



Recursion Application and Examples

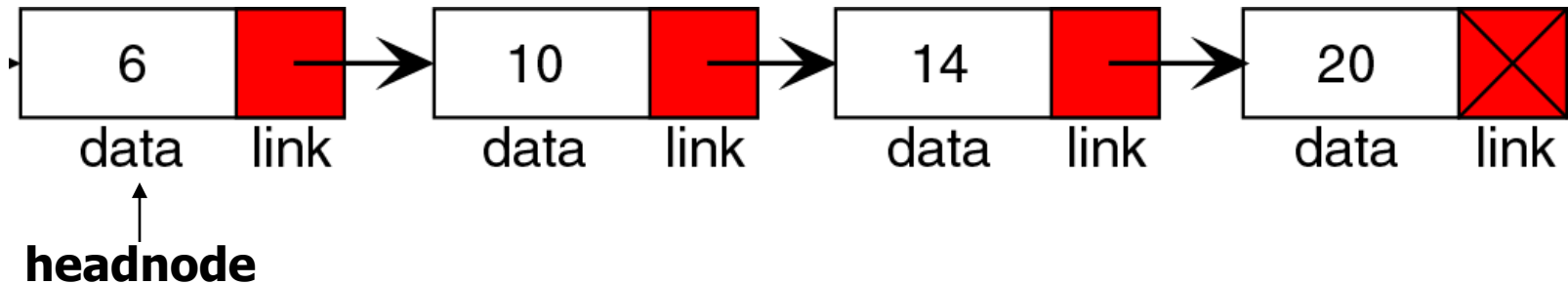


Application

- One application of recursion is reversing a list.
- we will implement the same function using recursive techniques.

Application

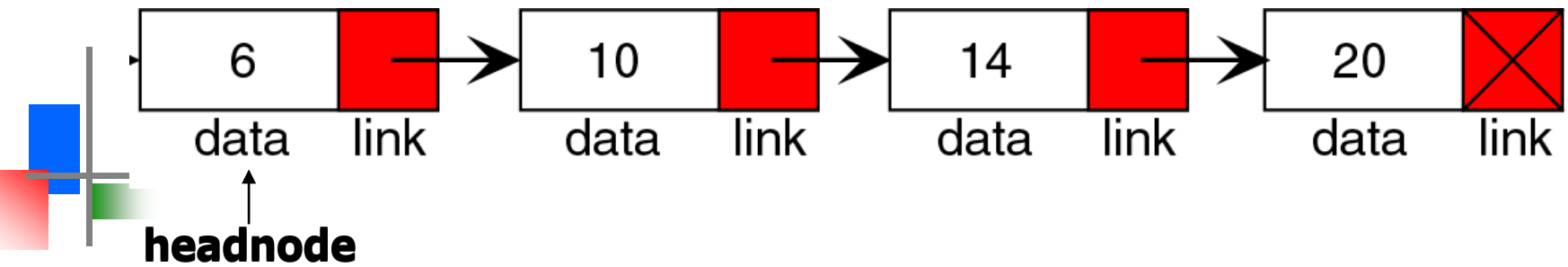
- Let's say we want to reverse the list below.
- The pseudocode to do this is shown on the next slide.





Reverse List Pseudocode

```
printReverse(list) {  
    if(null list)  
        return;  
    else  
        printReverse(list->next);  
    //Once we're here, the end of the list has  
    // been reached  
    print(list->data);  
    return;  
}
```



printReverse(6)

printReverse(10) //list->next()

`cout<<list->data();` **printReverse(14)**

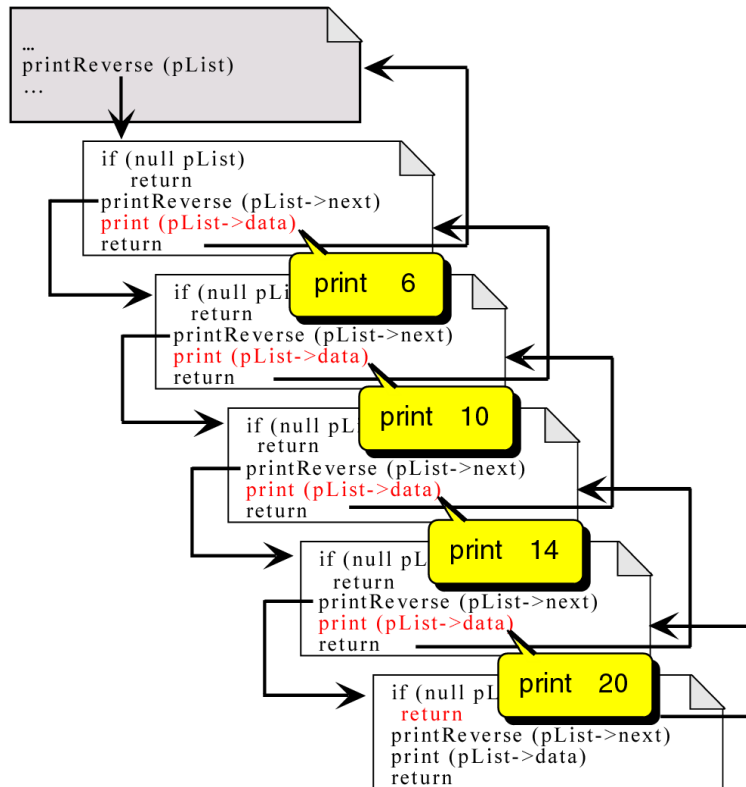
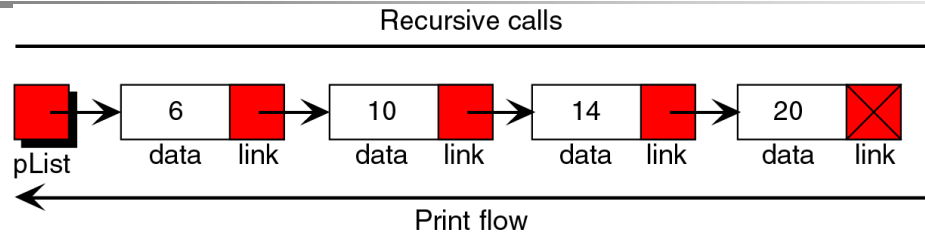
6 **10** `cout<<list->data();` **printReverse(20)**

14 `cout<<list->data();`

printReverse(null)

20 `cout<<list->data();`

Algorithm Flow





Example-Fibonacci series

- **Fibonacci Sequence**
- 0, 1, 1, 2, 3, 5, 8, 13, 21, 34,
- Each element is the sum of the two preceding elements with
 - $\text{fib}(0) = 0$
 - $\text{fib}(1) = 1$
 - $\text{fib}(n) = n$ if $n == 0$ or $n == 1$
 - $\text{fib}(n) = \text{fib}(n-2) + \text{fib}(n-1)$ if $n \geq 2$
- E.g.

Recursive Programming

- **Fibonacci Sequence (0,1,1,2,3,5,8,13,.....)**

$\text{fib}(n) = n$ if $n == 0$ or $n == 1$

$\text{fib}(n) = \text{fib}(n-2) + \text{fib}(n-1)$ if $n \geq 2$

```
int fib(int n)
```

```
{
```

```
    if(n == 0 || n == 1)
```

```
        return n;
```

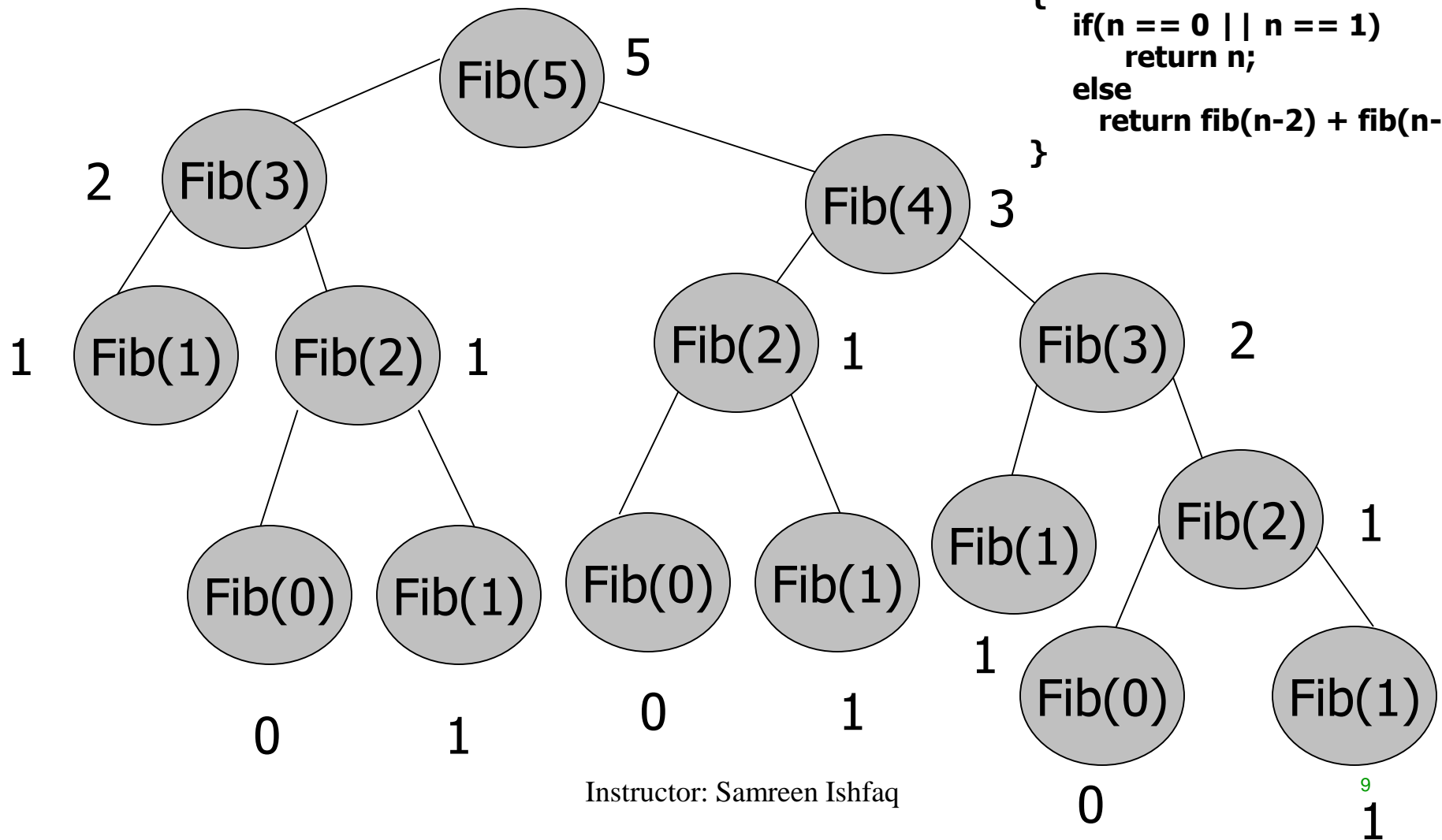
```
    else
```

```
        return fib(n-2) + fib(n-1)
```

```
}
```


Problem To Solved (Fib(5))

```
int fib(int n)
{
    if(n == 0 || n == 1)
        return n;
    else
        return fib(n-2) + fib(n-1);
}
```





Dry Run (Home Task)

- Find `fib(7)` and how many function calls were executed?



Conclusion

- A recursive solution solves a problem by solving a smaller instance of the same problem.
- It solves this new problem by solving an even smaller instance of the same problem.
- Eventually, the new problem will be so small that its solution will be either obvious or known.
- This solution will lead to the solution of the original problem.



Conclusion

- 4 questions for constructing recursive solutions:
 - How can you define the problem in terms of a smaller problem of the same type?
 - How does each recursive call diminish the size of the problem?
 - What instance of the problem can serve as the base case?
 - As the problem size diminishes, will you reach the base case?



Conclusion

- In general, there is no reason to incur the overhead of recursion when its use does not gain anything.
- Recursion is truly valuable when a problem has no simple iterative solution.



Example – Find

Home
Task

- **To find an element in an array**
- **Base case**
 - If array is empty, return false
- **Recursive step**
 - If 1st element of array is given value, return true
 - Skip 1st element and recur on remainder of array



Example – Count

Home
Task

- **To count # of elements in an array**
- **Base case**
 - **If array is empty, return 0**
- **Recursive step**
 - **Skip 1st element and recur on remainder of array**
 - **Add 1 to result**