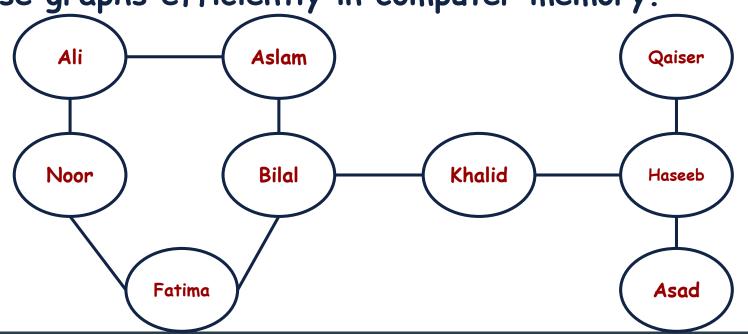


# Graphs



#### Graphs: Review

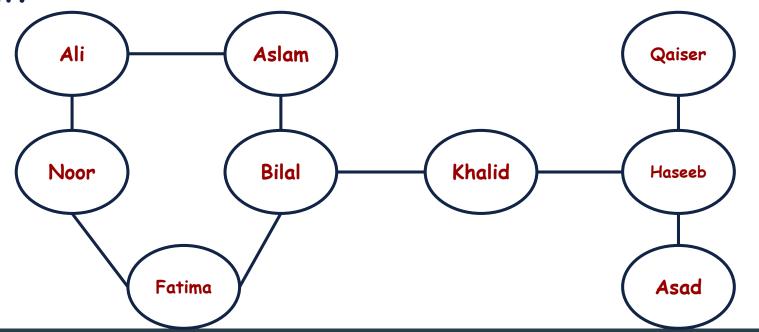
Previously, we had seen graphs and the way to store these graphs efficiently in computer memory.



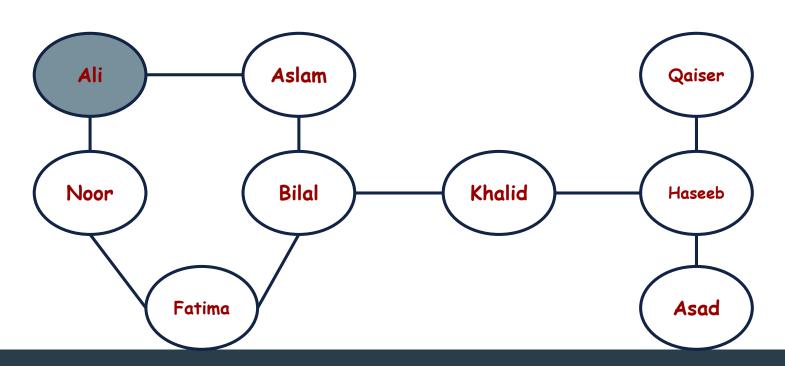
# Graphs: Implementations

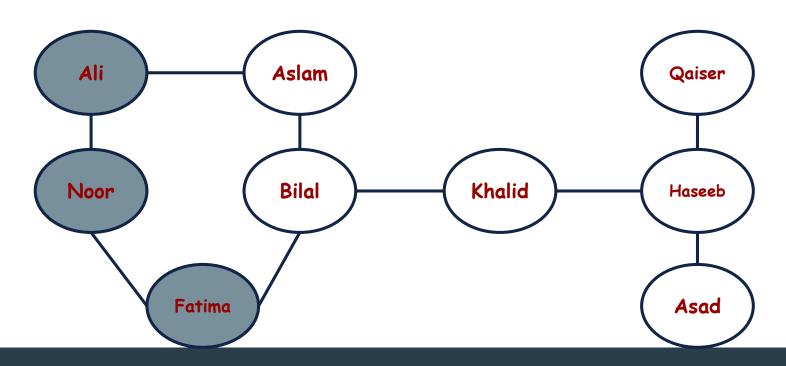
Representation	Time Complexity to find Adjacent nodes of a given node	Space Complexity
Edge List	O( E ) where E = V <sup>2</sup>	O( V  +  E )
Adjacency Matrix	O( V )	O( V  +  V  <sup>2</sup> )
Adjacency List	O(V) in case of Linked List O(1) in case of HashMaps	O( V  +  E )

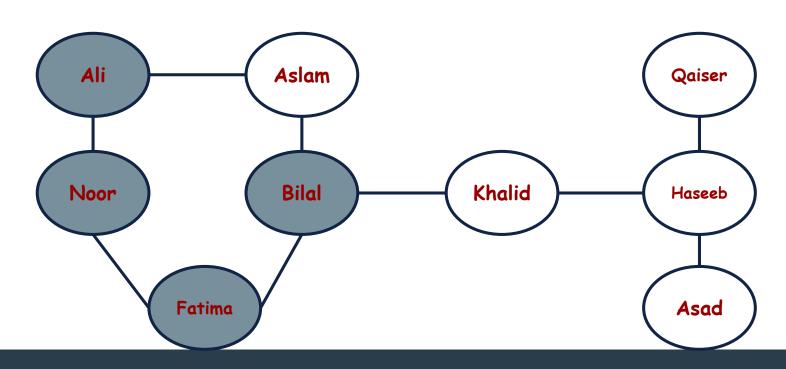
Now, we want to traverse the graph. How can we do that?

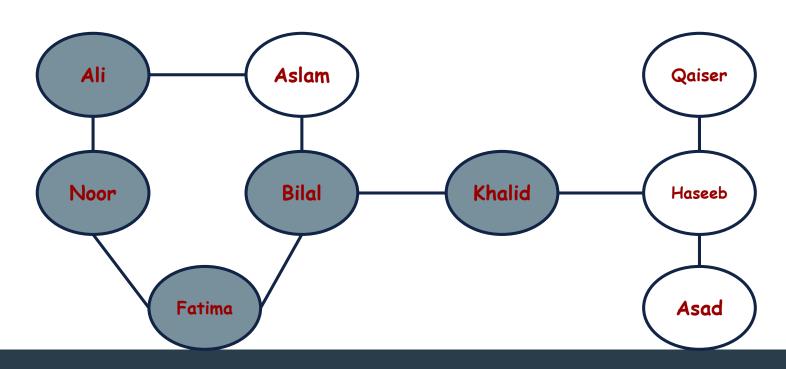


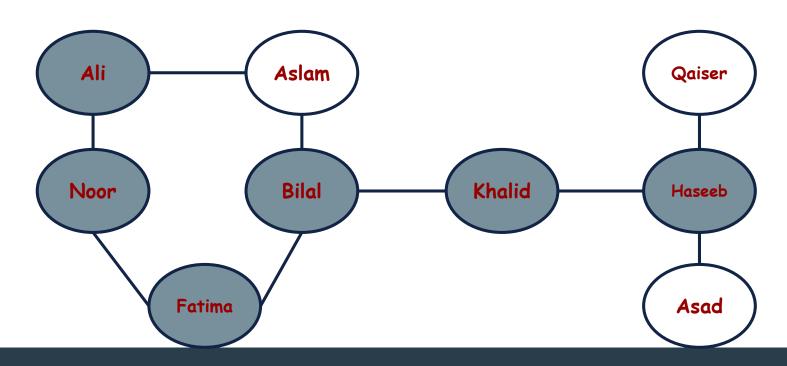
Let's say that the starting vertex is given which is Ali.

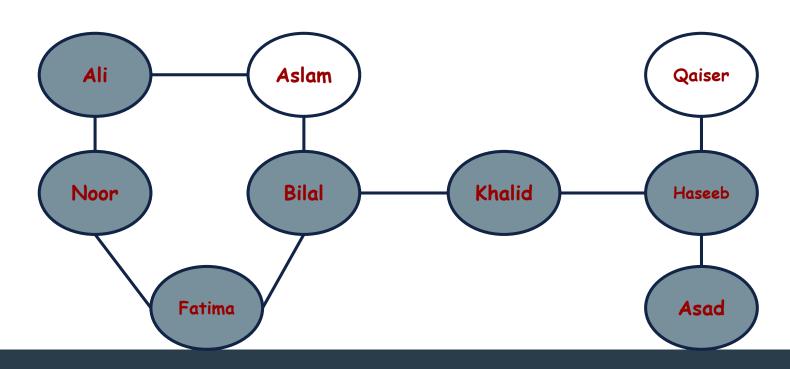




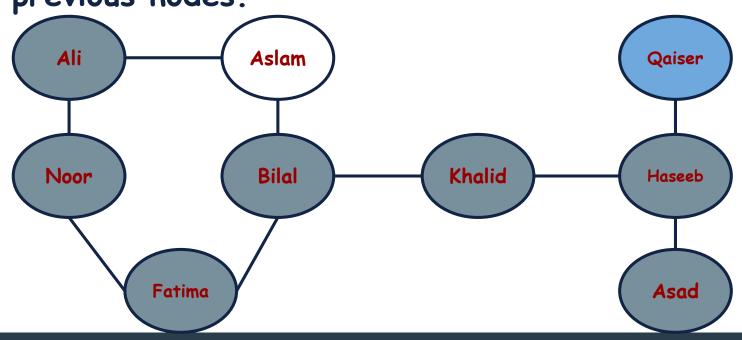




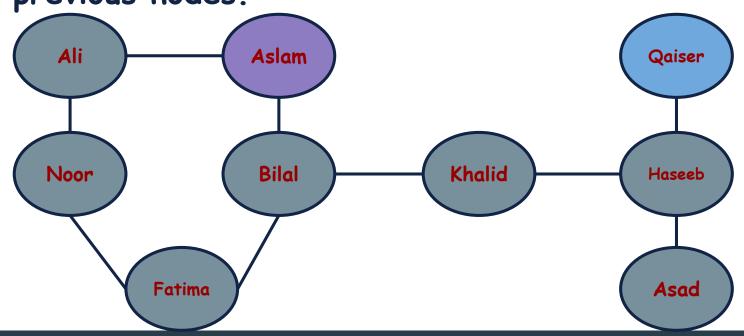




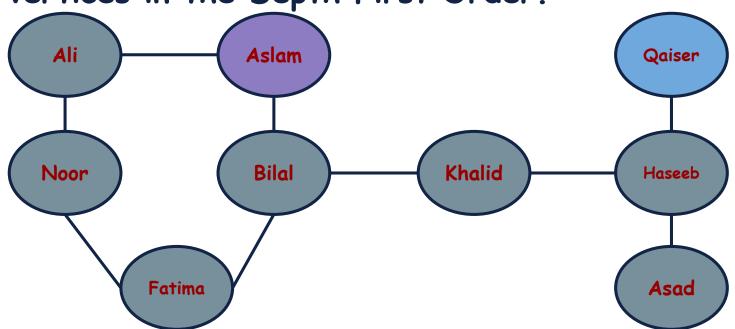
Now, we come back and traverse the remaining nodes of the previous nodes.



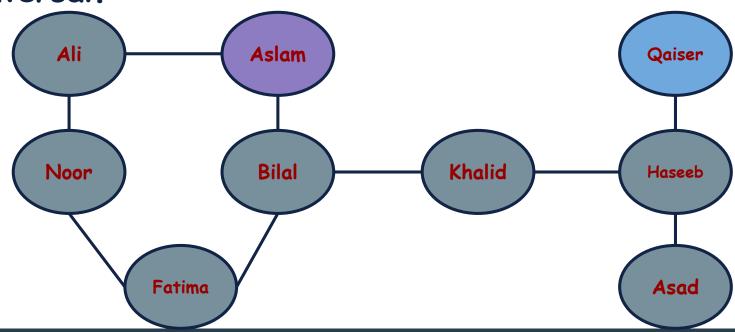
Now, we come back and traverse the remaining nodes of the previous nodes.



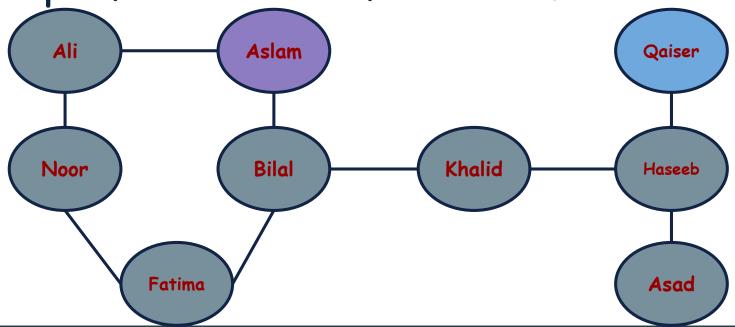
Here, the important thing to note is that we are visiting the vertices in the Depth First Order.



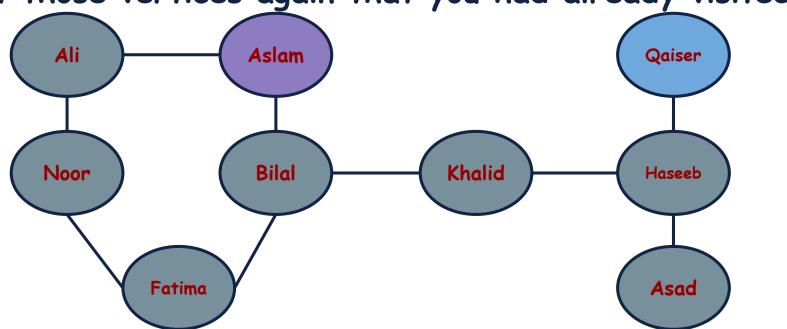
Therefore, this traversal is called as Depth First Traversal.



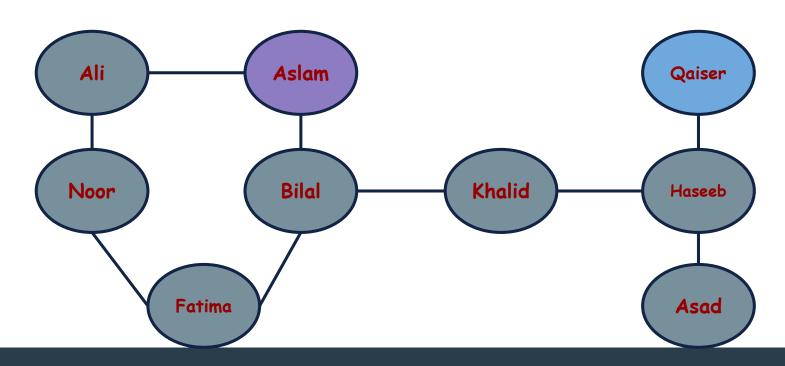
The depth first traversal algorithm of Graph is same as the depth first traversal of the Trees.



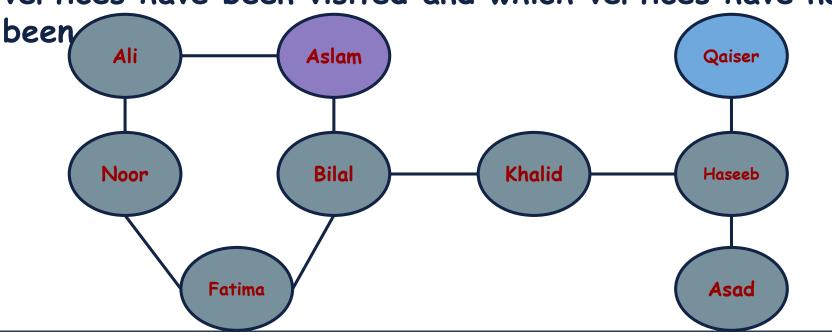
There is just one thing to make sure that you do not visit those vertices again that you had already visited.



How can you do that?



You can make an array/vector/hashmap to store which vertices have been visited and which vertices have not



Now, let's implement the depth first traversal for Graphs.

Hint: Do not forget the previous Data Structures that

we have studied before.

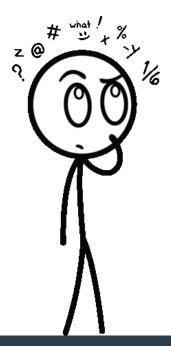


```
class Graph
{
    unordered_map<string, vector<string>> adjList;

public:
    void addEdge(string s, string d)
    {
        adjList[s].push_back(d);
        adjList[d].push_back(s);
    }
}
```

```
void DFS(string start)
    unordered map<string, bool> visited;
    stack<string> s;
    s.push(start);
    visited[start] = true;
    while (!s.empty())
        string current = s.top();
        s.pop();
        cout << current << " ";</pre>
        for (auto currentFriend : adjList.find(current)->second)
            if (visited.find(currentFriend) == visited.end())
                s.push(currentFriend);
                visited[currentFriend] = true;
```

What is the Time Complexity of this algorithm?



We know that we have traversed all the Vertices of the graph.

For Looping all the Vertices time complexity is O(|V|).

We know that we have traversed all the Vertices of the graph.

For Looping all the Vertices time complexity is O(|V|).

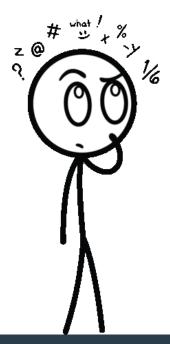
For each vertex in the HashMap we have to iterate all of its Edges.

For the undirected graph an edge is stored twice.

Therefore, for looping all the edges the time complexity is O(2|E|)

Overall Time Complexity is O(|V| + |E|).

What is the Space Complexity of this algorithm?



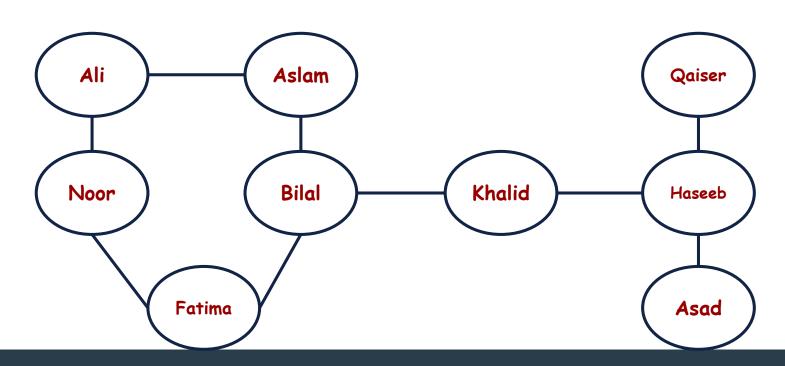
We are declaring a stack as well as the array/hashMap to store the information of visited and unvisited vertices.

Worst Space Complexity is O(|V|).

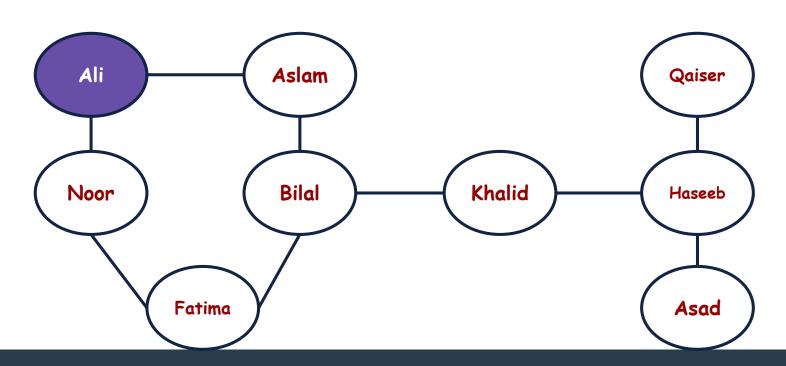
# Graphs: Traversal Algorithm

Algorithm	Time Complexity	Space Complexity
Depth First Traversal	O( V  +  E )	O( V )

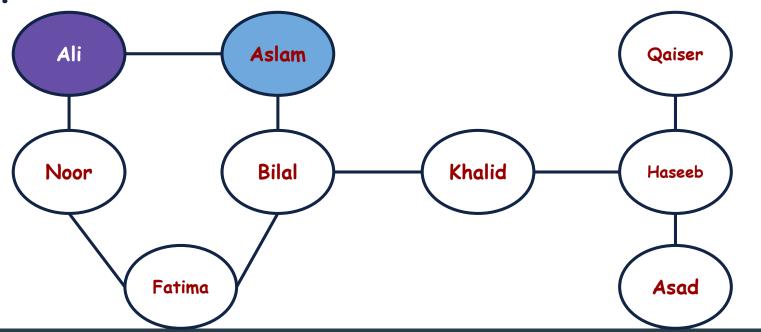
There are another way to traverse the graphs.



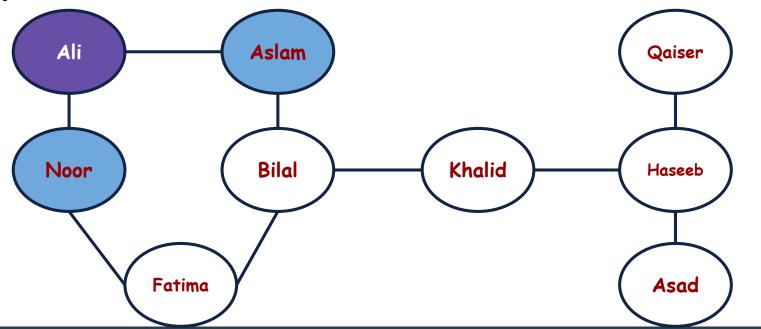
Let's say that the starting vertex is given which is Ali.

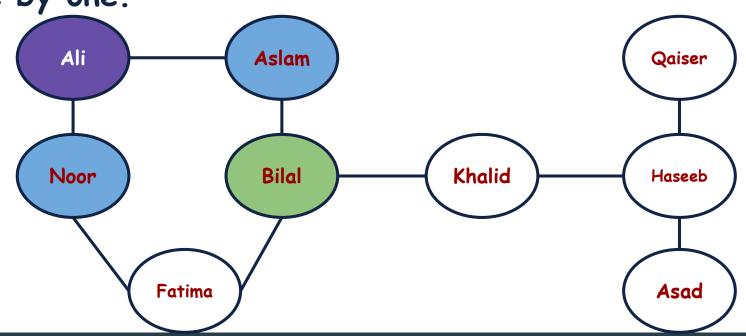


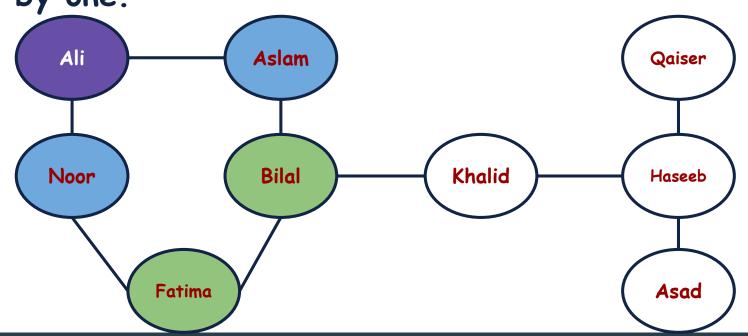
Now, first Visit all the adjacent nodes of Ali one by one.

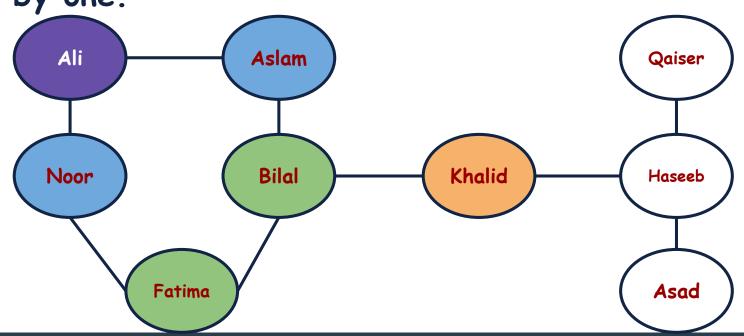


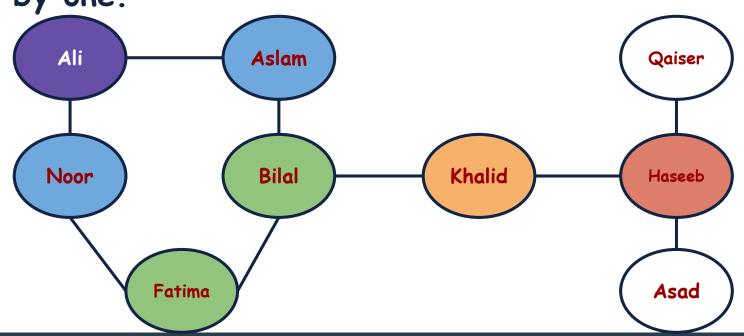
Now, first Visit all the adjacent nodes of Ali one by one.



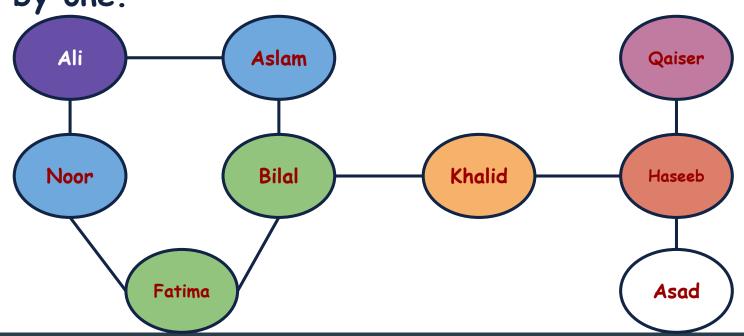




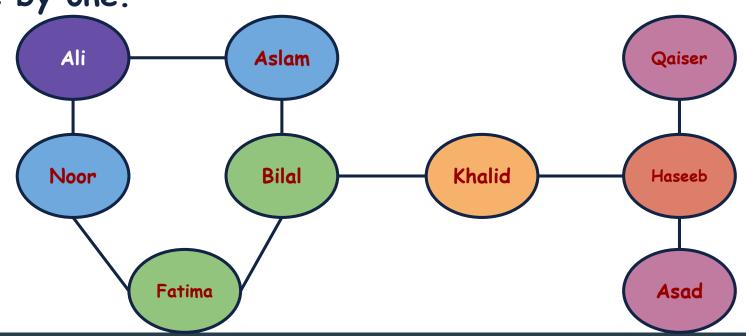




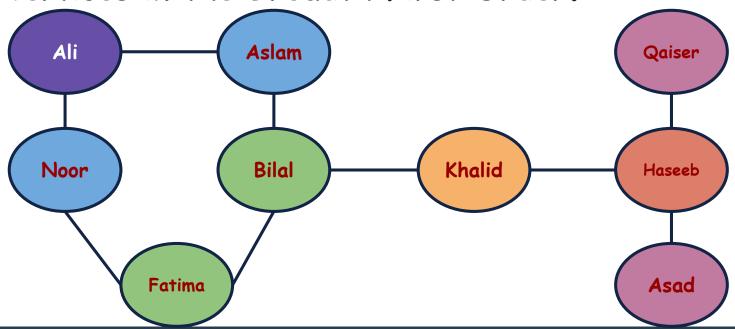
Now, Visit all the adjacent nodes of the visited nodes one by one.



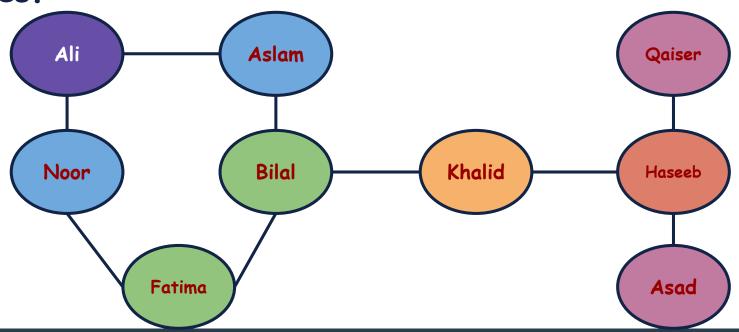
Now, Visit all the adjacent nodes of the visited nodes one by one.



Here, the important thing to note is that we are visiting the vertices in the Breadth First Order.



Again we have to keep track of the visited and unvisited nodes.



## Breadth First Traversal: Implementation

Now, let's implement the breath first traversal for Graphs.

Hint: Do not forget the previous Data Structures that we have studied before.



#### Breadth First Traversal: Implementation

```
void BFS(string start)
        unordered map<string, bool> visited;
        queue<string> q;
        q.push(start);
        visited[start] = true;
        while (!q.empty())
            string current = q.front();
            q.pop();
            cout << current << " ";</pre>
            for (auto currentFriend : adjList.find(current) ->second)
                if (visited.find(currentFriend) == visited.end())
                    q.push (currentFriend);
                    visited[currentFriend] = true;
```

## Breadth First Traversal: Implementation

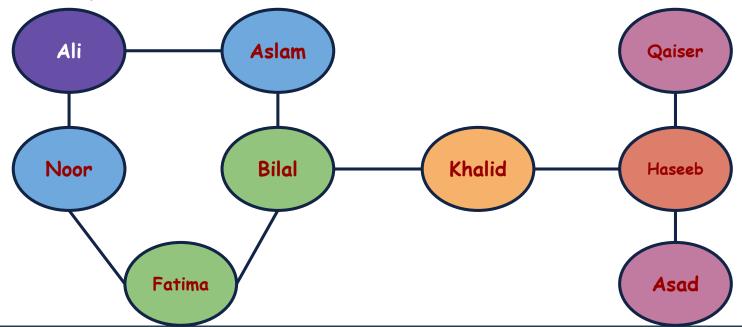
What is the Time and Space Complexity of this algorithm?



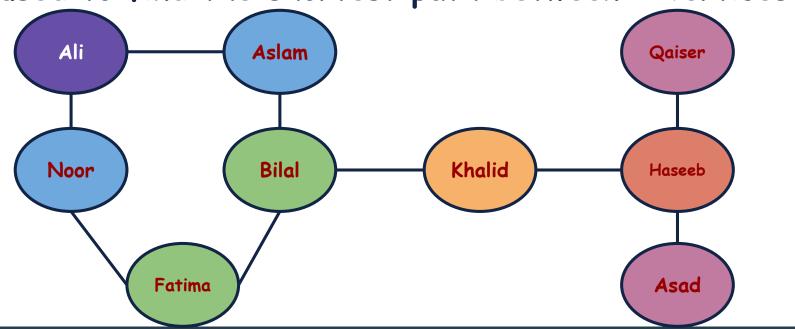
# Graphs: Traversal Algorithm

Algorithm	Time Complexity	Space Complexity
Depth First Traversal	O( V  +  E )	0( V )
Breadth First Traversal	0( V  +  E )	O( V )

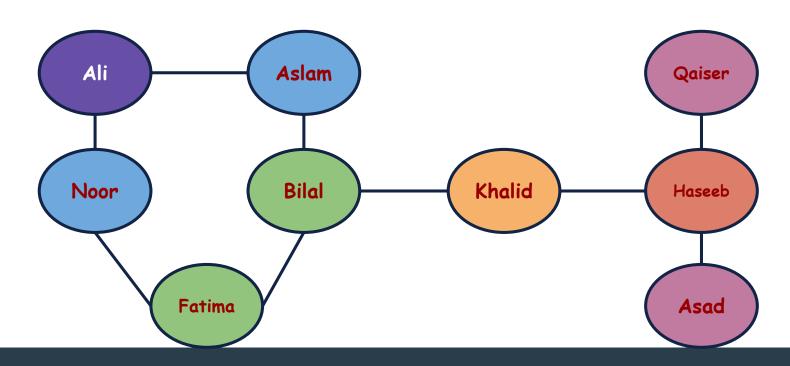
Now, i want to see what is the shortest path from Ali to Khalid. How can i do that?



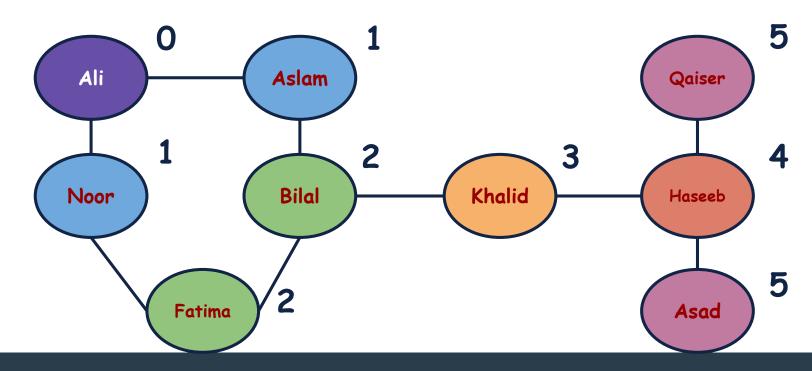
In case of undirected Graph, improvement of BFS can be used to find the shortest path between 2 vertices



Let's keep the cost to reach the next vertex.



Let's keep the cost to reach the next vertex.



#### Shortest Path (Undirected Graph): Implementation

Now, let's implement the solution.



#### Shortest Path (Undirected Graph): Implementation

```
int shortestDistance(string source, string destination) {
        unordered map<string, pair<string, int>> visited;
        queue<string> q;
        q.push(source);
        visited[source] = {"", 0};
        while (!q.empty())
            string current = q.front();
            q.pop();
            if (current == destination)
                break;
            for (auto currentFriend : adjList.find(current)->second)
                if (visited.find(currentFriend) == visited.end())
                    q.push(currentFriend);
                    visited[currentFriend] = {currentFriend, visited[current].second + 1};
        return visited[destination].second;
```

# Learning Objective

Students should be able to Traverse the graphs to solve real life problems.



#### Self Assessment

https://leetcode.com/problems/find-if-path-exists-in-graph/ https://leetcode.com/problems/keys-and-rooms/