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OBJECTIVE:

- Empirical Analysis of Polynomial Evaluation
- Writing DFS with dictionaries
- Writing BFS with dictionaries

Q1. Write a Python program that makes the empirical analysis of the polynomial evaluation with the below Brute-Force Algorithm;

- Writes a function that gets 'a' as a list and 'x', then calculates and returns the polynomial values of p(x).

Problem: Find the value of polynomial

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x^1 + a_0$$

at a point $x = x_0$

ALGORITHM POLINOM(A[0..n-1], X)

```

p ← a[0]
power ← 1
for i ← 1 to n do
    power ← power * x
    p ← p + a[i] * power
return p
    
```

- Program generates a random array. Size of the array is 1000 and the numbers between 0-100000.
- X value will be read by the main program.

Output:

Enter the value of X: 2

```

6546592718091443012521151843030979365516097314738788090621968610717843782688542839657966
7320017859566233980833847601454706135547097230656326397933767916101308117417790282004900
4362094967560417081240477729960406111244641301841378166718474052564821100655007023628964
7585305734363840534358989276459227193250879
    
```

0.0286100 seconds

Q2. Write a Python program that makes the empirical analysis of the polynomial evaluation with the below Brute-Force Algorithm; Set the value of X to 2.

ALGORITHM POLINOM(A[0..n-1], X)

```
p ← 0.0
for i ← n downto 0 do
    power ← 1
    for j ← 1 to i do
        power ← power * x
    p ← p + a[i] * power
return p
```

Output:

8.230999583414169e+306
0.1002443 seconds

Q3. Write a Python program which will print the DFS TRAVERSAL LIST for a given **connected graph**;

- Reads the number of vertexes for this graph
- Reads the VERTEX LIST in the given number as an one-dim array
- Reads two dimensional array for matrix representation of a graph – ADJACENCY MATRIX
- Defines a GRAPH as a dictionary which contains all the vertexes as a key, and it's neighbors as a list. You have to use the adjacency matrix and the vertex list that you read
- Implements the below recursive Depth First Search Algorithm that displays the visited graph vertices.

ALGORITHM DFS(Graph, vertex, path[0..n])

```
// Implements a depth-first-search traversal of a given graph
//INPUT: Graph{ vertex: list of neighbor vertexes }
//      vertex, beginning vertex to search
//      path will be used to construct traversal list in recursion
//OUTPUT: List of vertices in DFS traversal - path

//visits recursively all the unvisited vertices of a connected graph
add vertex to path
for each neighbor in graph[vertex] do

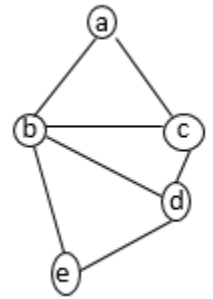
    if neighbor not in path          //for the non-visited neighbors
    then path ← DFS(Graph, neighbor, path)
return path
```

⇒ You may use the following examples for testing your program

Example 1:

Output:

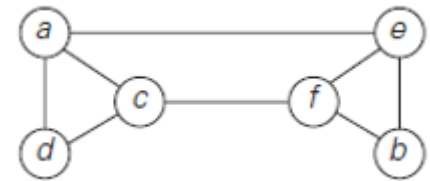
```
Enter the number of vertexes: 5
Enter the vertex list for graph:
abcde
Enter the adjacency matrix:
0 1 1 0 0
1 0 1 1 1
1 1 0 1 0
0 1 1 0 1
0 1 0 1 0
The graph is
{'a': ['b', 'c'], 'b': ['a', 'c', 'd', 'e'], 'c': ['a', 'b', 'd'], 'd': ['b', 'c', 'e'],
'e': ['b', 'd']}
DFS traversal:
['a', 'b', 'c', 'd', 'e']
```



Example 2:

Output:

```
Enter the number of vertexes: 6
Enter the vertex list for graph:
abcde
Enter the adjacency matrix:
0 0 1 1 1 0
0 0 0 0 1 1
1 0 0 1 0 1
1 0 1 0 0 0
1 1 0 0 0 1
0 1 1 0 1 0
The graph is
{'a': ['c', 'd', 'e'], 'b': ['e', 'f'], 'c': ['a', 'd', 'f'], 'd': ['a', 'c'], 'e':
['a', 'b', 'f'], f: ['b', 'c', 'e']}
DFS traversal:
['a', 'c', 'd', 'f', 'b', 'e']
```



Q4. Write a Python program which will print the BFS TRAVERSAL LIST for a given **connected graph**;

- Reads the number of vertexes for this graph
- Reads the VERTEX LIST in the given number as an one-dim array
- Reads two dimensional array for matrix representation of a graph – ADJACENCY MATRIX
- Defines a GRAPH as a dictionary which contains all the vertexes as a key, and it's neighbors as a list. You have to use the adjacency matrix and the vertex list that you read
- Implements the below algorithm for Breadth First Search Algorithm by using queues that displays the visited graph vertices.

ALGORITHM BFS(Graph, vertex)

// Implements a Breadth-first-search traversal of a given graph

//INPUT: Graph{ vertex: list of neighbor vertexes}

// vertex, beginning vertex to search

//OUTPUT: List of visited vertices in BFS traversal

//visits all the unvisited vertices of a connected graph using a queue

Put the beginning vertex to queue

Put the beginning vertex to visited list

while queue not ends do

 currvertex \leftarrow pop first element from queue

 for each neighbor in graph[currvertex] do

 if neighbor not in visited //for the non-visited neighbors

 then add neighbor to visited

 add neighbor to queue

return visited

\Rightarrow You may use the following examples for testing your program

Example 1:

Output:

Enter the number of vertexes: 5

Enter the vertex list for graph:

abcde

Enter the adjacency matrix:

0 1 1 0 0

1 0 1 1 1

1 1 0 1 0

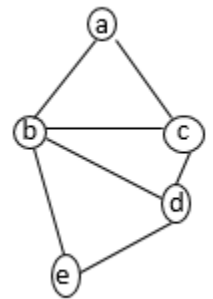
0 1 1 0 1

0 1 0 1 0

The graph is

{'a': ['b', 'c'], 'b': ['a', 'c', 'd', 'e'], 'c': ['a', 'b', 'd'], 'd': ['b', 'c', 'e'], 'e': ['b', 'd']}

BFS TRAVERSAL : ['a', 'b', 'c', 'd', 'e']



Example 2:

Output:

Enter the number of vertexes: 6

Enter the vertex list for graph:

abcdef

Enter the adjacency matrix:

0 0 1 1 1 0

0 0 0 0 1 1

1 0 0 1 0 1

1 0 1 0 0 0

1 1 0 0 0 1

0 1 1 0 1 0

The graph is

{'a': ['c', 'd', 'e'], 'b': ['e', 'f'], 'c': ['a', 'd', 'f'], 'd': ['a', 'c'], 'e': ['a', 'b', 'f'], f: ['b', 'c', 'e']}

BFS traversal:

['a', 'c', 'd', 'e', 'f', 'b']

