

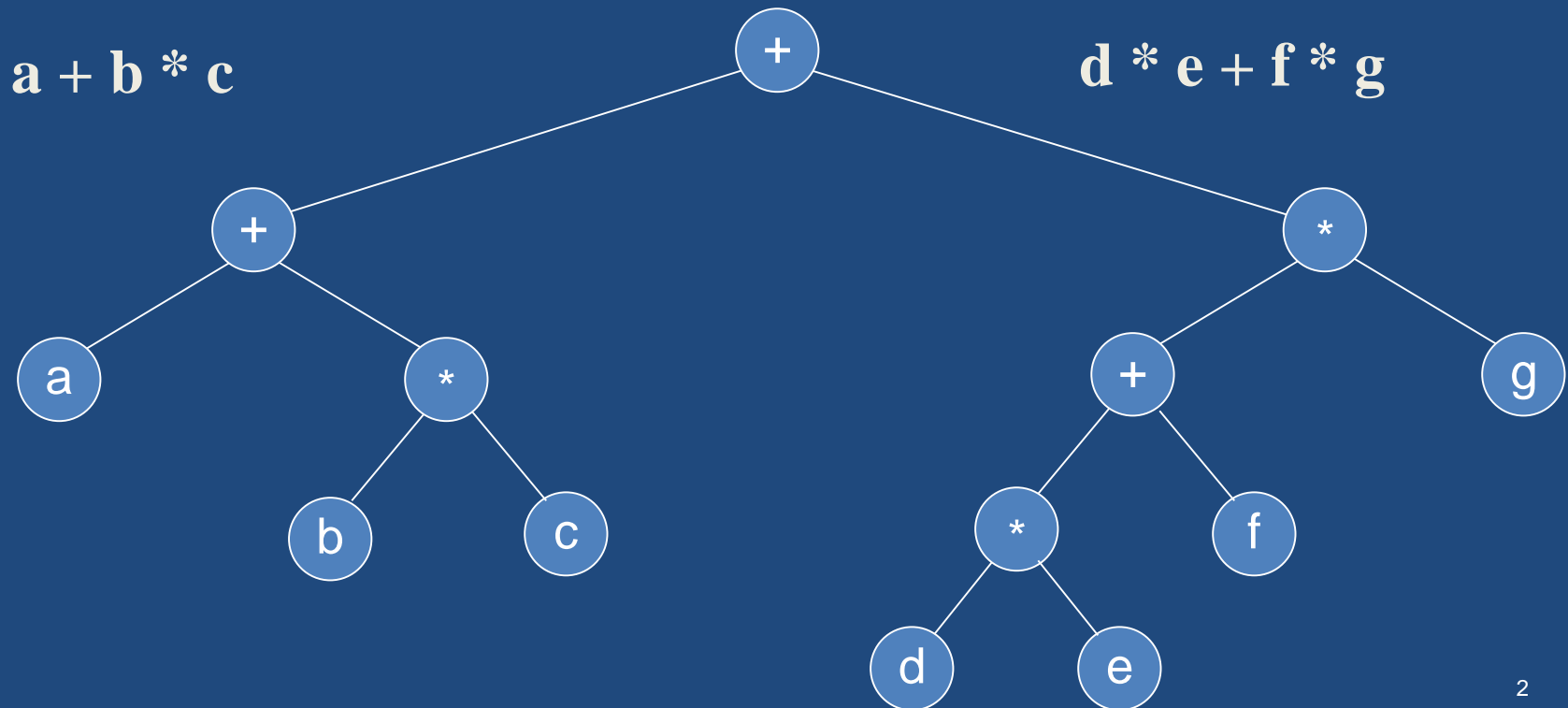


# Application of Binary Tree

## Expression Tree

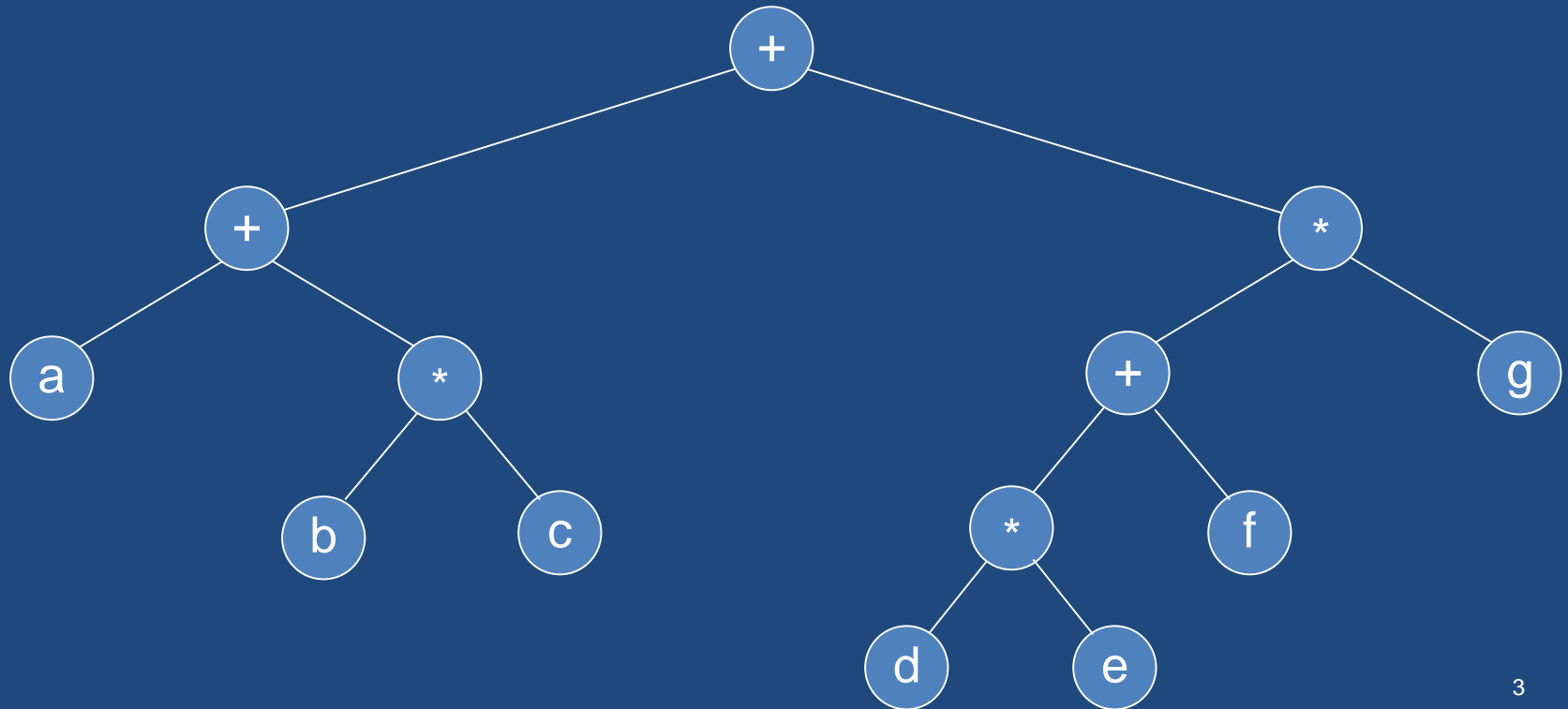
# Expression Tree

- The inner nodes contain operators while leaf nodes contain operands.



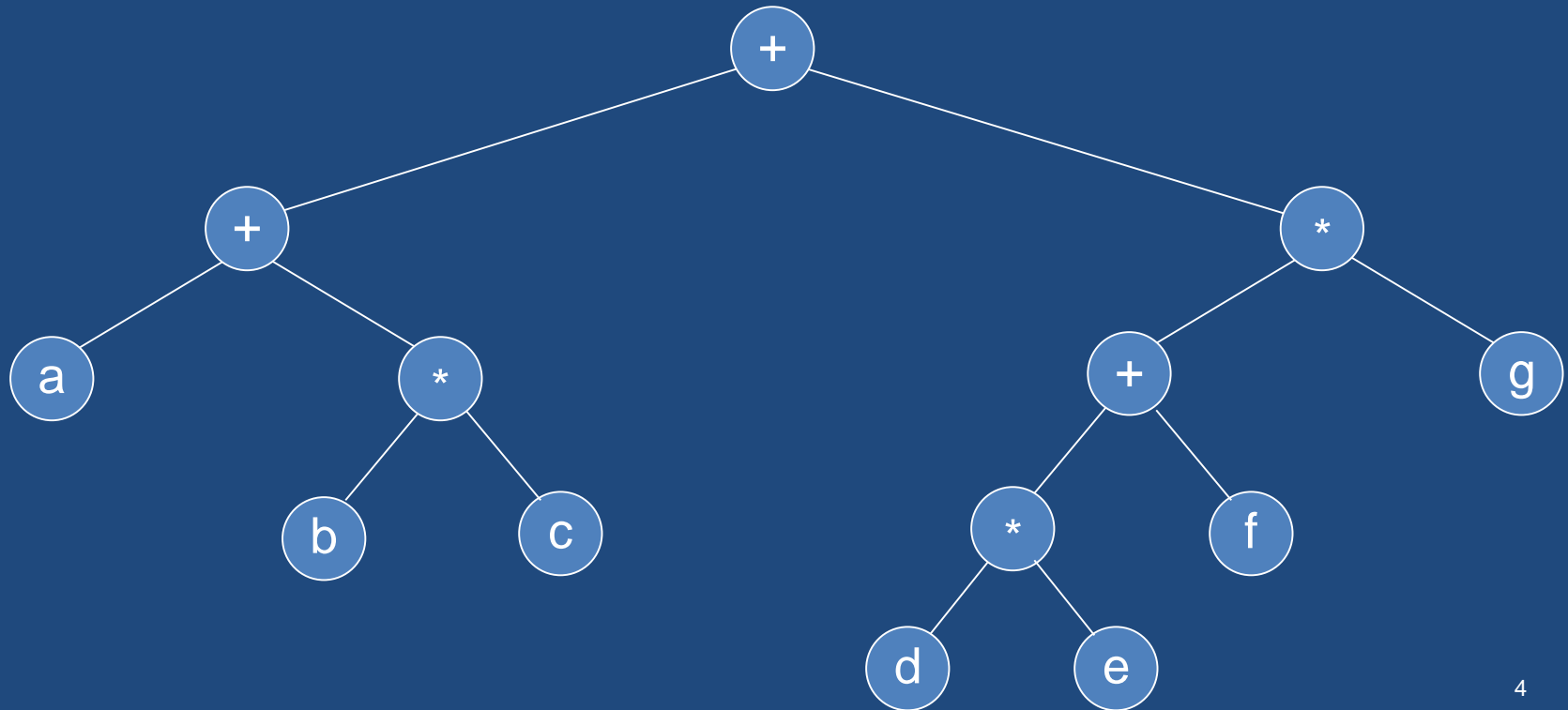
# Expression Tree

- The tree is binary because the operators are binary.



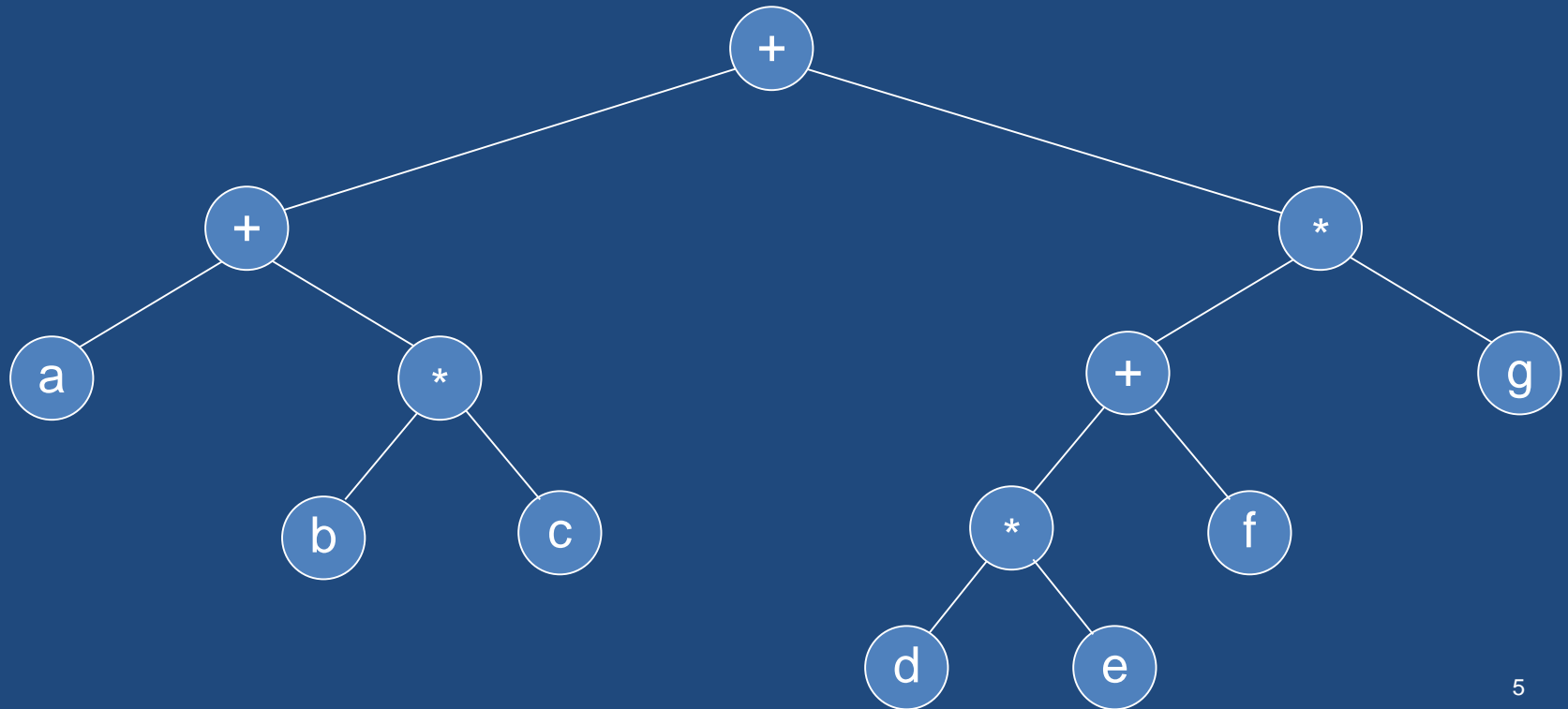
# Expression Tree

- This is not necessary. A unary operator (!, e.g.) will have only one subtree.



# Expression Tree

- Inorder traversal yields:  $a+b*c+d*e+f*g$

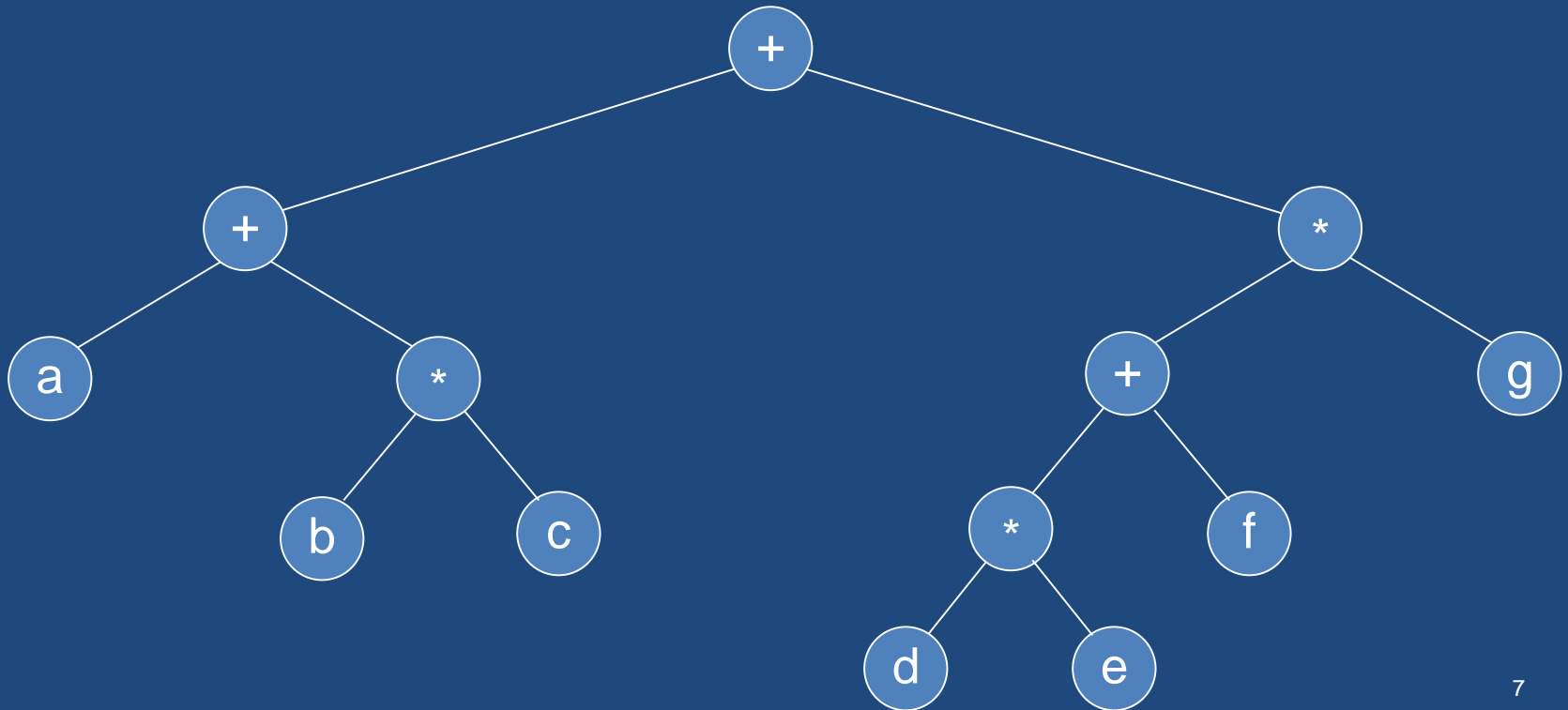


# Enforcing Parenthesis

```
void inorder(TreeNode<int>* treeNode)
{
    if( treeNode != NULL ){
        cout << "(";
        inorder(treeNode->getLeft());
        cout << ")";
        cout << *(treeNode->getInfo());
        cout << "(";
        inorder(treeNode->getRight());
        cout << ")";
    }
}
```

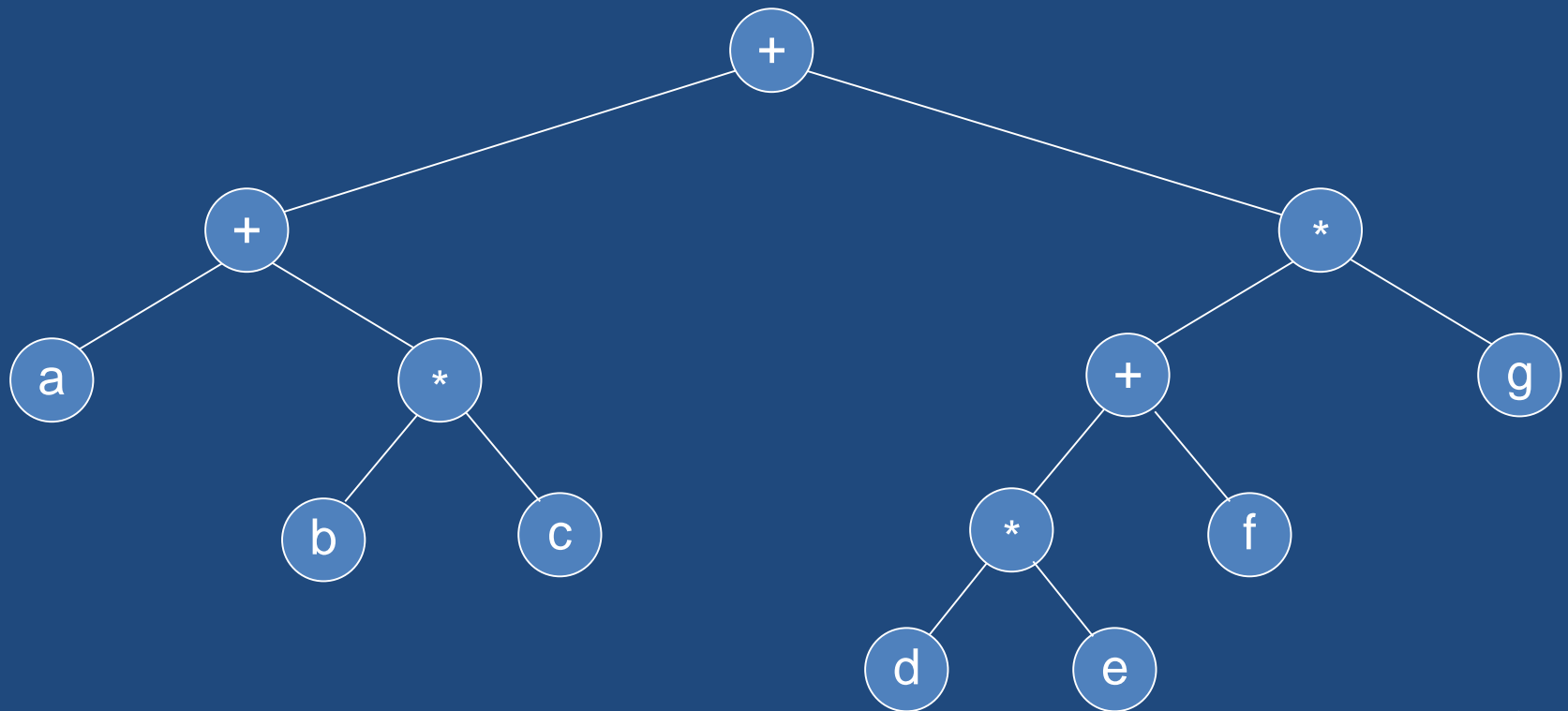
# Expression Tree

- Inorder :  $(a+(b*c))+(((d*e)+f)*g)$



# Expression Tree

- Postorder traversal:  $a\ b\ c\ *\ +\ d\ e\ *\ f\ +\ g\ *\ +$   
which is the postfix form.





# Constructing Expression Tree

- Algorithm to convert postfix expression into an expression tree.
- We already have an expression to convert an infix expression to postfix.
- Read a symbol from the postfix expression.
- If symbol is an operand, put it in a one node tree and push it on a stack.
- If symbol is an operator, pop two trees from the stack, form a new tree with operator as the root and  $T_1$  and  $T_2$  as left and right subtrees and push this tree on the stack.

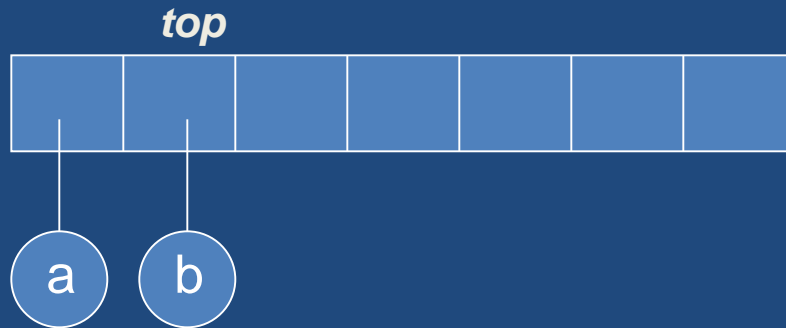
# Constructing Expression Tree

- $a b + c d e + * *$



# Constructing Expression Tree

- $a b + c d e + * *$



If symbol is an operand, put it in a one node tree and push it on a stack.

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*Stack is growing left to right*

# Constructing Expression Tree

•  $a b + c d e + * *$



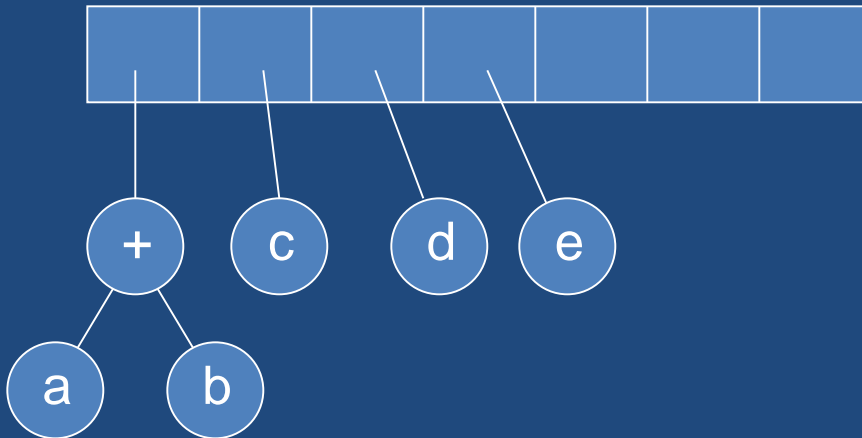
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*Stack is growing left to right*

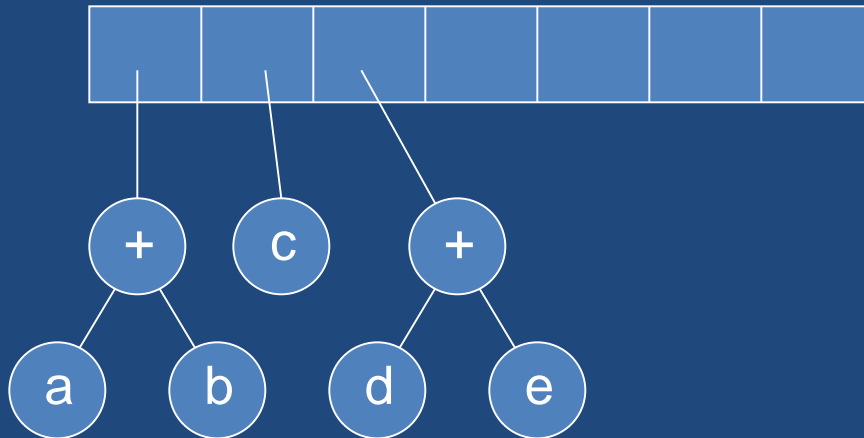
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- $a b + c d e + * *$



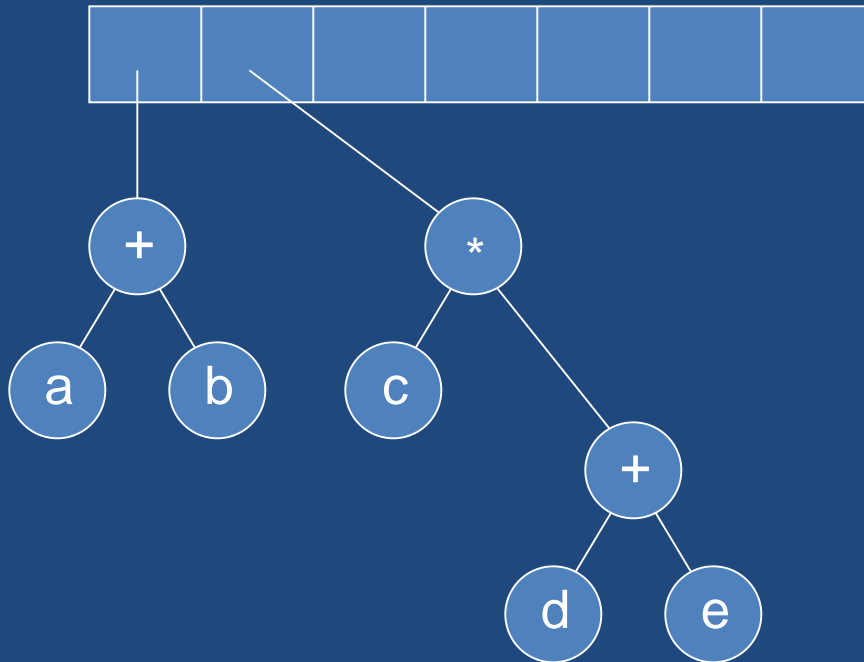
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