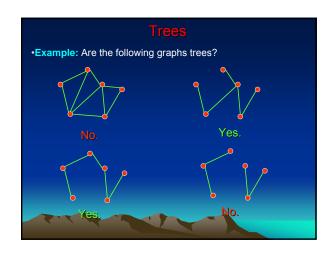
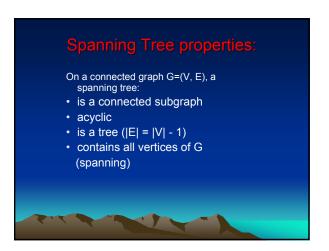
Minimum Spanning Tree, Kruskal's and Prim's Algorithms, Applications in Networking

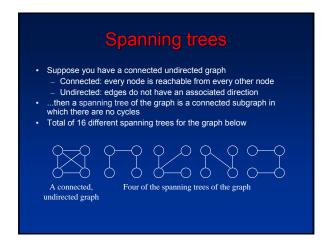


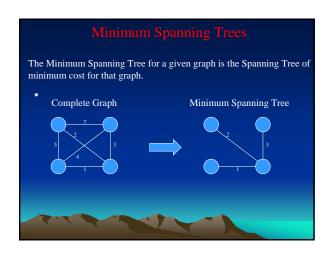
What is Tree ? Definition: A tree is a connected undirected graph with no simple circuits. Since a tree cannot have a simple circuit, a tree cannot contain multiple edges or loops. Therefore, any tree must be a simple graph. Theorem: An undirected graph is a tree if and only if there is a unique simple path between any of its vertices.

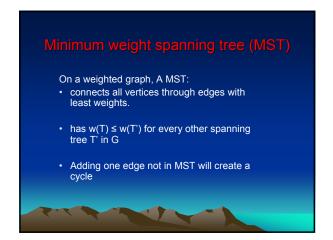


Spanning Trees A spanning tree of a graph is just a subgraph that contains all the vertices and is a tree. A graph may have many spanning trees



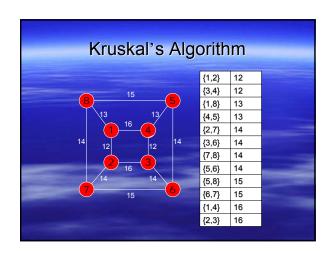


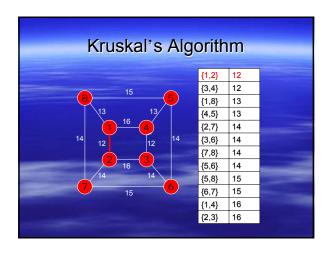


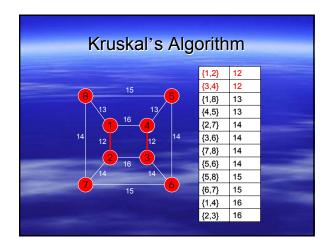


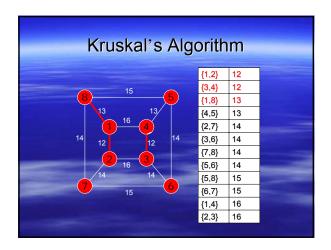


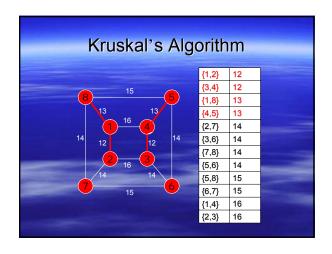


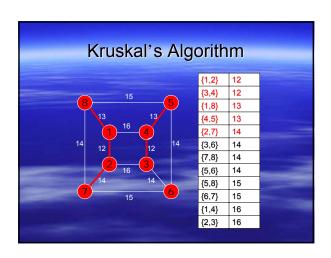


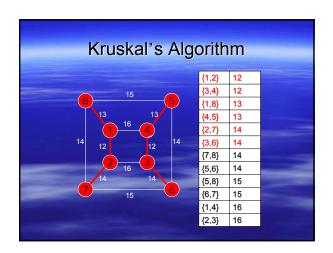


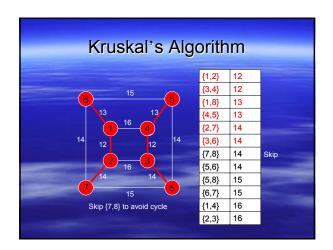


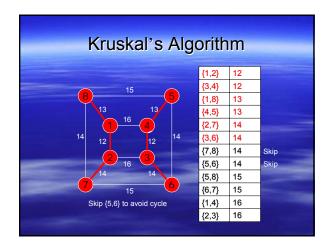


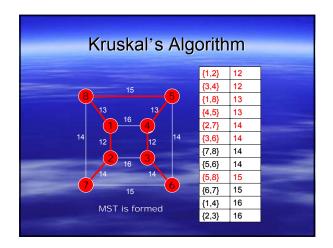


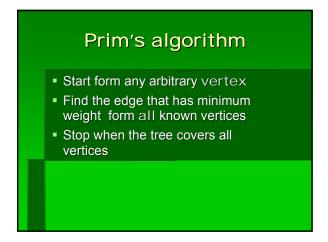


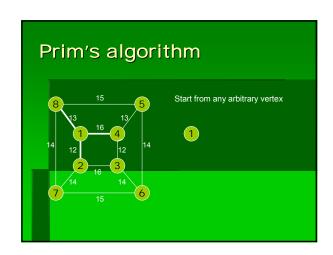


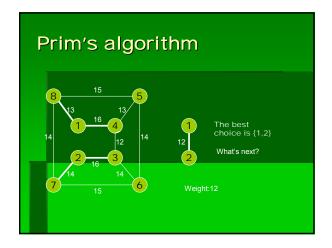


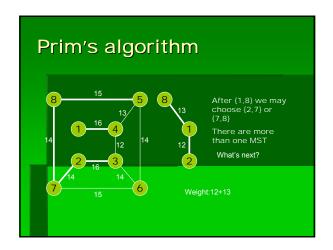


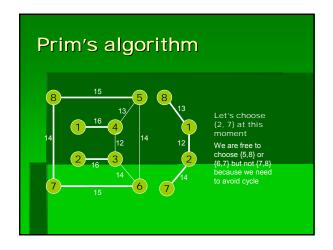


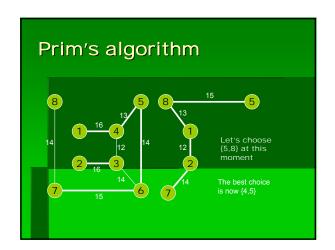


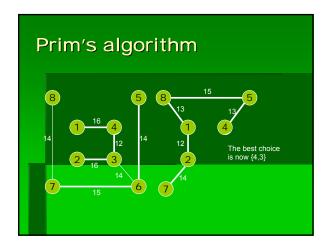


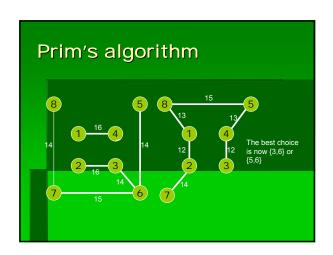


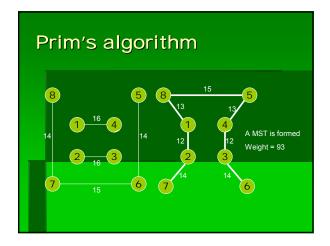


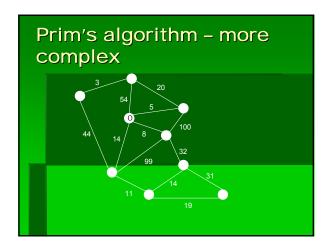


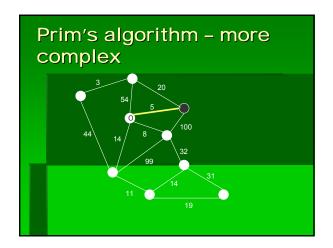


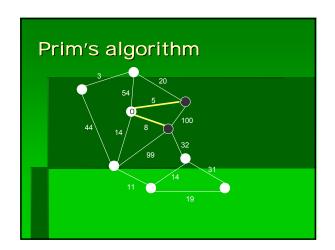


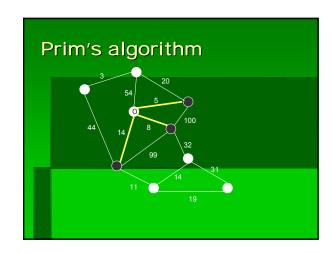


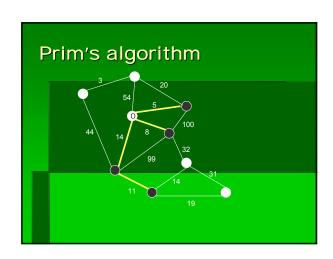


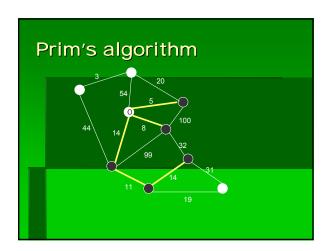


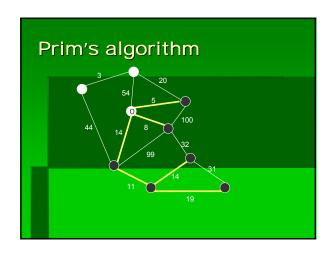


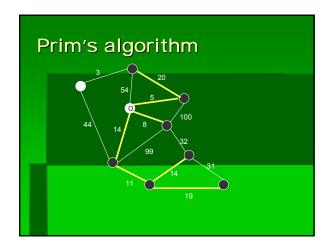


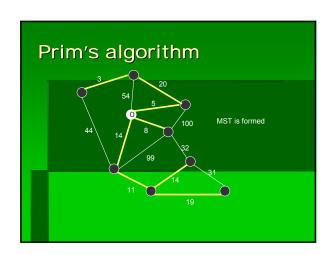


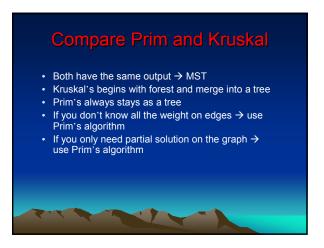


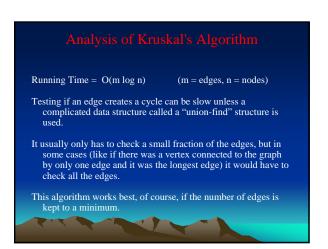












Analysis of Prim's Algorithm Running Time = O(m + n log n) (m = edges, n = nodes) If a heap is not used, the run time will be O(n^2) instead of O(m + n log n). However, using a heap complicates the code since you're complicating the data structure. A Fibonacci heap is the best kind of heap to use, but again, it complicates the code. Unlike Kruskal's, it doesn't need to see all of the graph at once. It can deal with it one piece at a time. It also doesn't need to worry if adding an edge will create a cycle since this algorithm deals primarily with the nodes, and not the edges. For this algorithm the number of nodes needs to be kept to a minimum in addition to the number of edges. For small graphs, the edges matter more, while for large graphs the number of nodes matters more.

Why do we need MST? a reasonable way for clustering points in space into natural groups can be used to give approximate solutions to hard problems

