

* Space Complexity or Auxiliary Space :-

i) Auxiliary space :- It is the extra space or temporary space taken by an algorithm.

\therefore Space complexity = input space + Auxiliary space.

o Suppose :-

Take an ip of array size N & do something with it.

So the space complexity will be the input you're taking from the size N + extra space the algo is using.

This is known as Space complexity.

- So, in the binary search the space complexity was constant. So, that means auxiliary space was constant it was not taking any extra space.
 - Taking 3 variable i.e. Start, End & Mid.
 - If the array is of size 100 or more than that. Every single time it's only going to take 3 variables i.e. start, end & mid.
- Hence, constant

for ($i = 1$; $i \leq N$;) {

for ($j = 1$; $j \leq k$; $j++$) {

// some operations that
takes time t

}

$i = i + k$

}

Here,

- 1) inner loop is running k times & for every time it's running it's taking t amount of time.

$\therefore O(kt)$ time.

- 2) If inner loop is running once, once, so it's taking t amount of time. So, here it's actually running k times. Hence kt .

- 3) Ans :- $O(kt)$ * times, outer loop is running/

conditions:- where i will start from 1, & the loop will break when i is $\leq N$ & i is incrementing with k

- 4) So let's say, $i = 1, 1+k, 1+2k, 1+3k, \dots, 1+xk$
So, if the ^{last} value is xk that means it
& satisfy the condition. Hence x should be $\leq N$

$1+xk$ is the value & x is the no. of times it's running

$$\therefore 1 + xk \leq N$$

$$xk \leq N-1$$

$$x = N - 1/k$$

There was a mistake here which is solved

$\therefore x$ = no of times
the outer loop
is running?

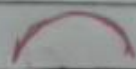
$$\text{Complexity} \therefore O\left(\cancel{k}t * \frac{(N-1)}{\cancel{k}}\right) \quad - \text{const are removed}$$

$$\therefore = O(N * t)$$

** Bubble sort :-

No swap.


Step 1



4	9	5	1	0
---	---	---	---	---

~~No~~ 3rd swap


itr 1



4	9	5	1	0
---	---	---	---	---

Swap


itr 2



4	5	9	1	0
---	---	---	---	---

swap

itr 3



4	5	1	9	0
---	---	---	---	---

swap

itr 4

4	5	1	0	9
---	---	---	---	---

// Ans.

* Worst & Average case time complexity :-
 $O(n * n)$

Worst case occurs when array is reverse sorted.

* Best case time complexity :-
 $O(n)$

Best case occurs when array is already sorted

* Auxiliary space
 $O(1)$

* Boundary cases :-

Bubble sort takes minimum time (order of n) when elements are already sorted.

* Sorting in place :- Yes

* Stable :- Yes

** Selection Sort :-

Worst Complexity : n^2

Average complexity : n^2

Best complexity : n^2

Space complexity : 1

Method : Selection

Stable : No

Note: The good thing about selection sort is it never makes more than $O(n)$ swaps & can be useful when memory write is a costly operation.

Eg:- (man) 4, (5), 1, 2, 3

Swap

(4), 3, 1, 2, 5

swap

2, (3), 1, 4, 5

swap

(2), 1, 3, 4, 5

Swap

1, 2, 3, 4, 5

** Insertion sort :-

Time complexity :- $O(n^2)$

Auxiliary Space :- $O(1)$

Boundary Cases :- Insertion sort takes a maximum time to sort if elements are sorted in reverse order.

And it takes minimum time (Order of n) when elements are already sorted.

Sorting in Place :- Yes.

Eg :-

5 , 3 , 4 , 1 , 2

3 , 5 , 4 , 1 , 2

3 , 4 , 5 , 1 , 2

1 , 3 , 4 , 5 , 2

1 , 2 , 3 , 4 , 5