

Part ①

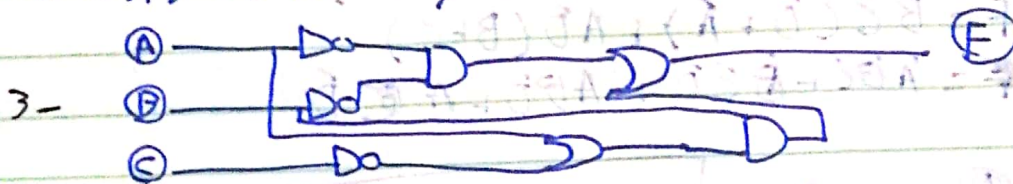
① 1- $F = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$

2- $F = \bar{A}\bar{B}(\bar{C}+C) + A\bar{B}(\bar{C}+C) + \bar{A}B\bar{C}$

$F = \bar{A}\bar{B} + A\bar{B} + \bar{A}B\bar{C}$

$F = \bar{A}\bar{B} + B(A + \bar{A}\bar{C})$

$F = \bar{A}\bar{B} + B(\bar{C} + A)$



② 1) $F = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + A\bar{B}C + A\bar{B}\bar{C}$

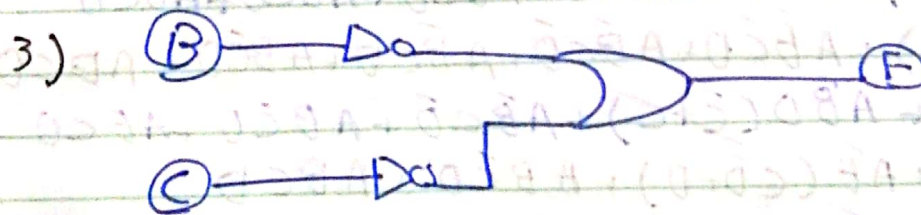
2) $F = \bar{A}\bar{B}(\bar{C}+C) + B\bar{C}(\bar{A}+A) + A\bar{B}(\bar{C}+C)$

$F = \bar{A}\bar{B} + B\bar{C} + A\bar{B}$

$F = \bar{B}(\bar{A}+A) + B\bar{C}$

$F = \bar{B} + B\bar{C}$

$F = \bar{B} + \bar{C}$



$$3) 1) F = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D}$$

$$2) F = \bar{A}\bar{B}\bar{C}(\bar{D} + D) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D}$$

$$F = \bar{B}\bar{C}(\bar{A} + A\bar{D}) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + A\bar{B}\bar{C}\bar{D}$$

$$F = \bar{B}\bar{C}(\bar{D} + \bar{A}) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + A\bar{B}\bar{C}\bar{D}$$

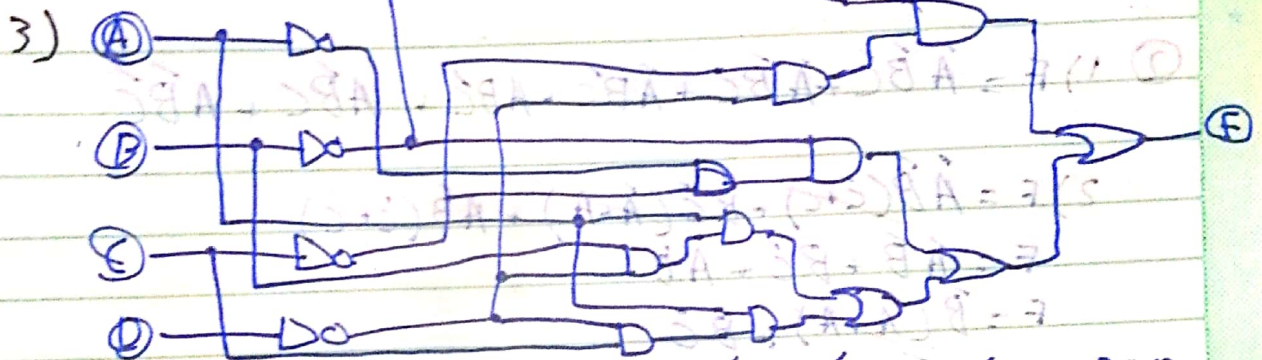
$$F = \bar{B}\bar{C}(\bar{D} + \bar{A}) + A\bar{C}\bar{D}(\bar{B} + B) + A\bar{B}\bar{C}\bar{D}$$

$$F = \bar{B}\bar{C}(\bar{D} + \bar{A}) + A\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D}$$

$$F = \bar{B}\bar{C}(\bar{D} + \bar{A}) + A\bar{D}(C + B\bar{C})$$

$$F = \bar{B}\bar{C}(\bar{D} + \bar{A}) + A\bar{D}(B + C)$$

$$F = \bar{A}\bar{B}\bar{C} + \bar{B}\bar{C}\bar{D} + A\bar{B}\bar{D} + A\bar{B}C\bar{D}$$



$$4) 1) F = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$2) F = \bar{A}\bar{B}\bar{D}(\bar{C} + C) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$F = \bar{B}\bar{D}(\bar{A}\bar{C} + \bar{A}) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + A\bar{B}\bar{D}(\bar{C} + C) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + A\bar{B}(C\bar{D} + D) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D$$

$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + A\bar{B}(C + D) + \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D$$

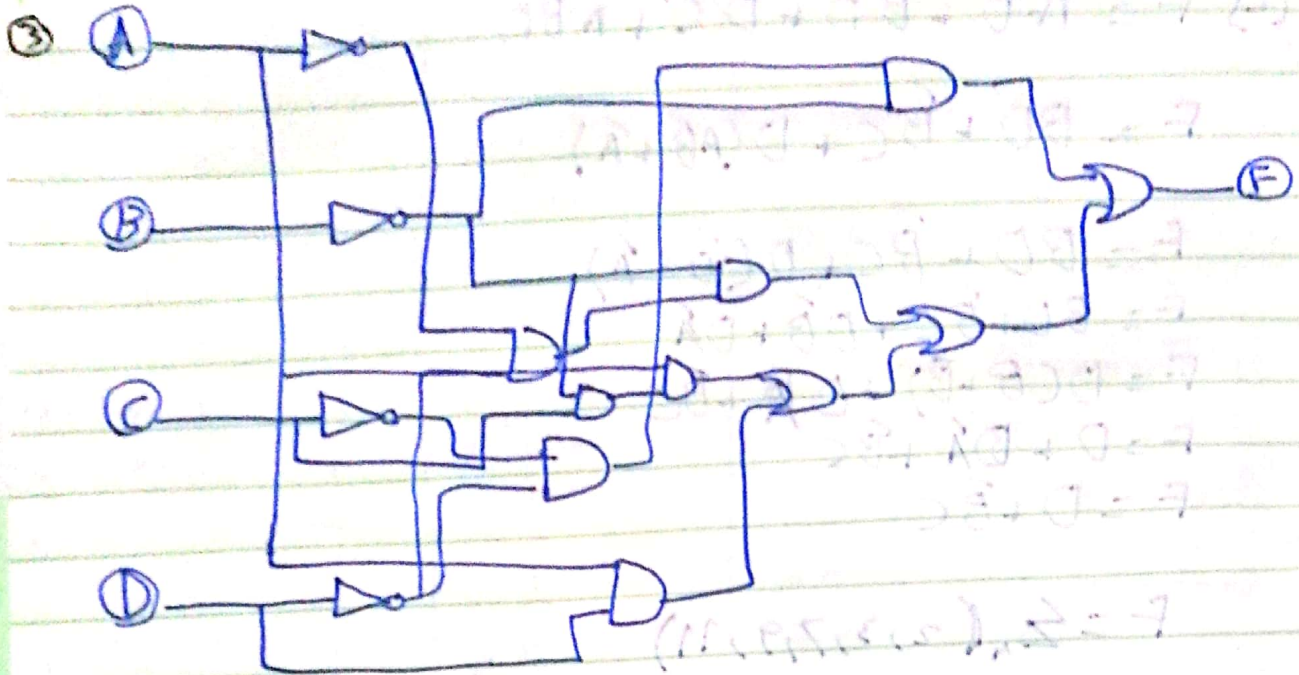
$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + A\bar{B}(C + D) + A\bar{B}\bar{D}(\bar{C} + C)$$

$$F = \bar{B}\bar{D}(\bar{C} + \bar{A}) + A\bar{B}(C + D) + A\bar{B}\bar{D}$$

$$F = \bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} + \bar{A}\bar{B}C + A\bar{B}\bar{D} + A\bar{B}D$$

$$F = \bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} + \bar{A}\bar{B}C + A\bar{B}(\bar{D} + D)$$

$$F = \bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{D} + \bar{A}\bar{B}C + A\bar{B}$$



Part 2 (1)

$$F = AD + \bar{A}\bar{C}D + ABC\bar{D}$$

$$11 + 001 + 1110$$

$$F = D(A + \bar{A}\bar{C}) + ABC\bar{D}$$

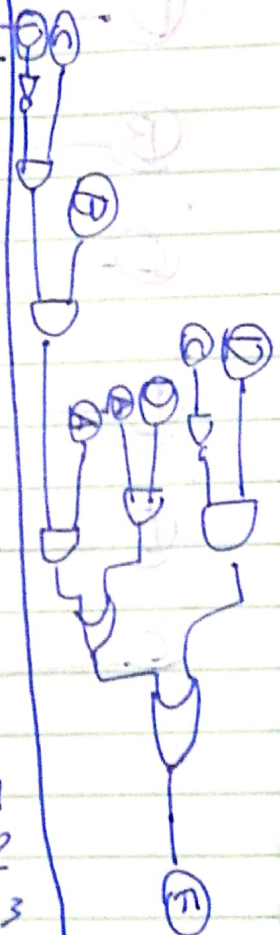
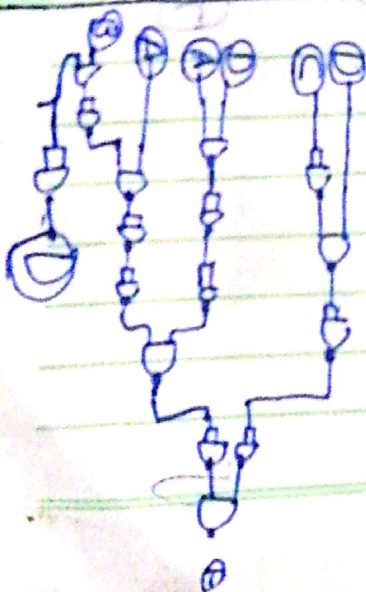
$$F = D(A + \bar{C}) + ABC\bar{D}$$

$$F = DA + D\bar{C} + ABC\bar{D}$$

$$11 + 10 + 1110$$

$$F = m(0, 3, 11, 15)$$

A	B	C	D	F	m
0	0	0	0	$\bar{A}\bar{B}\bar{C}\bar{D}$	✓ m ₀ ✓
0	0	0	1	$\bar{A}\bar{B}\bar{C}D$	m ₁
0	0	1	0	$\bar{A}\bar{B}C\bar{D}$	m ₂
0	0	1	1	$\bar{A}\bar{B}CD$	✓ m ₃ ✓
0	1	0	0	$\bar{A}B\bar{C}\bar{D}$	m ₄
0	1	0	1	$\bar{A}B\bar{C}D$	m ₅
0	1	1	0	$\bar{A}BC\bar{D}$	m ₆
0	1	1	1	$\bar{A}BCD$	m ₇
1	0	0	0	$A\bar{B}\bar{C}\bar{D}$	m ₈
1	0	0	1	$A\bar{B}\bar{C}D$	m ₉
1	0	1	0	$A\bar{B}C\bar{D}$	m ₁₀
1	0	1	1	$A\bar{B}CD$	✓ m ₁₁ ✓
1	1	0	0	$AB\bar{C}\bar{D}$	m ₁₂
1	1	0	1	$AB\bar{C}D$	m ₁₃
1	1	1	0	$ABC\bar{D}$	m ₁₄
1	1	1	1	$ABCD$	✓ m ₁₅ ✓



$$[2] F = \bar{A}b + BD + \bar{B}C + A\bar{B}D$$

$$F = BD + \bar{B}C + D(\bar{A} + A)$$

$$F = BD + \bar{B}C + D(\bar{B} + A)$$

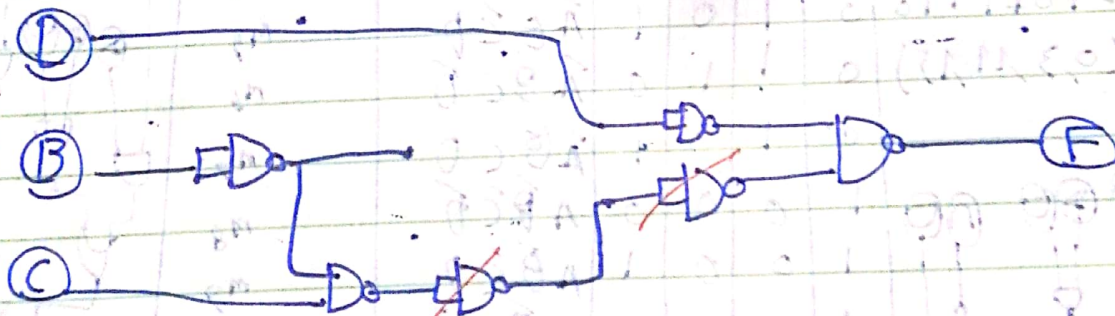
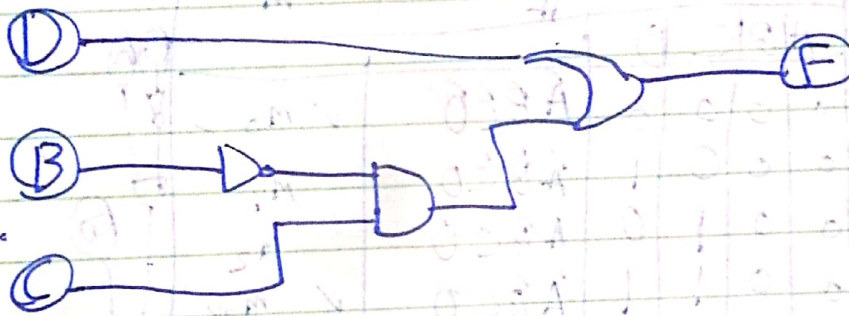
$$F = BD + \bar{B}C + D\bar{B} + DA$$

$$F = D(\bar{B} + B) + D\bar{A} + \bar{B}C$$

$$F = D + D\bar{A} + \bar{B}C$$

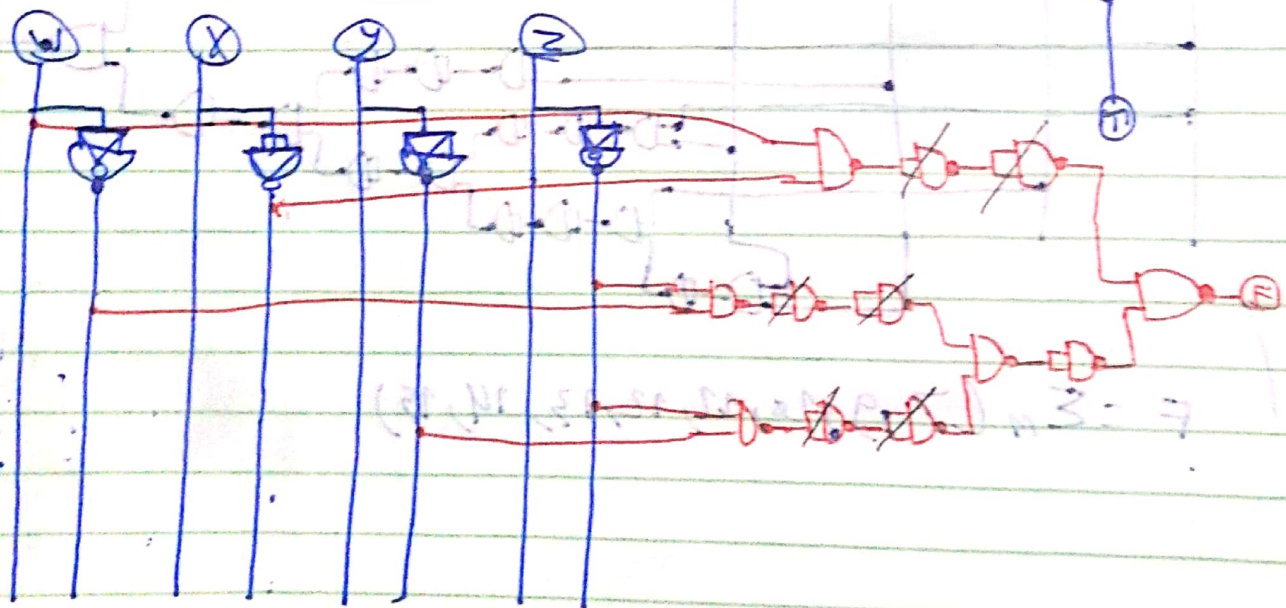
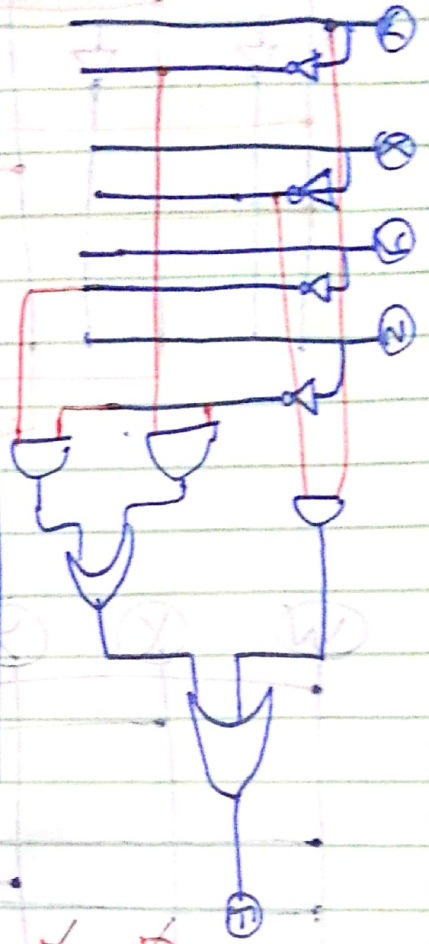
$$F = D + \bar{B}C$$

$$F = \sum_m(2, 3, 7, 9, 11)$$



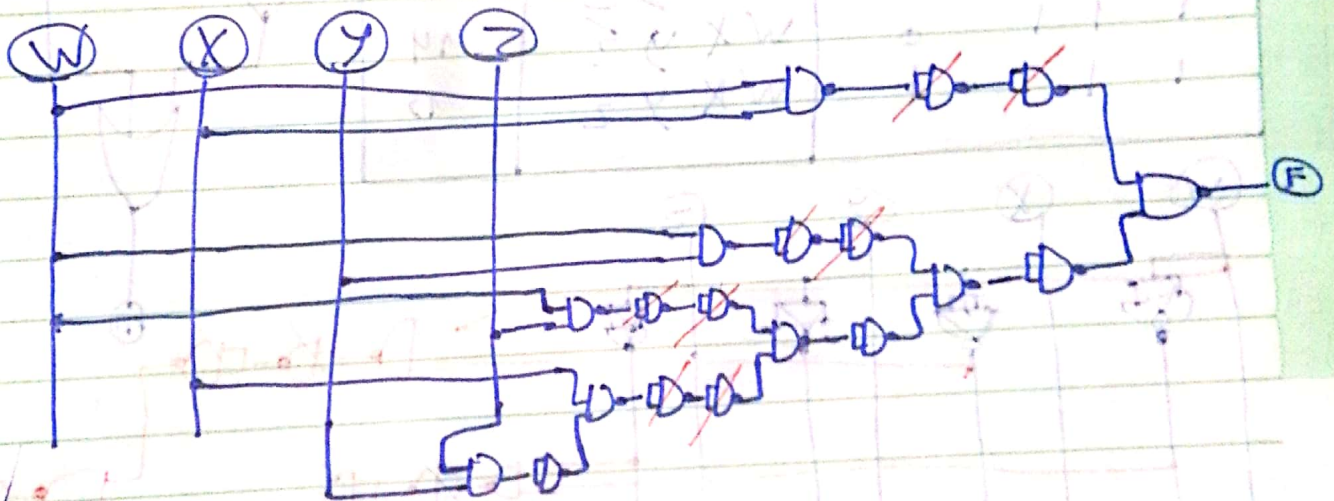
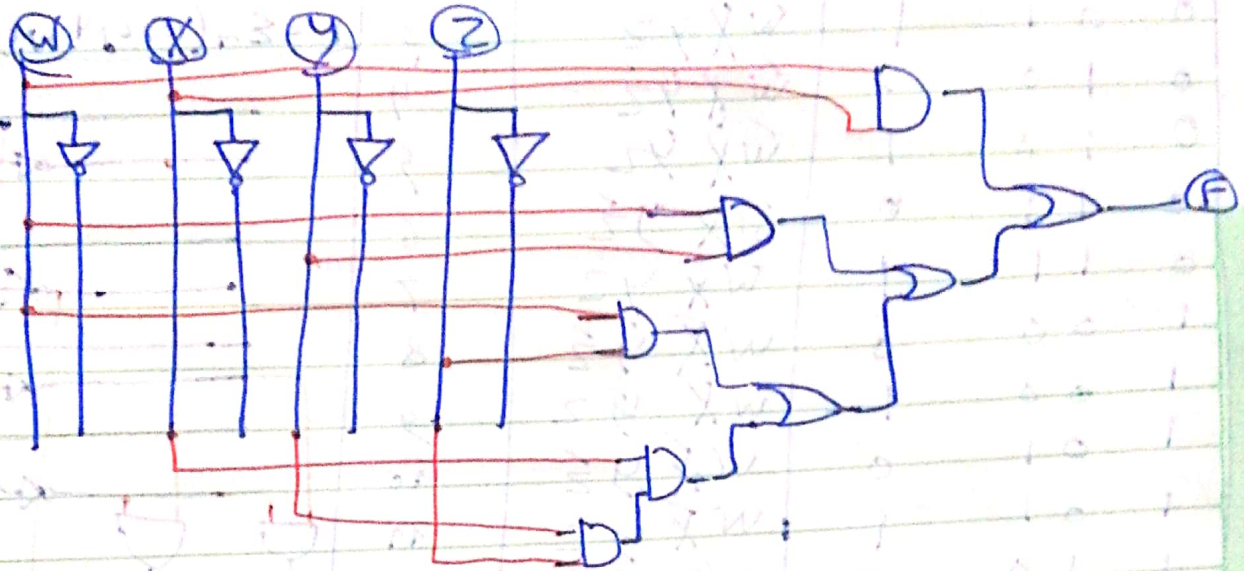
W	X	Y	Z	F
0	0	0	0	$\bar{W}\bar{X}\bar{Y}\bar{Z}$
0	0	0	1	$\bar{W}\bar{X}\bar{Y}Z$
0	0	1	0	$\bar{W}\bar{X}Y\bar{Z}$
0	0	1	1	$\bar{W}\bar{X}YZ$
0	1	0	0	$\bar{W}X\bar{Y}\bar{Z}$
0	1	0	1	$\bar{W}X\bar{Y}Z$
0	1	1	0	$\bar{W}XY\bar{Z}$
0	1	1	1	$\bar{W}XYZ$
1	0	0	0	$W\bar{X}\bar{Y}\bar{Z}$
1	0	0	1	$W\bar{X}\bar{Y}Z$
1	0	1	0	$W\bar{X}Y\bar{Z}$
1	0	1	1	$W\bar{X}YZ$
1	1	0	0	$WX\bar{Y}\bar{Z}$
1	1	0	1	$WX\bar{Y}Z$
1	1	1	0	$WXY\bar{Z}$
1	1	1	1	$WXYZ$

$F = W\bar{X}\bar{Y}\bar{Z} + \bar{W}YZ$
 $F = W\bar{X} + Z(WY + \bar{W})$
 $F = W\bar{X} + Z(\bar{W} + Y)$
 $F = W\bar{X} + Z\bar{W} + ZY$
 $F = \sum m(0, 2, 4, 6, 8, 9, 10, 11)$



* ④ $F = W(X + Y + Z) + XYZ$

$$F = WX + WY + WZ + XYZ$$



$$F = \sum m(7, 9, 10, 12, 13, 14, 15)$$