Question 1:

Answer the following True/False questions,

- 1. The two fundamental properties of sets are,
 - Duplicate elements are not allowed.
 - Order matters.

Answer: False, The order does not matter.

- 2. Let $S = \{3, 4, 5, 2, 1, 3, 0\}$, then $(-3 + 4 5 + 2 1 + 3) \in S$. **Answer**: **True**, Observe that -3 + 4 - 5 + 2 - 1 + 3 = 0 and $0 \in S$, so its true.
- 3. $\sqrt{4} \in \mathbb{Z}$. Answer: True, $\sqrt{4} = 2$ and $2 \in \mathbb{Z}$.
- 4. The vertex of $f(x) = 3(x+4)^2 + 1$

is (4,1).

Answer: False, The vertex here is (-4, 1).

5. The centre of the circle, $(x+1)^2 + (y+2)^2 = 4$

is (-1, -2).

Answer: True

6. The vertex of,

$$f(x) = -\frac{5}{3}(x-3)^2 - 4.$$

represents a minimum.

Answer: False, Since $a = -\frac{5}{3} < 0$, the vertex must represent a maximum.

7. The y-intercept of,

$$f(x) = -x^2 + 3x + 4.$$

is -4.

Answer: **False**, The y-intercept here is 4.

Question 2:

Write down the elements of the following sets. (Remember to use dots (...) where applicable)

(a)
$$A = \{t \in \mathbb{Z} \mid 0 \le t < 5\}$$

Solution:
$$A = \{0, 1, 2, 3, 4\}$$

(b)
$$R = \{ r \in \mathbb{Z} \mid r \ge 1 \}$$

Solution:
$$R = \{1, 2, 3, 4, 5, \dots\}$$

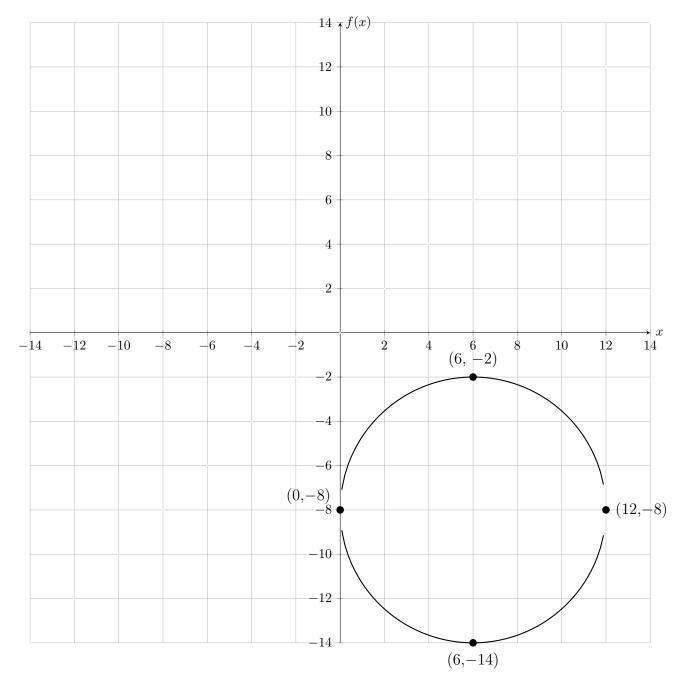
(c)
$$T = \{x \in \mathbb{Z} \mid x^2 = 1\}$$

Solution:
$$T = \{-1, 1\}$$

Question 3:

Graph the following circle,

$$(x-6)^2 + (y+8)^2 = 36.$$



Question 4:

Lets define the following function,

$$f: \mathbb{R} \to \mathbb{R}$$
$$f(x) = -x^2 + 2x + 8$$

(a) Complete the square to convert f into vertex form.

Solution:

Step 1:

$$0 = b^{2} - 4at$$

$$0 = 4 - 4(-1)(t)$$

$$0 = 4 + 4t$$

$$4t = -4$$

$$t = -1$$

Step 2:

$$f(x) = -x^{2} + 2x + t - t + 8$$

$$= -x^{2} + 2x + (-1) - (-1) + 8$$

$$= (-x^{2} + 2x + (-1)) + [8 - (-1)]$$

$$= -\left(x^{2} + \frac{2}{-1}x + \frac{(-1)}{-1}\right) + [8 + 1]$$

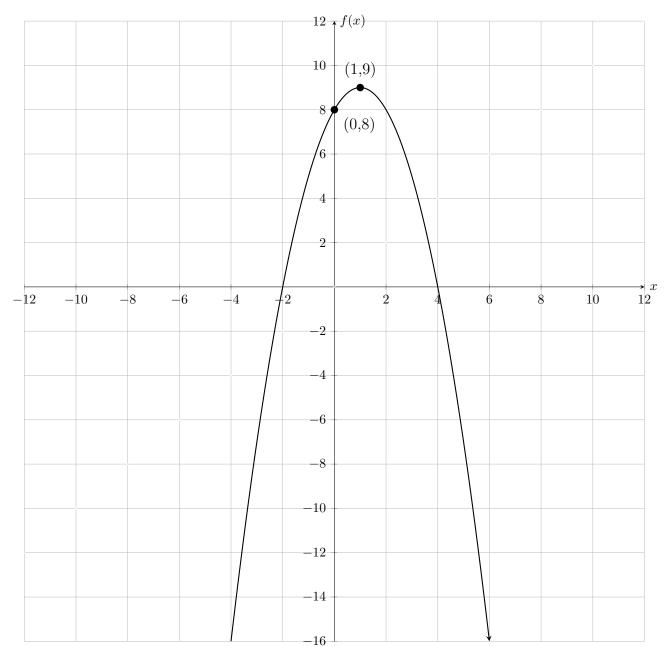
Step 3: Since $a \cdot b = -1 \cdot 2 = -2$ we conclude that $a \cdot b < 0$, so we proceed with the following replacement,

$$f(x) = -\left(x - \sqrt{\frac{t}{a}}\right)^2 + 9$$
$$= -\left(x - \sqrt{\frac{-1}{-1}}\right)^2 + 9$$
$$= -\left(x - \sqrt{\frac{1}{1}}\right)^2 + 9$$
$$= -(x - 1)^2 + 9$$

Step 4: Finally, we have f in vertex form,

$$f(x) = -(x-1)^2 + 9.$$

(b) Sketch the function using your answer from part (a) (**NOTE:** Make sure you label the y-intercept as well as the vertex).



Name: