

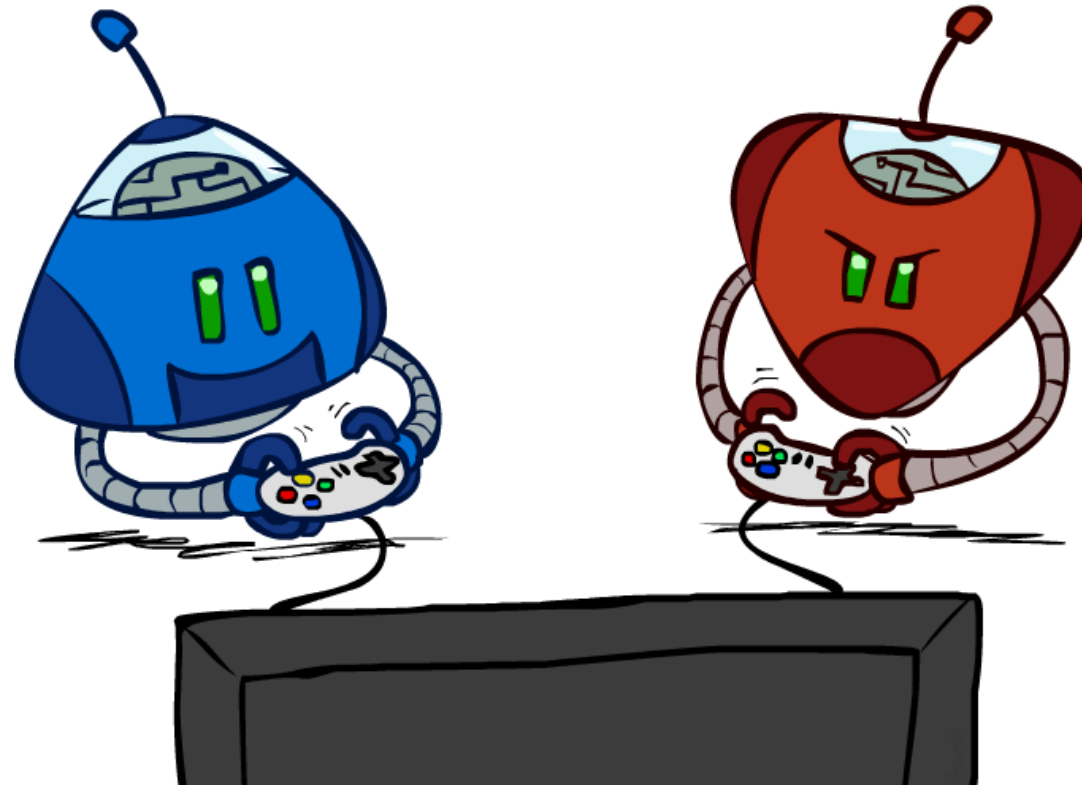
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Lecture 6

21st Oct 2023

AI: Representation and Problem Solving

Local Search



Slide credits: Pat Virtue, <http://ai.berkeley.edu>

Outline

- Beam Search
- Local Beam Search & Variants of Beam Search
- Grid Search
- Simulated Annealing

Beam Search

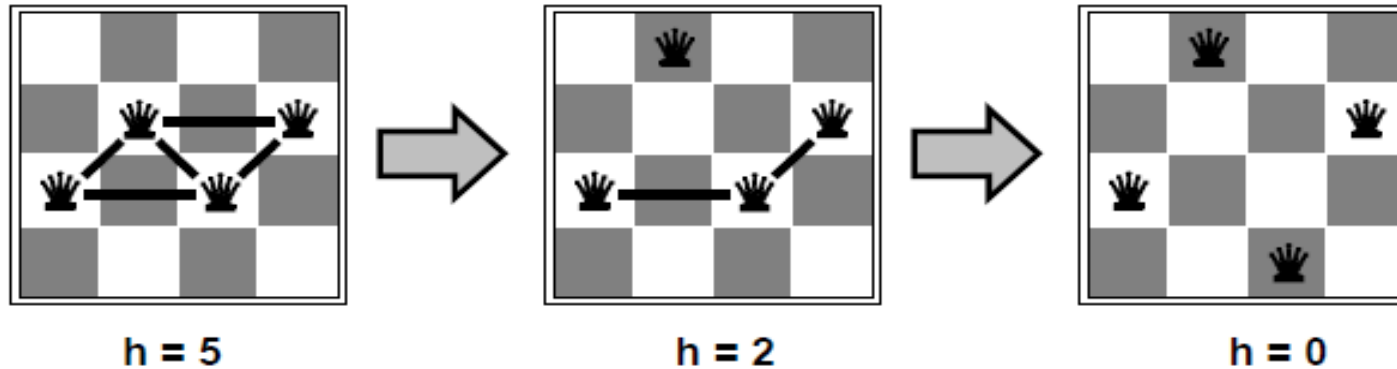
- Search Algorithms like BFS, DFS and A* etc. are infeasible on large search spaces.
- Beam Search was developed in an attempt to achieve the optimal (or sub-optimal) solution without consuming too much memory.
- It is used in many machine translation systems.

Where to use Beam Search?

- In many problems path is irrelevant, we are only interested in a solution (e.g. 8-queens problem)
- This class of problems includes
 - Integrated-circuit design
 - Factory-floor layout
 - Job scheduling
 - Network optimization
 - Vehicle routing
 - Traveling salesman problem
 - Machine translation

N-queens problem

- Put n queens on an $n \times n$ board with no two queens sharing a row, column, or diagonal



- move a queen to reduce number of conflicts.
- Solves n-queens problem very quickly for very large n .

Machine Translation

- To select the best translation, each part is processed.
- Many different ways of translating the words appear.
- The top best translations according to their sentence structures are kept.
- The rest are discarded.
- The translator then evaluates the translations according to a given criteria.
- Choosing the translation which best keeps the goals.
- The first use of a beam search was in the Harry

Beam Search

- Is heuristic approach where only the most promising β nodes (instead of all nodes) at each step of the search are retained for further branching.
- β is called Beam Width.
- Beam search is an optimization of best-first search that reduces its memory requirements.

Beam Search Algorithm

OPEN = {initial state}

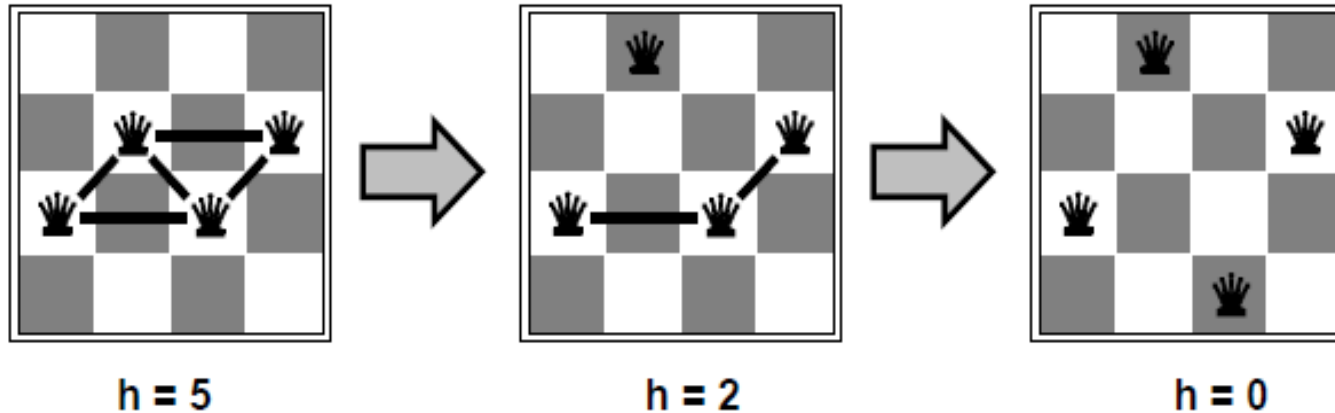
while OPEN is not empty do

1. Remove the best node from OPEN, call it n .
2. If n is the goal state, backtrace path to n (through recorded parents) and return path.
3. Create n 's successors.
4. Evaluate each successor, add it to OPEN, and record its parent.
5. If $|OPEN| > \beta$, take the best β nodes (according to heuristic) and remove the others from the OPEN.

done

Example of Beam Search

- 4-queen puzzle
- Initially, randomly put queens in each column
- h = no. of conflicts
- Let $\beta = 1$, and proceed as given below



Beam Search vs. A*

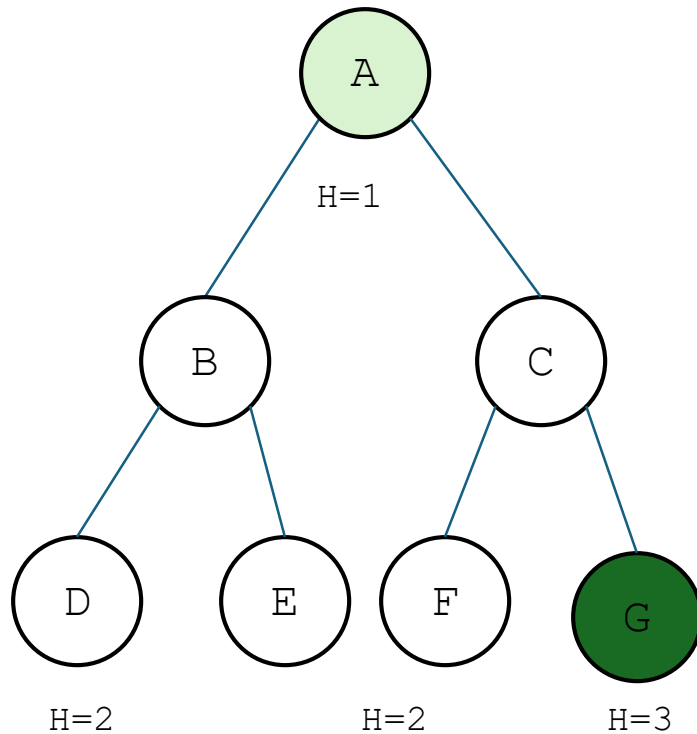
- In 48-tiles Puzzle, A* may run out of memory since the space requirements can go up to order of 10^{61} .
- Experiment conducted shows that beam search with a beam width of 10,000 solves about 80% of random problem instances of the 48-Puzzle (7x7 tile puzzle).



Completeness of Beam Search

- In general, the Beam Search Algorithm is not complete.
- Even given unlimited time and memory, it is possible for the Algorithm to miss the goal node when there is a path from the start node to the goal node (example in next slide).
- A more accurate heuristic function and a larger beam width can improve Beam Search's chances of finding the goal.

Example with $\beta=2$



Steps:

1. OPEN = {A}

H = 3

2. OPEN = {B, C}

3. OPEN = {D, E}

4. OPEN = {E}

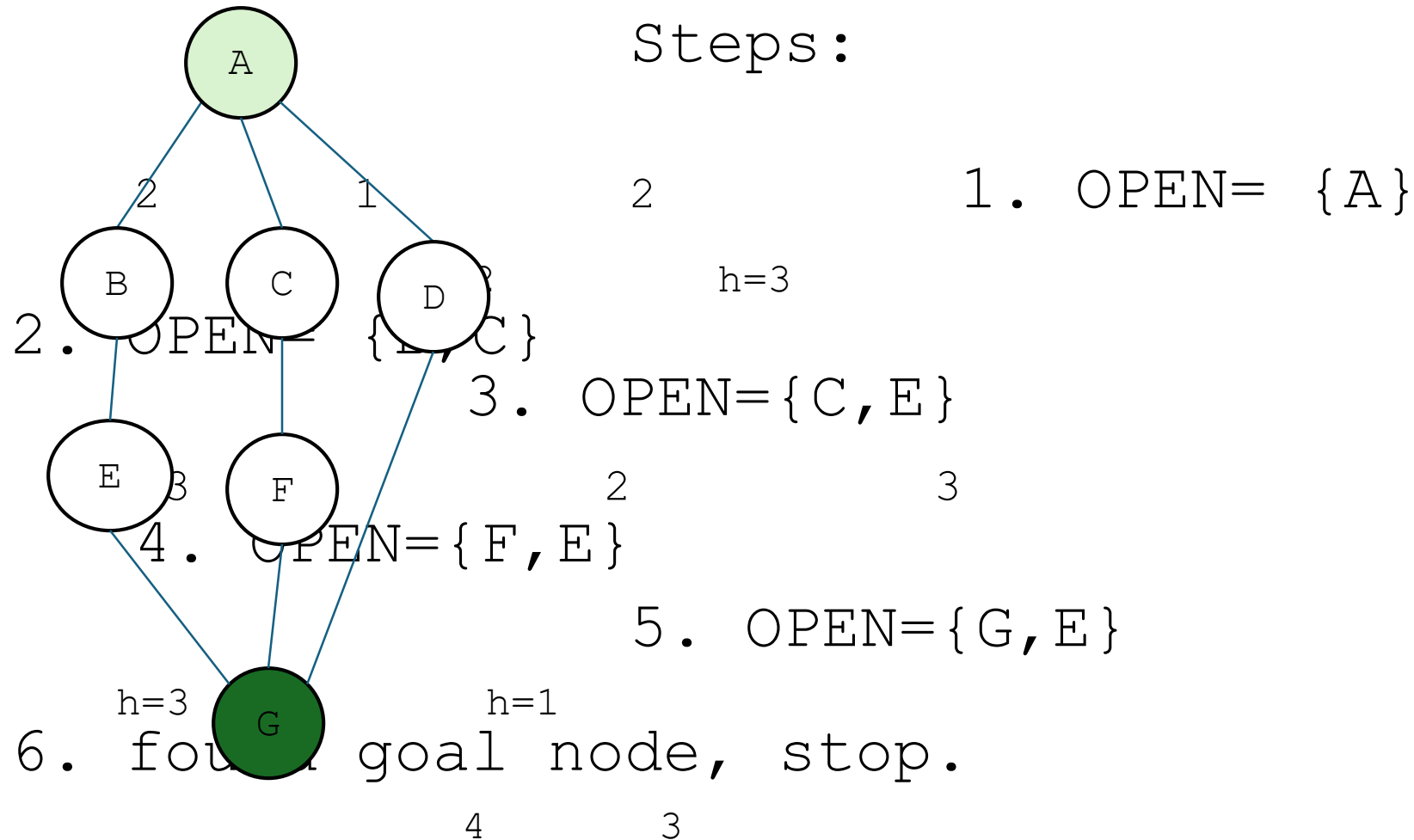
5. OPEN = { }

Clearly, open set becomes empty without finding goal node .
With $\beta = 3$, the algorithm succeeds to find goal node.

Optimality

- Just as the Algorithm is not complete, it is also not guaranteed to be optimal.
- This can happen because the beam width and an inaccurate heuristic function may cause the algorithm to miss expanding the shortest path.
- A more precise heuristic function and a larger beam width can make Beam Search more likely to find the optimal path to the goal.

Example with $\beta=2$



Time Complexity

- Depends on the accuracy of the heuristic function.
- In the worst case, the heuristic function leads Beam Search all the way to the deepest level in the search tree.
- The worst case time = **$O(B*m)$**

where B is the beam width and m is the maximum depth of any path in the search tree.

Space Complexity

- Beam Search's memory consumption is its most desirable trait.
- Since the algorithm only stores B nodes at each level in the search tree,

the worst-case space complexity =

$$O(B*m)$$

where B is the beam width, and m is the maximum depth of any path in the search tree.

- This linear memory consumption allows Beam Search to probe very deeply into large search spaces and potentially find solutions that other algorithms cannot reach.

Applications of Beam Search

- Job Scheduling - early/tardy scheduling problem
- Phrase-Based Translation Model

Local Beam Search

- Local beam search is a cross between beam search and local search (special case of beam search $\beta = 1$).
- Only the most promising β nodes at *each level* of the search tree are selected for further branching.
- remaining nodes are pruned off permanently.
- only β nodes are retained at each level, the running time is polynomial in the problem size.

Variants in Beam Search

- Flexible Beam Search:

- In case more than one child nodes have same heuristic value and one or more are included in the top B nodes, then all such nodes are included too.
- Increases the beam width temporarily.

- Recovery Beam Search

- Beam Stack Search

- BULB (Beam Search Using Limited Discrepancy Backtracking)

Conclusion

- A beam search is most often used to maintain tractability in large systems with insufficient amount of memory to store the entire search tree.
- Used widely in machine translation systems.
- Beam Search is neither complete nor optimal.
- Despite these disadvantages, beam search has found success in the practical areas of speech recognition, vision, planning, and machine learning (Zhang, 1999).