Structure	Point group	Graph	Formula	Dimensionality	Example	Dihedrals	Diagram
1	$T_d$	$K_4$	${ m A}_4$	Pyramidal	$P_4$	$\cos^{-1}\left(\frac{1}{3}\right)$	
2	$C_{3v}$	$S_3$	$A_3B$	Pyramidal	${ m H_3N}$	$\cos^{-1}\left(\frac{\cos\theta(1-\cos\theta)}{\sin^2\theta}\right)$	
3	$C_s$	$S_3$	$A_2BC$	Pyramidal	$\mathrm{Cl_2OS}$	$\cos^{-1}\left(\frac{\cos\theta - \cos^2\varphi}{\sin^2\varphi}\right)$	
4	$D_{2h}$	$K_4 - e$	$A_2B_2$	Planar	$\mathrm{Cl_2Cu_2}$	0 or 180	cu Ci Cu
5	$C_{2v}$	$K_4 - e$	$A_2B_2$	Pyramidal	$\mathrm{H_2Si_2}$	$\cos^{-1}\left(\frac{\cos\theta - \cos^2\varphi}{\sin^2\varphi}\right)$	
6	$C_2$	$P_4$	$A_2B_2$	Pyramidal	$\mathrm{H_2O_2}$	$\cos^{-1}\left(\frac{\cos\theta - \cos^2\varphi}{\sin^2\varphi}\right)$	
7	$C_1$	$P_4$	$A_2BC$	Pyramidal	${ m H_2OS}$	$\cos^{-1}\left(\frac{\cos\theta - \cos\varphi\cos\phi}{\sin\varphi\sin\phi}\right)$	<b>§</b> — <b>®</b>
8	$D_{3h}$	$S_3$	$A_3B$	Planar	$\mathrm{BH}_3$	0 or 180	
9	$C_s$	$P_4$	$A_2BC$	Planar	$\mathrm{HNSi}_2$	0 or 180	SI1 — N— (52
10	$D_{2h}$	$C_4$	$A_2B_2$	Planar	$\mathrm{Br_2Na_2}$	0 or 180	
11	$C_{2v}$	$P_4$	$A_2B_2$	Planar	$O_2S_2$	0 or 180	
12	$C_{2v}$	$S_3$	$A_2BC$	Planar	$CFO_2$	0 or 180	
13	$D_{\infty h}$	$P_4$	$A_2B_2$	Linear	$C_2H_2$	0 or 180	
14	$C_{\infty v}$	$P_4$	$A_2BC$	Linear	$\mathrm{C}_2\mathrm{AuH}$	0 or 180	Au C C
15	$C_s$	$T_{3,1}$	$A_2B_2$	Planar	$\mathrm{H_2Si_2}$	0 or 180	H(1) (H(2) (S(2) (
16	$C_s$	$S_3$	ABCD	Planar	CBrFO	0 or 180	FOO GR
17	$C_{2v}$	$K_4 - e$	$A_3B$	Planar	$C_3Si$	0 or 180	
18	$C_{2v}$	$K_4 - e$	$A_3B$	Planar	$C_3Si$	0 or 180	s C(1)

Structure	Point group	Graph	Formula	Dimensionality	Example	Dihedrals	Diagram
19	$C_{3v}$	$K_4$	$A_3B$	Pyramidal	$\mathrm{AsP}_3$		
20	$C_{2h}$	$P_4$	$A_2B_2$	Planar	$\mathrm{H_2N_2}$		

### Shape 1: $P_4$

Information provided
P-P bond length

Information missing

 $\begin{array}{ll} \theta & \text{P-P-P bond angle} \\ \varphi & \text{P-P-P-P dihedral angle} \end{array}$ 

Since all faces of a regular tetrahedron are equilateral triangles,  $\theta = 60^{\circ}$ . The dihedral angles  $\varphi$  in a regular tetrahedron are given by  $\cos^{-1}\left(\frac{1}{3}\right)$ . We therefore have the following z-matrix:

 $\begin{array}{|c|c|c|c|c|c|c|} \hline P & & & & & \\ P & 1 & r & & & \\ P & 1 & r & 2 & \theta_3 & & \\ P & 1 & r & 2 & \theta_3 & 3 & \varphi \\ \hline \end{array}$ 

## Shape 2: NH<sub>3</sub>

Information provided

 $r_1$  N-H bond length

 $\theta_1$  H-N-H bond angle

Information missing

 $r_2$  H-H distance

 $\theta_2$  H-H-H bond angle

 $\theta_3$  H-H-N bond angle

 $\varphi_i$  Dihedral angles between various pairs of planes

Since the three H atoms form an equilateral triangle,  $\theta_2 = 60^{\circ}$ . Also, (at least some of) the dihedral angles  $\varphi$  are given by the following simplified form for the dihedral law of cosines:

$$\varphi = \cos^{-1} \left( \frac{\cos \theta \left( 1 - \cos \theta \right)}{\sin^2 \theta} \right). \tag{1}$$

We therefore have the following z-matrix:

## Shape 3: Cl<sub>2</sub>OS

	Information provided						
$r_1$	S-O bond length						
$r_2$	S-Cl bond length						
$ heta_1$	Cl-S-O bond angle						
$\theta_2$	Cl-S-Cl bond angle						
$\varphi$	Cl-S-O-Cl dihedral angle						
Information missing							
$r_3$	Cl-O distance						
$\theta_3$							
$\theta_4$							
$\theta_5$							
$\varphi_i$	Dihedral angles between various other pairs of planes						

They gave the dihedral angle but didn't need to, because it's exactly what we would get from the dihedral law of cosines. The missing geometric information is provided below:

$$r_3 = \sqrt{r_1^2 + r_2^2 - 2\cos\theta_1} \tag{2}$$

# Shape 4: Cl<sub>2</sub>Cu<sub>2</sub>

We need to first undersated why one pair of atoms has a dashed line between them and the other pair does not.

	Information provided
$r_1 \\ \theta_1$	
	Information missing
$r_2 \\ \theta_2 \\ \varphi_i$	Dihedral angles between various pairs of planes

We therefore have the following z-matrix:

### Shape 5: $H_2Si_2$

T f 1 :	
Information	provided

- $r_1$  Si-Si bond length
- $r_2$  Si-H bond length
- $\varphi$  Dihedral angle between two Si-Si-H planes

#### Information missing

 $r_3$  H-H distance

 $\theta_1$  H-Si-H bond angle

 $\theta_2$  Si-H-Si bond angle

 $\theta_3$  Si-Si-H bond angle

 $\theta_4$  H-H-Si angle

 $\varphi_i$  Dihedral angles between various other pairs of planes

For a z-matrix, in addition to the information provided we would need at least one planar angle, despite none being provided from the experimental paper. The missing geometric information can be provided based on the information provided from the experimental paper though:

$$r_3 = \sin\frac{\varphi}{2}\sqrt{4r_2^2 - r_1^2},\tag{3}$$

$$\theta_1 = \cos^{-1} \left( \frac{\cos \varphi \left( 4r_1^2 - r_2^2 \right) + r_2^2}{4r_1^2} \right),\tag{4}$$

$$\theta_2 = \cos^{-1}\left(1 - \frac{1}{2}\left(\frac{r_1}{r_2}\right)^2\right),\tag{5}$$

$$\theta_3 = \cos^{-1}\left(\frac{r_1}{2r_2}\right),\tag{6}$$

$$\theta_4 = \frac{\pi - \theta_1}{2}.\tag{7}$$

An alternative formula for  $\theta_1$  is:

$$\theta_1 = \sin^{-1}\left(\frac{\sin\left(\frac{\varphi}{2}\right)\sqrt{4r_2^2 - r_1^2}}{r_2}\right). \tag{8}$$

For the first column of the z-matrix, we have 6 possibilities which are listed below along with the possible planar angles that could be used for each of these possibilities:

This means that if we know  $\theta_3$  or  $\theta_4$  then we have enough to complete the planar angles column of the z-matrix, but if we only know  $\theta_1$  or  $\theta_2$ , we would need to determine two of the angles rather than one. Since  $\theta_3$  is a "bond angle" in the original reference and  $\theta_4$  is not, we will present a formula for  $\theta_3$ :

We can now write a z-matrix. Since the first option in the above table will lead to usage of  $r_1$  and  $r_2$  in lexicographical order (these bond angles are presented as they were in Landolt-Bornstein), we will use that option:

$$\begin{array}{|c|c|c|c|c|c|c|c|c|} \hline \text{Si} & & & & & \\ \text{Si} & 1 & r_1 & & & \\ \text{H} & 1 & r_2 & 2 & \theta_3 & \\ \text{H} & 1 & r_3 & 2 & \theta_3 & 3 & \text{Dihedral} \\ \hline \end{array}$$

## Shape 6: $H_2O_2$

#### Information provided

- H-O bond length  $r_1$
- O-O bond length  $r_2$
- H-O-O bond angle  $\theta_1$
- H-O-O-H dihedral angle

#### Information missing

- H...H distance  $r_3$
- O...H distance  $r_4$
- $\theta_2$ H-H-B bond angle
- H-H-H angle  $\theta_3$
- Dihedral angles between various pairs of planes

We therefore have the following z-matrix:

### Shape 7: $H_2OS$

Peilin's molecule

#### Information provided

- H-O bond length  $r_1$
- O-S bond length  $r_2$
- S-H bond length  $r_3$
- H-O-S bond angle  $\theta_1$
- H-S-O bond angle
- H-O-S-H dihedral angle  $\varphi$

#### Information missing

- H...H distance  $r_4$
- H...O distance  $r_5$
- H...S distance  $r_6$
- H...H-O angle  $\theta_3$
- $\theta_4$ H...H...O angle
- $\theta_5$ H-O...H angle  $\theta_6$ H...O-S angle
- H-S...H angle  $\theta_7$
- $\theta_8$  $\operatorname{H...S-O}$  angle
- Dihedral angles between various pairs of planes  $\varphi_i$

We therefore have the following z-matrix:

$$\begin{bmatrix} \mathsf{B} \\ \mathsf{H} & 1 & r_1 \\ \mathsf{H} & 1 & r_1 & 2 & \theta_1 \\ \mathsf{H} & 1 & r_1 & 2 & \theta_1 & 3 & \varphi \\ \end{bmatrix}$$

## Shape 8: BH<sub>3</sub>

Hemanth's molecule

	Information provided
$r_1$	B-H bond length
	Information missing
$egin{array}{c} r_2 \  heta_1 \  heta_2 \  heta_1 \end{array}$	H-H distance H-B-H bond angle H-H-B bond angle H-H-H angle
$\theta_3$ $\varphi_i$	Dihedral angles between various pairs of planes

Since the three H atoms form an equilateral triangle,  $\theta_3=60^\circ$ . We therefore have the following z-matrix:

## Shape 9: HNSi<sub>2</sub>

Mia finished this but still needs to type it in LaTeX.

	Information provided						
$r_1$	H-Si bond length						
$r_2$	Si-N bond length						
$r_3$	N-Si bond length						
$ heta_1$	Si-N-Si bond angle						
$\theta_2$	H-Si-N bond angle						
	Information missing						
$r_4$	NH distance						
$r_5$	SiSi distance						
$r_6$	SiH distance						
$\theta_3$	N=SiSi angle						
$ heta_4$	HSiSi angle						
$\theta_5$	H-SiSi angle						
$\theta_6$	HSi-N angle						
$\varphi_i$	Dihedral angles between various other pairs of planes						

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

## Shape 10: $Br_2Na_2$

Abdul's molecule

	Information provided
$r_1 \\ \theta_1$	Br-Na bond length Br-Na-Br bond angle
	Information missing

- $r_2$  Br...Br distance
- $r_3$  Na...Na distance
- $\theta_1$  Br...Br-Na angle
- $\theta_2$  Br-Na...Na angle
- $\theta_3$  Na-Br-Na angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Abdul): But we can make the z-matrix with only information given to us originally:

Si						
N	1	$r_1$				
Si	2	$r_2$	1	$ heta_1$		
Н	3	$r_3$	2	$\theta_2$	1	$\varphi$

## Shape 11: $O_2S_2$

Abdul's molecule

#### Information provided

- $r_1$  O-S bond length
- $r_2$  S-S bond length
- $\theta_1$  O-S-S bond angle

#### Information missing

- $r_3$  O...O distance
- $r_4$  O...S distance
- $\theta_2$  O...O-S angle
- $\theta_3$  O...O...S angle
- $\theta_4$  O-S...O angle
- $\theta_5$  O...S-S angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Abdul): But we can make the z-matrix with only information given to us originally:

## Shape 12: $CBrO_2$

Hemanth's molecule

Information	provided
THO DIMAGNOTI	provided

- $r_1$  C-Cl bond length
- $r_2$  C=O bond length
- $\theta_1$  Cl-C-Cl bond angle

#### Information missing

- $r_3$  Cl...Cl distance
- $r_4$  Cl...O distance
- $\theta_2$  C-Cl...Cl angle
- $\theta_3$  C-Cl...O angle
- $\theta_4$  C-O...Cl angle
- $\theta_5$  Cl-C...O angle
- $\theta_6$  Cl...Cl...O angle
- $\theta_7$  Cl...O-C angle
- $\theta_8$  Cl...O...Cl angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information:

$$r_3 = \sqrt{2r_1^2 - 2r_1^2 \cos \theta_1},\tag{9}$$

$$r_4 = \sqrt{r_1^2 + r_2^2 - 2r_1r_2\cos\theta_2},\tag{10}$$

$$_{2} = \tag{11}$$

But we can make the z-matrix with only information given to us originally:

$$\begin{array}{|c|c|c|c|c|c|c|c|c|} \hline \text{Si} & & & & & \\ \text{N} & 1 & r_1 & & & \\ \text{Si} & 2 & r_2 & 1 & \theta_1 & & \\ \text{H} & 3 & r_3 & 2 & \theta_2 & 1 & \varphi \\ \hline \end{array}$$

# Shape 13: $C_2H_2$

Aimun's molecule

#### Information provided

- $r_1$  H-Si bond length
- $r_2$  Si-N bond length
- $r_3$  N-Si bond length
- $\theta_1$  Si-N-Si bond angle
- $\theta_2$  H-Si-N bond angle

#### Information missing

- $r_4$  N...H distance
- $r_5$  Si...Si distance
- $r_6$  Si...H distance
- $\theta_3$  N=Si...Si angle
- $\theta_4$  H...Si...Si angle
- $\theta_5$  H-Si...Si angle
- $\theta_6$  H...Si-N angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

Si						
N	1	$r_1$				
Si	2	$r_2$	1	$ heta_1$		
Н	3	$r_3$	2	$\theta_2$	1	$\varphi$

### Shape 15: $H_2Si_2$

Justin's molecule

#### Information provided

- $r_1$  Si-Si bond length
- $r_2$  Si-N bond length
- $r_3$  N-Si bond length
- $\theta_1$  Si-N-Si bond angle
- $\theta_2$  H-Si-N bond angle

#### Information missing

- $r_4$  N...H distance
- $r_5$  Si...Si distance
- $r_6$  Si...H distance
- $\theta_3$  N=Si...Si angle
- $\theta_4$  H...Si...Si angle
- $\theta_5$  H-Si...Si angle
- $\theta_6$  H...Si-N angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

## Shape 16: CBrFO

Hemanth's molecule

#### Information provided

- $r_1$  C-F bond length
- $r_2$  C=O bond length
- $\theta_1$  Si-N-Si bond angle
- $\theta_2$  H-Si-N bond angle

#### Information missing

- $r_4$  N...H distance
- $r_5$  Si...Si distance
- $r_6$  Si...H distance
- $\theta_3$  N=Si...Si angle
- $\theta_4$  H...Si...Si angle
- $\theta_5$  H-Si...Si angle
- $\theta_6$  H...Si-N angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

Si						
N	1	$r_1$				
Si	2	$r_2$	1	$ heta_1$		
Н	3	$r_3$	2	$\theta_2$	1	$\varphi$

## Shape 17: C<sub>3</sub>Si

Sam's molecule

T f 4 :	
Information	provided

- $r_1$  H-Si bond length
- $r_2$  Si-N bond length
- $r_3$  N-Si bond length
- $\theta_1$  Si-N-Si bond angle
- $\theta_2$  H-Si-N bond angle

#### Information missing

- $r_4$  N...H distance
- $r_5$  Si...Si distance
- $r_6$  Si...H distance
- $\theta_3$  N=Si...Si angle
- $\theta_4$  H...Si...Si angle
- $\theta_5$  H-Si...Si angle
- $\theta_6$  H...Si-N angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

## Shape 18: C<sub>3</sub>Si

Sam's molecule

#### Information provided

- $r_1$  H-Si bond length
- $r_2$  Si-N bond length
- $r_3$  N-Si bond length
- $\theta_1$  Si-N-Si bond angle
- $\theta_2$  H-Si-N bond angle

#### Information missing

- $r_4$  N...H distance
- $r_5$  Si...Si distance
- $r_6$  Si...H distance
- $\theta_3$  N=Si...Si angle
- $\theta_4$  H...Si...Si angle
- $\theta_5$  H-Si...Si angle
- $\theta_6$  H...Si-N angle
- $\varphi_i$  Dihedral angles between various other pairs of planes

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

## Shape 19: AsP<sub>3</sub>

Sichao's molecule

Information provided							
$r_1$	H-Si bond length						
$r_2$	Si-N bond length						
$r_3$	N-Si bond length						
$ heta_1$	Si-N-Si bond angle						
$\theta_2$	H-Si-N bond angle						
Information missing							
$r_4$	NH distance						
$r_5$	SiSi distance						
$r_6$	SiH distance						
$\theta_3$	N=SiSi angle						
$ heta_4$	HSiSi angle						
$\theta_5$	H-SiSi angle						
$\theta_6$	HSi-N angle						
$\varphi_i$	Dihedral angles between various other pairs of planes						

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

# Shape 20: $H_2N_2$

Justin's molecule

Information provided							
$r_1$	H-Si bond length						
$r_2$	Si-N bond length						
$r_3$	N-Si bond length						
$ heta_1$	Si-N-Si bond angle						
$\theta_2$	H-Si-N bond angle						
Information missing							
$r_4$	NH distance						
$r_5$	SiSi distance						
$r_6$	SiH distance						
$\theta_3$	N=SiSi angle						
$\theta_4$	HSiSi angle						
$\theta_5$	H-SiSi angle						
$\theta_6$	HSi-N angle						
$\varphi_i$	Dihedral angles between various other pairs of planes						

We have the following expressions for the missing geometric information (waiting for Mia): But we can make the z-matrix with only information given to us originally:

Si						
N	1	$r_1$				
Si	2	$r_2$	1	$ heta_1$		
Н	3	$r_3$	2	$\theta_2$	1	$\varphi$