


National University of Computer and Emerging Sciences, Lahore Campus			
	Course:	Calculus and Analytical Geometry	Course Code: MT-119
	Program:	BS(CS), BS(DS), BS(SE)	Semester: Fall 2020
	Duration:	90 min	Total Marks: 50%
	Paper Date:	25-11-20	Weight 15%
	Section:	All	Page(s): 2
	Exam:	MID II	Roll No:
Instruction/Notes:		Attempt All Questions, Programmable calculators are not allowed.	

Question 1[6] [CLO-3]: Verify that $P(2,3)$ lies on the curve given below and find the lines that are tangent and normal to the given curve:

$$x^2 + xy - y^2 = 1.$$

Question 2[8] [CLO-4]: For the function $f(x) = |x^3 - 9x|$, determine the following:

- Does $f'(0)$ exist?
- Does $f'(3)$ exist?
- Does $f'(-3)$ exist?
- Determine all extrema of $f(x)$?

Question 3[5] [CLO-4]: For what value of a , m and b does the function

$$f(x) = \begin{cases} 3 & x = 0 \\ -x^2 + 3x + a & 0 < x < 1 \\ mx + b & 1 \leq x \leq 2 \end{cases}$$

Satisfy the hypotheses of Mean Value Theorem on the interval $[0, 2]$?

Question 4[15] [CLO-4]: Sketch the graph of the function $f(x) = 1 - 9x - 6x^2 - x^3$ using the following steps

- Determine the **Domain** and **Range** of $f(x)$,
- Find the **Critical point(s)** and point(s) of **Inflection** (if any),
- Identify where the **Extrema** of $f(x)$ may occur,
- Find the interval(s) on which $f(x)$ is **Increasing/Decreasing**,
- Find where the graph of $f(x)$ is **Concave up/Concave down**,
- Sketch the **General Shape** of the graph of $f(x)$.
- Plot some specific points such as **local maximum** and **minimum** points, **points of inflection** and **intercepts** then sketch the curve.

Question 5[8] [CLO-4]: Use the L'Hopital rule to find the limits

a) $\lim_{h \rightarrow 0} \frac{\sin(a+h) - \sin a}{h}$

b) $\lim_{x \rightarrow \infty} (x - \sqrt{x^2 + x})$.

Question No.6 [8] [CLO- 3]: If x , y and z are lengths of the edges of a rectangular box, the common length of "f(x)" the box diagonal is $s = \sqrt{x^2 + y^2 + z^2}$

- Assuming that x , y and z are differentiable function of t , how is ds/dt related to dx/dt , dy/dt and dz/dt ?
- How ds/dt related to dy/dt and dz/dt if x is constant?
- How dx/dt , dy/dt and dz/dt related if s is constant?

BONUS QUESTION [10]: Suppose that " f " is a continuous on $[0, 2]$ and differentiable function on $(0, 2)$ with range as set of real numbers. Suppose that $f(0) = 0$, $f(1) = 1$ and $f(2) = 1$:

- Show that there exist C_1 in $(0,1)$ such that derivative of $f(x)$ at C_1 equals 1,
- Show that there exist C_2 in $(1,2)$ such that derivative of $f(x)$ at C_2 equals 0,
- Show that there exist C in $(0,2)$ such that derivative of $f(x)$ at C equals $1/3$,

Best of Luck