



**UNIVERSIDAD  
DE GRANADA**

Computational intelligence

Practica neural network

Optical character recognition

MNIST

course 2019-2020

Master in Ingeniería Inform

ática

Department of Sciences Computaci

on and on artificial intelligence

# Practice 1

## MNIST

The purpose of this is to solve a problem practical pattern recognition using artificial neural networks. Deber'a evaluate the use of several types of neural networks to solve a problem OCR recognition of handwritten manuscripts of the database MNIST ( <http://yann.lecun.com/exdb/mnist/>).

### 1 Implementation

To perform this practical, you can choose to implement algorithms yourself or use as a basis for many libraries that implement these algorithms and estimate the decisions about can influence in their final classification quality.

Although the majority of sequential algorithms neural network training is not particularly complex, you can be found at the Internet multiple libraries that implement some of the algorithms described in class so efficient. Such implementations available for multiple languages programming, usually designed to take advantage of the various microprocessors or ability to compute a GPU, if you have one available. If, Instead of using a language programming of your choice, General bear, prefers to use a mathematical tool, you can find **toolboxes Matlab or packages in R** practically for any type of neural network you want to evaluate. However, the use of libraries provided by third parties has some drawbacks that must be taken into account. First, no one guarantees that implementation is available completely free of errors and, although as is, it may prove difficult to adapt the implementation

available on our needs concrete when we want to perform a particular experiment.

**IMPORTANT:** Use third-party implementations without making the corresponding attributes is constitutive of plagiarism, a crime against intellectual property that carries a suspension of Penthouse in the subject.

## On the computation of the gradient

When making your implementation, we recommend using a strategy of TDD type [ *test-driven development* ] or, at least, perform unit tests to ensure that the C++

gradient computation is performed correctly. To perform this comprobaci3n, remember the definition of the derivative:

$$\frac{dJ}{d\theta}(\theta) = \lim_{\epsilon \rightarrow 0} \frac{J(\theta + \epsilon) - J(\theta - \epsilon)}{2\epsilon}. \quad (1.1)$$

For any value  $\theta$ , You can approximate the derivative using a value of epsilon ( $\epsilon$ ) pequeño, eg  $10^{-4}$  (a value too pequeño podr3a not cause rounding errors, so you should not rush too in this regard):

$$g(\theta) \approx \frac{J(\theta + \epsilon) - J(\theta - \epsilon)}{2\epsilon}. \quad (1.2)$$

How  $\theta$  It is a vector of par3metros, not a simple n3mero. Real UMBER, we will have committed bar the gradient is calculated correctly for each  $\theta_i$ . For each vector par3metros  $\theta$ , evaluate  $g_i(\theta)$  as an approximation of  $\frac{\partial J}{\partial \theta_i}(\theta)$ . We can define  $\theta^{(i+)} = \theta + \epsilon \tilde{e}_i$  where  $\tilde{e}_i$  and  $\tilde{e}_i$  it is a vector with a one in the posici3n  $i$ th and zeros dem3s:

$$\tilde{e}_i = \begin{bmatrix} 0 \\ \vdots \\ 0 \dots \\ \vdots \\ 1 \dots \\ \vdots \\ 0 \end{bmatrix} \quad (1.3)$$

So  $\theta^{(i+)}$  is similar to  $\theta$ , unless the  $i$ th component has increased. In the same way, we can get  $\theta^{(i-)} = \theta - \epsilon \tilde{e}_i$  vector  $\theta$  with its  $i$ th component reduced. With this we can veri fi car num3ricamente gradient for each par3metro:

$$g_i(\theta) \approx \frac{J(\theta^{(i+)}) - J(\theta^{(i-)})}{2\epsilon}. \quad (1.4)$$

S3lo we have to repeat the C++ computation for different values of  $\theta$ , with the objective of check that the difference between the values calculated by our implementaci3n on and num3ricamente approximate values do not differ too much.

Another interesting alternative is the utilizaci3n of t3cnicas of autom3tico diferenciaci3n atica ( [https://en.wikipedia.org/wiki/Automatic\\_differentiation](https://en.wikipedia.org/wiki/Automatic_differentiation)). However, implementaci3n of such t3cnicas I s3lo can compensate for larger projects. B3asicamente, the diferenciaci3n on autom3tico atica is responsible for calcular the gradient of a function for us, so that potential errors are avoided implementaci3n on that, otherwise, podr3an get to go unnoticed.

## 2 results Analysis

When solving a problem classification, the classifier is trained with the training set. In this case, the training set contains examples labeled 60000. Examples of training are images

pixels- standard 28x28 thumbnails

and they are in the file `train-images-idx3-ubyte`, while for Examples labels can be found in the file `train-labels-idx1-ubyte`.

Evaluate the quality of a classifier using the same data that you train may be engaging, why you have a separate set of data, that is not used during training. Said test assembly, stored in the same format as the training set can be found in the files

`t10k-images-idx3-ubyte (images)` and `t10k-labels-idx1-ubyte (tags)`.

While almost any technique of learning automatic can get results exceptional on the training set, techniques not all are equally good when it comes to the test set. Some techniques of overfitting (excess adapt to the training set with the model trains) and then not generalize properly, so they get poor results on different data sets to the training set.

To evaluate the results of the practice use the error rate on the test set (the number of test set instances that our neural network does not classifies correctly). As a guideline Inventors, these are the results that should get some concrete models of neural networks artificial:

- simple neural network with an input layer and an output layer softmax type: 7.8% error on the test set and 5.6% error on the training set (training time required: about one minute using a implementation on an interpreted language like Matlab).
- multilayer neural network with one hidden layer 256 logistic units and an output layer softmax type: 3.0% error on the test set and 0.0% error on the training set (training time required: about four minutes using a implementation in an interpreted language as Matlab).
- convolutional neural network trained with stochastic gradient descent: 2.7% error on the test set (training time required: about 13 minutes using a implementation in an interpreted language as Matlab).
- "Deep learning" using pre-training to extract autoencoders characteristics of images techniques thumbnails using unsupervised neural network and single with a layer of softmax type: from 1.8% to 2.2% error on the test set (training time required: about twenty minutes using a implementation on an interpreted language like Matlab).

The proposal by Yann LeCun network, convolutional type and multiple hidden layers, able to reduce the error rate to 0.82% (82 errors 10000 examples set)

test). Using an algorithm of "deep learning" m so as fi sticado, the error can  
 reduced to 0.35% (35 errors on 10000). combining m ultiple neural networks  
 You can reduce a one M's error, to 0.23% (s olo 23 errors over 10000). In the  
 p'agina MNIST website ( <http://yann.lecun.com/exdb/mnist/>) you can find the results that have been obtained with  
 many t'ecnicas classi fi caci on, including several  
 types of artificial neural networks.

### 3 Documentación and delivery pr'actica

- Train different neural networks on artificial training set MNIST and eval  
 ue the results obtained using the test set. Env'ie  
 the results that are obtained at the p'trav'es Agina web enabled purpose  
 ( <https://goo.gl/xiXVSK>). You can send your results many times as desired, s'  
 olo is tendr' to consider the best result obtained.  
  
 NOTE: The env'io results must be performed using the same direcci' on email  
 with whom he appears registered in DECSAI and must include all necessary par'ámetros to replicate the  
 experiment, including topolog'ia of the neural network used (n'  
 umber of layers, layer neurons, neurons type ...) and the algorithm  
 Training used to adjust the weights of the network (with combinaci' on  
 par'ámetros particular there is used).
- Create a memory in which is collected experimentaci'on performed during elaboraci'  
 on this pr'actica and cos phi gr'a considered appropriate to illustrate the results obtained. Memory  
 deber' to be delivered in PDF format and ir' to accom-  
 pa- nothing of all fi les for the various implementations made (and the corresponding links to external libraries  
 that have employed). Memory delivery and PDF fi les c'odigo in a ZIP deber'  
 to reali-  
 zarse access to trav'es identi fi ed DECSAI ( <https://decsai.ugr.es/>) before the December 8, 2019 at 23:59.

## Evaluation on the project

- 30% work implementation points:
  - 10% maximum if you use a implementation on external algorithms learning neural network (0% if it merely replicate experiments algorithm a tutorial available on the Internet).
  - 30% at most if you develop your own implementation on algorithms Learning neural networks.
- 40% by memory project Actica (documentation on experiments and tests An 'done with his Alisis results):
  - 20% by description its implementation and on the algorithms used realization during the project Actica.
  - 20% by description of the experiments you made to establish parameters your neural network and An parsing the results obtained.
- 30% by the results obtained (using a linear ranking function on the error rates obtained on the test set).