Review on Factoring

1 Difference of Squares factoring $(f(x) = ax^2 + c)$

IF c < 0 then you can factor the quadratic as follows,

$$f(x) = \left(\sqrt{a}x + \sqrt{|c|}\right)\left(\sqrt{a}x - \sqrt{|c|}\right).$$

ELSE IF a < 0 then you can factor the quadratic as follows,

$$f(x) = -\left(\sqrt{|a|}x + \sqrt{c}\right)\left(\sqrt{|a|}x - \sqrt{c}\right).$$

2 Simple Factoring $(f(x) = x^2 + bx + c)$

IF a = 1, then the factoring is known as 'simple' because the procedure is quite straight forward. As such we call quadratics with a = 1 simple trinomials. So assume that we are working with a quadratic function with a = 1,

$$f(x) = x^2 + bx + c.$$

Step 1. Find the integers p, q such that,

$$p + q = b$$
$$p \cdot q = c.$$

Step 2. Factor the quadratic as follows,

$$f(x) = (x - q)(x - p).$$

3 Non-Simple Factoring $(f(x) = ax^2 + bx + c)$

If $a \neq 1$ then proceed with the following steps,

Step 1. IF b **and** c are divisible by a, then factor a out of the polynomial. Then apply simple factoring to the polynomial leftover and your done!

Step 2. ELSE, find the integers p, q such that,

$$p + q = b$$
$$p \cdot q = ac.$$

Step 3. Then,

- Find the gcd(|a|, |p|), let that integer be t.
- Find the gcd(|q|, |c|), let that integer be k.

Step 4. Complete the factorization by writing,

$$f(x) = (tx + k)\left(\frac{a}{t}x + \frac{p}{t}\right).$$

Practice Problems:

Completely factor the following quadratics. (I will typeset the solutions to these problems soon, just ask me in class if you feel uncertain about an answer).

1.
$$f(x) = x^2 + 16x + 64$$

$$2. \ g(x) = -x^2 - 15x - 26$$

3.
$$f(x) = 9x^2 - 49$$

4.
$$r(x) = 6x^2 + x - 2$$

5.
$$q(x) = -9x^2 + 6x - 1$$

6.
$$Y(x) = 21x^2 + 27x + 6$$

7.
$$I(x) = 12x^2 - 26x - 16$$

(Make life easy by first factoring out a 4)

8.
$$A(x) = 2x^2 + 7x + 5$$

9.
$$f(x) = 4x^2 + 16x + 16$$

10.
$$r(x) = -x^2 + 13x - 22$$

11.
$$f(x) = 121 - 100x^2$$

12.
$$f(x) = 7x^2 + 15 - 18$$

13.
$$L(x) = 4 - 9x^2$$

14.
$$\Gamma(x) = 12x^2 + 17x + 6$$

15.
$$\Lambda(x) = -2x^2 + 8x + 24$$

16.
$$\Phi(x) = -5x^2 + 2x + 7$$

17.
$$\Theta(x) = -3x^2 - 9x + 30$$

18.
$$\xi(x) = x^2 + 4x - 77$$

19.
$$\alpha(x) = 2x^2 - 3x - 14$$

$$20. S(x) = 6x^2 + 5x - 6$$