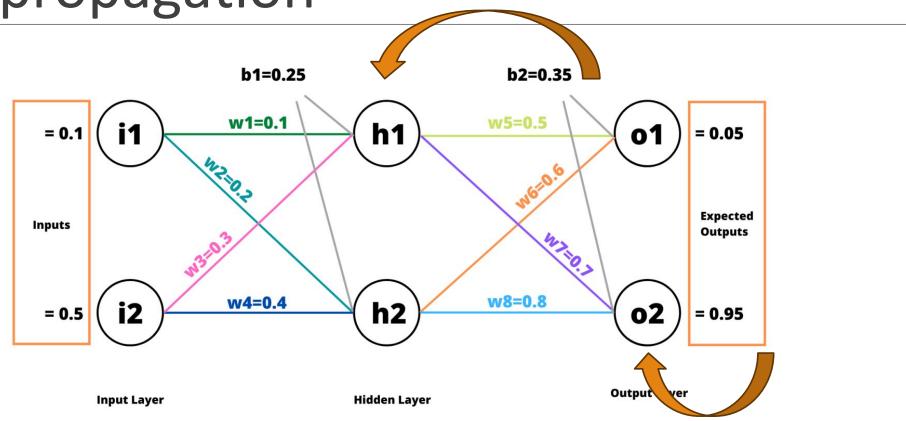
Computing the total error

$$E_{total} = \sum \frac{1}{2} (target - output)^2$$

$$E_1 = \frac{1}{2}(target_1 - output_{o1})^2$$
 $E_2 = \frac{1}{2}(target_2 - output_{o2})^2$ $E_1 = \frac{1}{2}(0.05 - 0.73492)^2 = 0.23456$ $E_2 = \frac{1}{2}(0.95 - 0.77955)^2 = 0.01452$

$$E_{total} = E_1 + E_2 = 0.24908$$

Back propagation

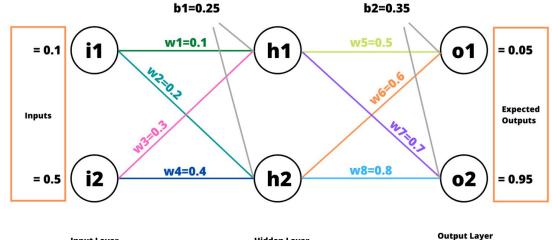


Chain Rule

If we have y=f(u) and u=g(x) then we can write the derivative of y as:

$$\frac{dy}{dx} = \frac{dy}{du} * \frac{du}{dx}$$

For weights in the output layer (w5, w6, w7, w8)



$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial w_5}$$

Component 1: partial derivative of Error w.r.t. Output

$$E_{total} = \sum rac{1}{2} (target-output)^2$$

$$E_{total} = rac{1}{2}(target_1 - output_{o1})^2 + rac{1}{2}(target_2 - output_{o2})^2$$

$$\frac{\partial E_{total}}{\partial output_{o1}} = 2 * \frac{1}{2} * (target_1 - output_{o1}) * -1$$
$$= output_{o1} - target_1$$

For weights in the output layer (w5, w6, w7, w8)

Component 2: partial derivative of Output w.r.t. Sum

$$rac{\partial E_{total}}{\partial w5} = rac{\partial E_{total}}{\partial output_{o1}} * rac{\partial output_{o1}}{\partial sum_{o1}} * rac{\partial sum_{o1}}{\partial w5}$$

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

$$\frac{\mathrm{d}}{\mathrm{dx}}\sigma(x) = \sigma(x)(1 - \sigma(x))$$

$$\frac{\partial output_{o1}}{\partial sum_{o1}} = output_{o1}(1 - output_{o1})$$

 Component 3: partial derivative of Sum w.r.t. Weight

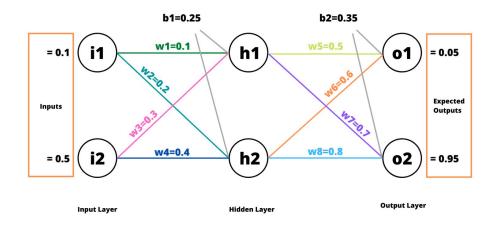
$$\frac{\partial E_{total}}{\partial w5} = \frac{\partial E_{total}}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial w5}$$

$$sum_{o1} = output_{h1} * w_5 + output_{h2} * w_6 + b_2$$

Therefore,

$$\frac{\partial sum_{o1}}{\partial w_{5}} = output_{h1}$$

For weights in the output layer (w5, w6, w7, w8)



Putting them together,

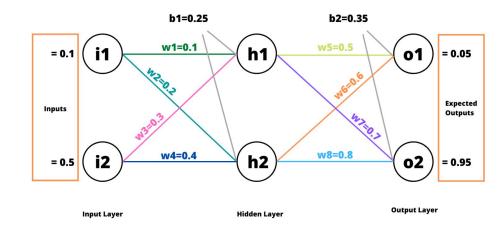
$$\begin{split} \frac{\partial E_{total}}{\partial w5} &= \frac{\partial E_{total}}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial w5} \\ \frac{\partial E_{total}}{\partial w5} &= [output_{o1} - target_1] * [output_{o1}(1 - output_{o1})] * [output_{h1}] \\ \frac{\partial E_{total}}{\partial w5} &= 0.68492 * 0.19480 * 0.60108 \\ \frac{\partial E_{total}}{\partial w5} &= 0.08020 \end{split}$$

The new_w_5 is,

 $new_w_5 = w_5 - n * rac{\partial E_{total}}{\partial w_5}$, where n is learning rate.

$$new_{-}w_{5} = 0.5 - 0.6 * 0.08020$$

 $new_{-}w_{5} = 0.45187$



For w6,

$$\frac{\partial E_{total}}{\partial w6} = \frac{\partial E_{total}}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial w6}$$

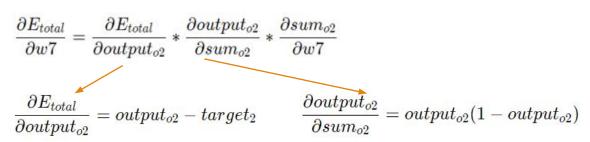
$$\frac{\partial sum_{o1}}{\partial w_6} = output_{h2}$$
.

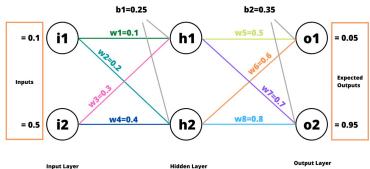
$$\frac{\partial E_{total}}{\partial w6} = 0.68492 * 0.19480 * 0.61538 = 0.08211$$

The new_w_6 is,

$$new_w_6 = w6 - n * \frac{\partial E_{total}}{\partial w6}$$
 $new_w_6 = 0.6 - 0.6 * 0.08211$ $new_w_6 = 0.55073$

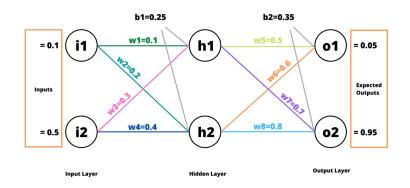
For w7,





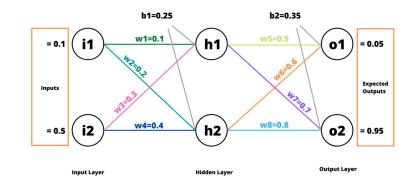
$$\frac{\partial sum_{o2}}{\partial w7} = output_{h1}$$

$$\frac{\partial E_{total}}{\partial w7} = [output_{o2} - target_2] * [output_{o2}(1 - output_{o2})] * [output_{h1}]$$
 The new_w_7 is,
$$\frac{\partial E_{total}}{\partial w7} = -0.17044 * 0.17184 * 0.60108$$
 $new_w_7 = w7 - n * \frac{\partial E_{total}}{\partial w7}$
$$\frac{\partial E_{total}}{\partial w7} = -0.01760$$
 $new_w_7 = 0.7 - 0.6 * -0.01760$
$$new_w_7 = 0.71056$$



Proceeding similarly, we get $new_w_8=0.81081$ (with $\frac{\partial E_{total}}{\partial w8}=-0.01802$).

$$\frac{\partial E_1}{\partial w1} = \frac{\partial E_1}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial output_{h1}} * \frac{\partial output_{h1}}{\partial sum_{h1}} * \frac{\partial sum_{h1}}{\partial w1}$$



Component 1

$$\frac{\partial E_1}{\partial output_{o1}} = output_{o1} - target_1$$

Component 3

$$sum_{o1} = output_{h1} * w_5 + output_{h2} * w_6 + b_2$$

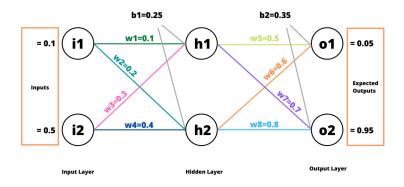
$$\frac{\partial sum_{o1}}{\partial output_{h1}} = w5$$

Component 4

$$\frac{\partial output_{h1}}{\partial sum_{h1}} = output_{h1}*(1 - output_{h1})$$

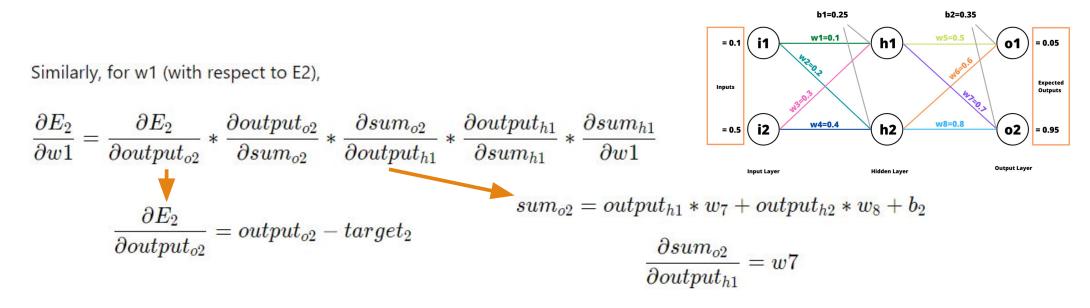
Component 5

$$sum_{h1}=i_1*w_1+i_2*w_3+b_1$$
 $rac{\partial sum_{h1}}{\partial w1}=i_1$



Putting them all together,

$$\frac{\partial E_1}{\partial w1} = \frac{\partial E_1}{\partial output_{o1}} * \frac{\partial output_{o1}}{\partial sum_{o1}} * \frac{\partial sum_{o1}}{\partial output_{h1}} * \frac{\partial output_{h1}}{\partial sum_{h1}} * \frac{\partial sum_{h1}}{\partial w1}$$
$$\frac{\partial E_1}{\partial w1} = 0.68492 * 0.19480 * 0.5 * 0.23978 * 0.1 = 0.00159$$



$$\frac{\partial E_2}{\partial w1} = \frac{\partial E_2}{\partial output_{o2}} * \frac{\partial output_{o2}}{\partial sum_{o2}} * \frac{\partial sum_{o2}}{\partial output_{h1}} * \frac{\partial output_{h1}}{\partial sum_{h1}} * \frac{\partial sum_{h1}}{\partial w1}$$

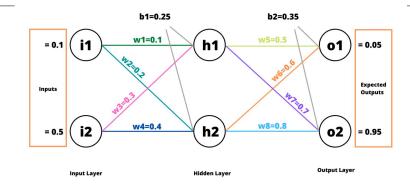
$$\frac{\partial E_2}{\partial w1} = -0.17044 * 0.17184 * 0.7 * 0.23978 * 0.1 = -0.00049$$

Now we can compute $\frac{\partial E_{total}}{\partial w1} = \frac{\partial E_1}{\partial w1} + \frac{\partial E_2}{\partial w1}$.

$$\frac{\partial E_{total}}{\partial w_1} = 0.00159 + (-0.00049) = 0.00110.$$

The $new_{-}w_{1}$ is,

$$new_{-}w_{1} = w1 - n * \frac{\partial E_{total}}{\partial w1}$$
 $new_{-}w_{1} = 0.1 - 0.6 * 0.00110$
 $new_{-}w_{1} = 0.09933$



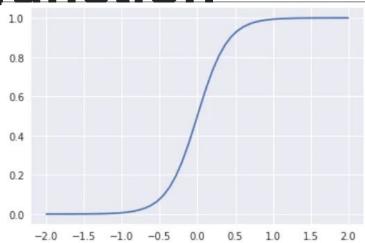
$$new_{-}w_2 = 0.19919$$

$$new_{-}w_{3} = 0.29667$$

$$new_{-}w_{4} = 0.39597$$

Activation Functions

Sigmoid or Logistic activation function



Advantage :-

a) As output of sigmoid function ranges between 0 to 1 hence this helps to normalize(or scale data) and to achieve non linearity of the data set. b) As we can also perform differentiation which help the NN to learn during backward propagation.

```
f(x) = 1 / (1 + exp(-x)), Result ranges between 0 to 1

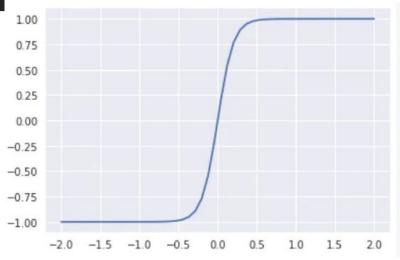
f'(x) = f(x)(1-f(x)), Result ranges between 0 to 0.25
```

Disadvantage:-

- a) As Sigmoid function is not a zero centric function (does not cross origin) so it always gives gradient into +ve direction, which is not good and make optimiser hard to learn/adjust weight of NN.
- b) Vanishing gradient issue: As the differential value of Sigmoid function ranges between 0 to 1, hence effect of gradient decreases layer by layer which cause issue during learning of neural network or very less impact on first layer of the Neuron.
- c) As Sigmoid function is combination of exponential function (exp(x)), hence it **required lots of computational power** which makes this **more expensive**.

Tanh or Hyper tangent Act.

function



```
f(x) = (epx(x) - exp(-x))/ (exp(x) + exp(-x)) f'(x) = 1 - (f(x))2 , Result ranges between 0 to 1 We can also represent Tanh function in form of Sigmoid like below f(tanh) = 2 * Sigmoid(2x) -1
```

Advantage :-

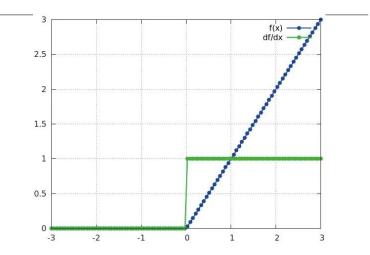
- a) Zero centric function, hence this will give gradient in both +ve and -ve direction.
- b) Modified version of Sigmoid and comparatively better sigmoid function..

Disadvantage:-

- a) For large layers this function also faces vanishing gradient issue.
- b) As this is modified version of sigmoid hence bit more expensive computational power.

function

Function	Equation	Range	Derivative
ReLu (Rectified Linear Unit)	$f(x) = \begin{cases} 0 & \text{for } x < 0 \\ x & \text{for } x \ge 0 \end{cases}$	0,+∞	$f'(x) = \begin{cases} 0 & \text{for } x < 0 \\ 1 & \text{for } x \ge 0 \end{cases}$



Advantage:-

- a. This **overcomes the vanishing gradient** issue as differential is going to give the output range between 0 to 1.
- b. Main advantage of ReLu, it does not activate all neurons at a time. if the output of one neuron is zero then this will activate that neuron.

Disadvantage:-

- a. This is not zero centric function so it gives only +ve direction gradient
- b. For -ve input it does not do anything, which is not good for learning of Neural Network.
- c. Dead neuron is the biggest issue of ReLu as it deactivates the neurons for -ve data set & do not provide learning -ve direction.

Leaky ReLU Act. function

Function	Equation	Range	Derivative	10
Leaky ReLu	$f(x) = \begin{cases} \alpha x & \text{for } x < 0 \\ x & \text{for } x \ge 0 \end{cases}$	-∞, +∞	$f'(x) = \begin{cases} \alpha & \text{for } x < 0 \\ 1 & \text{for } x \ge 0 \end{cases}$	-10 10
				$\alpha = 0.01$

Advantage:-

- a. Overcomes the dead neuron issue by adding constant slope alpha.
- b. Less computational expensive compare to sigmoid and tanh function
- Disadvantage : -
- a. It does not provide much leaning for -ve dataset/input as alpha value is constant.

Softmax Activation Function

Formula:

$$\operatorname{softmax}(x_i) = \frac{e^{x_i}}{\sum_j e^{x_j}}$$

Range: (0, 1), where the sum of outputs is equal to 1.

Characteristics:

Converts the raw output into a probability distribution over multiple classes.

Advantages:

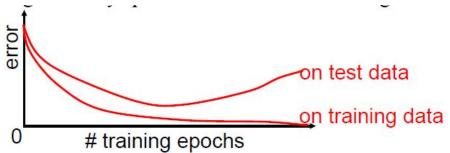
Ideal for multi-class classification tasks, providing a probabilistic output.

Disadvantages:

Susceptible to the vanishing gradient problem in deep networks

Over-Training Prevention

Running too many epochs can result in over-fitting.



Keep a hold-out validation set and test accuracy on it after every epoch. Stop training when additional epochs actually increase validation error.

Too few hidden units prevents the network from adequately fitting the data.

Too many hidden units can result in over-fitting

Artificial Neural Networks

Advantages

- The output of ANNs can be discrete-valued, real-valued, or a vector of multiple real or discrete-valued characteristics, while the target function can be discrete-valued, real-valued, or a vector of numerous real or discrete-valued attributes.
- Noise in the training data is not a problem for ANN learning techniques. There may be mistakes in the training samples, but they will not affect the final result.

Disadvantages

- Hardware Dependence
- It acts like a black box. Output is not explainable.

Sucessful Applications

Fraud detection

Financial Applications

HNC (eventually bought by Fair Isaac)

Chemical Plant Control

Pavillion Technologies

Automated Vehicles

Game Playing

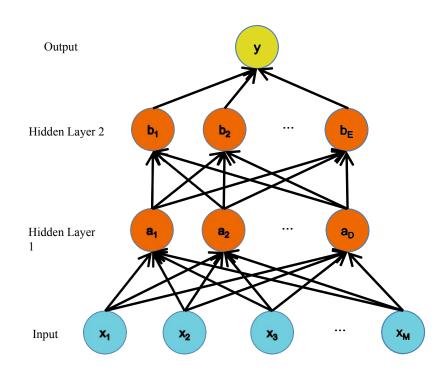
Neurogammon

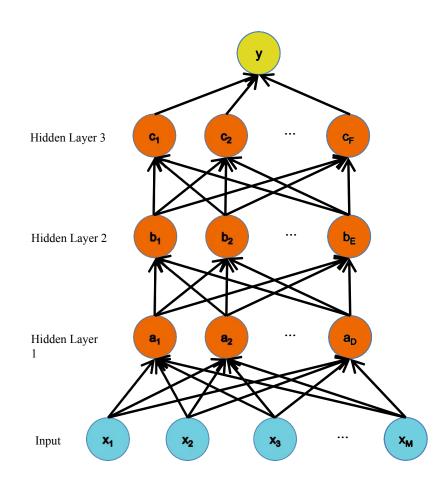
Handwriting recognition

DEEPER NETWORKS

DEEPER NETWORKS

Deeper Networks



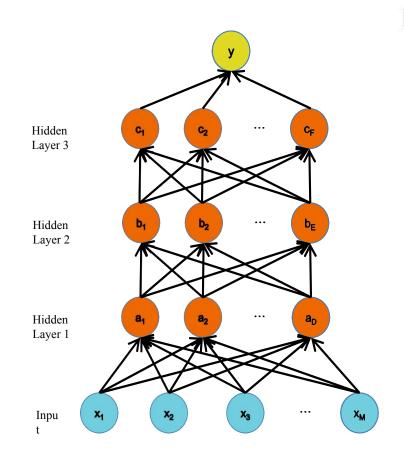


Different Levels of Abstraction

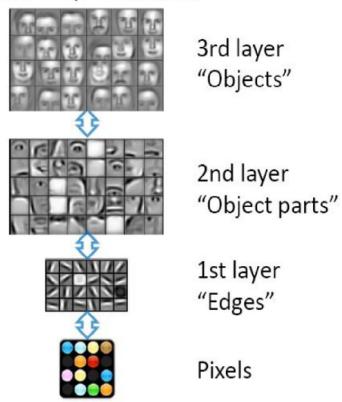
- We don't know the "right" levels of abstraction
- So let the model figure it out!

Face Recognition:

- Deep Network can build up increasingly higher levels of abstraction
- Lines, parts, regions



Feature representation



Example from Honglak Lee (NIPS 2010)

Feedforward Neural Networks (FNN)

Concept: The simplest type of neural network where information flows in one direction, from the input layer to the output layer, without any loops.

Applications: Basic classification and regression tasks where there are no temporal or spatial dependencies in the data.

Convolutional Neural Networks (CNNs)

Concept: CNNs are specialized for processing grid-like data, such as images. They consist of convolutional layers that apply filters (kernels) to extract spatial features (e.g., edges, textures) from the data.

Key Components:

- Convolutional Layers: Apply filters to the input to create feature maps that highlight important spatial patterns.
- ☐ Pooling Layers: Reduce the spatial dimensions of feature maps to lower computational complexity and make the network more robust to small translations in the input.
- ☐ Fully Connected Layers: Flatten the feature maps and connect every neuron to every other neuron to produce the final output.

Applications: Image classification, object detection, semantic segmentation, and other vision-related tasks.

Transformer Networks

Concept: Transformers use self-attention mechanisms to process sequential data without relying on recurrence. They handle long-range dependencies effectively and process data in parallel, making them efficient for large-scale tasks.

Key Components:

- □ **Self-Attention:** Calculates attention scores between elements of the sequence, allowing the model to weigh the importance of each element when making predictions.
- ☐ **Multi-Head Attention:** Uses multiple attention mechanisms in parallel to capture different aspects of the sequence relationships.
- ☐ **Positional Encoding**: Adds positional information to the input to retain the order of elements in the sequence.

Applications: NLP tasks (e.g., translation, summarization), image classification (e.g., Vision Transformers), and multi-modal tasks (e.g., text and image fusion).

Generative Adversarial Networks (GANs)

Concept: GANs consist of two neural networks, a generator and a discriminator, that compete against each other. The generator tries to create realistic data samples, while the discriminator attempts to distinguish between real and generated samples.

Training Process:

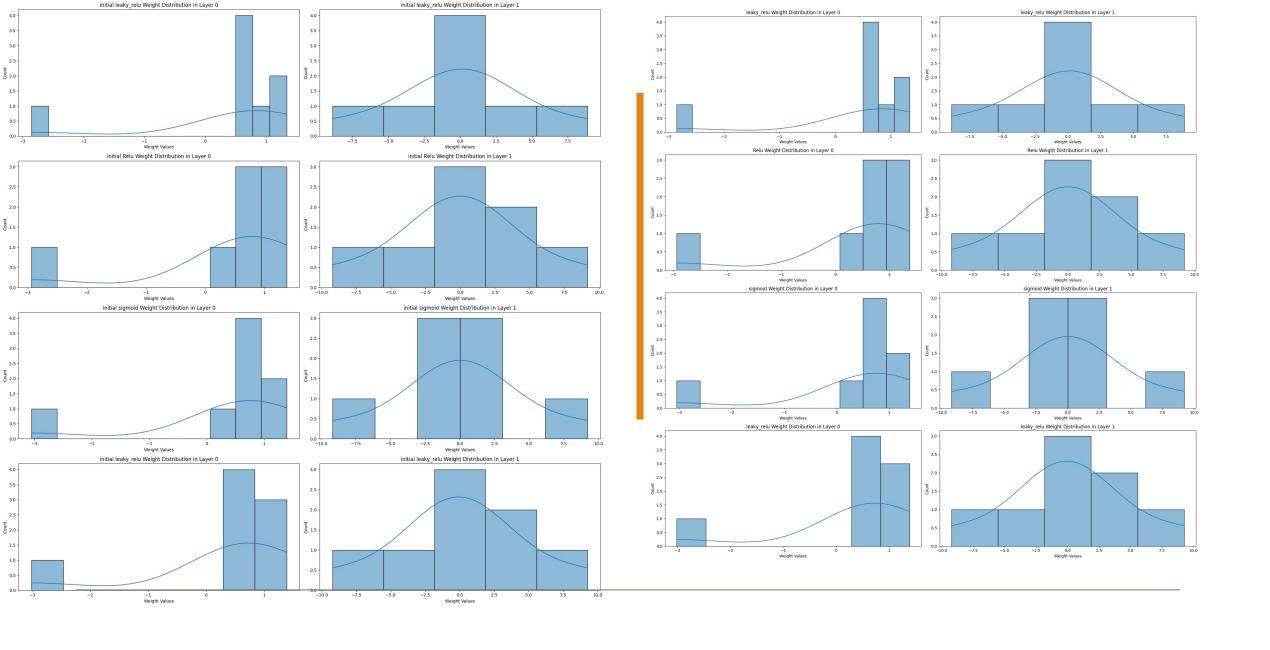
- ☐ The generator produces fake samples from random noise.
- ☐ The discriminator evaluates both real and generated samples, providing feedback to the generator to improve its output.

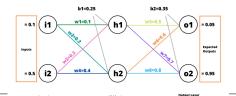
Applications: Image generation, style transfer, super-resolution, and data augmentation.

Thank You

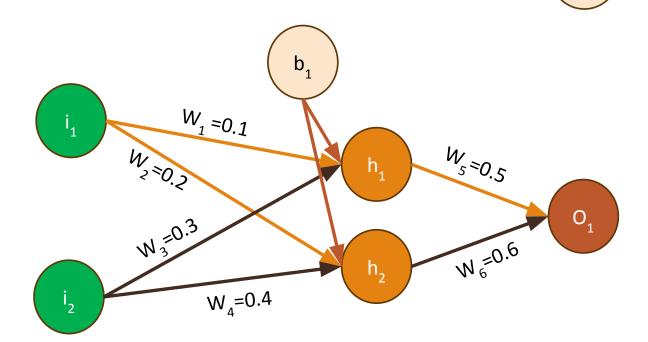
Reference

- https://theneuralblog.com/forward-pass-backpropagation-example/
- https://medium.com/@santosh76792/activation-functions-and-their-advantages-disadvantages-d5eaa1717805

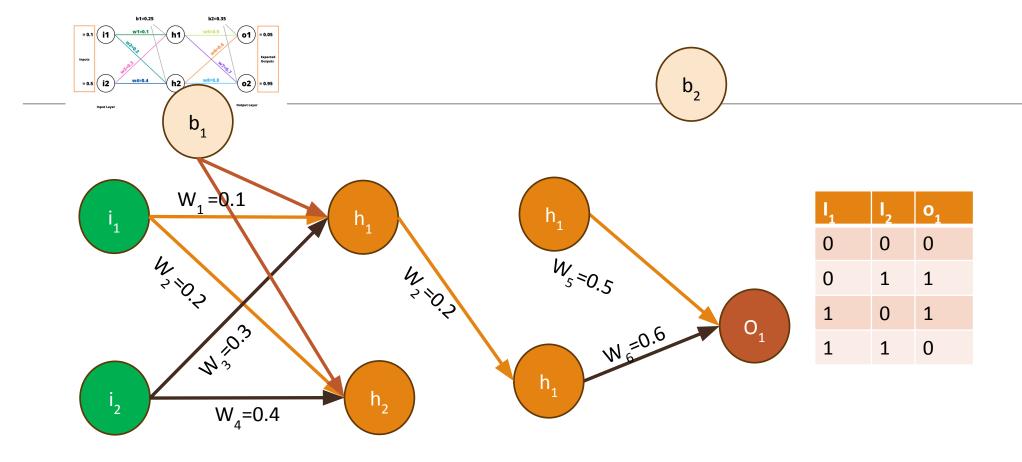




b₂



l ₁	l ₂	o ₁
0	0	0
0	1	1
1	0	1
1	1	0



Example Network

