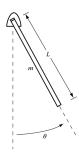
National University of Computer and Emerging Sciences, Lahore Campus

ARTIONAL UNIVERSE	Course:	Computer Modeling and Simulation	Course Code:	CS-421
WILL SOLL	Program:	BS(Computer Science)	Semester:	Spring 2017
	Duration:	1 hour	Total Marks:	40
A Solution	Paper Date:	6 th April, 2017	Weight:	15%
STATER & EMERGINES	Section:	All	Page(s):	1
SEMERA.	Exam:	Mid-2	Roll No.	

Instructions/Notes: Write answers clearly and precisely, if the answers are not easily readable then it will result in deduction of marks.

Question 1 (15 points): The pendulum shown in the figure is a rod of length L and mass m. It is put into motion by rotating the rod to an angle θ_0 and releasing it from rest. Neglecting air resistance and frictional force around the pivot point of the pendulum, develop an expression for the position θ of the pendulum as a function of time.

- Draw Free Body Diagram
- Label the FBD with equation of forces
- Write the system in terms of system of equations.
- Write the meaning of each and every symbol you use in the equation in a separate table.



Question 2 (5 points): Prove Markov's inequality, and state it in terms of probability of getting a random variable *X* greater than a constant *a*.

Question 3 (5 points): Prove Chebyshev's inequality, and state it in terms of number of values of a random variable X, close to its means μ .

Question 4 (5 points): Show that $(E \cup F)^c = E^c \cap F^c$

Question 5 (5 points): Suppose each of three persons tosses a coin. If the outcome of one of the tosses differs from the other outcomes, then the game ends. If not, then the persons start over and toss their coins again. Assuming fair coins, what is the probability that the game will end with the first round of tosses? If all three coins are biased and have probability 1/4 of landing heads, what is the probability that the game will end at the first round?

Question 6 (5 points): Consider n independent flips of a coin having probability p of landing heads. Say a changeover occurs whenever an outcome differs from the one preceding it. For instance, if the results of the flips are HHTHTHHT, then there are a total of five changeovers. If p = 1/2, what is the probability there are k changeovers?