

## # Quick Sort:

Arr[] = {5, 4, 3, 2, 1}

There is a concept of 'pivot' in Quick Sort which acts as a reference point.

### \* pivot:

Choose any element as a reference.  $\rightarrow$  after first pass all the elements " $<$ " (less than pivot) will be on the left hand side of pivot and the elements greater than pivot will be on the right side.

### (\*) Recursive Quick Sort:

arr = {5, 4, 3, 2, 1}

p = 4 (pivot)

$\downarrow$   
[1, 3, 2, 4, 5]  $\xrightarrow{\text{1st pass}}$  may or may not be sorted

$\rightarrow$  After every pass we put pivot at the correct position.

recursion will call the LHS and RHS of pivot.

$\swarrow$   
1, 3, 2

$\searrow$  [5]  $\rightarrow$  sorted.

[1, 2, 3]  $\swarrow$  pivot = 3



In merge sort, even when the array get sorted the recursive call checks until the base condition but in QuickSort, that doesn't happen

(\*) Here, we will have void return type as we are not creating new array, we are sorting the existing array.

(\*) How to put pivot ?

(s) (p) (e)  
 [ 5 , 4 , 3 , 2 , 1 ]

we make a condition for the pivot and if any elements violates it, we change its position.

(s,p) (e)  
 ( 1 , 4 , 3 , 2 , 5 )

[ 1 , 2 , 3 , 4 , 5 ]  
 (s,e)

↳ (condition met)

(\*) Checking Violation :

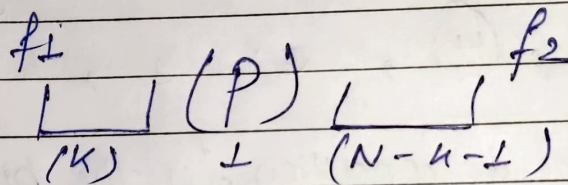
→ while  $n[s] < p$  :  
 // keep moving forward.  
 $s++$ ;  
 → while  $n[e] > p$  :  
 $e--$ ;



(\*) The idea is to put pivot( $p$ ) in its correct position.

- Pick a random element as pivot. Or,
- Corner elements. Or
- Pick the middle elements.

(\*) Recursive relation of this approach is that we are dividing the approach with two function calls



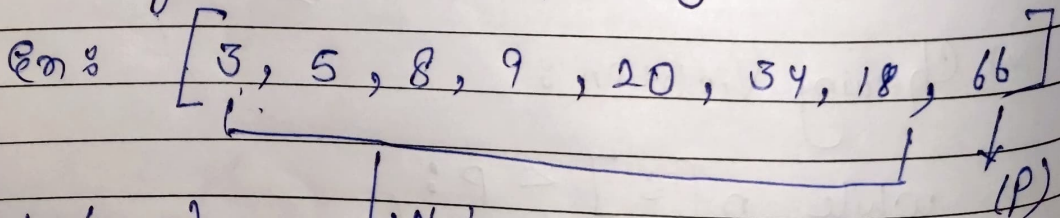
Total elements =  $N$

$$\rightarrow T(N) = T(k) + T(N-k-1) + O(N) \quad \text{for pivot}$$

↳ Recurrence relation of Quick Sort.

→ Worst Case :

If the pivot element is either smallest or largest element in an array.



when  $k=0$ ,

$$\begin{aligned}
 T(N) &= T(0) + T(N-1) + O(N) \\
 &= O(N^2)
 \end{aligned}$$



→ Best Case <sup>3</sup>

Pivot is in the middle of element  
 $k = N/2$

$$T(N) = T\left(\frac{N}{2}\right) + T\left(\frac{N}{2}\right) + O(N)$$

$$T(N) = 2T\left(\frac{N}{2}\right) + O(N)$$

$$= O(N \log N) \quad \left[ \text{Through Akra-Bazzi formula} \right]$$

(\*) Notes :

→ Not Stable

→ Merge Sort is better in linked list due to memory allocations. → not contiguous.

→ MS takes  $O(N)$  extra space.

# Hybrid Sorting Algo: (Tim Sort)

↳ Internal algorithms uses  
 Merge Sort + Insertion Sort

↳ works well with partially sorted data.