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- The interface to the List stayed the same, i.e., add(), get(), find(),update(),remove() etc.
- The list is thus an abstract data type; we use it without being concerned with how it is implemented.



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- We will publish the interface and keep the freedom to change the implementation of ADT without effecting users of the ADT.
- The C++ classes provide us the ability to create such ADTs.



Data abstraction is a programming (and design) technique that relies on the separation of interface and implementation.



Stacks

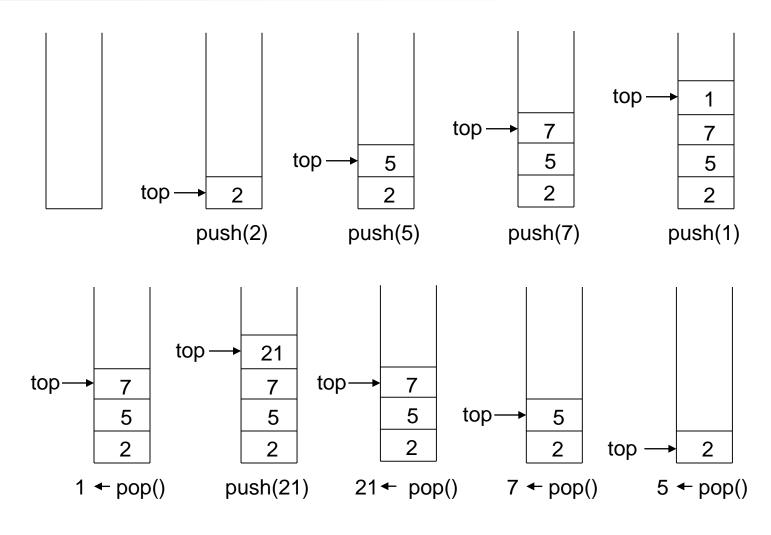
- Stacks in real life: stack of books, stack of plates
- Add new items at the top
- Remove an item at the top
- Stack data structure similar to real life: collection of elements arranged in a linear order.
- Can only access element at the top



Stack Operations

- Push(X) insert X as the top element of the stack
- Pop() remove the top element of the stack and return it.
- Tos() return the top element without removing it from the stack.

Stack Operations





Stack Operation

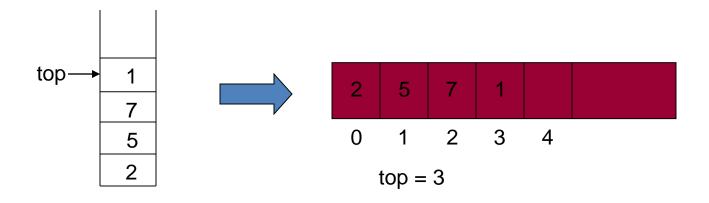
- The last element to go into the stack is the first to come out: LIFO – Last In First Out.
- What happens if we call pop() and there is no element?(Under Flow condition)
- Have IsEmpty() boolean function that returns true if stack is empty, false otherwise.
- Throw StackEmpty exception: advanced C++ concept.



Stack Implementation: Array

- Worst case for insertion and deletion from an array when insert and delete from the beginning: shift elements to the left.
- Best case for insert and delete is at the end of the array – no need to shift any elements.
- Implement push() and pop() by inserting and deleting at the end of an array.

Stack using an Array





Stack using an Array

- In case of an array, it is possible that the array may "fill-up" if we push enough elements. (Over Flow condition)
- Have a boolean function IsFull() which returns true is stack (array) is full, false otherwise.
- We would call this function before calling push(x).

Stack Operations with Array

```
int pop()
    return A[current--];
void push(int x)
    A[++current] = x;
```

Stack Operations with Array

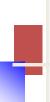
```
int tos()
    return A[current];
int IsEmpty()
    return ( current == -1 );
int IsFull()
    return ( current == size-1);
```

 A quick examination shows that all five operations take constant time.



Stack Using Linked List

- We can avoid the size limitation of a stack implemented with an array by using a linked list to hold the stack elements.
- As with array, however, we need to decide where to insert elements in the list and where to delete them so that push and pop will run the fastest.

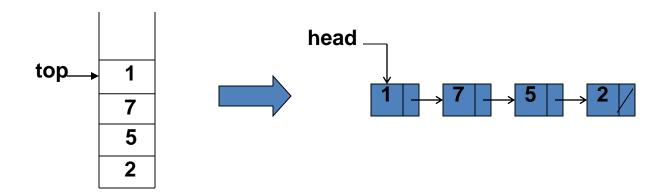


Stack Using Linked List

- For a singly-linked list, insert at start or end takes constant time using the head and current pointers respectively.
- Removing an element at the start is constant time but removal at the end required traversing the list to the node one before the last.
- Make sense to place stack elements at the start of the list because insert and removal are constant time.

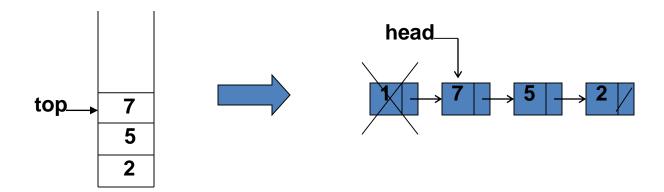
Stack Using Linked List

No need for the current pointer; head is enough.



Stack Operation: List

```
int pop()
{
    int x = head->get();
    Node* p = head;
    head = head->getNext();
    delete p;
    return x;
}
```



Stack Operation: List

```
void push(int x)
    Node* newNode = new Node();
    newNode->set(x);
    newNode->setNext(head);
    head = newNode;
                     head
    top_
                 newNode_
         2
               push (9)
```

Stack Operation: List

```
int top()
{
    return head->get();
}
int IsEmpty()
{
    return ( head == NULL );
}
```

All four operations take constant time.

Stack: Array or List

- Since both implementations support stack operations in constant time, any reason to choose one over the other?
- Allocating and deallocating memory for list nodes does take more time than pre allocated array.
- List uses only as much memory as required by the nodes; array requires allocation ahead of time.
- List pointers (head, next) require extra memory.
- Array has an upper limit; List is limited by dynamic memory allocation.