COMP 10280 Programming I (Conversion)

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COMP 10280 Programming I (Conversion)/Lecture 11

Outline

Program to calculate the factorial

Program to calculate the Fibonacci Series

The factorial

- In mathematics, the factorial of a non-negative integer is the product of all positive integers less than or equal to the number
- The factorial of a number n is denoted by n!
- For example, the factorial of 6, 6!, is $6 \times 5 \times 4 \times 3 \times 2 \times 1 = 120$
- 0! is defined to be 1
- 1! is defined to be 1

Defining the factorial

· The factorial may be defined formally as follows:

$$n! = \begin{cases} 1 & n = 0 \\ 1 & n = 1 \\ n \times n - 1 \times n - 2 \times \dots \times 1 & n > 1 \end{cases}$$

Python program 1 to calculate the factorial

```
# Calculating the factorial of a number
# Program prompts the user for the number
# Prompt the user for a number
number = int(input('Enter the number for which you wish
                       to calculate the factorial (an int >= 0): '))
if number < 0:
    print ('Error: Number entered was less than 0.')
elif number == 0:
    fact = 1
elif number == 1:
   fact = 1
else:
   fact = 1
    i = 1
    while i <= number:
        fact *= i
        i += 1
print ('Factorial of', number, 'is', fact)
print ('Finished!')
```

Corrected Python program 1 to calculate the factorial

```
# Calculating the factorial of a number
# Program prompts the user for the number
# Prompt the user for a number
number = int(input('Enter the number for which you wish
                        to calculate the factorial (an int \geq = 0): '))
if number < 0:
   print ('Error: Number entered was less than 0.')
else:
    if number == 0:
        fact = 1
    elif number == 1:
        fact = 1
    else:
        fact = 1
        i = 1
        while i <= number:
            fact. *=i
            i += 1
    print ('Factorial of', number, 'is', fact)
print ('Finished!')
```

Python program 2 to calculate the factorial

```
# Calculating the factorial of a number
# Program prompts the user for the number
# Uses a for loop
# Prompt the user for a number
number = int(input('Enter the number for which you wish
                       to calculate the factorial (an int >= 0): '))
if number < 0:
    print('Error: Number entered was less than 0.')
elif number == 0:
   fact = 1
elif number == 1:
   fact = 1
else:
    fact = 1
    for i in range (1, number + 1):
        fact *= i
print ('Factorial of', number, 'is', fact)
print('Finished!')
```

Corrected Python program 2 to calculate the factorial

```
# Calculating the factorial of a number
# Program prompts the user for the number
# Uses a for loop
# Prompt the user for a number
number = int(input('Enter the number for which you wish
                       to calculate the factorial (an int >= 0): '))
if number < 0:
    print ('Error: Number entered was less than 0.')
else:
    if number == 0:
       fact = 1
    elif number == 1:
        fact = 1
    else:
        fact = 1
        for i in range(1, number + 1):
            fact. *= i
    print ('Factorial of', number, 'is', fact)
print ('Finished!')
```

The Fibonacci Series

 In mathematics, the Fibonacci Series or Fibonacci numbers are the numbers in the following sequence:

or

- By definition, the first two numbers in the Fibonacci series are either 1 and 1 or 0 and 1, depending on the chosen starting point
- Each subsequent number is the sum of the previous two numbers
- For example, the next number in the series is 21 + 34 = 55

Applications of the Fibonacci Series

- Mathematics (eg computational analysis of Euclid's Greatest Common Divisor algorithm)
- Economics
- The breeding of rabbits (Fibonacci's own [unrealistic] example)
- Branching in trees
- · The arrangement of leaves on a stem
- The fruitlets of a pineapple
- · The flowering of artichoke
- An uncurling fern
- The arrangement of a pine cone
- The family tree of honeybees

• . . .

Defining the Fibonacci Series

The Fibonacci Series may be defined formally as follows:

$$f(n) = \begin{cases} 0 & n = 0 \\ 1 & n = 1 \\ f(n-1) + f(n-2) & n > 1 \end{cases}$$

Program to calculate the Fibonacci Series

```
Prompt the user for the number of terms to calculate
Read limit
if limit == 1 then
       print 0
else if limit == 2 then
       print 0, 1
else
       print 0, 1
       a = 0
       b = 1
       i = 2
       while i < limit do
            fib = b + a
            Print fib
            a = b
            b = fib
            Increment i
```

Python program to calculate the Fibonacci Series (1)

```
# Calculating the Fibonacci Series
# Program prompts the user for the number of terms
# Uses a while loop
f 0 = 0
f 1 = 1
# Prompt the user for how far they want to go
limit = int(input('Enter the number of terms
                       you want to calculate (an int > 0): '))
if limit. <= 0:
    print ('Error: Number entered was less than or equal to 0')
elif limit == 1:
    print ('Series is:', f 0)
elif limit == 2:
    print('Series is: ', f_0, ', ', f_1, sep = "")
```

Python program to calculate the Fibonacci Series (2)

```
else:
    print('Series is: ', f_0, ', ', f_1, sep = "", end = "")
    a = f 0
    b = f_1
    i = 2
    while i < limit:
        fib = b + a
        print(',', fib, end = "")
        a = b
        b = fib
        i += 1
# Print a newline
print()
print('Finished!')
```

Python program to calculate the Fibonacci Series (3)

Using a for loop

```
else:
    print('Series is: ', f_0, ', ', f_1, sep = "", end = "")
    a = f 0
    b = f 1
    for i in range(2, limit):
        fib = b + a
        print(',', fib, end = "")
        a = b
        b = fib
# Print a newline
print()
print('Finished!')
```

Python program to calculate the Fibonacci Series (4)

Using multiple assignment

```
else:
    print('Series is: ', f_0, ', ', f_1, sep = "", end = "")
    b, a = f_1, f_0
    for i in range(2, limit):
        fib = b + a
        print(',', fib, end = "")
        b, a = fib, b

# Print a newline
print()
print('Finished!')
```

Python program to calculate the Fibonacci Series (5)

Without using the variable fib

```
else:
    print('Series is: ', f_0, ', ', f_1, sep = "", end = "")
    b, a = f_1, f_0
    for i in range(2, limit):
        b, a = b + a, b
        print(',', b, end = "")

# Print a newline
print()
print('Finished!')
```