

Bitwise Operators

Be able to:

- explain the difference between bitwise operations and operations on Boolean variables
- perform AND and OR bitwise operations on bytes of data
- explain the role of bitwise operations in masks, e.g. subnet masks


Bitwise operators?

bitwise

adjective **COMPUTING**

denoting an operator in a programming language which manipulates the individual bits in a byte or word.

operator

/ˈɒpəreɪtə/ 

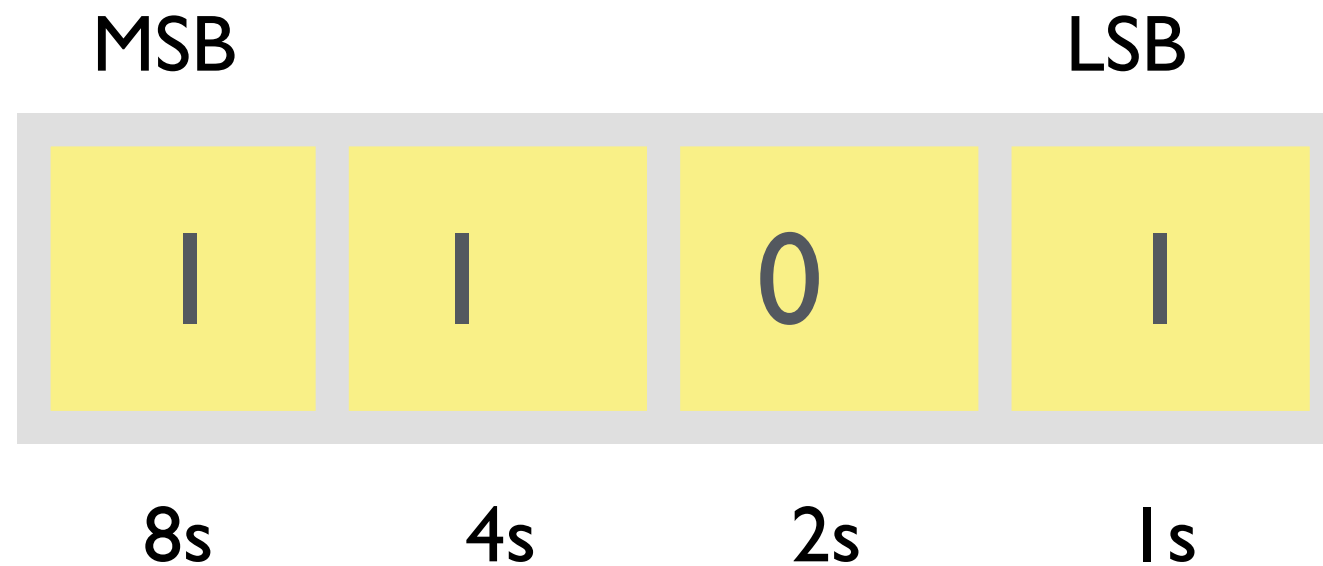
noun

noun: **operator**; plural noun: **operators**

4. **MATHEMATICS**

a symbol or function denoting an operation (e.g. \times , $+$).

Binary Number System BASE 2



MSB: most significant bit

LSB: least significant bit

Boolean variables in Python

Python has a data type `bool`

`True` or `False`

define `playOrNot` function

call `playOrNot` with argument 16
returns `True`

call `playOrNot` with argument 10
returns `False`

set `decision` to what `playOrNot`
returns

find type of `decision`

```
def playOrNot (temp):
    play = True
    if temp < 12:
        play = False
    return play
```

```
playOrNot(16)
```

```
Out[12]:
```

```
True
```

```
playOrNot(10)
```

```
Out[13]:
```

```
False
```

```
decision = playOrNot(11)
```

```
type(decision)
```

```
Out[15]:
```

```
bool
```

Hex in Python

```
hex(255)
```

```
Out[30]:
```

```
'0xff'
```

```
15*16+15
```

```
Out[32]:
```

```
255
```

```
0xFFFF
```

```
Out[22]:
```

```
65535
```

```
hex(65535)
```

```
Out[23]:
```

```
'0xffff'
```

`hex` function to convert decimal to hex
0x notation for hexadecimal numbers

check if 0xff is 255

convert from hex to decimal

convert back to hex

Bit-wise operations in Python

$x \ll y$

Returns x with the bits shifted to the left by y places (and new bits on the right-hand-side are zeros).

- Same as multiplying x by 2^y .

$x \gg y$

Returns x with the bits shifted to the right by y places.

- This is the same as dividing x by 2^y .

$x \& y$

bitwise and

- and operation, a bit at a time

$x | y$

bitwise or

- or operation, a bit at a time

Binary Addition

```
  0111
  0111
-----
  ????

```

Bitwise Operation

```
      0111
AND   1111
-----
      ????

```

Bitwise operations - AND

$a = b \text{ AND } c$

a is TRUE if b and c are TRUE

a is FALSE otherwise

e.g. 01101101
 & 00111100
 00101100

or clearing bits:

 01101101
 & 11110000 ← Bit mask
 01100000

net masks

www.iplocation.net/subnet-mask

AND	0	1
0	0	0
1	0	1

AND &

The & operator compares each binary digit and returns a new integer.

AND	0	1
0	0	0
1	0	1

37	0	0	1	0	0	1	0	1
&23	0	0	0	1	0	1	1	1
	?	?	?	?	?	?	?	?

In Python

```
#AND & in python
res = 0b00100101 & 0b00010111
bin(res)
Out[20]:
'0b101'
```

Bitwise operations - OR

$a = b \text{ OR } c$

a is TRUE if b or c are TRUE

a is FALSE otherwise

OR	0	1
0	0	1
1	1	1

e.g.

```

  01101101
| 00111100
 $\hline$ 
  01111101

```

Useful for setting bits:

```

  01101101
| 00001110 ← Bit mask
 $\hline$ 
  01101111

```

OR |

OR	0	1
0	0	1
1	1	1

37	0	0	1	0	0	1	0	1
23	0	0	0	1	0	1	1	1
	?	?	?	?	?	?	?	?

In Python

```
#OR | in python
res = 0b00100101 | 0b00010111
bin(res)
```

```
Out[21]: '0b110111'
```

Bitwise NOT

$$\sim 01101101 = 10010010$$

NOT	0	1
	1	0

Truth table

37	0	0	1	0	0	1	0	1
~	?	?	?	?	?	?	?	?

Bit shifting

Registers (processor register) – small amount of storage within a digital processor

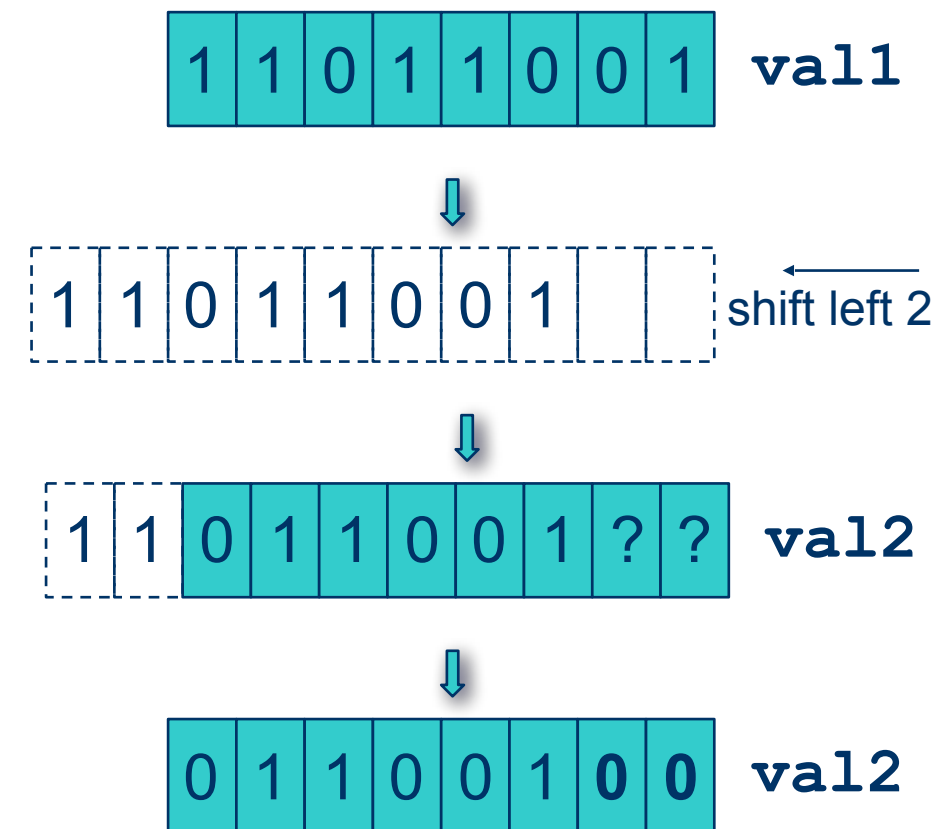
More on memory types later

Have fixed length – 8-bit register, 32-bit register etc

Bit shifting – shift bits out of the register on one end, while other bits are shifted in at the other

Bit-wise shift left

- Shift left operator: \ll
 - E.g. `val2 = val1 << 2;`
 - Shift bits/digits in `val1` left by 2
 - Store in `val2`
 - 2 leftmost bits discarded
 - 2 rightmost bits = 0
- Examples show a byte
 - same principle for all operand sizes
- Arithmetic interpretation:



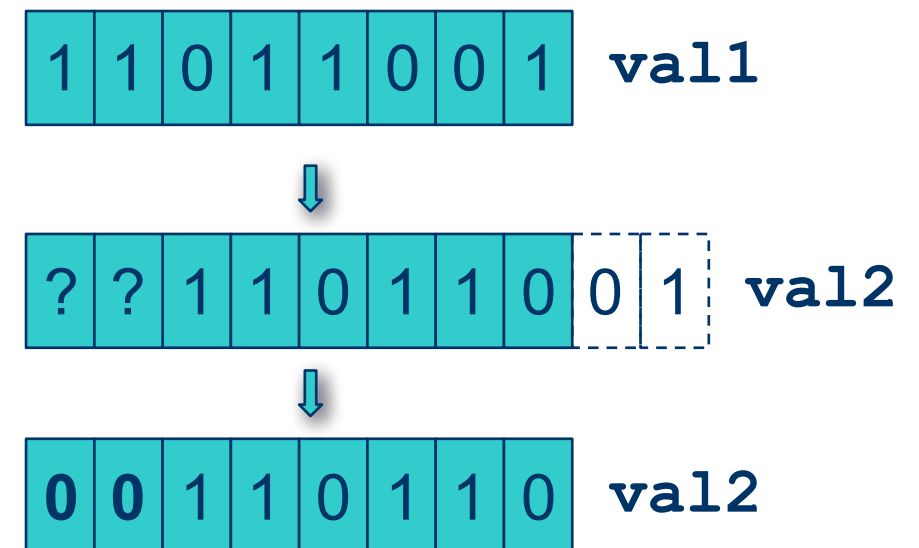
$$\underline{x \ll n = xB^n}$$

B=10: $13_{10} \ll 2 = 1300_{10} = 13 * 10^2$

B=2: $101_2 \ll 3 = 101000_2$
 $(5_{10}) \ll 3 = (40_{10}) = 5 * 2^3$

Bit-wise shift right

- Shift right operator: `>>`
 - E.g. `val2 = val1 >> 2;`
 - Shift bits/digits in `val1` right by 2
 - Store in `val2`
 - 2 rightmost bits discarded
 - 2 leftmost bits = 0
- Examples show a byte
- same principle for all operand sizes
- Arithmetic interpretation:



$$B=10: \quad 430_{10} \gg \textcircled{1} = 43_{10} = 430 / \textcircled{10} \textcircled{1}$$

$$B=2: \quad \text{1011}_2 \gg 2 = 10_2$$

$$(11_{10}) \gg 2 = (2_{10}) = 11 / 2^2$$

Note: value of bits discarded = remainder

$$x \gg n = \frac{x}{B^n}$$

More examples of binary operation uses

“short-cuts”/alternative ways to do certain operations
Check if number odd or even

Masks in image processing

Taken from:

- [https://en.wikipedia.org/wiki/Mask_\(computing\)](https://en.wikipedia.org/wiki/Mask_(computing))

First step:

- Mask out the pixels where the characters will go

Second step:

- Mask in the characters

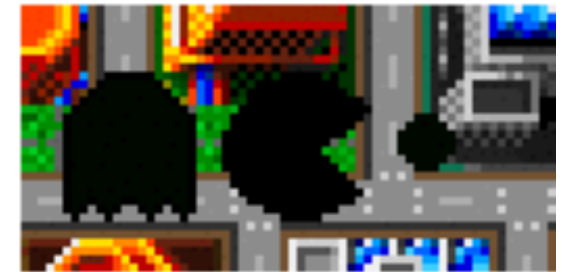
First step:



AND



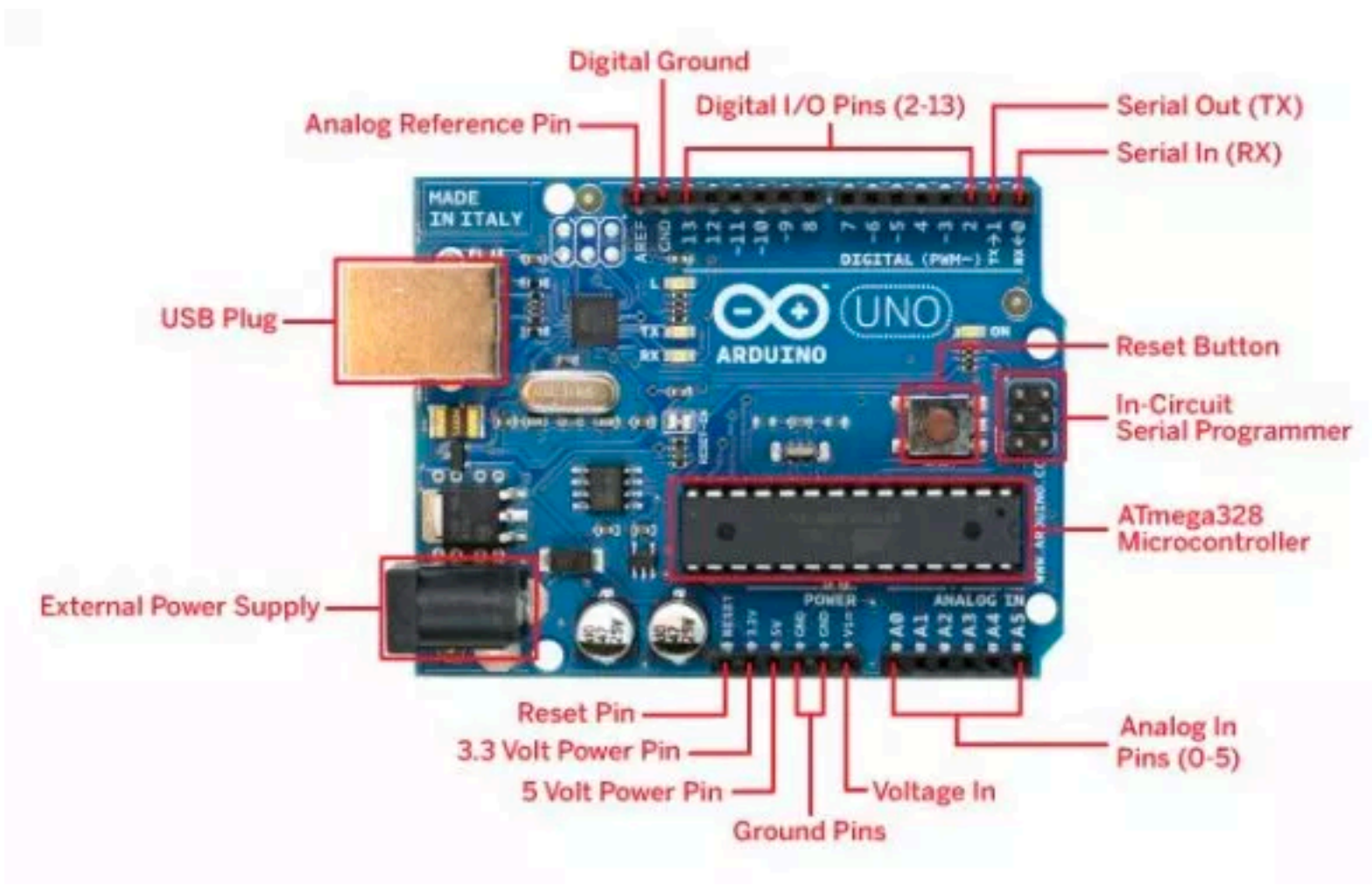
Second step:



OR



Arduino



Tutorial 2: Q6 and Q7

Bitwise Operations

1. Determine the results (in hexadecimal) of the following bitwise operations:

1. $0x96 \wedge 0xf0$
2. $0x96 \vee 0x0f$
3. $0xaa \otimes 0xf0$
4. $\neg 0xa5$

2. Consider an IPv4 Internet address 192.168.192.23. If this is a Class C network address, then the rightmost byte is the host address and the other three bytes are the network address.

1. What subnet mask is required to mask the network address?
2. What bitwise logic operation will hide (set to 0s) the host address?

see: <https://www.iplocation.net/subnet-mask>

Registers & Bitwise Operators

Be able to:

explain the difference between bitwise operations and operations on Boolean variables

perform AND and OR bitwise operations on bytes of data

explain the role of bitwise operations in masks, e.g. subnet masks