



THE LINK LAYER

COMP 30650: NETWORKS AND INTERNET SYSTEMS

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RECAP

Link Layer

- Framing
 - Byte/Bit stuffing
 - PPP on SONET
- Errors
 - Hamming Distance
 - Detection
 - Correction



TODAY'S PLAN

Error Detection

- Parity
- Checksum
- CRC



ERROR DETECTION

Some bits may be received in error due to noise.

How do we detect this?

- Parity
- Checksums
- CRCs

Detection will let us fix the error, for example, by retransmission.



SIMPLE ERROR DETECTION – PARITY BIT

Take D data bits, add 1 check bit that is the sum of the D bits

- Sum is modulo 2 or XOR



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$1 + 1 + 1 = 1$ ($3/2 = 1$ with remainder is **1** (parity bit))

$3\%2 = 1$ (parity bit)

PARITY BIT

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- What is the distance of the code?
 - How many errors will it detect/correct?
 - What about larger errors?
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 - Flip 1 bit parity sum wrong
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 - Detect:
 - Correct:
- What about larger errors?



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- What about larger errors?
 - Parity detects all odd number of errors



CHECKSUMS

Idea: sum up data in N-bit words

- Widely used in, e.g., TCP/IP/UDP

Stronger protection than parity



INTERNET CHECKSUM (2)

Sending:

1. Arrange data in 16-bit words
2. Put zero in checksum position, add
3. Add any carryover back to get 16 bits
4. Negate (complement) to get sum

```
0001
f203
f4f5
f6f7
+ (0000)
-----
2ddf0
  ↓
ddf0
+    2
-----
ddf2
  ↓
220d
```

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0 1 2 3 4 5 6 7 8 9 a b c d e f

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-----
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  ↓
220d
```

Negating:

```
Ffff
-ddf2
-----
220d
```


INTERNET CHECKSUM

Receiving:

1. Arrange data in 16-bit words

2. Checksum will be non-zero, add

3. Add any carryover back to get 16 bits

4. Negate the result and check it is 0

```
0001
f203
f4f5
f6f7
+ 220d
-----
2fffd
  ↓
  fffd
+    2
-----
ffff
0000
```

INTERNET CHECKSUM

Receiving:

1. Arrange data in 16-bit words

2. Checksum will be non-zero, add

3. Add any carryover back to get 16 bits

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ffff
  ↓
0000
```

INTERNET CHECKSUM

How well does the checksum work?

- What is the distance of the code?
 - Two corresponding errors could fool this checksum (e.g. add 16 and remove 16) sum is ok and it is valid codeword
 - 2
- How many errors will it detect/correct?
 - Detect: 1
 - Correct: 0

What about larger errors?


- This is where its better
 - Will find all burst errors up to 16
 - Burst – sequence/window of errors in a row.
 - Errors of 16 or less will be detected

CYCLIC REDUNDANCY CHECK (CRC)

Even stronger protection

- Given n data bits, generate k check bits such that the $n+k$ bits are **evenly** divisible by a **generator C**

Example with numbers:

- $n = 302$, $k = \text{one digit}$, $C = 3$
 - $3\ 0\ 2\ _$ should be divisible by 3 evenly
 - $3\ 0\ 2\ 0 / 3 = \text{remainder is } 2 \rightarrow 1 \text{ short of even divisible}$
 - $3\ 0\ 2\ 1$ is evenly divisible
- 

CRCS

Send Procedure:

1. Extend the n data bits with k zeros
2. Divide by the generator value C
3. Keep remainder, ignore quotient
4. Adjust k check bits by remainder

Receive Procedure:

1. Divide and check for zero remainder



CRCS

Data bits: 1 0 0 1 1 | 1 1 0 1 0 1 1 1 1 1
1101011111

Check bits:

$$C(x) = x^4 + x^1 + 1$$

$$C = 10011$$

$$k = 4$$

USE XOR NOT SUBTRACTRION!

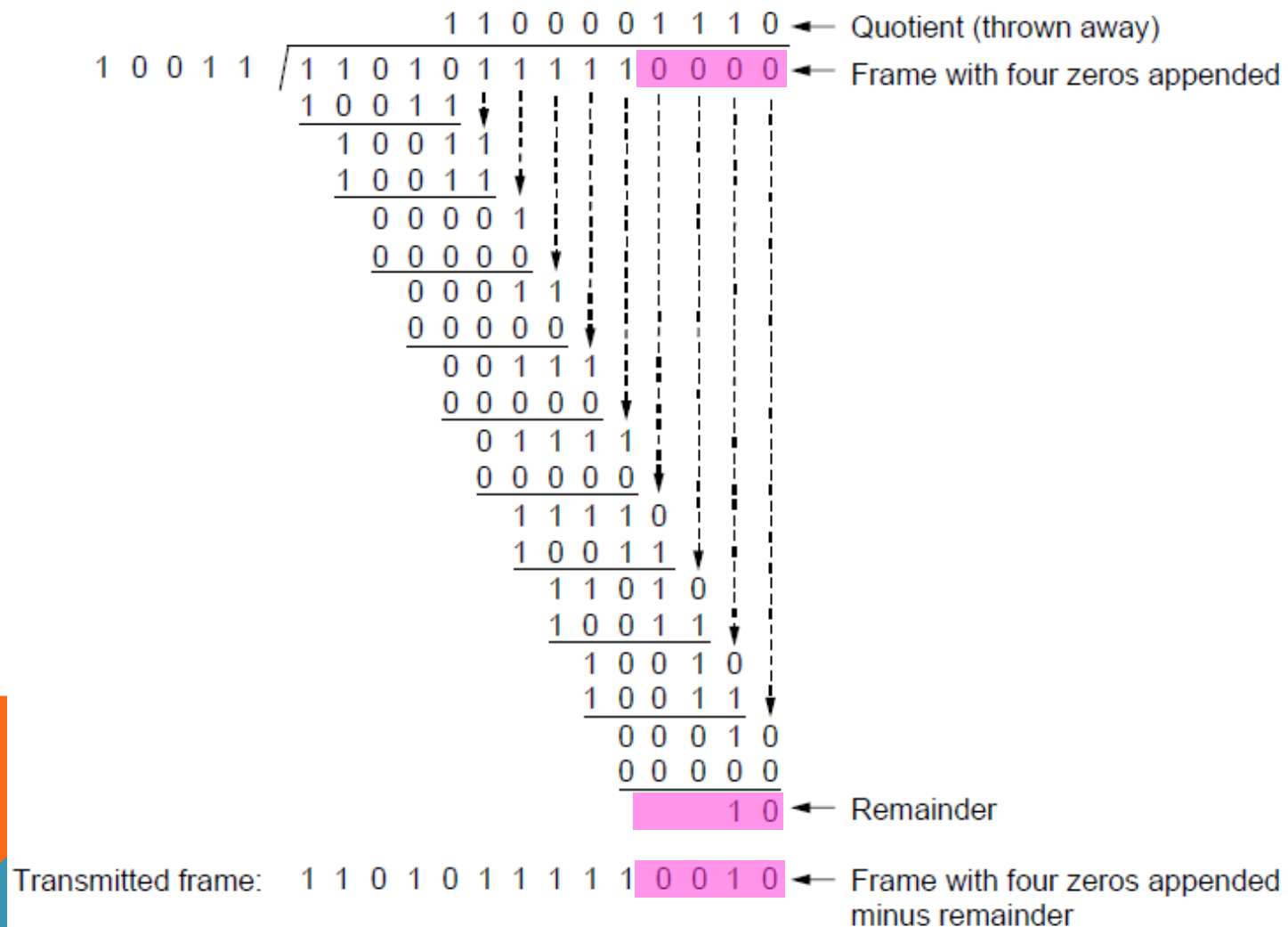
0 XOR 0 -> 0

0 XOR 1 -> 1

1 XOR 1 -> 0

1 XOR 0 -> 1

CRCS



CRCS

Protection depend on generator

- Standard CRC-32 is 1 0000 0100 1100 0001 0001 1101 1011 0111

Properties:

- HD=4, detects up to triple bit errors
- Also odd number of errors
- And bursts of up to k bits in error
- Not vulnerable to systematic errors like checksums
 - Eg adding zeros to a sum cause no errors.

ERROR DETECTION IN PRACTICE

CRCs are widely used on links

- Ethernet, 802.11, ADSL, Cable ...

Checksum used in Internet

- IP, TCP, UDP ... but it is weak

Parity

- Is little used

