



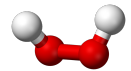


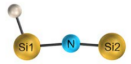



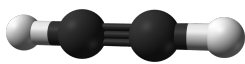
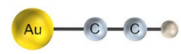
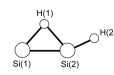



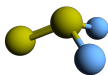




| Structure | Point group    | Graph     | Formula  | Dimensionality | Example    | Dihedrals  | Diagram   |
|-----------|----------------|-----------|----------|----------------|------------|--|---|
| 1         | $T_d$          | $K_4$     | $A_4$    | Pyramidal      | $P_4$      | $\cos^{-1} \left( \frac{1}{3} \right)$   |    |
| 2         | $C_{3v}$       | $S_3$     | $A_3B$   | Pyramidal      | $H_3N$     | $\cos^{-1} \left( \frac{\cos \theta (1 - \cos \theta)}{\sin^2 \theta} \right)$                 |    |
| 3         | $C_s$          | $S_3$     | $A_2BC$  | Pyramidal      | $Cl_2OS$   | $\cos^{-1} \left( \frac{\cos \theta - \cos^2 \varphi}{\sin^2 \varphi} \right)$                 |    |
| 4         | $D_{2h}$       | $K_4 - e$ | $A_2B_2$ | Planar         | $Cl_2Cu_2$ | 0 or 180   |    |
| 5         | $C_{2v}$       | $K_4 - e$ | $A_2B_2$ | Pyramidal      | $H_2Si_2$  | $\cos^{-1} \left( \frac{\cos \theta - \cos^2 \varphi}{\sin^2 \varphi} \right)$                 |   |
| 6         | $C_2$          | $P_4$     | $A_2B_2$ | Pyramidal      | $H_2O_2$   | $\cos^{-1} \left( \frac{\cos \theta - \cos^2 \varphi}{\sin^2 \varphi} \right)$                 |    |
| 7         | $C_1$          | $P_4$     | $A_2BC$  | Pyramidal      | $H_2OS$    | $\cos^{-1} \left( \frac{\cos \theta - \cos \varphi \cos \phi}{\sin \varphi \sin \phi} \right)$ |    |
| 8         | $D_{3h}$       | $S_3$     | $A_3B$   | Planar         | $BH_3$     | 0 or 180   |    |
| 9         | $C_s$          | $P_4$     | $A_2BC$  | Planar         | $HNSi_2$   | 0 or 180   |    |
| 10        | $D_{2h}$       | $C_4$     | $A_2B_2$ | Planar         | $Br_2Na_2$ | 0 or 180   |  |
| 11        | $C_{2v}$       | $P_4$     | $A_2B_2$ | Planar         | $O_2S_2$   | 0 or 180   |  |
| 12        | $C_{2v}$       | $S_3$     | $A_2BC$  | Planar         | $CFO_2$    | 0 or 180   |  |
| 13        | $D_{\infty h}$ | $P_4$     | $A_2B_2$ | Linear         | $C_2H_2$   | 0 or 180   |  |
| 14        | $C_{\infty v}$ | $P_4$     | $A_2BC$  | Linear         | $C_2AuH$   | 0 or 180   |  |
| 15        | $C_s$          | $T_{3,1}$ | $A_2B_2$ | Planar         | $H_2Si_2$  | 0 or 180   |  |
| 16        | $C_s$          | $S_3$     | ABCD     | Planar         | $CBrFO$    | 0 or 180   |  |
| 17        | $C_{2v}$       | $K_4 - e$ | $A_3B$   | Planar         | $C_3Si$    | 0 or 180   |  |
| 18        | $C_{2v}$       | $K_4 - e$ | $A_3B$   | Planar         | $C_3Si$    | 0 or 180   |  |

| Structure | Point group | Graph     | Formula  | Dimensionality | Example  | Dihedrals  | Diagram   |
|-----------|-------------|-----------|----------|----------------|----------|--|---|
| 19        | $C_{3v}$    | $K_4$     | $A_3B$   | Pyramidal      | $AsP_3$  |  |   |
| 20        | $C_{2h}$    | $P_4$     | $A_2B_2$ | Planar         | $H_2N_2$ |  |   |
| 21        | $C_s$       | $S_3$     | $A_2B_2$ | Pyramidal      | $S_2F_2$ | $\cos^{-1}\left(\frac{\cos\theta - \cos^2\varphi}{\sin^2\varphi}\right)$ |  |
| 22        | $C_{2v}$    | $T_{3,1}$ | $A_3B$   | Planar         | $C_3H$   | 0 or 180   |  |
| 23        | $C_{2v}$    | $C_4$     | $ABC_2$  | Planar         | $CsNO_2$ | 0 or 180   |  |

## Shape 1: $\text{P}_4$

| Information provided |                        |
|----------------------|------------------------|
| $r$                  | P-P bond length        |
| Information missing  |                        |
| $\theta$             | P-P-P bond angle       |
| $\varphi$            | P-P-P-P dihedral angle |

Since all faces of a regular tetrahedron are equilateral triangles,  $\theta = 60^\circ$ . The dihedral angles  $\varphi$  in a regular tetrahedron are given by  $\cos^{-1}(\frac{1}{3})$ . We therefore have the following z-matrix:

|   |   |     |   |            |   |           |
|---|---|-----|---|------------|---|-----------|
| P |   |     |   |            |   |           |
| P | 1 | $r$ |   |            |   |           |
| P | 1 | $r$ | 2 | $\theta_3$ |   |           |
| P | 1 | $r$ | 2 | $\theta_3$ | 3 | $\varphi$ |

## Shape 2: $\text{NH}_3$

| Information provided |   |
|----------------------|---|
| $r_1$                | N-H bond length                                 |
| $\theta_1$           | H-N-H bond angle                                |
| Information missing  |   |
| $r_2$                | H-H distance                                    |
| $\theta_2$           | H-H-H bond angle                                |
| $\theta_3$           | H-H-N bond angle                                |
| $\varphi_i$          | Dihedral angles between various pairs of planes |

Since the three H atoms form an equilateral triangle,  $\theta_2 = 60^\circ$ . Also, (at least some of) the dihedral angles  $\varphi$  are given by the following simplified form for the dihedral law of cosines:

$$\varphi = \cos^{-1} \left( \frac{\cos \theta (1 - \cos \theta)}{\sin^2 \theta} \right). \quad (1)$$

We therefore have the following z-matrix:

|   |   |       |   |            |   |           |
|---|---|-------|---|------------|---|-----------|
| N |   |       |   |            |   |           |
| H | 1 | $r_1$ |   |            |   |           |
| H | 1 | $r_1$ | 2 | $\theta_1$ |   |           |
| H | 1 | $r_1$ | 2 | $\theta_1$ | 3 | $\varphi$ |

### Shape 3: Cl<sub>2</sub>OS

| Information provided |   |
|----------------------|---|
| $r_1$                | S-O bond length                                       |
| $r_2$                | S-Cl bond length                                      |
| $\theta_1$           | Cl-S-O bond angle                                     |
| $\theta_2$           | Cl-S-Cl bond angle                                    |
| $\varphi$            | Cl-S-O-Cl dihedral angle                              |
| Information missing  |   |
| $r_3$                | Cl-O distance   |
| $\theta_3$           |   |
| $\theta_4$           |   |
| $\theta_5$           |   |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

They gave the dihedral angle but didn't need to, because it's exactly what we would get from the dihedral law of cosines.

The missing geometric information is provided below:

$$r_3 = \sqrt{r_1^2 + r_2^2 - 2 \cos \theta_1} \quad (2)$$

### Shape 4: Cl<sub>2</sub>Cu<sub>2</sub>

We need to first undersatnd why one pair of atoms has a dashed line between them and the other pair does not.

| Information provided |   |
|----------------------|---|
| $r_1$                |   |
| $\theta_1$           |   |
| Information missing  |   |
| $r_2$                |   |
| $\theta_2$           |   |
| $\varphi_i$          | Dihedral angles between various pairs of planes |

We therefore have the following z-matrix:

|   |   |       |   |            |   |           |  |
|---|---|-------|---|------------|---|-----------|--|
| N |   |       |   |            |   |           |  |
| H | 1 | $r_2$ |   |            |   |           |  |
| H | 1 | $r_2$ | 2 | $\theta_1$ |   |           |  |
| H | 1 | $r_2$ | 2 | $\theta_1$ | 3 | $\varphi$ |  |

## Shape 5: H<sub>2</sub>Si<sub>2</sub>

| Information provided |   |
|----------------------|---|
| $r_1$                | Si-Si bond length                                     |
| $r_2$                | Si-H bond length                                      |
| $\varphi$            | Dihedral angle between two Si-Si-H planes             |
| Information missing  |   |
| $r_3$                | H-H distance  |
| $\theta_1$           | H-Si-H bond angle                                     |
| $\theta_2$           | Si-H-Si bond angle                                    |
| $\theta_3$           | Si-Si-H bond angle                                    |
| $\theta_4$           | H-H-Si angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

For a z-matrix, in addition to the information provided we would need *at least* one planar angle, despite none being provided from the experimental paper. The missing geometric information can be provided based on the information provided from the experimental paper though:

$$r_3 = \sin \frac{\varphi}{2} \sqrt{4r_2^2 - r_1^2}, \quad (3)$$

$$\theta_1 = \cos^{-1} \left( \frac{\cos \varphi (4r_1^2 - r_2^2) + r_2^2}{4r_1^2} \right), \quad (4)$$

$$\theta_2 = \cos^{-1} \left( 1 - \frac{1}{2} \left( \frac{r_1}{r_2} \right)^2 \right), \quad (5)$$

$$\theta_3 = \cos^{-1} \left( \frac{r_1}{2r_2} \right), \quad (6)$$

$$\theta_4 = \frac{\pi - \theta_1}{2}. \quad (7)$$

An alternative formula for  $\theta_1$  is:

$$\theta_1 = \sin^{-1} \left( \frac{\sin \left( \frac{\varphi}{2} \right) \sqrt{4r_2^2 - r_1^2}}{r_2} \right). \quad (8)$$

For the first column of the z-matrix, we have 6 possibilities which are listed below along with the possible planar angles that could be used for each of these possibilities:

| 1  |   | 2  |   | 3  |   | 4  |   | 5  |   | 6  |   |
|----|---|----|---|----|---|----|---|----|---|----|---|
| Si | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_3</math><br/> <math>\theta_1, \theta_3, \theta_4</math> </div> | Si | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_3, \theta_2</math><br/> <math>\theta_1, \theta_3, \theta_4</math> </div> | Si | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_1, \theta_4</math><br/> <math>\theta_2, \theta_3, \theta_4</math> </div> | H  | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_2, \theta_3</math><br/> <math>\theta_1, \theta_3, \theta_4</math> </div> | H  | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_1, \theta_4</math><br/> <math>\theta_2, \theta_3, \theta_4</math> </div> | H  | <div style="border: 1px solid black; padding: 5px; display: inline-block;"> <math>\theta_4</math><br/> <math>\theta_2, \theta_3, \theta_4</math> </div> |
| Si |   | H  |   | H  |   | Si |   | Si |   | H  |   |
| H  |   | Si |   | H  |   | Si |   | H  |   | Si |   |
| H  |   | H  |   | Si |   | H  |   | Si |   | Si |   |

This means that if we know  $\theta_3$  or  $\theta_4$  then we have enough to complete the planar angles column of the z-matrix, but if we only know  $\theta_1$  or  $\theta_2$ , we would need to determine two of the angles rather than one. Since  $\theta_3$  is a “bond angle” in the original reference and  $\theta_4$  is not, we will present a formula for  $\theta_3$ :

We can now write a z-matrix. Since the first option in the above table will lead to usage of  $r_1$  and  $r_2$  in lexicographical order (these bond angles are presented as they were in Landolt-Bornstein), we will use that option:

|    |   |       |   |            |   |          |  |
|----|---|-------|---|------------|---|----------|--|
| Si |   |       |   |            |   |          |  |
| Si | 1 | $r_1$ |   |            |   |          |  |
| H  | 1 | $r_2$ | 2 | $\theta_3$ |   |          |  |
| H  | 1 | $r_3$ | 2 | $\theta_3$ | 3 | Dihedral |  |

## Shape 6: H<sub>2</sub>O<sub>2</sub>

| Information provided |   |
|----------------------|---|
| $r_1$                | H-O bond length                                 |
| $r_2$                | O-O bond length                                 |
| $\theta_1$           | H-O-O bond angle                                |
| $\varphi$            | H-O-O-H dihedral angle                          |
| Information missing  |   |
| $r_3$                | H...H distance                                  |
| $r_4$                | O...H distance                                  |
| $\theta_2$           | H-H-B bond angle                                |
| $\theta_3$           | H-H-H angle                                     |
| $\varphi_i$          | Dihedral angles between various pairs of planes |

We therefore have the following z-matrix:

|   |   |       |   |            |   |           |  |
|---|---|-------|---|------------|---|-----------|--|
| O |   |       |   |            |   |           |  |
| O | 1 | $r_2$ |   |            |   |           |  |
| H | 1 | $r_1$ | 2 | $\theta_1$ |   |           |  |
| H | 2 | $r_1$ | 1 | $\theta_1$ | 3 | $\varphi$ |  |

## Shape 7: H<sub>2</sub>OS

Peilin's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | H-O bond length                                 |
| $r_2$                | O-S bond length                                 |
| $r_3$                | S-H bond length                                 |
| $\theta_1$           | H-O-S bond angle                                |
| $\theta_2$           | H-S-O bond angle                                |
| $\varphi$            | H-O-S-H dihedral angle                          |
| Information missing  |   |
| $r_4$                | H...H distance                                  |
| $r_5$                | H...O distance                                  |
| $r_6$                | H...S distance                                  |
| $\theta_3$           | H...H-O angle                                   |
| $\theta_4$           | H...H...O angle                                 |
| $\theta_5$           | H-O...H angle                                   |
| $\theta_6$           | H...O-S angle                                   |
| $\theta_7$           | H-S...H angle                                   |
| $\theta_8$           | H...S-O angle                                   |
| $\varphi_i$          | Dihedral angles between various pairs of planes |

We therefore have the following z-matrix:

|   |   |       |   |            |   |           |  |
|---|---|-------|---|------------|---|-----------|--|
| B |   |       |   |            |   |           |  |
| H | 1 | $r_1$ |   |            |   |           |  |
| H | 1 | $r_1$ | 2 | $\theta_1$ |   |           |  |
| H | 1 | $r_1$ | 2 | $\theta_1$ | 3 | $\varphi$ |  |

## Shape 8: BH<sub>3</sub>

Hemanth's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | B-H bond length                                 |
| Information missing  |   |
| $r_2$                | H-H distance                                    |
| $\theta_1$           | H-B-H bond angle                                |
| $\theta_2$           | H-H-B bond angle                                |
| $\theta_3$           | H-H-H angle                                     |
| $\varphi_i$          | Dihedral angles between various pairs of planes |

Since the three H atoms form an equilateral triangle,  $\theta_3 = 60^\circ$ .

We therefore have the following z-matrix:

|   |   |       |   |            |   |           |  |
|---|---|-------|---|------------|---|-----------|--|
| B |   |       |   |            |   |           |  |
| H | 1 | $r_1$ |   |            |   |           |  |
| H | 1 | $r_1$ | 2 | $\theta_1$ |   |           |  |
| H | 1 | $r_1$ | 2 | $\theta_1$ | 3 | $\varphi$ |  |

## Shape 9: HNSi<sub>2</sub>

Mia finished this but still needs to type it in LaTeX.

| Information provided |   |
|----------------------|---|
| $r_1$                | H-Si bond length                                      |
| $r_2$                | Si-N bond length                                      |
| $r_3$                | N-Si bond length                                      |
| $\theta_1$           | Si-N-Si bond angle                                    |
| $\theta_2$           | H-Si-N bond angle                                     |
| Information missing  |   |
| $r_4$                | N...H distance  |
| $r_5$                | Si...Si distance                                      |
| $r_6$                | Si...H distance                                       |
| $\theta_3$           | N=Si...Si angle                                       |
| $\theta_4$           | H...Si...Si angle                                     |
| $\theta_5$           | H-Si...Si angle                                       |
| $\theta_6$           | H...Si-N angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Mia):

But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |  |
|----|---|-------|---|------------|---|-----------|--|
| Si |   |       |   |            |   |           |  |
| N  | 1 | $r_1$ |   |            |   |           |  |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |  |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |  |

## Shape 10: Br<sub>2</sub>Na<sub>2</sub>

Abdul's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | Br-Na bond length                                     |
| $\theta_1$           | Br-Na-Br bond angle                                   |
| Information missing  |   |
| $r_2$                | Br...Br distance                                      |
| $r_3$                | Na...Na distance                                      |
| $\theta_1$           | Br...Br-Na angle                                      |
| $\theta_2$           | Br-Na...Na angle                                      |
| $\theta_3$           | Na-Br-Na angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Abdul):  
But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 11: O<sub>2</sub>S<sub>2</sub>

Abdul's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | O-S bond length                                       |
| $r_2$                | S-S bond length                                       |
| $\theta_1$           | O-S-S bond angle                                      |
| Information missing  |   |
| $r_3$                | O...O distance  |
| $r_4$                | O...S distance  |
| $\theta_2$           | O...O-S angle   |
| $\theta_3$           | O...O...S angle                                       |
| $\theta_4$           | O-S...O angle   |
| $\theta_5$           | O...S-S angle   |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Abdul):  
But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 12: CBrO<sub>2</sub>

Hemanth's molecule



| Information provided |   |
|----------------------|---|
| $r_1$                | C-Cl bond length                                      |
| $r_2$                | C=O bond length                                       |
| $\theta_1$           | Cl-C-Cl bond angle                                    |
| Information missing  |   |
| $r_3$                | Cl...Cl distance                                      |
| $r_4$                | Cl...O distance                                       |
| $\theta_2$           | C-Cl...Cl angle                                       |
| $\theta_3$           | C-Cl...O angle  |
| $\theta_4$           | C-O...Cl angle  |
| $\theta_5$           | Cl-C...O angle  |
| $\theta_6$           | Cl...Cl...O angle                                     |
| $\theta_7$           | Cl...O-C angle  |
| $\theta_8$           | Cl...O...Cl angle                                     |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information:

$$r_3 = \sqrt{2r_1^2 - 2r_1^2 \cos \theta_1}, \quad (9)$$

$$r_4 = \sqrt{r_1^2 + r_2^2 - 2r_1 r_2 \cos \theta_2}, \quad (10)$$

$$\theta_2 = \quad (11)$$

But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 13: C<sub>2</sub>H<sub>2</sub>

Aimun's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | H-Si bond length                                      |
| $r_2$                | Si-N bond length                                      |
| $r_3$                | N-Si bond length                                      |
| $\theta_1$           | Si-N-Si bond angle                                    |
| $\theta_2$           | H-Si-N bond angle                                     |
| Information missing  |   |
| $r_4$                | N...H distance  |
| $r_5$                | Si...Si distance                                      |
| $r_6$                | Si...H distance                                       |
| $\theta_3$           | N=Si...Si angle                                       |
| $\theta_4$           | H...Si...Si angle                                     |
| $\theta_5$           | H-Si...Si angle                                       |
| $\theta_6$           | H...Si-N angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Mia):

But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 15: $\text{H}_2\text{Si}_2$

Justin's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | Si-Si bond length                                     |
| $r_2$                | Si-N bond length                                      |
| $r_3$                | N-Si bond length                                      |
| $\theta_1$           | Si-N-Si bond angle                                    |
| $\theta_2$           | H-Si-N bond angle                                     |
| Information missing  |   |
| $r_4$                | N...H distance  |
| $r_5$                | Si...Si distance                                      |
| $r_6$                | Si...H distance                                       |
| $\theta_3$           | N=Si...Si angle                                       |
| $\theta_4$           | H...Si...Si angle                                     |
| $\theta_5$           | H-Si...Si angle                                       |
| $\theta_6$           | H...Si-N angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Mia):  
But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 16: $\text{CBrFO}$

Hemanth's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | C-F bond length                                       |
| $r_2$                | C=O bond length                                       |
| $\theta_1$           | Si-N-Si bond angle                                    |
| $\theta_2$           | H-Si-N bond angle                                     |
| Information missing  |   |
| $r_4$                | N...H distance  |
| $r_5$                | Si...Si distance                                      |
| $r_6$                | Si...H distance                                       |
| $\theta_3$           | N=Si...Si angle                                       |
| $\theta_4$           | H...Si...Si angle                                     |
| $\theta_5$           | H-Si...Si angle                                       |
| $\theta_6$           | H...Si-N angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Mia):  
But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 17: C<sub>3</sub>Si

Sam's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | C(1)-C(2) bond length                                 |
| $r_2$                | C(2)-C(2)' bond length                                |
| $r_3$                | C(2)-Si bond length                                   |
| Information missing  |   |
| $r_4$                | C(1)...Si distance                                    |
| $\theta_1$           | C(2)-C(1)-C(2)', angle                                |
| $\theta_2$           | C(1)-C(2)-C(2)', angle                                |
| $\theta_3$           | Si-C(2)-C(2)', angle                                  |
| $\theta_4$           | C(2)-Si-C(2)', angle                                  |
| $\theta_5$           | Si-C(2)-C(1) angle                                    |
| $\theta_6$           | Si...C(1)-C(2) angle                                  |
| $\theta_7$           | C(1)...Si-C(2) angle                                  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information:

$$r_4 = r_3 \sqrt{1 - \frac{r_2^2}{4r_3^2}} + r_1 \sqrt{1 - \frac{r_2^2}{4r_1^2}} \quad (12)$$

$$\theta_1 = \arccos \left( 1 - \frac{r_2^2}{2r_1^2} \right) \quad (13)$$

$$\theta_2 = \arccos \left( \frac{r_2}{2r_1} \right) \quad (14)$$

$$\theta_3 = \arccos \left( \frac{r_2}{2r_3} \right) \quad (15)$$

$$\theta_4 = \arccos \left( 1 - \frac{r_2^2}{2r_3^2} \right) \quad (16)$$

$$\theta_5 = \arccos \left( \frac{r_2}{2r_1} \right) + \arccos \left( \frac{r_2}{2r_3} \right) \quad (17)$$

$$\theta_6 = \frac{1}{2} \arccos \left( 1 - \frac{r_2^2}{2r_1^2} \right) \quad (18)$$

$$\theta_7 = \frac{1}{2} \arccos \left( 1 - \frac{r_2^2}{2r_3^2} \right) \quad (19)$$

The z-matrix can be constructed as shown using both calculated and originally provided information:

|       |   |       |   |            |   |           |
|-------|---|-------|---|------------|---|-----------|
| C(1)  |   |       |   |            |   |           |
| C(2)  | 1 | $r_1$ |   |            |   |           |
| C(2)' | 2 | $r_2$ | 1 | $\theta_2$ |   |           |
| Si    | 3 | $r_3$ | 2 | $\theta_3$ | 1 | $\varphi$ |

# Shape 18: C<sub>3</sub>Si

Sam's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | C(1)-C(2) bond length                                 |
| $r_2$                | Si-C(2) bond length                                   |
| $r_3$                | Si-C(1) bond length                                   |
| Information missing  |   |
| $r_4$                | C(1)...C(1)' distance                                 |
| $\theta_1$           | C(1)...C(1)'-C(2) angle                               |
| $\theta_2$           | C(1)-C(2)-C(1)' angle                                 |
| $\theta_3$           | C(1)-C(2)-Si angle                                    |
| $\theta_4$           | Si-C(1)-C(2) angle                                    |
| $\theta_5$           | C(1)-Si-C(2) angle                                    |
| $\theta_6$           | C(1)-Si-C(1)' angle                                   |
| $\theta_7$           | C(1)...C(1)'-Si angle                                 |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information:

$$r_4 = 2r_1 \cos \left( 90 - \arccos \left( \frac{r_1^2 + r_2^2 - r_3^2}{2r_1 r_2} \right) \right) \quad (20)$$

$$\theta_1 = 90 - \arccos \left( \frac{r_1^2 + r_2^2 - r_3^2}{2r_1 r_2} \right) \quad (21)$$

$$\theta_2 = 2 \arccos \left( \frac{r_1^2 + r_2^2 - r_3^2}{2r_1 r_2} \right) \quad (22)$$

$$\theta_3 = \arccos \left( \frac{r_1^2 + r_2^2 - r_3^2}{2r_1 r_2} \right) \quad (23)$$

$$\theta_4 = \arccos \left( \frac{r_1^2 + r_3^2 - r_2^2}{2r_1 r_3} \right) \quad (24)$$

$$\theta_5 = \arccos \left( \frac{r_2^2 + r_3^2 - r_1^2}{2r_2 r_3} \right) \quad (25)$$

$$\theta_6 = 2 \arccos \left( \frac{r_2^2 + r_3^2 - r_1^2}{2r_2 r_3} \right) \quad (26)$$

$$\theta_7 = 90 - \arccos \left( \frac{r_2^2 + r_3^2 - r_1^2}{2r_2 r_3} \right) \quad (27)$$

The z-matrix can be constructed as shown using both calculated and originally provided information:

|       |   |       |   |            |   |           |
|-------|---|-------|---|------------|---|-----------|
| C(1)  |   |       |   |            |   |           |
| C(2)  | 1 | $r_1$ |   |            |   |           |
| C(1)' | 2 | $r_1$ | 1 | $\theta_2$ |   |           |
| Si    | 3 | $r_3$ | 2 | $\theta_4$ | 1 | $\varphi$ |

## Shape 19: AsP<sub>3</sub>

Sichao's molecule

| Information provided |  |
|----------------------|--|
| $r_1$                | As-P bond length                                       |
| $r_2$                | P-P bond length  |
| Information missing  |  |
| $\theta_1$           | P-As-P angles  |
| $\theta_2$           | As-P-P angle   |
| $\theta_3$           | P-P-P angle  |
| $\varphi_1$          | Dihedral angle between $AsP_2$ plane and $AsP_2$ plane |
| $\varphi_2$          | Dihedral angle between $AsP_2$ plane and $P_3$ plane   |

We have the following expressions for the missing geometric information:

$$\begin{aligned}\theta_1 &= \cos^{-1} \left( \frac{2r_1^2 - r_2^2}{2r_1^2} \right) \\ \theta_2 &= \frac{180 - \theta_1}{2} \\ \theta_3 &= 60 \\ \varphi_1 &= \cos^{-1} \left( \frac{\cos \theta_1 (1 - \cos \theta_1)}{\sin^2 \theta_1} \right) \\ \varphi_2 &= \cos^{-1} \left( \frac{\cot \theta_2}{\sqrt{3}} \right)\end{aligned}$$

We are able to construct the z-matrix using just the information on  $r_1, \theta_1$  and  $\varphi_1$ :

|           |   |       |   |            |   |             |  |
|-----------|---|-------|---|------------|---|-------------|--|
| <b>As</b> |   |       |   |            |   |             |  |
| P         | 1 | $r_1$ |   |            |   |             |  |
| P         | 1 | $r_1$ | 2 | $\theta_1$ |   |             |  |
| P         | 1 | $r_1$ | 2 | $\theta_1$ | 3 | $\varphi_1$ |  |

## Shape 20: H<sub>2</sub>N<sub>2</sub>

Justin's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | H-Si bond length                                      |
| $r_2$                | Si-N bond length                                      |
| $r_3$                | N-Si bond length                                      |
| $\theta_1$           | Si-N-Si bond angle                                    |
| $\theta_2$           | H-Si-N bond angle                                     |
| Information missing  |   |
| $r_4$                | N...H distance  |
| $r_5$                | Si...Si distance                                      |
| $r_6$                | Si...H distance                                       |
| $\theta_3$           | N=Si...Si angle                                       |
| $\theta_4$           | H...Si...Si angle                                     |
| $\theta_5$           | H-Si...Si angle                                       |
| $\theta_6$           | H...Si-N angle  |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information (waiting for Mia):  
But we can make the z-matrix with only information given to us originally:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Si |   |       |   |            |   |           |
| N  | 1 | $r_1$ |   |            |   |           |
| Si | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H  | 3 | $r_3$ | 2 | $\theta_2$ | 1 | $\varphi$ |

## Shape 21: S<sub>2</sub>F<sub>2</sub>

Sam's molecule

| Information provided |  |
|----------------------|--|
| $r_1$                | F-S bond length                                      |
| $r_2$                | S=S bond length                                      |
| $\theta_1$           | F-S-F bond angle                                     |
| $\theta_2$           | F-S=S bond angle                                     |
| Information missing  |  |
| $r_3$                | F...F distance                                       |
| $r_4$                | F...S distance                                       |
| $\theta_3$           | S-F...F angle  |
| $\theta_4$           | S...F...F angle                                      |
| $\theta_5$           | S...F-S angle  |
| $\theta_6$           | F...S=S angle  |
| $\varphi_1$          | Dihedral angle between $S_2F$ plane and $S_2F$ plane |
| $\varphi_2$          | Dihedral angle between $SF_2$ plane and $S_2F$ plane |

We have the following expressions for the missing geometric information:

$$r_3 = r_1 \sqrt{2(1 - \cos \theta_1)} \quad (28)$$

$$r_4 = \sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos \theta_2} \quad (29)$$

$$\theta_3 = \frac{180 - \theta_1}{2} \quad (30)$$

$$\theta_4 = \arccos \left( r_1 \sqrt{\frac{1 - \cos \theta_1}{2(r_1^2 + r_2^2 - 2r_1r_2 \cos \theta_2)}} \right) \quad (31)$$

$$\theta_5 = \arccos \left( \frac{r_1 - r_2 \cos \theta_2}{\sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos \theta_2}} \right) \quad (32)$$

$$\theta_6 = \arccos \left( \frac{r_2 - r_1 \cos \theta_2}{\sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos \theta_2}} \right) \quad (33)$$

$$\varphi_1 = \arccos \left( \frac{\cos \theta_1 - \cos^2 \theta_2}{\sin^2 \theta_2} \right) \quad (34)$$

$$\varphi_2 = \arccos \left( \frac{\cos \theta_2 (1 - \cos \theta_1)}{\sin \theta_1 \sin \theta_2} \right) \quad (35)$$

The z-matrix can be constructed as shown using both calculated and originally provided information:

|   |   |       |   |            |   |             |
|---|---|-------|---|------------|---|-------------|
| F |   |       |   |            |   |             |
| S | 1 | $r_1$ |   |            |   |             |
| S | 2 | $r_2$ | 1 | $\theta_2$ |   |             |
| F | 2 | $r_1$ | 3 | $\theta_2$ | 1 | $\varphi_1$ |

## Shape 22: C<sub>3</sub>H

Sam's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | C $\equiv$ C bond length                              |
| $r_2$                | C-C bond length                                       |
| $r_3$                | C-H bond length                                       |
| Information missing  |   |
| $r_4$                | C...H distance  |
| $\theta_1$           | C $\equiv$ C-C bond angle                             |
| $\theta_2$           | C-C-C bond angle                                      |
| $\theta_3$           | C-C-H bond angle                                      |
| $\theta_4$           | C $\equiv$ C...H angle                                |
| $\theta_5$           | C-C...H angle   |
| $\theta_6$           | C-H...C angle   |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information:

$$r_4 = \sqrt{r_2^2 + r_3^2 - 2r_2r_3 \cos\left(90 + \arccos\left(\frac{r_1}{2r_2}\right)\right)} \quad (36)$$

$$\theta_1 = \arccos\left(\frac{r_1}{2r_2}\right) \quad (37)$$

$$\theta_2 = 180 - 2 \arccos\left(\frac{r_1}{2r_2}\right) \quad (38)$$

$$\theta_3 = 90 + \arccos\left(\frac{r_1}{2r_2}\right) \quad (39)$$

$$\theta_4 = \arccos\left(\frac{r_1}{2\sqrt{r_2^2 + r_3^2 - 2r_2r_3 \cos\left(90 + \arccos\left(\frac{r_1}{2r_2}\right)\right)}}\right) \quad (40)$$

$$\theta_5 = \arccos\left(\frac{r_1}{2\sqrt{r_2^2 + r_3^2 - 2r_2r_3 \cos\left(90 + \arccos\left(\frac{r_1}{2r_2}\right)\right)}}\right) - \arccos\left(\frac{r_1}{2r_2}\right) \quad (41)$$

$$\theta_6 = \arcsin\left(\frac{r_1}{2\sqrt{r_2^2 + r_3^2 - 2r_2r_3 \cos\left(90 + \arccos\left(\frac{r_1}{2r_2}\right)\right)}}\right) \quad (42)$$

The z-matrix can be constructed as shown using both calculated and originally provided information:

|   |   |       |   |            |   |           |
|---|---|-------|---|------------|---|-----------|
| C |   |       |   |            |   |           |
| C | 1 | $r_1$ |   |            |   |           |
| C | 2 | $r_2$ | 1 | $\theta_1$ |   |           |
| H | 3 | $r_3$ | 2 | $\theta_3$ | 1 | $\varphi$ |

## Shape 23: CsNO<sub>2</sub>

Sam's molecule

| Information provided |   |
|----------------------|---|
| $r_1$                | Cs-O bond length                                      |
| $r_2$                | O-N bond length                                       |
| $\theta_1$           | O-N-O bond angle                                      |
| Information missing  |   |
| $r_3$                | Cs...N distance                                       |
| $r_4$                | O...NO distance                                       |
| $\theta_2$           | Cs-O-N bond angle                                     |
| $\theta_3$           | O-Cs-O bond angle                                     |
| $\theta_4$           | Cs...N-O angle  |
| $\theta_5$           | Cs-O...O angle  |
| $\theta_6$           | N...Cs-O angle  |
| $\theta_7$           | O...O-N angle   |
| $\varphi_i$          | Dihedral angles between various other pairs of planes |

We have the following expressions for the missing geometric information:

$$r_3 = \sqrt{r_1^2 + r_2^2 - 2r_1r_2 \cos \left( \frac{180 - \theta_1}{2} + \arccos \left( \frac{r_2}{2r_1} \sqrt{2(1 - \cos \theta_1)} \right) \right)} \quad (43)$$

$$r_4 = r_2 \sqrt{2(1 - \cos \theta_1)} \quad (44)$$

$$\theta_2 = \frac{180 - \theta_1}{2} + \arccos \left( \frac{r_2}{2r_1} \sqrt{2(1 - \cos \theta_1)} \right) \quad (45)$$

$$\theta_3 = 2 \arcsin \left( \frac{r_2}{2r_1} \sqrt{2(1 - \cos \theta_1)} \right) \quad (46)$$

$$\theta_4 = \frac{\theta_1}{2} \quad (47)$$

$$\theta_5 = \arccos \left( \frac{r_2}{2r_1} \sqrt{2(1 - \cos \theta_1)} \right) \quad (48)$$

$$\theta_6 = \arcsin \left( \frac{r_2}{2r_1} \sqrt{2(1 - \cos \theta_1)} \right) \quad (49)$$

$$\theta_7 = \frac{180 - \theta_1}{2} \quad (50)$$

The z-matrix can be constructed as shown using both calculated and originally provided information:

|    |   |       |   |            |   |           |
|----|---|-------|---|------------|---|-----------|
| Cs |   |       |   |            |   |           |
| O  | 1 | $r_1$ |   |            |   |           |
| N  | 2 | $r_2$ | 1 | $\theta_2$ |   |           |
| O  | 3 | $r_2$ | 2 | $\theta_1$ | 1 | $\varphi$ |