

Q: arr = [2, 3, 5, 9, 14, 16, 18], target = 14

Ceiling = smallest element in array greater or = target.

$$\text{Ceiling}(\text{arr}, \text{target} = 14) = 14$$

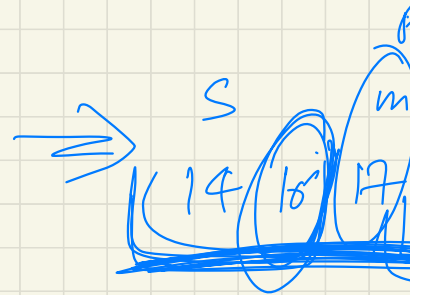
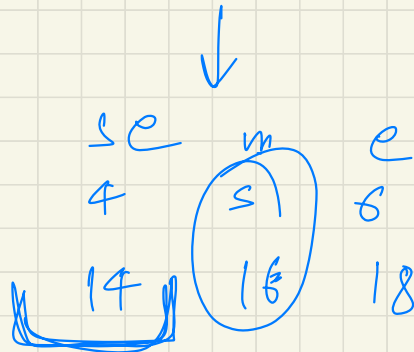
$$\text{Ceiling}(\text{arr}, \text{target} = 15) = 16$$

$$\text{target} = 4 = 5$$

$$\text{target} = 9 = \underline{\underline{9}}$$

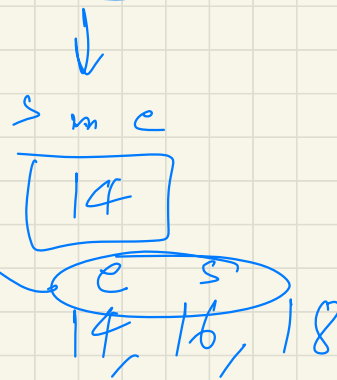
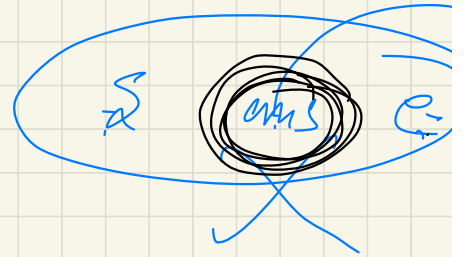
arr = [2, 3, 5, 9, 14, 16, 18]

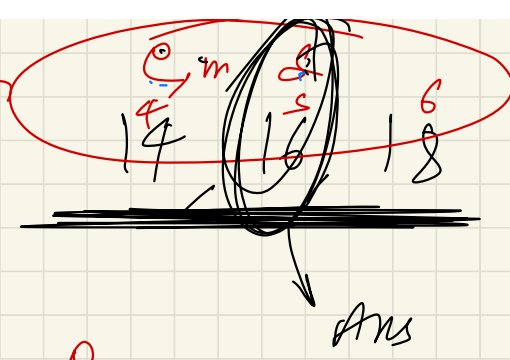
target = 15



breaking of
leaf

while ($s \leq e$)


$$\text{forget} > \text{mid} \\ \Rightarrow s = m + 1$$




let's talk about
start & end point

Q: Find a no
 \geq target

Q target e
||
e target s

→ e target s // condition for while loop no.

start \leq end \Rightarrow when while loop breaks
start \neq end + 1

next big no, when no are found = start element. reqd

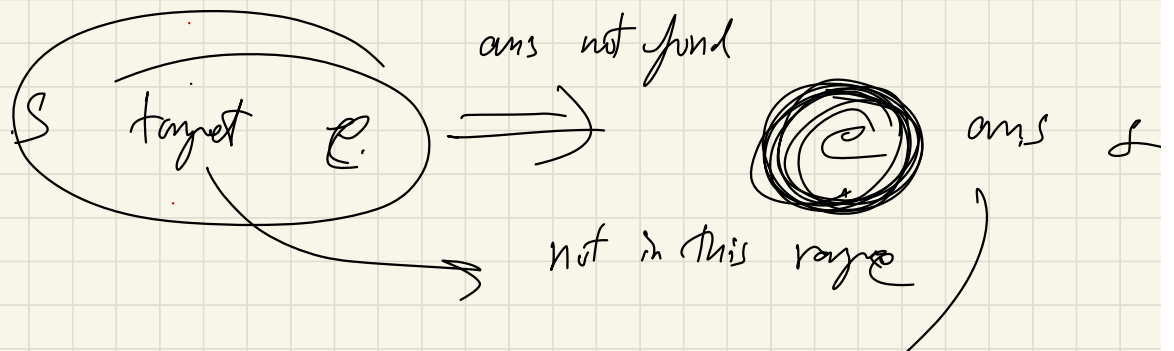
Q: Find the floor of a number.

Floor = greatest number smaller or = target

arr = [2, 3, 5, 9, 14, 16, 18] (Floor of 14)

Ans = 14

// same thing as before, just return end instead of -1, if no. not found.



When ~~condition~~ it violated,
 $d = e + 1$
 $\underline{\underline{s > e}}$

- 3: ① Exact same approach for finding of no.
② Ignore the target = what we are looking for
③ arr = ['c', 'd', 'y', 'j'] target: ~~c~~, 2

condition violated : $start = end + 1 \Rightarrow \text{length} = 1$

return $S \% N$

~~$2 \% 4 = 2$~~ // re
st
==

$4 \% 4 = 0$

if $S == N$:

return 0

7 :

arr = [5, 7, 7, 7, 7, 8, 8, 10]

target = 7

Find first occurrence of 7

Ans m

e s e m e

1

last occurrence:

s = m + 1

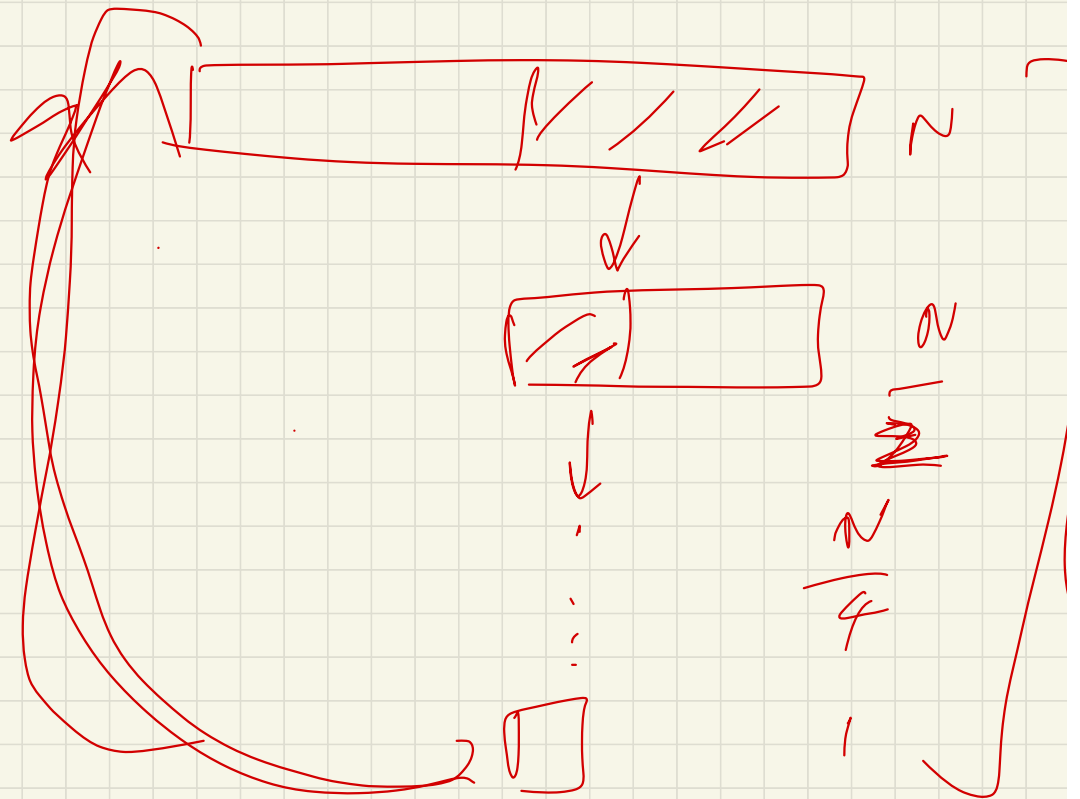
[1, 4]

e = m - 1

s = m + 1

target = 15

log N



$5, 2, 3, 5, 6, 7, 8, 10, 11, 12, 15, 20, 23,$
 $0, 1, 2, 3, 4, 5, 6$

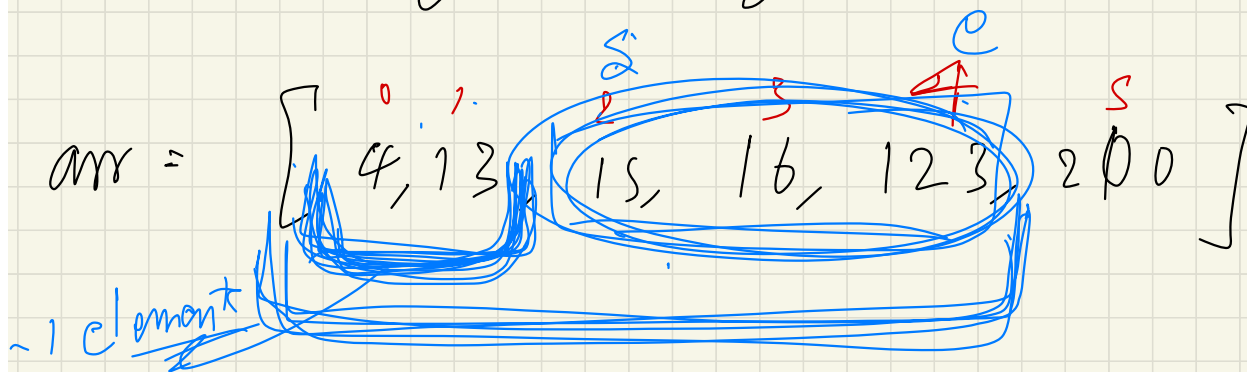
$$1 + 4 = 5$$

\downarrow
only BS

$$5 + 2 \times 4 = 8 + 5 = 13$$

$$\begin{aligned}
 4 &= e - s + 1 \\
 &= 5 - 2 + 1 = 4
 \end{aligned}$$

Finding size of array by indices:

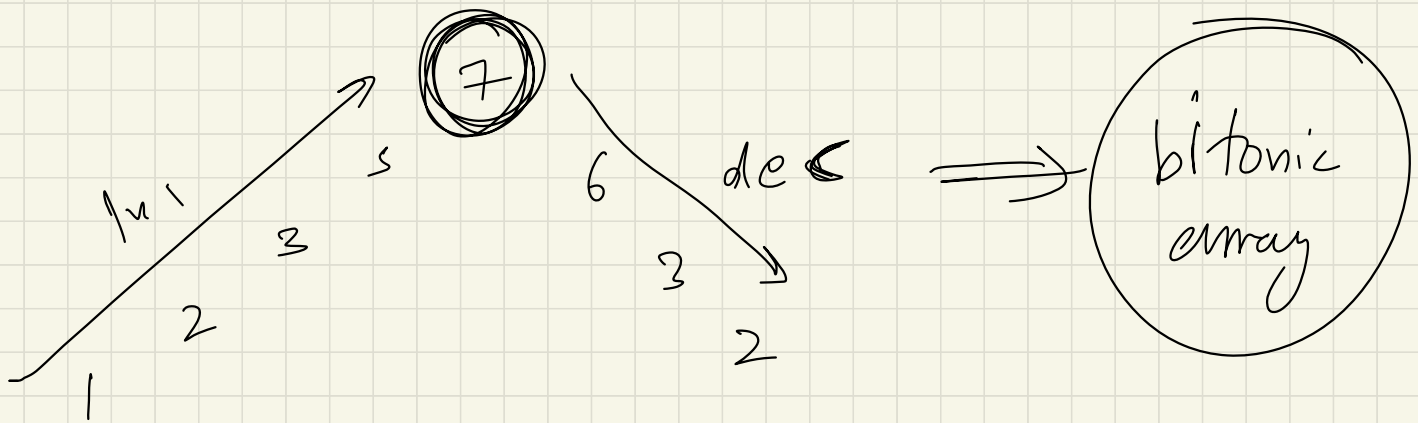


$$e - (s - 1) = (e - s + 1)$$

Ans

$$4 - 2 + 1 = 3$$

arr = [1, 2, 3, 5, 7, 6, 3, 2]



Find peak in mountain array.

① → Ans
0 0

arr = [0, 3, 1, 0]

② → Ans index
0 1 0

arr = [1, 2, 3, 5, 6, 4, 3, 2]

Indices: 0 1 2 3 4 5 6 7

Annotations: A red line connects index 0 to index 4. A blue line connects index 4 to index 6. Both the element 5 at index 3 and the element 3 at index 6 are circled in blue and labeled 'm'.

1) if $e[mid] > e[mid+1] \Rightarrow$ You are in the dec part of array
 $\Rightarrow e = mid$
// check in l.h.

s $\left[\begin{array}{c} m \\ e \end{array} \right]$ e

2) $e[mid] < e[mid+1] \Rightarrow$ You are in the inc part of

$\Rightarrow e = mid + 1$

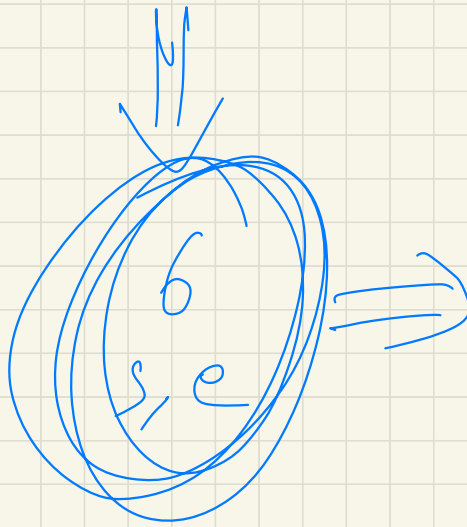
\Rightarrow s $\left[\begin{array}{c} m \\ m+1 \\ e \end{array} \right]$

3) when will loop break?

⁰ 1 2 3 4 5 6 7
1, 2, 3, 5, 6, 4, 3, 2
s m e

6, 4, 3, 2
s m e

4 s
6, 4
s e
m



In the end,
s & e both
will pt to
the large
no.

Ans

why? ① & ②

\therefore
= arr = [1, 2, 3, 4, 5, 3, 1]
target = 3

ns'
=

- ① Find peak element \Rightarrow 4 index
- ② ^{Binary} Search in arr array \Rightarrow (0, 4)
- ③ If not found, binary search in \Rightarrow [4, 6]

Rotated Binary Search:

arr = [2, 4, 5, 7, 8, 9, 10, 12]

After 1 rotation:

= [12, 2, 4, 5, 7, 8, 9, 10]

1 rotation

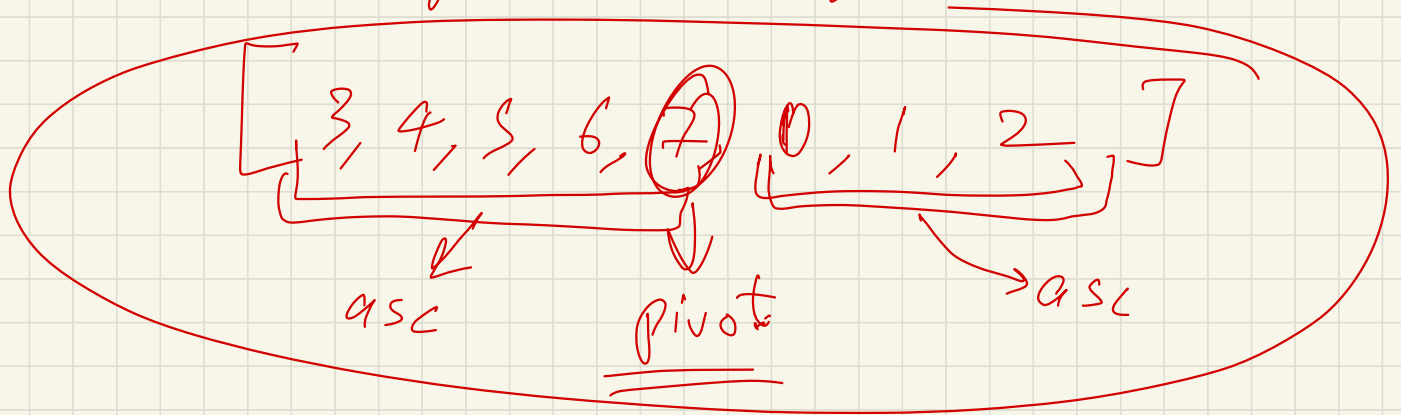
2nd rotation

= [10, 12, 2, 4, 5, 7, 8, 9]

12 is pivot

⇒ Find the pivot in the array.

pivot ⇒ from where your next nos are



* Find pivot

* Search in first half ⇒ Simple BS.
(0, pivot)

↳ otherwise, search in second half: $(pt+1, e$

∴ find pivot :

$\begin{bmatrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 3 & 4 & 5 & 6 & 7 & 0 & 1 & 2 \end{bmatrix}$
s m e

only these 2 will

when? → when you find that $mid >^{dc} mid+1$
element, i.e. pivot. // core 1

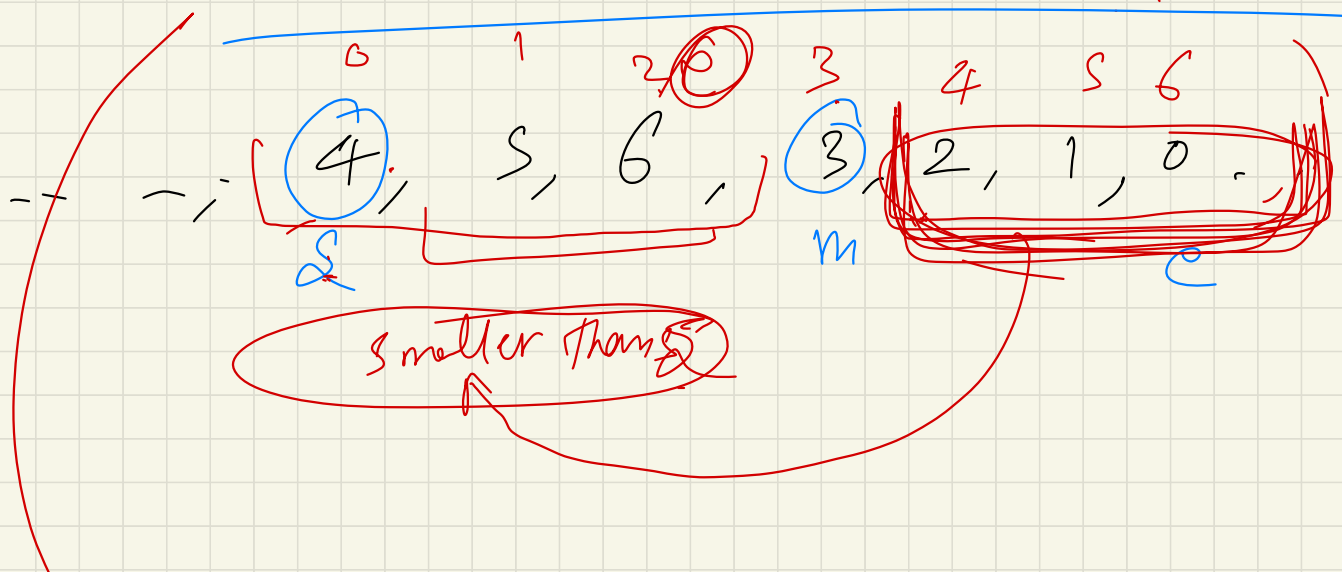
2/ if

mid element $<$ (mid-1) element

i.e also my ans \Rightarrow ans = $n-1$

use 3

start element $>$ mid-element



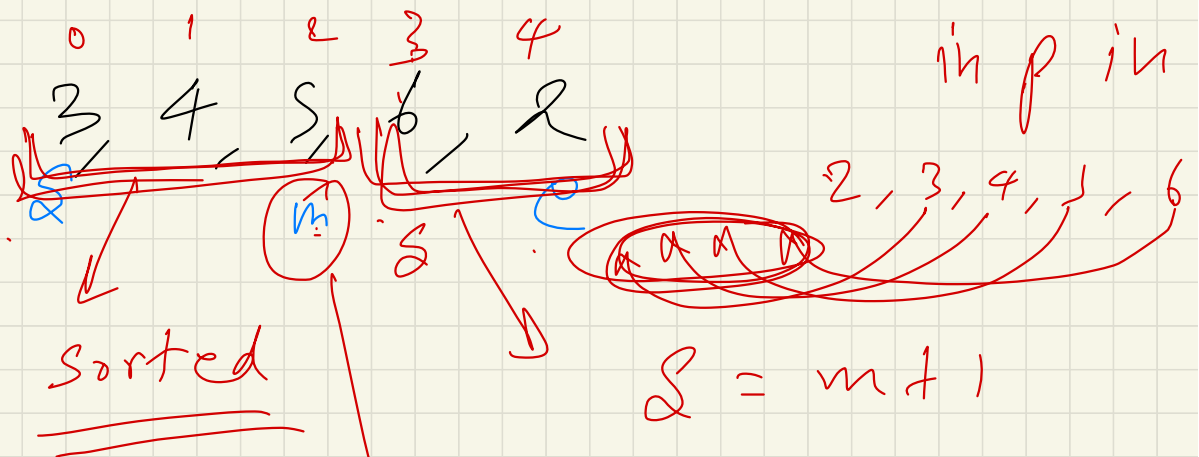
→ In this case, all elements from n will be $<$ start.

Hence, we can ignore all these elements since we are looking for peak i.e. largest element.

$$e = \text{mid} - 1$$

me 4:

\leq element $<$ mid element



If this way pivot,
it would've been
returned in case 1 & 2

Here moved, first bigger no. [↙] lie after
Here, ignore mid & put $s = mid$

to RBS using pivot.

arr = [4, 5, 6, 7 | 0, 1, 2]

s p e

we 1 : pivot element = target // thus

we 2 : target > start element // search for (
 search space = $(s, p-1)$

why? cuz all nos. after pivot
are < s

we 3 : target < start element

i.e. we know that all elements
from s, pivot are too going to

bigger than target. // target = 1

Search space = (pivot + 1 till e

arr = [2, 2, 2, 2, 9]

⇓ rotate twice

⁰
[2, ¹9, ²2, ³2, ⁴2]
₂ ₁₁ _c

arr = [4, 5, 6, 7, 0, 1, 2]



Rotated 4 times from original

0 1 2 3
4 5 6 7
~~4~~ ~~5~~ 6 ~~7~~

4 5 6 7
0 1 2 3

~~4~~ ~~5~~ ~~6~~ ~~7~~

pivot = 3

Ans = 11

arr = [7, 2, 5, 10, 8], m = 2

7, 2, 5, 10
24

8
8

⇒

largest
24

7, 2, 5
14

10, 8
18

18

7, 2
9

5, 10, 8
23

23

2
2

7, 5, 10, 8
30

30

≤ ① min n. of partitions that we can make

② what is the max n. of partitions / m that can be = N

arr = [3, 4, 1, 2] \Rightarrow [3], [4], [1], [2]

next will be the ans in case ① :

[7, 2, 5, 10, 8]

Sum of entire array

= 32

Case (2) :

Ans for this = max element in
array = 4

max value of ans of question = case 1

min value of ans of question = case 2

minAns = max value in array

maxAns = sum of all values in array.

start = 10

[10, 32]

end = 32

Here it dis-
tinct we
BS.

$$\text{mid} = \frac{\text{start}}{2} = \frac{42}{2} = 21$$

Try to see if you can split the array with 21
or the max sum.

7, 2, 5, 8, 10

[7, 2, 5], [8, 10]

pieces
~~2~~ 2

check 1 if (pieces \leq m) \Rightarrow end = mid

start = 10, end = 21

mid = 15

7, 2, 5, 8, 10

[7, 2, 5], [8], [10] pieces

if pieces > m
 \Rightarrow start = mid + 1

$$s = 16, \quad e = 21$$

$$m = 18$$

$$7, 2, 5, 8, 10$$

$$[7, 2, 5], [8, 10]$$

$$\underline{\underline{\text{pieces} = 2}}$$

$$\Rightarrow s = 17, \quad e = 18$$

$$m = 17$$

$$7, 2, 5, 8$$

$$[7, 2, 5], [8], [17]$$

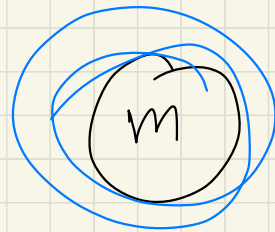
$$\underline{\underline{\text{pieces} = 3}}$$

$$Q \geq m+1 = 18$$

$$S = 18, \quad c = 18$$

$$m = 18$$

Ans



// The ans exists definitely, hence by the above 2 checks we will reach it